

DECENTRALIZED REPUTATION MODEL AND GENERAL TRUST FRAMEWORK
BASED ON BLOCKCHAIN & SMARTCONTRACTS

Dissertation in partial fulfillment of the requirements for the degree of

MASTER PROGRAMME IN COMPUTER SCIENCE



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Abstract

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List of Abbreviations

1 Introduction

1.1 Definition

1.1.1 Trust and Reputation

Trust and Reputation encompass a broad spectrum of domains and is context dependent. Therefore, a universally agreed upon single definition doesn't exist. From a game theoretic sense, trust can be interpreted as a subjective probability, by which an individual, A, expects another individual, B, to perform a given action on which its welfare depends according to a previous agreement. [1] Reputation, on the other hand, is the perception of an individuals character or standing. Individuals in online systems are identified by their online identities which can be anything and not necessarily attached to real-world identities.[2] Online identities play a crucial role in digital interactions and require unknown entities to trust each other based on the reputation system of the platform in use.

1.1.2 Blockchain

Blockchain can be defined as a distributed record of state changes that let anybody on the network audit state changes and proves with mathematical certainty that the transactions transpired according to the blockchain rules. There exist several definitions of blockchain technology each specific to their closest use case. A formal standard definition of Blockchain is under development as ISO/TC 307.¹ Vitalik Buterin, the founder of Ethereum, puts it this way. "A blockchain is a magic computer that anyone can upload programs to and leave the programs to self-execute, where the current and all previous states of every program are always publicly visible, and which carries a very strong cryptoeconomically secured guarantee that programs running on the chain will continue to execute in exactly the way that the blockchain protocol specifies." This definition provides a broad overview of what blockchain does.² As a continually developing discipline, it needs to keep adapting to a new definition while maintaining the essence. This thesis will discuss the topic in more detail in the background section.

¹<https://www.iso.org/committee/6266604/x/catalogue/p/0/u/1/w/0/d/0>

²<https://blog.ethereum.org/2015/04/13/visions-part-1-the-value-of-blockchain-technology>

1.2 Motivation

Consider a simple scenario where Alice wants to buy a pair of headphones for which she browses a buy/sell platform. When she finds a relevant product on the platform published by Bob, unknown entity to Alice, she needs to rely on the ratings/feedback that Bob has received on the platform from his previous customers and also on the platform in use for not tampering with the data in any form. The entity claiming to be Bob could be Eve who found a way to bypass the platform's security and inflate his reputation on the system. Eve could delete the ad and associated account when the payment is complete, or she could gather Alice's personal details to misuse it later. Any malformed decision on the trustworthiness of an entity could be expensive and deal severe damage to the user. Thus, it is interesting to study about reputation model and methods to make it more reliable and accurate in its measure. Reputation model offers a way to measure the trustworthiness of entities to aid interacting users in making an informed decision about carrying forward the transaction or dropping it.

Studying interactions between entities and analyzing their behavior to generalize a trust framework is, therefore, a riveting problem. Graph theory and network flow algorithms have been researched in both centralized and decentralized environment before. This thesis proposes a blockchain based solution to record users behavior and compute a trust score for each of them.

1.3 Purpose and research questions

The main goal of this thesis is to use blockchain technology and smart contracts to simulate an endorsement network where entities can endorse each other based on physical or digital acquaintance. The endorsement values will be quantified to infer reputation score and a trust value that can be used on any transaction network. The nodes and their relationship will be studied to identify honest or malicious participants. Generalization of this endorsement network to serve other use cases will also be discussed. The research questions that this thesis aims to address are :

1. How can graph theories and relevant reputation algorithms be used to model the interaction between entities and detect/identify honest and malicious nodes in the network? How can the interaction graph be modeled?
2. What are the requirements for storing trust values and linking them to associated identities stored off a blockchain network? How can a blockchain application be built to define a general trust framework for a transactional network? How could the overall system architecture look like?
3. How can the discussed endorsement network ensure trustworthiness while also preserving users anonymity and how can it be generalized to other transactional

network or added on top of it to serve other use cases such as content filtering, E-Commerce etc?

