

# Parsing

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# Bottom-up Parsing

## Example

### Grammar

$$\begin{array}{ll} E & \rightarrow E + T \mid T \\ T & \rightarrow T * F \mid F \\ F & \rightarrow (E) \\ & \mid \text{id} \end{array}$$

Input:     1 \* 2

# Bottom-up Parsing

## Example

id \* id

### Grammar

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T * F \mid F \\ F &\rightarrow (E) \\ &\quad \mid \text{id} \end{aligned}$$

Input: 1 \* 2

# Bottom-up Parsing

## Example

### Grammar

$$\begin{aligned}
 E &\rightarrow E + T \mid T \\
 T &\rightarrow T * F \mid F \\
 F &\rightarrow (E) \\
 &\quad \mid \text{id}
 \end{aligned}$$

Input: 1 \* 2

id \* id

$F$  \* id  
 $\mid$   
 id

# Bottom-up Parsing

## Example

### Grammar

$$\begin{aligned}
 E &\rightarrow E + T \mid T \\
 T &\rightarrow T * F \mid F \\
 F &\rightarrow (E) \\
 &\quad \mid \text{id}
 \end{aligned}$$

Input: 1 \* 2

id \* id

$F$  \* id  
 $\mid$   
 id

$T$  \* id  
 $\mid$   
 $F$   
 $\mid$   
 id

# Bottom-up Parsing

## Example

### Grammar

$$\begin{aligned}
 E &\rightarrow E + T \mid T \\
 T &\rightarrow T * F \mid F \\
 F &\rightarrow (E) \\
 &\quad \mid \text{id}
 \end{aligned}$$

Input: 1 \* 2

$$\text{id} \quad * \quad \text{id}$$

$$\begin{array}{c}
 F \quad * \quad \text{id} \\
 | \\
 \text{id}
 \end{array}$$

$$\begin{array}{c}
 T \quad * \quad \text{id} \\
 | \\
 F \\
 | \\
 \text{id}
 \end{array}$$

$$\begin{array}{c}
 T \quad * \quad F \\
 | \quad \quad | \\
 F \quad \quad \text{id} \\
 | \\
 \text{id}
 \end{array}$$

# Bottom-up Parsing

## Example

### Grammar

$$\begin{aligned}
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 T &\rightarrow T * F \mid F \\
 F &\rightarrow (E) \mid \text{id}
 \end{aligned}$$

Input: 1 \* 2

id \* id

$$\begin{array}{ccc}
 T & * & F \\
 | & & | \\
 F & & \text{id} \\
 | & & \\
 \text{id} & & 
 \end{array}$$

$$\begin{array}{ccc}
 F & * & \text{id} \\
 | & & \\
 \text{id} & & 
 \end{array}$$

$$\begin{array}{ccccc}
 & & T & & \\
 & \swarrow & | & \searrow & \\
 T & & * & & F \\
 | & & & & | \\
 F & & & & \text{id} \\
 | & & & & \\
 \text{id} & & & & 
 \end{array}$$

$$\begin{array}{ccc}
 T & * & \text{id} \\
 | & & \\
 F & & \\
 | & & \\
 \text{id} & & 
 \end{array}$$

# Bottom-up Parsing

## Example

### Grammar

$$\begin{aligned}
 E &\rightarrow E + T \mid T \\
 T &\rightarrow T * F \mid F \\
 F &\rightarrow (E) \mid \text{id}
 \end{aligned}$$

