Package 'dualtrees'

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License	What license is it under?				
Depend	R = 3.5.0				
Descrip	tion What the package does (one paragraph).				
Version	0.0.1				
Title Decimated and Undecimated 2D complex dual-tree wavelet transform					

Description

Matrices supposedly needed in order to eliminate the effect of "spectral leakage" for the local dtcwt-spectra. Used by biascor(\dots).

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Usage

```
A_b_bp
```

 A_b

Format

A list with entries N512, N256, N128, N64, N32, each containing the bias correction matrix of appropriate size

Source

Calculated by hand via /user/s6sebusc/wavelets_verification/general_scripts/Amats_cdtwt.r

Examples

```
image( A_b_bp$N512 )
```

biascor

spectral bias correction, implemented in FORTRAN

Description

Unfold scale and direction into a vector and multiply by A at each grid point

Usage

```
biascor(en, a)
```

Arguments

en J x nx x ny x 6 array of squared wavelet coefficients

a bias correction matrix

Value

an array of the same dimensions as en

Note

this step can introduce negative values into the spctrum which have no intuitive interpretation in terms of energy and need to be dealt with.

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blossom

Two meteorologists in front of cherry blossoms

Description

A very beautiful image.

Usage

blossom

Format

A 512x512 matrix of gray-scale values

Source

real life

Examples

```
image(blossom, col=gray.colors(32,0,1))
```

boundaries

Various boundary conditions for the 2D wavelet transform.

Description

Various boundary conditions for the 2D wavelet transform.

Usage

```
pad(x, N, Ny = N, value = min(x, na.rm = TRUE))
put_in_mirror(x, N, Ny = N)
period_bc(x, N, Ny = N)
```

Arguments

x a real matrix

N the number of rows of the desired output

Ny the number of columns of the desired output, defaults to N

value the value with which the picture is padded by pad

Details

pad pads the fields with a constant value on all sides, be careful what you pick here. put_in_mirror reflects the input at all edges (with repeated end samples), period_bc simply repeats the input periodically. In any case, you can retrieve the initial area via bc\$res[bc\$px, bc\$py].

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Value

```
an object of class bc_field
```

Examples

```
bc <- pad( boys, N=300 )
image( bc$res, col=grey.colors(32) )
print( range( bc$res[ bc$px, bc$py ] - boys ) )</pre>
```

boys

Two stromchasers in the sun

Description

Another classic image.

Usage

boys

Format

A 256x256 matrix of gray-scale values

Source

real life

Examples

```
image(boys, col=gray.colors(32,0,1))
```

cen2uv

centre to vector

Description

transforms the angle and radius component of the spectral centre into vector components for visualization

Usage

```
cen2uv(cen)
```

Arguments

cen

an nx x ny x 3 array, the output of dt2cen

dt2cen 5

Details

The resulting vector field represents the degree of anisotropy and dominant direction, averaged over all scales. In principle, large and small edges might compensate one another, but the result typically looks as one would intuitively expect.

Value

an nx x ny x 2 array, the two matrices representing the u- and v-component of the vector field.

See Also

```
dt2cen, uvplot
```

Examples

```
dt <- fld2dt(blossom)
ce <- dt2cen(dt)
uv <- cen2uv(ce)
uvplot( uv, z=blossom )</pre>
```

dt2cen

centre of the DT-spectrum

Description

calculate the centre of mass of the local spectra in hexagonal geometry

Usage

```
dt2cen(pyr)
```

Arguments

pyr

a J x nx x ny x 6 array of spectral energies, the output of fld2dt

Details

Each of the J x 6 spectral values is assigned a coordinate in 3D space with $x(d,j)=\cos(60*(d-1))$, $y(d,j)=\sin(60*(d-1)),z(d,j)=j+1$. Then the centre of mass in this space is calculated, the spectral values being the masses at each vertex. The x- and y-coordinate are then transform into a radius rho=sqrt(x^2+y^2) and and angle phi=15+0.5*atan2(y,x). rho measures the degree of anisotropy at each pixel, phi the orientation of edges in the image, and the third coordinate, z, the central scale.