1.4 Scope

This thesis work attempts to answer all the research questions mentioned in section 1.3.

To answer research question1, literature survey will be performed on existing reputation algorithms along with the presentation of background overview that will lead to graph simulation of endorsement network.

For research question2, interpretation and quantification of reputation scores and trust metrics will be manifested. Comparative analysis of on chain and off-chain storage requirements will be studied resulting in an overall design of endorsement system architecture.

For research question3, relevant use cases will be presented, and the network will be tested on with various predefined cases and attack models to see how well it behaves in a dynamic environment.

1.5 Structure of Report

1.5.1 acronyms

2 Literature Review

2.1 Existing Reputation Systems

2.2 Problems & Limitations

Existing reputation models aggregate feedbacks and evaluate actions and interactions of users and store them in a centralized database. i.e., A trusted node has the access control and rights to publish information to the network which implies that it could tamper with the data at will. The traditional client-server architecture is also susceptible to DDOS attack as the target is known and holds a single point of failure. Another challenge that is not limited to the centralized system is Sybil attack. In any digital platform that doesn't require one to reveal personally identifiable information, creating multiple pseudonymous identities to exploit the system is usually cheaper with nothing to lose. Sybil attack is one of the most significant challenges in a distributed computing environment. It is usually challenging to detect and has been mathematically proven to be impossible to prevent in a distributed environment.

2.2.1 Sybil Attack

Sybil attack is a widely used attack model in the peer-to-peer reputation system. Peers in the network create multiple pseudonymous identities with a purpose of inflating their reputation or damaging some other peers reputation. If a peer gets a bad reputation in the system for its activity or other reputation models defined parameters, then usually it is both cheaper and faster to create a new identity and start afresh then to try and recuperate the damaged reputation. As the network makes it so easy to create identities with nothing at stake, participants opt for it and exploit this feature to perform Sybil attack.

3 Background

3.1 Reputation algorithms

3.1.1 Graph properties

A graph, as the name suggests can be used to represent objects and their relationships graphically. A graph G is an ordered triple (V, E, φ_G) where V is a non empty set of vertices v , E is a non empty set of edges e that connects two vertices and $v \in V, e \in E$. φ_G is an incidence function that assigns pair of vertices to each edge of the graph G . $\varphi_G(e) = uv$ represents that e is an edge that joins vertices u and v . Graph properties can be leveraged to serve as an interaction graph of network for reputation system. Each node on the network, v can represent individuals and the edges that connect the nodes can represent the relationships between those nodes. The edge can have varying weights to represent the strength of relationship between the nodes. [3]

3.1.2 EigenTrust

EigenTrust is a reputation management algorithm for P2P network that aims to minimize malicious behaviour in the network and is based on the notion of transitive trust. i.e. If a peer i trusts a peer j then all other peers trusted by j is also trusted by i . In EigenTrust, global reputation of each peer i is given by local trust value assigned to peer i by other peers and is weighted by the global reputation of assigning peers. A local trust value s_{ij} is calculated by each peer i which represents the opinion i has of j . s_{ij} is the difference of satisfactory and unsatisfactory transactions peer i had with other peers j .

$$s_{ij} = \text{sat}(i, j) - \text{unsat}(i, j) \quad (3.1)$$

where $\text{sat}(i, j)$ represents number of satisfactory transactions that i had with j whereas $\text{unsat}(i, j)$ represents number of unsatisfactory transactions.

To prevent malicious peers from assigning arbitrarily high local trust values to other malicious peers, the local trust value is normalized as c_{ij} before aggregating them.