Input: 1 \* 2

id \* id

$$\begin{array}{c}
 T \quad * \quad F \\
 | \quad \quad | \\
 F \quad \quad \text{id} \\
 | \\
 \text{id}
 \end{array}$$

$$\begin{array}{c}
 F \quad * \quad \text{id} \\
 | \\
 \text{id}
 \end{array}$$

$$\begin{array}{c}
 T \\
 / \quad | \quad \backslash \\
 T \quad * \quad F \\
 | \quad \quad | \\
 F \quad \quad \text{id} \\
 | \\
 \text{id}
 \end{array}$$

$$\begin{array}{c}
 T \quad * \quad \text{id} \\
 | \\
 F \\
 | \\
 \text{id}
 \end{array}$$

$$\begin{array}{c}
 E \\
 | \\
 T \\
 / \quad | \quad \backslash \\
 T \quad * \quad F \\
 | \quad \quad | \\
 F \quad \quad \text{id} \\
 | \\
 \text{id}
 \end{array}$$



# Bottom-up Parsing

## Example

id \* id

$F$  \* id  
|  
id

$T$  \* id  
|  
 $F$   
|  
id

$T$  \*  $F$   
| |  
 $F$  id  
|  
id

$T$   
/ | \  
 $T$  \*  $F$   
| |  
 $F$  id  
|  
id

$E$   
|  
 $T$   
/ | \  
 $T$  \*  $F$   
| |  
 $F$  id  
|  
id

Derivation :

$E \Rightarrow T \Rightarrow T * F \Rightarrow T * id \Rightarrow F * id \Rightarrow id * id$

# Bottom-up Parsing

## Example

id \* id

$F$  \* id  
|  
id

$T$  \* id  
|  
 $F$   
|  
id

$T$  \*  $F$   
| |  
 $F$  id  
|  
id

$T$   
/ | \  
 $T$  \*  $F$   
| |  
 $F$  id  
|  
id

$E$   
|  
 $T$   
/ | \  
 $T$  \*  $F$   
| |  
 $F$  id  
|  
id

Derivation :

$E \Rightarrow T \Rightarrow T * F \Rightarrow T * id \Rightarrow F * id \Rightarrow id * id$

1 Rightmost derivation

# Bottom-up Parsing

## Example

id \* id

$F$  \* id  
|  
id

$T$  \* id  
|  
 $F$   
|  
id

$T$  \*  $F$   
| |  
 $F$  id  
|  
id

$T$   
/ | \  
 $T$  \*  $F$   
| |  
 $F$  id  
|  
id

$E$   
|  
 $T$   
/ | \  
 $T$  \*  $F$   
| |  
 $F$  id  
|  
id

Derivation :

$E \Rightarrow T \Rightarrow T * F \Rightarrow T * id \Rightarrow F * id \Rightarrow id * id$

- 1 Rightmost derivation
- 2 Reverse rightmost derivation – *Reduction*

# Bottom-up Parsing

## Right Sentential Form

- **Right Sentential Form.** Strings of grammar symbols that occur anytime during a rightmost derivation from a grammar  $G$
- All *frontiers* during a bottom-up parse are right sentential forms.

# Bottom-up Parsing

## Handle

- **Handle.** A sub-string of a right-sentential form that appears as a right hand side of a grammar production, and which can be used to reduce the string to its *previous* right-sentential form
- $S \xRightarrow{*} \alpha Aw \Rightarrow \alpha \beta w$  with a production  $A \rightarrow \beta$ , then  $A \rightarrow \beta$  is a handle.

# Bottom-up Parsing

## Handle

- **Handle.** A sub-string of a right-sentential form that appears as a right hand side of a grammar production, and which can be used to reduce the string to its *previous* right-sentential form
- $S \xRightarrow{*} \alpha Aw \Rightarrow \alpha \beta w$  with a production  $A \rightarrow \beta$ , then  $A \rightarrow \beta$  is a handle.
- Bottom-up parsing can be viewed as the process of locating a handle in the  $n$ -th right-sentential form of  $S$ , and replacing that with the LHS of the production to get the  $(n - 1)$ th right-sentential form.

