# Lexical Analysis Programming Languages

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### Non-Deterministic FSA (NFA)

- $\blacksquare$  Finite set of states -(S)
- $\blacksquare$  Alphabet  $(\sum)$
- Transition function  $(T: S \times \sum \rightarrow 2^S)$
- Initial state  $(S_0)$
- Final/accepting states  $(F \subseteq S)$

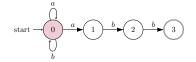
### Non-Deterministic FSA (NFA)

- $\blacksquare$  Finite set of states -(S)
- Alphabet  $(\sum)$
- Transition function  $(T: S \times \sum \rightarrow 2^S)$
- Initial state  $(S_0)$
- Final/accepting states  $(F \subseteq S)$
- Acceptance of a string: When there exists a path corresponding to the input leading to an accepting state.

Salient Points

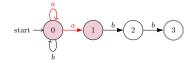
- Possibly more than one outgoing transitions with the same label.
- $\epsilon$ -transitions
- More than one paths can be traced during the same run.
- All the possible traces have to be tracked.
- Multiple states can be active at the same time.

#### Example 1



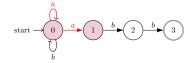
0

#### Example 1



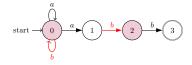


#### Example 1



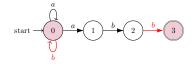


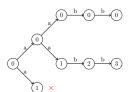
#### Example 1



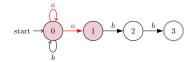


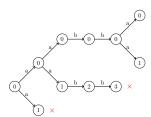
#### Example 1



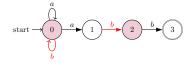


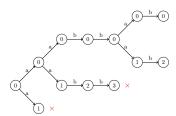
### Example 1



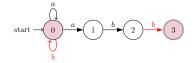


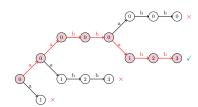
## Example 1



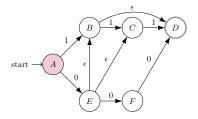


#### Example 1





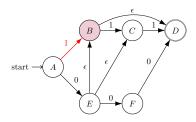
#### Example 2.1



**Input:** 1...

 $\epsilon$ -closure

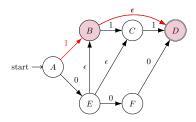
#### Example 2.1



Input: 1...

 $\epsilon$ -closure

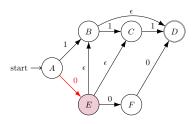
#### Example 2.1



Input: 1...

 $\epsilon$ -closure

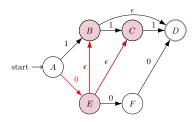
#### Example 2.2



Input: 0...

 $\epsilon$ -closure

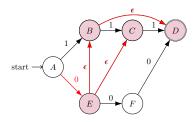
### Example 2.2



Input: 0...

 $\epsilon$ -closure

#### Example 2.2



Input: 0...

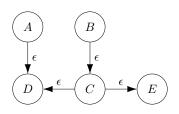
 $\epsilon$ -closure

- $\bullet$  e-closure: computed on a set of states
- Transitive closure of all states reachable through ε-transitions
- From a source state set  $S_1$ , on an input symbol a, the destination state set  $S_2$  is computed as:

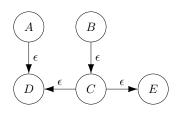
$$U = \bigcup_{s \in S_1} Trans[s, a]$$
  
$$S_1 = \epsilon - closure(U)$$

 $\bullet$ -closure – a reflexive relation

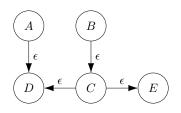
```
procedure \epsilon-CLOSURE(s)
   stack.PUSH(s)
   ep.ADD(s)
   while stack is not empty do
       t \leftarrow stack.POP
       U \leftarrow \{u : u \in M.Trans[t, \epsilon]\}
       for u \in U do
           if u \notin ep then
               stack.PUSH(u)
               ep.ADD(u)
           end if
       end for
   end while
   return ep
end procedure
```



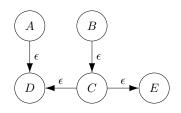
| ep | stack |
|----|-------|
|    |       |
|    |       |



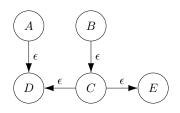
| ep   | stack |
|------|-------|
|      |       |
| A, B | B, A  |
| A, D | D, A  |



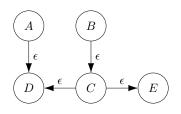
| tack       | staci | ep      |
|------------|-------|---------|
|            |       |         |
| $\beta, A$ | B, A  | A, B    |
| 3, D       | B, L  | A, B, D |
| 3, .       | B,    | A, B, D |



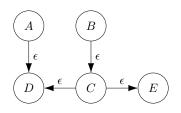
| ep      | stack |
|---------|-------|
|         |       |
| A, B    | B, A  |
| A, B, D | B, D  |
| A, B, D | В     |
|         |       |



| ep         | stack |
|------------|-------|
|            |       |
| A, B       | B, A  |
| A, B, D    | B, D  |
| A, B, D    | B     |
| A, B, D, C | C     |
|            |       |



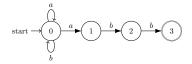
| stack |
|-------|
|       |
| B, A  |
| B, D  |
| В     |
| C     |
| E     |
|       |



| ep            | stack |
|---------------|-------|
|               |       |
| A, B          | B, A  |
| A, B, D       | B, D  |
| A, B, D       | B     |
| A, B, D, C    | C     |
| A, B, D, C, E | E     |
| A, B, D, C, E |       |
|               |       |

# Simulating FSAs

# Representating transition function using transition tables

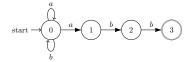


#### **Transition Table:**

| State | a | b |
|-------|---|---|
| 0     |   |   |
| 1     |   |   |
| 2     |   |   |
| 3     |   |   |

# Simulating FSAs

# Representating transition function using transition tables



#### **Transition Table:**

| State | a          | b   |
|-------|------------|-----|
| 0     | $\{0, 1\}$ | {0} |
| 1     | {}         | {2} |
| 2     | {}         | {3} |
| 3     | {}         | {}  |

 $\mathbf{procedure} \ \mathtt{SIMNFA}(N, \, inp)$ 

```
procedure SIMNFA(N, inp)
    S \leftarrow \epsilon-CLOSURE(\{N.s_0\})
    while there is input left do
        c \leftarrow \text{NEXTCHAR}
        T' \leftarrow \text{MOVE}(S, c)
        S \leftarrow \epsilon-CLOSURE(T')
    end while
    if S \cap N.F \neq \{\} then
        return true
    else
        return false
    end if
end procedure
```

```
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    S \leftarrow \epsilon-CLOSURE(\{N.s_0\})
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```

#### Next

Conversion of NFA to DFA