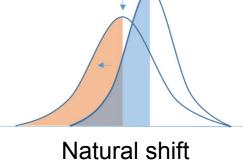
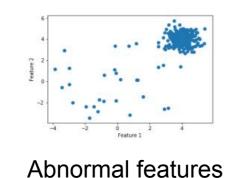
# Dynamic Uncertainty Minimization with Adaptive Batch Normalization Statistic (DUMBS)

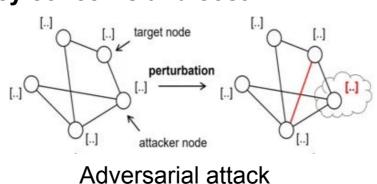
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#### **Abstract**

Graph neural networks (GNNs) demonstrate strong representation learning performance on training and testing data when both are drawn from the same distribution. However, their performance degrades significantly when there is a distribution shift between training and testing data, such as abnormal features and adversarial structure attacks. Traditional approaches suggest using labeled data from both the training and test-time distributions to address this issue. However, this is impractical in real-world scenarios due to privacy concerns and cost.







GTrans [4], the data-centric approach to adapt graph data at test time is proposed to improve performance under the domain shift. However, solely focusing on data adaptation without optimizing the modeling aspect and batch normalization statistic can lead to suboptimal results. Recognizing this opportunity, we propose a method named DUMBS: Dynamic Uncertainty Minimization with Adaptive Batch Normalization Statistic which concurrently minimizes the uncertainty of submodels generated from Monte Carlo dropout inference and optimizes batch normalization statistics during test time. This approach aims to fully leverage all available optimization parameters of the model to better mitigate the effects of domain shift and enhance overall adaptation performance. Remarkably, **DUMBS achieves better performance compare to baselines** as well as surpasses state-of-the-art method such as GTrans on the majority of dataset used.

Motivation Distribution Shift problem is solved by Test-Time Training! **Training Data Test Data** • Artificial Transformation **Validate** • Temporal Evolution Acc 97% **Cross-domain Transfers Test Acc 30%** Test **Trained Untrained** Model Test Acc 95% **Train Test** (Supervised) (Unsupervised) **Training Phase Testing Phase** 

## **Proposed Method DUMPS: Dynamic Uncertainty Minimization with Adaptive Batch Normalization Statistic Back-propagate to all sub-models** Filter out High **Entropy Trained** Model Mean + AdaBN Logit\_2 Logit **Calculate Entropy Loss** $H = -\sum p(x)\log p(x)$ Logit\_N

# **Setting and Dataset** Out-Of-Distribution (OOD) Setting for Node Classification Task **Dataset : Twitch-Explicit [9]** Dataset : Cora [7] Dataset : Elliptic [8] Bitcoin Transactions graph Mutual Friendship graph Citation Network from different regions evolves as time goes by Dataset: Amazon-photo [6] **Purchasing Network Cross-Domain Transfers Artificial Transformation Temporal Evolution**

# **Empirical Evaluation : Main Experiment**

DUMBS significantly outperforms all S.O.T.A. baselines in GCN

Backbone	Method		Average			
		Amz-Photo [6]	Cora [7]	Elliptic [8]	Twitch-E [9]	Average
GCN	ERM	93.79 (±0.97)	91.59 (±1.44)	50.90 (±1.51)	59.89 (±0.50)	74.04±(1.11
	DropEdge [1]	92.11 (±0.31)	81.01 (±1.33)	53.96 (±4.91)	59.95 (±0.39)	71.76±(1.74
	TENT [2]	94.03 (±1.07)	91.87 (±1.36)	51.71 (±2.00)	59.46 (±0.55)	74.27±(1.25
	EERM [3]	94.05 (±0.40)	87.21 (±0.53)	53.96 (±0.65)	59.85 (±0.85)	73.77±(0.61
	GTrans [4]	94.13 (±0.77)	94.66 (±0.63)	55.88 (±3.10)	60.42 (±0.86)	76.27±(1.34
	DUMPS (ours)	<b>96.18</b> (±0.27)	<b>98.31</b> (±0.21)	<b>62.20</b> (±1.17)	<b>60.45</b> (±0.39)	<b>79.29</b> ±(0.51

# **Empirical Evaluation: Additional Experiment**

Robustness of DUMBS is generalized to SAGE and GAT architecture!

