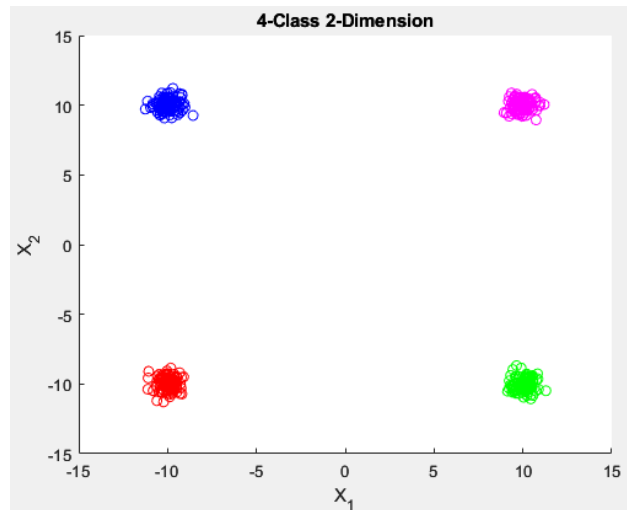


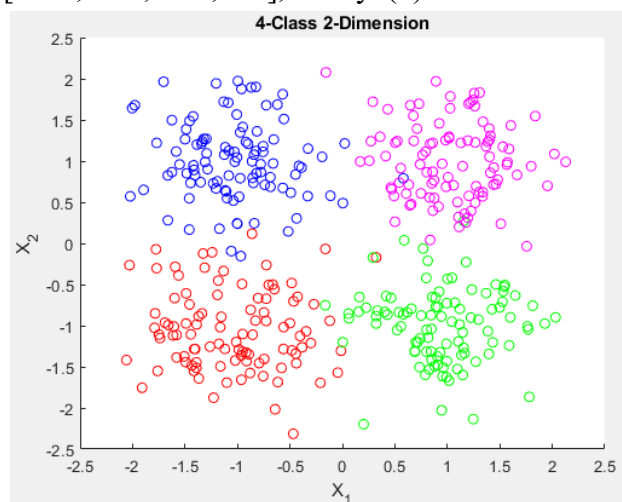
Pattern Recognition ex3

1. Scatter Matrices and Criterion J3

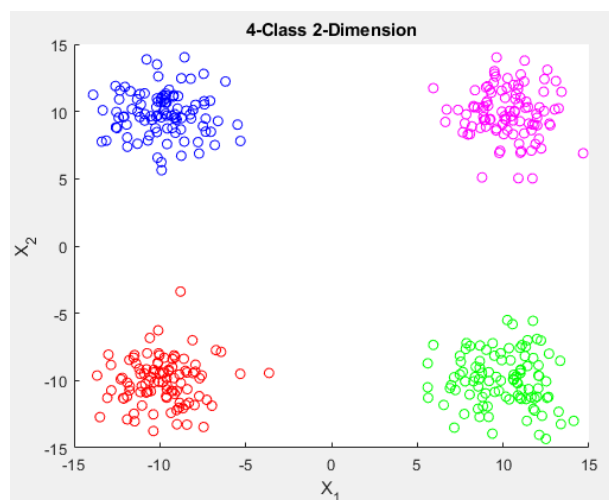
(a)  $[-10 \ -10; -10 \ 10; 10 \ -10; 10 \ 10], 0.2 \text{ eye}(2)$



(b)  $[-1 \ -1; -1 \ 1; 1 \ -1; 1 \ 1], 0.2 \text{ eye}(2)$



(c)  $[-10 \ -10; -10 \ 10; 10 \ -10; 10 \ 10], 1.0 \text{ eye}(2)$



Results:

```
>> ex3_1
```

(a)

```
Sw: [0.207183 0.00675828; 0.00675828 0.202538]
```

```
Sb: [99.7442 -0.42041; -0.42041 100.136]
```

```
Sm: [99.9514 -0.413652; -0.413652 100.338]
```

```
J3: 979.035
```

(b)

```
Sw: [0.21784 -0.0156265; -0.0156265 0.218595]
```

```
Sb: [1.02527 0.0381738; 0.0381738 1.01658]
```

```
Sm: [1.24311 0.0225472; 0.0225472 1.23518]
```

```
J3: 11.4305
```

(c)

```
Sw: [3.19029 -0.106465; -0.106465 3.16818]
```

```
Sb: [99.6931 1.31687; 1.31687 98.701]
```

```
Sm: [102.883 1.21041; 1.21041 101.869]
```