Value

a nx x ny x 3 array where the third dimension denotes degree of anisotropy, angle and central scale, respectively.

Note

Since the centre of mass is not defined for negative mass, any values below zero are removed at this point.

6 dtcwt

Examples

```
dt <- fld2dt(blossom)
ce <- dt2cen(dt)
image( ce[,,3], col=gray.colors(32, 0, 1) )</pre>
```

dtcwt

The 2D forward dualtree complex wavelet transform

Description

This function performs the dualtree complex wavelet analysis, either with or withour decimation

Usage

```
dtcwt(mat, fb1 = near_sym_b, fb2 = qshift_b, J = NULL, dec = TRUE,
  mode = NULL, verbose = TRUE, boundaries = "periodic")
```

Arguments

mat	the real matrix we wish to transform
fb1	A list of analysis filter coefficients for the first level. Currently only near_sym_b and near_sym_b_bp are implemented
fb2	A list of analysis filter coefficients for all following levels. Currently only qshift_b and qshift_b_bp are implemented
J	number of levels for the decomposition. Defaults to log2($min(Nx,Ny)$) in the decimated case and log2($min(Nx,Ny)$) - 3 otherwise
dec	whether or not the decimated transform is desired
mode	how to perform the convolutions, either "direct" (default if $dec=TRUE$) or "FFT" (default if $dec=FALSE$)
verbose	if TRUE, the function tells you which level it is working on
boundaries	how to handle the internal boundary conditions of the convolutions, has no effect if mode="direct"

Details

This is the 2D complex dualtree wavelet transform as described by Selesnick et al 2005. It consists of four discerete wavelet transform trees, generated from two filter banks a and b by applying one set of filters to the rows and the same ot the other to the columns. In the decimated case (dec=TRUE), each convolution is followed by a downsampling, meaining that the size of the six coefficient fields is cut in half at each level. In this case, it is supposedly efficient to use direct convolutions (mode="direct"), the boundary conditions of which are steered by the boundaries-argument. If dec=FALSE, direct convolutions may be slow and you should use mode="FFT". In that case, you need to handle the boundary conditions externally (enter a nice 2^N x 2^M matrix) and the maximum level J is smaller than log2(N) due to the construction of the filters via an 'algorithme a trous'.

Value

if dec=TRUE a list of complex coefficient fields, otherwise a complex J * Nx * Ny * 6 array.

filterbanks 7

Note

Periodic and reflective boundaries are both implemented for the decimated case, but only the periodic boundaries are actually invertible at this point.

References

Selesnick, I.W., R.G. Baraniuk, and N.C. Kingsbury. "The Dual-Tree Complex Wavelet Transform." IEEE Signal Processing Magazine 22, no. 6 (November 2005): 123–51. https://doi.org/10.1109/MSP.2005.1550194.

See Also

idtcwt

Examples

```
dt <- dtcwt( boys )
par( mfrow=c(2,3), mar=rep(2,4) )
for( j in 1:6 ){
   image( boys, col=grey.colors(32,0,1) )
   contour( Mod( dt[[3]][ ,,j ] )**2, add=TRUE, col="green" )
}</pre>
```

filterbanks

filterbanks for the dtcwt

Description

Some of the filters implemented in the python package dtcwt.

Usage

```
qshift_b
qshift_b_bp
near_sym_b
near_sym_b_bp
```

Format

A list of high- and low-pass filters for analysis and synthesis

Details

The near-sym filterbanks are biorthogonal wavelets used for the first level, they have 13 and 19 taps. The qshift filterbanks, each with 14 taps, are suitable for all higher levels of the dtcwt, as the a- and b-filters for an approximate Hilbert-pair. The naming convention follows the python-package:

```
h: analysis
g: synthesis
```

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0: low-pass1: high-passa,b: shifted filters

The b_bp-versions of the filterbanks contain a second high-pass for the diagonal directions, denoted by 2.