Backbone	Method		Average			
		Amz-Photo [6]	Cora [7]	Elliptic [8]	Twitch-E [9]	Average
GCN	ERM	93.79 (±0.97)	91.59 (±1.44)	50.90 (±1.51)	59.89 (±0.50)	74.04 (±1.11)
	DropEdge [1]	92.11 (±0.31)	81.01 (±1.33)	53.96 (±4.91)	59.95 (±0.39)	71.76 (±1.74)
	TENT [2]	94.03 (±1.07)	91.87 (±1.36)	51.71 (±2.00)	59.46 (±0.55)	74.27 (±1.25)
	EERM [3]	94.05 (±0.40)	87.21 (±0.53)	53.96 (±0.65)	59.85 (±0.85)	73.77 (±0.61)
	GTrans [4]	94.13 (±0.77)	94.66 (±0.63)	55.88 (±3.10)	60.42 (±0.86)	76.27 (±1.34)
	<b>DUMPS</b> (ours)	<b>96.18</b> (±0.27)	<b>98.31</b> (±0.21)	<b>62.20</b> (±1.17)	<b>60.45</b> (±0.39)	<b>79.29</b> (±0.51)
SAGE	ERM	95.09 (±0.60)	99.67 (±0.14)	56.12 (±4.47)	62.06 (±0.09)	78.24 (±1.33)
	DropEdge [1]	92.61 (±0.56)	95.85 (±0.30)	52.38 (±3.11)	62.14 (±0.12)	75.75 (±1.02)
	TENT [2]	95.72 (±0.43)	99.80 (±0.10)	55.89 (±4.87)	62.09 (±0.09)	78.38 (±1.37)
	EERM [3]	95.57 (±0.13)	98.77 (±0.14)	58.20 (±3.55)	62.11 (±0.12)	78.66 (±0.99)
	GTrans [4]	96.91 (±0.68)	99.45 (±0.13)	60.81 (±5.19)	62.15 (±0.13)	79.83 (±1.53)
	<b>DUMPS</b> (ours)	<b>99.33</b> (±0.25)	<b>99.99</b> (±0.02)	<b>62.48</b> (±5.07)	<b>62.41</b> (±0.14)	<b>81.05</b> (±1.37)
GAT	ERM	96.30 (±0.79)	94.81 (±1.44)	65.36 (±2.70)	58.53 (±1.00)	78.75 (±1.48)
	DropEdge [1]	90.70 (±0.29)	76.91 (±1.55)	63.78 (±2.39)	58.89 (±1.01)	72.57 (±1.31)
	TENT [2]	95.99 (±0.46)	95.91 (±1.14)	66.07 (±1.66)	58.33 (±1.18)	79.08 (±1.11)
	EERM [3]	95.57 (±1.32)	85.00 (±0.96)	58.14 (±4.71)	<b>59.84</b> (±0.71)	74.64 (±1.93)
	GTrans [4]	96.67 (±0.74)	96.37 (±1.00)	<b>66.43</b> (±2.57)	58.59 (±1.07)	79.52 (±1.35)
	<b>DUMPS</b> (ours)	<b>98.10</b> (±0.74)	<b>99.72</b> (±0.12)	62.15 (±1.15)	58.42 (±1.40)	<b>79.60</b> (±0.85)

## **Ablation Study**

Ablation Study to show impacts of different components of DUMPS

Backbone	Components		Avorago			
		Amz-Photo [6]	Cora [7]	Elliptic [8]	Twitch-E [9]	Average
GCN	No Adapt	93.79 (±0.97)	91.59 (±1.44)	50.90 (±1.51)	59.89 (±0.50)	74.04 (±1.11)
	AdaBN	95.98 (±0.14)	94.15 (±0.51)	56.42 (±1.21)	58.91 (±0.55)	76.37 (±0.60)
	AdaBN + MC	96.05 (±0.23)	97.14 (±0.12)	60.19 (±1.14)	60.23 (±0.21)	78.40 (±0.43)
	AdaBN + MC + EntThreshold	<b>96.18</b> (±0.27)	<b>98.31</b> (±0.21)	<b>62.20</b> (±1.17)	<b>60.45</b> (±0.39)	<b>79.29</b> (±0.51)

## **Conclusion & Reference**

### Conclusion

GNNs tend to yield unsatisfying performance when the presented data is sub-optimal. While approaches like GTrans [4] that focus on data adaptation at test time can lead to a better performance on distribution shift data, solely prioritizing this aspect can lead to sub-optimal outcomes. To address this, we propose **DUMBS: Dynamic Uncertainty** Minimization with Adaptive Batch Normalization Statistic that concurrently minimizes the uncertainty of submodels generated from Monte Carlo dropout inference and optimizes batch normalization statistics during test time. Experimental results on out-of-distribution (OOD) dataset for node classification task have demonstrated the effectiveness of our method. DUMBS outperforming various state-of-the-art method in GCN baseline as well as achieving generalization in SAGE and GAT architecture.

#### Reference

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