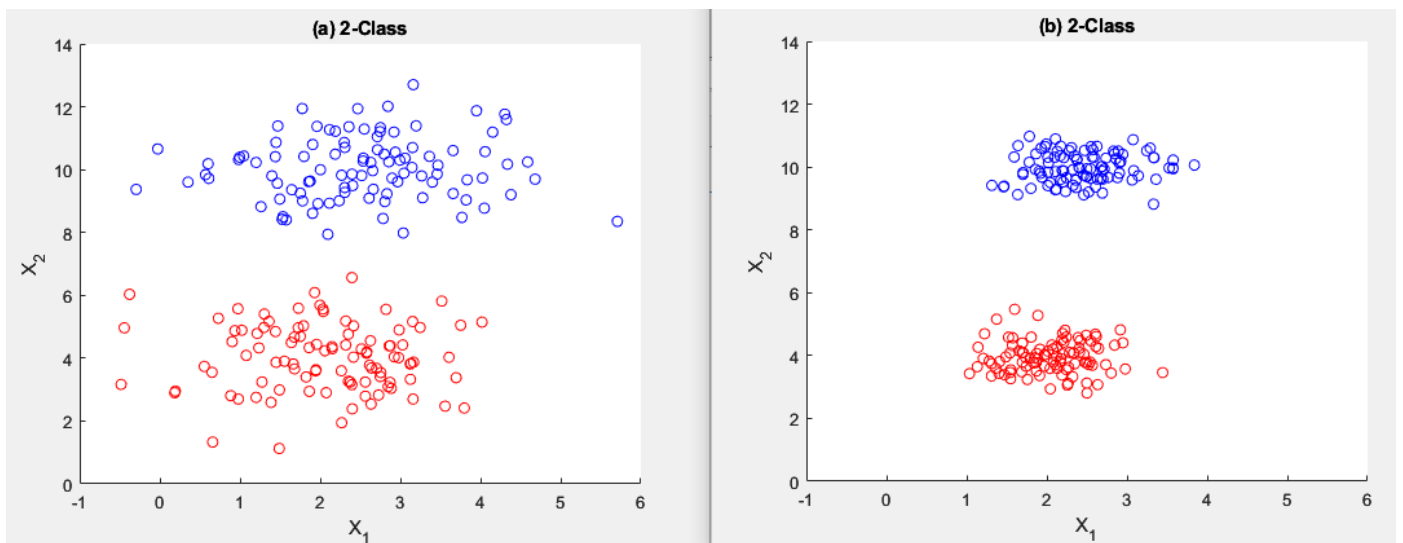
```
J3: 64.5006
```

Class a's within-class spread is small and between-class spread is large, so it has the largest value.

Class c's between-class spread is large, but within-class spread is larger than class a, so it has a smaller value.

Class b is the worst with large within-class spread and small between-class spread.

## 2. FDR



Results:

```
>> ex3_2
(a) :
FDR1: 0.0978121
FDR2: 1.78363
(b) :
FDR1: 0.29577
FDR2: 1.93878
```

Fisher's discriminant ratio is used to quantify the separability capabilities of individual features.