# Shift-Reduce Parsing

Stack Input	
\$	$w$ \$

# Shift-Reduce Parsing

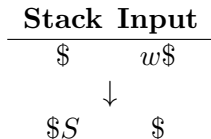
Stack	Input
\$	$w$ \$
↓	
$\$S$	\$

Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2$ \$	shift



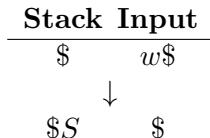
# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2 \$$	shift
$\$ \text{id}_1$	$* \text{id}_2 \$$	reduce by $F \rightarrow \text{id}$

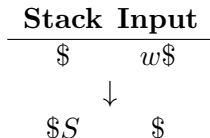
# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2 \$$	shift
$\$ \text{id}_1$	$* \text{id}_2 \$$	reduce by $F \rightarrow \text{id}$
$\$ F$	$* \text{id}_2 \$$	reduce by $T \rightarrow F$

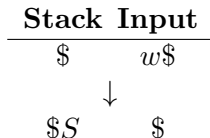
# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2 \$$	shift
$\$ \text{id}_1$	$* \text{id}_2 \$$	reduce by $F \rightarrow \text{id}$
$\$ F$	$* \text{id}_2 \$$	reduce by $T \rightarrow F$
$\$ T$	$* \text{id}_2 \$$	shift

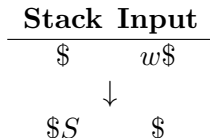
# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2$ \$	shift
\$ $\text{id}_1$	$* \text{id}_2$ \$	reduce by $F \rightarrow \text{id}$
\$ $F$	$* \text{id}_2$ \$	reduce by $T \rightarrow F$
\$ $T$	$* \text{id}_2$ \$	shift
\$ $T*$	$\text{id}_2$ \$	shift

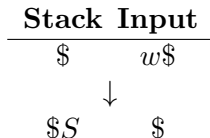
# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2 \$$	shift
$\$ \text{id}_1$	$* \text{id}_2 \$$	reduce by $F \rightarrow \text{id}$
$\$ F$	$* \text{id}_2 \$$	reduce by $T \rightarrow F$
$\$ T$	$* \text{id}_2 \$$	shift
$\$ T *$	$\text{id}_2 \$$	shift
$\$ T * \text{id}_2$	$\$$	reduce by $F \rightarrow \text{id}$

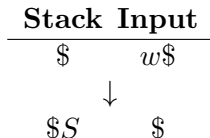
# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2 \$$	shift
$\$ \text{id}_1$	$* \text{id}_2 \$$	reduce by $F \rightarrow \text{id}$
$\$ F$	$* \text{id}_2 \$$	reduce by $T \rightarrow F$
$\$ T$	$* \text{id}_2 \$$	shift
$\$ T *$	$\text{id}_2 \$$	shift
$\$ T * \text{id}_2$	$\$$	reduce by $F \rightarrow \text{id}$
$\$ T * F$	$\$$	reduce by $T \rightarrow + T * F$

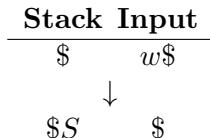
# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2 \$$	shift
$\$ \text{id}_1$	$* \text{id}_2 \$$	reduce by $F \rightarrow \text{id}$
$\$ F$	$* \text{id}_2 \$$	reduce by $T \rightarrow F$
$\$ T$	$* \text{id}_2 \$$	shift
$\$ T *$	$\text{id}_2 \$$	shift
$\$ T * \text{id}_2$	$\$$	reduce by $F \rightarrow \text{id}$
$\$ T * F$	$\$$	reduce by $T \rightarrow +T * F$
$\$ T$	$\$$	reduce by $E \rightarrow T$

# Shift-Reduce Parsing



Example:

Stack	Input	Action
\$	$\text{id}_1 * \text{id}_2 \$$	shift
$\$ \text{id}_1$	$* \text{id}_2 \$$	reduce by $F \rightarrow \text{id}$
$\$ F$	$* \text{id}_2 \$$	reduce by $T \rightarrow F$
$\$ T$	$* \text{id}_2 \$$	shift
$\$ T *$	$\text{id}_2 \$$	shift
$\$ T * \text{id}_2$	$\$$	reduce by $F \rightarrow \text{id}$
$\$ T * F$	$\$$	reduce by $T \rightarrow + T * F$
$\$ T$	$\$$	reduce by $E \rightarrow T$
$\$ E$	$\$$	



# Shift-Reduce Parsing

## Parser Actions

- 1 **Shift:** Shift the next input symbol onto the stack.
- 2 **Reduce:** Reduce a contiguous portion of the stack content including the top-of-stack by the LHS of an appropriate grammar production.