$$c_{ij} = \frac{\max(s_{ij}, 0)}{\sum_j \max(s_{ij}, 0)} \quad (3.2)$$

C_{ij} keeps changing depending on the good or bad interaction between peer i and peer j . Based on the local trust value assigned by other peers, each peer has a global trust value that determines their standing in the network. To aggregate the normalized local

trust values, the approach used is friend-friend reference where a peer i would ask its acquaintances about their opinion about other peers. Trust that peer i places in peer k by asking his friends can be denoted by t_{ik} as :

$$t_{ik} = \sum_j c_{ij} c_{jk} \quad (3.3)$$

Each peer asks other peers about their opinion which is weighted based on how much peer i trusts them. If we define C as a matrix $[c_{ij}]$ and t_i as a vector containing values t_{ik} , then $t_{ik} = C^T \vec{c}_i$. This helps a peer get a wider view of the network more than its own experience. This can continue for many nodes until peer i asks his friend's friend's and friend's friend can be consulted further to receive a broader view of the network. For n nodes, we can represent t as $t = (C^T)^n c_i$. For a large enough value of n , trust vector \vec{t}_i will converge to same vector for every peer i and could give complete view of the network. t is the global trust vector where t_j quantifies the trust system places in peer j . EigenTrust is robust to malicious peers and good for decreasing inauthentic file downloads in a P2P network. However, it doesn't address the issues such as inactive peers, where a peer doesn't download from anywhere else, malicious collectiveness, where malicious peers collude to inflate the trust value. It also doesn't have a way to calculate negative trust and is entirely based on user feedback. [4]

3.1.3 Net flow Rate convergence

Net flow rate convergence can help to determine anomaly in the network. By looking at how fast the net flow converges to zero, it can detect unusual behaviour in the network. The flow in a network can be measured by looking at inflow and outflow edges and calculating their differences. Inflow edges are all incoming edges in the graph and outflow edges are all outgoing edges. (diagram) Net flow convergence rate is the rate at which the net flow converges to the global net flow which is zero. Depending upon how fast the net flow in a graph converges to zero, it can be useful to detect anomaly.(example diagram)

3.2 Cryptography

3.2.1 Basic Concepts

Cryptography offers algorithms to achieve confidentiality, integrity, authenticity, and non-repudiation. Confidentiality and integrity ensure that the information being communicated is not disclosed or has been modified to or by any unauthorized parties. The data is hidden or encrypted such that only the authorized parties can make sense out of it, i.e. decrypt using the previously agreed upon key.

Asymmetric key cryptography makes use of key pairs, private key, known only to the owner and public key, that can be publicly distributed. It ensures authenticity, a proof

that sender is who he claims to be and non-repudiation, the sender cannot deny having sent the message. Public key verifies the holder of the private key and encryption of the message. That paired private key can only decrypt this encrypted message. One of the significant application of public key cryptography is Digital Signatures, described in more detail in section (Blockchain section ..) which is useful in preserving the properties of authenticity and non repudiation.

A cryptosystem can be seen as a five tuple (P, C, K, E, D) that satisfies the following conditions:

P is a finite set of plain texts.

C is a finite set of cipher texts.

K , the keyspace is a finite set of keys

E , set of encryption rules $e_k: P \Rightarrow C$

D , set of decryption rules $d_k: C \Rightarrow P$.

for each $k \in K$, there is $e_k \in E$ and $d_k \in D$ such that $d_k(e_k(m)) = m$ for every plaintext $m \in P$.

3.2.2 Hash functions

Cryptographic hash functions are a one-way function, also known as mathematical trapdoor function that transforms an input message into a fixed length binary output. It is one way because although converting a message input to a hash value or a message digest can be done in constant time, reversing the operation is practically impossible to achieve as its computationally inefficient. Earlier hash functions include MD5 which produces a 128-bit hash value but is vulnerable and can be cracked by brute force attack. The predecessors hash functions are sha-256 preceded by sha-1, sha-2 and others. Their applications include the digital signature, message authentication both of which are interesting for blockchain as will be discussed in section(name). The essential characteristics of hash functions are their deterministic output, meaning given a fixed input; it will always generate the same output. It offers collision resistant property, i.e. it is impossible or extremely rare to get the same hash value for two different messages. If m_1 and m_2 are the message and $h(m_1)$ and $h(m_2)$ are hash functions applied to them respectively, collision resistant ensures that $h(m_1) \neq h(m_2)$. Another important characteristic of a hash function is that the hash value does not indicate the original information that was hashed thus making it efficient for hiding information.