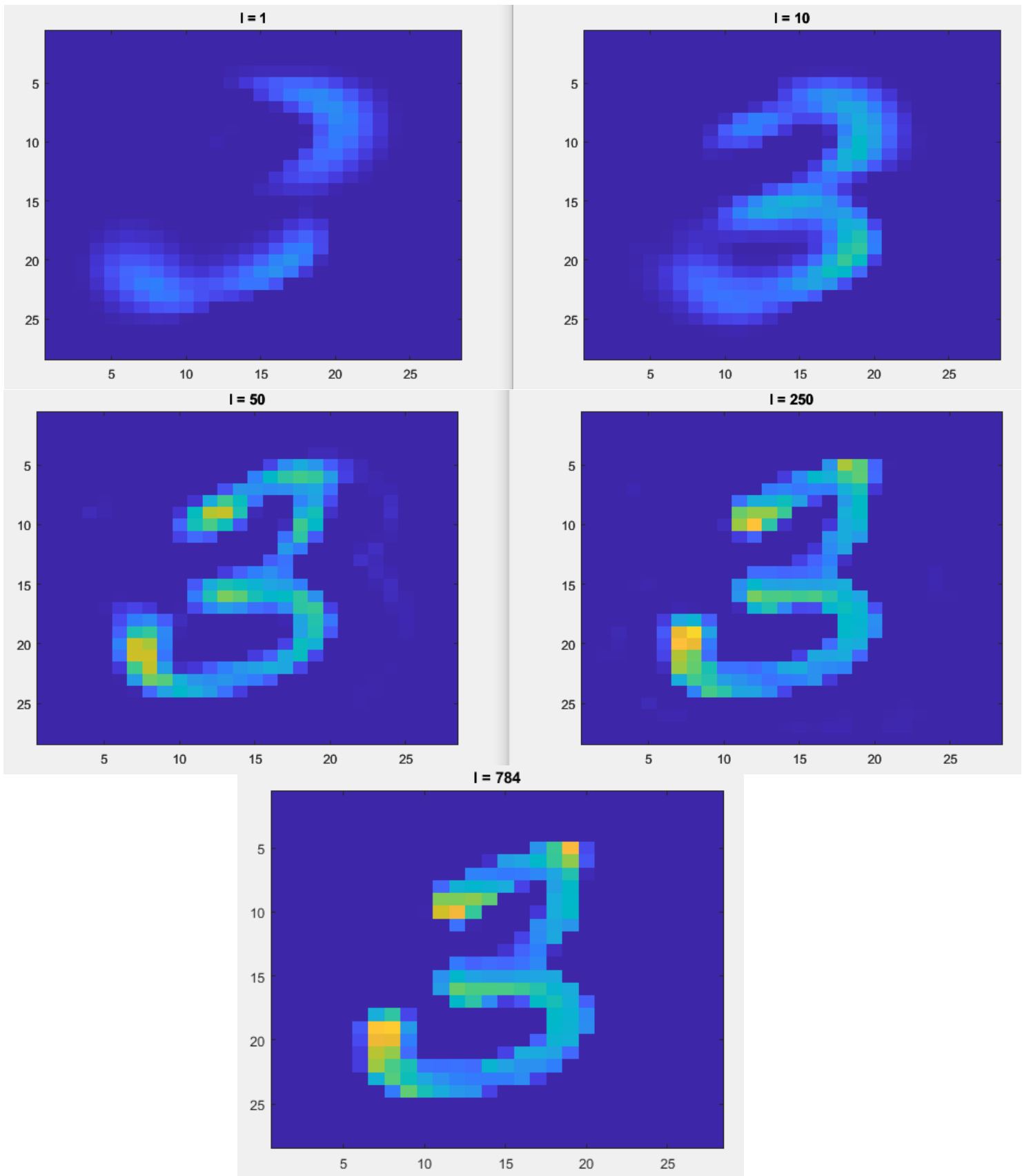
First, let's compare the features,  $X_1$  and  $X_2$ . The FDR of  $X_2$  is always larger than the FDR of  $X_1$ . In both classes, the distribution of  $X_2$  is much tighter than  $X_1$ , and it is obviously observed through above images.

Next, let's compare between two datasets. Both features got higher FDR score in the second dataset, which has a smaller covariance matrix. The distribution is obviously tighter than the first dataset's, and therefore easier to separate.

### 3. MNIST

When  $l=10$ , it is obvious already.

When  $l = 50$ , there's barely different from the origin image.



Result

```
>> ex3_3
N = 500, l = 1, MSE = 7477.673918
N = 500, l = 10, MSE = 2193.390327
N = 500, l = 50, MSE = 755.167479
N = 500, l = 250, MSE = 122.762091
N = 500, l = 784, MSE = 0.000000
N = 1000, l = 1, MSE = 7463.150634
N = 1000, l = 10, MSE = 2056.518439
N = 1000, l = 50, MSE = 677.292931
N = 1000, l = 250, MSE = 88.231810
N = 1000, l = 784, MSE = 0.000000
N = 1500, l = 1, MSE = 7514.999442
N = 1500, l = 10, MSE = 1949.039542
N = 1500, l = 50, MSE = 630.867404
N = 1500, l = 250, MSE = 70.498335
N = 1500, l = 784, MSE = 0.000000
N = 2000, l = 1, MSE = 7347.916712
N = 2000, l = 10, MSE = 1946.028734
N = 2000, l = 50, MSE = 628.985818
N = 2000, l = 250, MSE = 66.289092
N = 2000, l = 784, MSE = 0.000000
```

N:

As the training data (N) increases, the evaluation error decreases when  $L = 10, 50$  or  $250$ . N doesn't affect the result when  $L = 1$  or  $784$ , because  $L=1$  has little impact, and  $L=784$  is the origin image.

L:

As L increase, the loss significantly decreases when L is still low. There are great impact on the first few coefficients, and made the error decreased a lot.