

## Principles of Machine Learning: Exercise 2

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## Task 2.1.1-2 :: Loading

Instead of removing the outliers, its easier to keep the inliers:

```
inliers = w > 0
X = np.stack([h[inliers], w[inliers]])
# X.shape = [2, 37] = [F, N]
```

Maximum Likelihood Estimation of a Gaussian via empirical mean and covariance:

```
μ = np.mean(X, axis=1, keepdims=True)
# μ = [[175.729], [73.865]]
S = np.cov(X - μ, ddof=1) # ddof = degree of freedom = scales with 1/(n-1)
# S == (1 / (N-1)) * (X - μ) @ (X - μ).T
# S == [[ 75.925,  64.546 ],
#        [ 64.546, 186.953]]
```

## Task 2.1.3 :: Predictions

Conditional Probability of a Gaussian:

```
for h in np.arange(140, 220, step=10):  
    pw = p[1] + S[1, 0] * S[0, 0]**(-1) * (h - p[0])  
    Sw = S[1, 1] - S[1, 0] * S[0, 0]**(-1) * S[0, 1]
```

	Height	Weight	Covariance
0	140	43.490072	132.081358
1	150	51.991338	132.081358
2	160	60.492604	132.081358
3	170	68.993869	132.081358
4	180	77.495135	132.081358
5	190	85.996401	132.081358
6	200	94.497666	132.081358
7	210	102.998932	132.081358

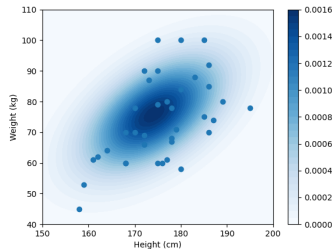


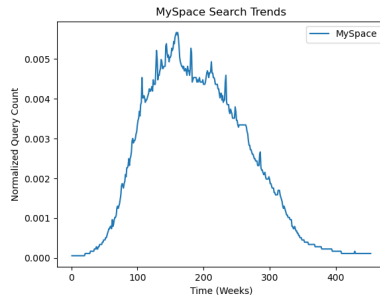
Figure: Estimated PDF and given data

## Task 2.1.3 :: Pondering

- + Results seem plausible – mostly so around the mean
  - Fixed variance doesn't match expectations (taller people → more variance)
  - Cube-Square-Law / BMI suggests a non-linear / quadratic relationship?
- Plausibility? Test-Set!

## Task 2.2.1 :: Loading

```
import pandas as pd
# Loading data as pandas Dataframe
df = pd.read_csv("myspace.csv",
                 header=None,
                 names=["Week", "Accesses"])
# Filter leading zeros only with cumulative sum
df = df[np.cumsum(df.Accesses) > 0]
h = np.array(df.Accesses, dtype=float)
t = np.arange(1, len(h)+1, dtype=float)
```

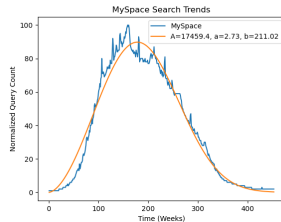


## Task 2.2.1 :: ManuDiff Newton

## Task 2.3 :: Scipy CurveFit

```
def weibull(t, A, alpha, beta):  
    ab, tb = alpha / beta, t / beta  
    return A * ab * tb**(alpha - 1) * np.exp(-tb**alpha)  
(A, alpha, beta), _ = curve_fit(weibull, t, h, p0=[1000, 1.0, 1.0])
```

● ...



## Task 2.4



## Task 2.5 :: Scipy Minimize

```
def KL(f, q): return np.sum(f * np.log(f / q))

def objective(x):
    return KL(weibull(t, alpha=x[0], beta=x[1]), q)
result = minimize(objective, x0=[1.0, 100.], bounds=[(0, 10), (0, 500)])
```

- Bounds are important, but also not:  $[-\infty, \infty]$  also works
  - Feels odd anyway, because gradient methods optimizing  $1 \rightarrow 2.8$  shouldn't come near 0 anyway
- ⇒ Bounds just change the optimizer underneath
- Without bounds 'BFGS' is chosen and doesn't quite work
  - 'L-BFGS-B' or 'SLSQP' without bounds works equally