3.2.3 Digital Signature

A digital signature acts as an intermediary to prove that an entity A , has the password without ever requiring A to reveal it. To create a digital signature, one would need to apply signing algorithm to the private key along with the message. Likewise, anyone can verify the generated signature by applying it to a verification algorithm along with

the public key and the message. If a node A intends to send a transaction to B on a blockchain network, A needs to prove that he is the rightful owner of the public address from where the message originated. This is done by creating a digital signature using A's private key from the transaction message. Once the transaction is broadcasted, any node in the network can verify that signature corresponds with A's public key. The signature is dependent on the message, and thus any attempt by a malicious node on the network to modify the message will refute the signature.

3.3 Blockchain Technology

Blockchain, as the name suggests is a chain of blocks, where each block had the consensus of all the nodes on the network before being unlocked. A block consists of a list of transactions that a miner accumulated at a particular point in time. Blockchain shows the ordering of transactions in the network.

Block0 -> Block 1 -> Block 2 -> . . .
—————Time—————>

3.3.1 Evolution & Categories

Bitcoin was the first application that made use of Blockchain technology which was a peer-to-peer electronic cash system. The major contribution of this project was distributed trust at scale without using a trusted intermediary. Along the dimension of validation and access control, blockchain can be categorized as public permissionless, public permissioned, private permissioned.

While various use cases and diverse domains have shown an interest in the technology, it is crucial to make a distinction on when and for what purpose does it make more sense.

Hashgraph, which is a new project that claims to have solved the scalability issue of blockchain while maintaining security describes the different stages of evolution as:

Leader Based System

Proof-of-work blockchain

Economy based systems

Voting based systems

Hashgraph with virtual voting

3.3.2 Consensus algorithms

Consensus algorithm is the defining element in any blockchain network based on which all nodes agree about the transactions ordering and timestamps of all messages.

proof-of-work: This was the first consensus algorithm in use and has been proven to be

robust regarding security. However, it comes with a trade offs such as scalability.

proof-of-stake :

DAGs: Byzantine Fault Tolerance

3.3.3 Smart contracts

Smart Contracts

3.3.4 Applications

4 Methodology and Implementation

The problem of measuring the trustworthiness of communicating entities is an essential aspect of any online system where they interact with each other for any purpose, be it shopping, content delivery or file sharing. This chapter follows on a discussion of a proposed endorsement network where physically or digitally acquainted entities can endorse each other or their presented information. The model will address several concerns such as the roles and requirements of participants as endorser and endorsee, why a participant would play by the rule and what is to stop them from not doing so, threat models, etc. With a system of smart contracts, PoC design will confer interaction between entities, aggregation of information and assignment of scores for final computation. The storage of data both on and off-chain will be discussed.

4.1 Problem Statement

To be able to rely on the trustworthiness of an entity as presented by any online systems, the underlying reputation system needs to be robust and as transparent as possible. The assurance that available information has not been tampered with and correctness of claimed identity should be provided to sustain minimal risk of fraud. The immutable, trustless, decentralized and distributed attribute of blockchain protocol is a recommended solution on a public permissionless network.

4.2 User stories & Requirements

Anyone can join the network and become a participant in the endorsement system. The two notable roles of a user are endorser and endorsee. An endorser can initiate the transaction by sending an endorsement to the participant they trust which is accepted by the endorsee. The same user can assume both positions as long as a set of predefined requirements are met.

The system requirements can be listed in points as :

1. Allow anyone to join the network and become a member of endorsement system. Once registered, there must be a way for users to add profile information and view/edit them.