# Shift-Reduce Parsing

## Parser Actions

- 1 **Shift:** Shift the next input symbol onto the stack.
- 2 **Reduce:** Reduce a contiguous portion of the stack content including the top-of-stack by the LHS of an appropriate grammar production.
- 3 **Accept:** Declare success.
- 4 **Error:** Discover a syntax error.

# Shift-Reduce Parsing

Reductions happen only at the top of the stack

$$1 \quad S \xRightarrow{*}_{rm} \alpha Az \Rightarrow \alpha \beta Byz \xRightarrow{*}_{rm} \alpha \beta \gamma yz$$

$$2 \quad S \xRightarrow{*}_{rm} \alpha Bx Az \Rightarrow \alpha Bxyz \xRightarrow{*}_{rm} \alpha \gamma xyz$$

# Shift-Reduce Parsing

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$$2 \quad S \xRightarrow{*}_{rm} \alpha Bx Az \Rightarrow \alpha Bxyz \xRightarrow{*}_{rm} \alpha \gamma xyz$$

Derivations to the left happen later. Reductions to the left happen earlier.

# Shift-Reduce Parsing

## Condition for a Successful Parse

# Shift-Reduce Parsing

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### Viable Prefix

A prefix of a right-sentential form.

# Shift-Reduce Parsing

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### Viable Prefix

A prefix of a right-sentential form.

### Conflicts

- 1 **Shift-Reduce**
- 2 **Reduce-Reduce**

# Shift-Reduce Parsing

## Conflicts

### Example

$stmt \rightarrow$

	if $expr$ then $stmt$
	if $expr$ then $stmt$ else $stmt$
	other



# Bottom-up Parsing

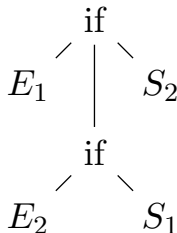
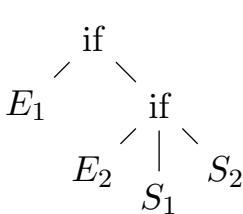
## Conflict – Example

**input:** if  $E_1$  then if  $E_2$  then  $S_1$  else  $S_2$

# Bottom-up Parsing

## Conflict – Example

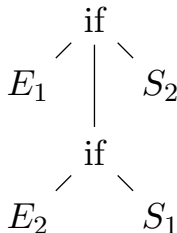
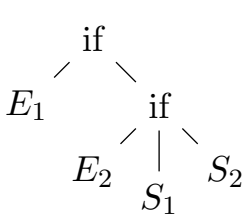
**input:** if  $E_1$  then if  $E_2$  then  $S_1$  else  $S_2$



# Bottom-up Parsing

## Conflict – Example

**input:** if  $E_1$  then if  $E_2$  then  $S_1$  else  $S_2$



- if  $E_1$  then if  $E_2$  then  $S_1$  else  $S_2$
- if  $E_1$  then if  $E_2$  then  $S_1$  else  $S_2$

# Bottom-up Parsing

## LR Parsing

### Properties

- Table driven
- LR grammars

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- Table driven
- LR grammars

### Advantages

- LR grammars are quite general.
- Syntax errors are detected early.
- $LR(k) \supset LL(k)$

# Bottom-up Parsing

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### Properties

- Table driven
- LR grammars

### Advantages

- LR grammars are quite general.
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- $LR(k) \supset LL(k)$

# SLR Parsing

## Parser Architecture