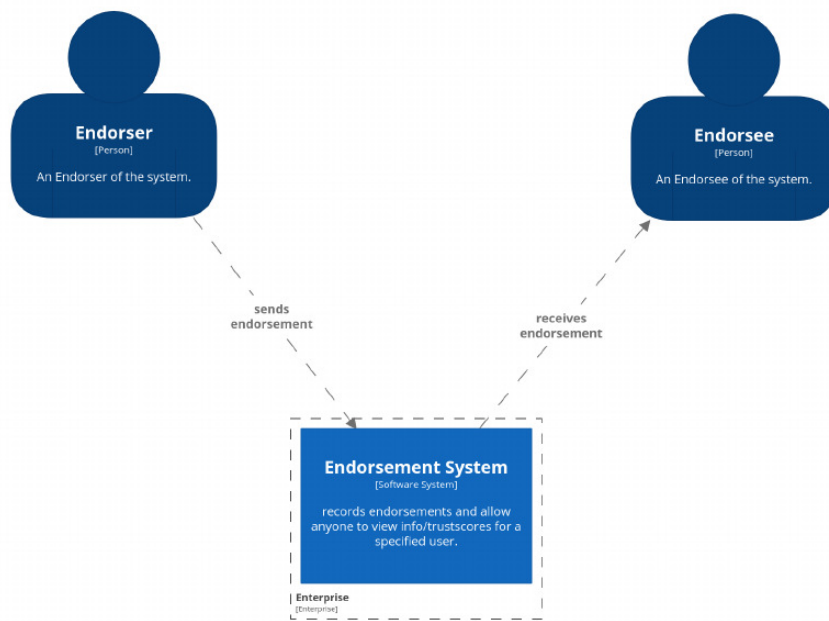


Figure 4.1: Context Layer

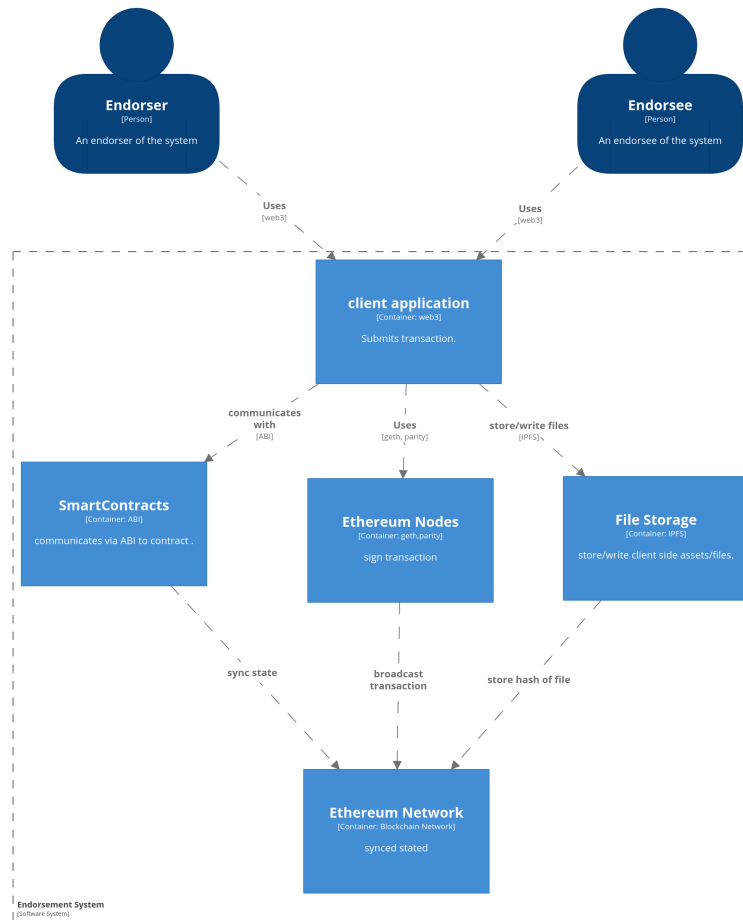
2. Any registered user must be allowed to send an endorsement which should be immediately transferred to the specified receiver's address. The endorser must securely sign this transaction in a way that identifies them such that any other participants in the network can verify it.
3. All the successfully recorded endorsements should have immutable traceability so that anyone can go back and verify the chain of ownership and order in a time when it took place. Each endorsement must have a mapping from endorser to endorsee to trace list of endorser for a given endorsee and vice-versa.
4. Allow the elimination/update of the relevant state variable if an endorser decides to take back the endorsement given in the past. This change should be evident on the network.
5. It must be possible for anyone within or outside the endorsement network to compute the total endorsement impact of any members.
6. The public key hashes of network participants must be linked to their respective final score(total endorsement impact). This score must be publicly visible to anyone while preserving the anonymity. i.e., no personally identifiable information is shared publicly.
7. Any form of an attempt to change the successfully recorded ledger should be evident on the network.

The functional requirement for each user types specifically are presented in the table(cite)

As an	I need to be able to..	Traceability
Endorser	send an endorsement to anyone I wish to as long as they are registered on the network so that it contributes to the positive impact on the system.	R2
	remove previously assigned endorsement so that my trust towards my endorsees can be reflected in real time.	R4
	view a list of endorsees so that i can see to whom i have sent endorsements.	R2 & R4
	view or edit my personal information so that i can keep it up to date	R1
Endorsee	view a list of endorsers so that I can see from whom I have received endorsements.	R2.1
	identify me in a cryptographically secure manner so that anyone can verify my claim of a score on the network before the transaction.	R3
	view or edit my profile information so that i can keep it up to date.	R1
anyone	compute the total endorsement impact(i.e., final computed score) of any registered participants on the network so that I can make an informed decision about the future transaction.	R5
	join the network so that I can start sending/receiving endorsements.	R1

The non-functional system requirements are :

- Security:
- Reliability:
- It must be possible for anyone within or outside the endorsement network to compute the total endorsement impact of any members.
- The public key hashes of network participants must be linked to their respective final score(total endorsement impact). This score must be publicly visible to anyone while preserving the anonymity. i.e., no personally identifiable information is shared publicly.
- Any form of an attempt to change the successfully recorded ledger should be evident on the network.
- Performance:



Container diagram for Endorsement System

The container diagram for the Endorsement System.
Last modified: Wednesday 02 May 2018 20:49 UTC

4.3 Component Diagram

d

4.4 The Model - Endorsement Network

The initial assumption is that all nodes are honest and as such receive equal points that they can spend at will once registered on the network. The received points are the consumable power that keeps depleting with every endorsement connection made along the way. As depicted in figure 4.2, these points follow a convergent sequence that converges to the limit 0 as the number of connection 'n' increases. As such, increasing the number of connection alone will not be enough to achieve a higher impact on the network.

Terminologies that will be used for this network are briefly described below :

nEG: The number of connection to whom a peer has given endorsement.

nER: The number of connection from whom a peer has received endorsement.

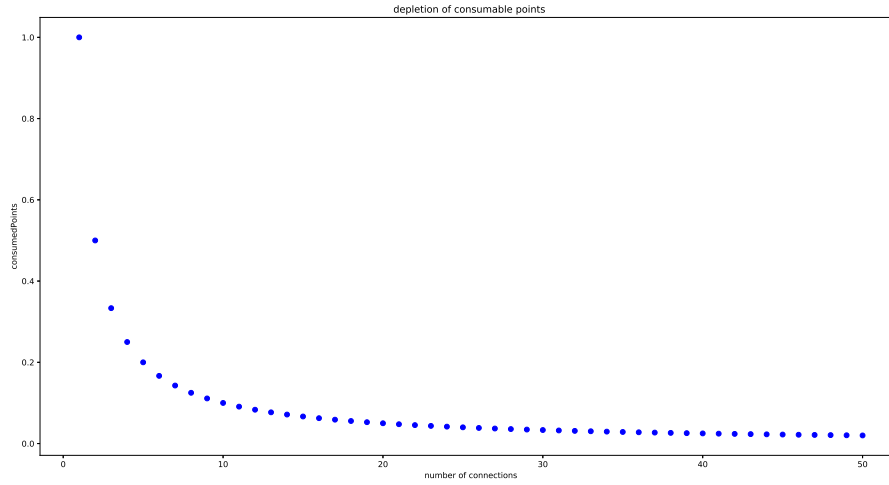


Figure 4.2: Convergent behaviour of consumable points as 'n' increases

Initial Endorsement Power (iep): This is the initial endorsement power granted by the network for being a participating node in the network. *itEndorsement power (ep)*: Endorsement power is measured by how much points has been given by the endorser which can be determined by the number of connections. If a peer i uses his iep to give to n number of peers, then the ep_i is $1/n$. For instance, if A endorses 20 acquaintances, then ep_a will be $1/20$, if A endorses 50 acquaintances, ep_a will be $1/50$ and so on.

Endorsement impact (ei): Endorsement impact is not only associated with how much endorsement an entity has given but also with how much it has received. The ratio of endorsement given (EG) and of endorsement received (ER) has to be taken into account to create a balance in the network for each nodes. Assume the EG:ER is x and y respectively, let total value of received endorsement be RE , the ei can be calculated as

$$ei = \frac{\min(x,y)}{\max(x,y)} * ep * RE \quad (4.1)$$

This is to ensure that EG and ER and not too far off from each other.

Received endorsement, RE is the total sum of all the endorsement received. If a peer receives endorsement from n peers, then the RE is given by:

$$RE = \sum_{i=0}^n ep_i \quad (4.2)$$

Total endorsement impact (tei): The total endorsement impact determines the impact a node has on the network. To get a value for this, we would simply have to multiply the ei

with the number of connections to which they have given endorsement. Assuming a peer i has given endorsement to n peers in the network, then the tei would be:

$$tei = ei * n \quad (4.3)$$

It shows how much impact they have made on the network. This value corresponds to the trust score and higher the score, higher is the trustworthiness of an entity.

4.5 Honest vs. Malicious Nodes

In endorsement network, honest nodes are assumed to endorse only the nodes on whom they have full confidence that they will perform the fair/legitimate action on the system. In other words, they are ready to take the risk if the identities they trusted performs malicious activity. It takes time to build a reputation and gain enough trust value and therefore giving it all up by endorsing malicious node would not be a rational decision. Another assumption is that an honest node will have a negligibly low difference between nEG and nER . On the other hand, a malicious node will have imbalanced ration between nEG and nER . Using the ratio of nEG and nER as one of the metrics may also alleviate the common free rider problem discussed earlier.

4.6 Trust Metrics

Every node keeps track of its neighbouring node and whenever an intera

4.7 Design of PoC

Any registered user can assume both the role of endorser and endorsee. An endorser, A must be able to join the network and start sending endorsement right away to existing participants in the network. The only requirement for an entity to send or receive endorsement is that they both must have joined the network before transacting. The maximum limit is set to 300 for a participant to send or receive an endorsement. Based on the definition of Dunbar's number, it is the cognitive limit to the number of people one can maintain the social relationship with. There is nothing to stop a participant from creating multiple identities and endorsing itself but doing so would require twice the time which when spent on receiving or sending honest endorsement can be worth much more. The initial points received keeps getting replenished until the number hits the maximum limit. The contract also allows for eliminating any endorsement previously assigned. Thus, even when a maximum limit is reached, users can still actively participate in the network. Other additional requirement includes, A node cannot self-endorse or endorse any node more than once.

4.8 Sequence Diagram

4.9 Smart contracts

The Endorsement contract handles the logic for sending and receiving endorsements.

4.10 Experimental Setup

4.11 second section

5 Results

5.1 Interaction graph

5.2 Analysis

5.3 Measurement

5.4 Comparison

6 Discussion & Analysis

6.1 Generalization

6.2 first section

The results presented in Chapter 4 are discussed and analyzed, including comments and reflections from the author. It may include the following: Comparison of obtained results with discussion, interpretation and evaluation of results. Results of analysis or modeling are described. Interpretations are drawn and connected to previous work

7 Conclusion

7.1 first section

7.1.1 first subsection

Synopsis of findings, limitations, further proposals for future work on the subject. Clear conclusions are drawn that stem from the previous analysis. Present the conclusions drawn and the evidence and arguments that support the conclusions.

Do not include new findings, but only refer to results already discussed in the thesis. Relevant further work in the field is summarized.

Literature

- [1] C. Castelfranchi and R. Falcone, "Trust and control: A dialectic link", *Applied Artificial Intelligence*, vol. 14, no. 8, pp. 799–823, 2000.
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