Source

dtcwt python package

fld2dt

transform a field into an array of spectral energies

Description

Handles the transformation itself, boundary conditions and bias correction and returns the unbiased local wavelet spectrum at each grid-point.

Usage

```
fld2dt(fld, Nx = NULL, Ny = NULL, J = NULL, mode = NULL,
  correct = NULL, verbose = FALSE, boundary = "pad",
  fb1 = near_sym_b_bp, fb2 = qshift_b_bp)
```

Arguments

fld	a real matrix
Nx	size to which the field is padded in x-direction
Ny	size to which the field is padded in y-direction
J	number of levels for the decomposition
mode	how to handle the convolutions
correct	how to correct the bias, either "fast", "b" or "b_bp" - any other value results in no correction
verbose	whether or not you want the transform to talk to you
boundary	how to handle the boundary conditions, either "pad", "mirror" or "periodic"
fb1	filter bank for level 1
fb2	filter bank for all further levels

Details

The input is blown up to $Nx \times Ny$ and the thrown into dtcwt. Then the original domain is cut out, the coefficients are squared and the bias is corrected.

Value

```
an array of size J x nx x ny x 6 where dim(fld)=c(nx,ny)
```

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See Also

biascor

Examples

```
dt <- fld2dt( boys )</pre>
par( mfrow=c(2,2), mar=rep(2,4) )
for( j in 1:4 ){
    image( boys, col=gray.colors(128, 0,1), xaxt="n", yaxt="n" )
    for(d in 1:6) contour( dt[j,,,d], levels=quantile(dt[,,,], .995),
                            col=d+1, add=TRUE, lwd=2, drawlabels=FALSE )
    title( main=paste0("j=",j) )
}
x0 <- seq(.1,.5,,6)
y0 <- rep(0.01,6)
   <- .075
phi <- seq( 15,,30,6 )*pi/180
x1 <- x0 + a*cos(phi)
y1 <- y0 + a*sin( phi )
rect( min(x0,x1)-.05, min(y0,y1)-.05,
      \max(x0,x1)+.05, \max(y0,y1), col="black", border=NA)
arrows( x0, y0, x1, y1, length=.05, col=2:7, lwd=2, code=3 )
```

get_en

get energy from the dualtree transform

Description

square the wavelet coefficients and apply some form of correction

Usage

```
get_en(pyr, correct = "fast")
```

Arguments

```
pyr array of J x nx x ny x 6 complex wavelet coefficients, output of dtcwt(..., dec=FALSE) correct type of correction, either "b", "b_bp" or "fast"
```

Details

The bias correction matrix should correspond to the filter bank used in the transform. It is computed by brute force for the so-called auto-correlation wavelets, for more details, see Nelson et al 2017 and Eckley et al 2010.

Value

an array of the same dimensions as pyr

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References

Eckley, Idris A., Guy P. Nason, and Robert L. Treloar. "Locally Stationary Wavelet Fields with Application to the Modelling and Analysis of Image Texture: Modelling and Analysis of Image Texture." Journal of the Royal Statistical Society: Series C (Applied Statistics), June 21, 2010, no-no. https://doi.org/10.1111/j.1467-9876.2009.00721.x.

Nelson, J. D. B., A. J. Gibberd, C. Nafornita, and N. Kingsbury. "The Locally Stationary Dual-Tree Complex Wavelet Model." Statistics and Computing 28, no. 6 (November 2018): 1139–54. https://doi.org/10.1007/s11222-017-9784-0.

See Also

Α

idtcwt

The 2D inverse dualtree complex wavelet transform

Description

Reconstructs an image from the pyramid of complex directional wavelet coefficients.

Usage

```
idtcwt(pyr, fb1 = near_sym_b, fb2 = qshift_b, verbose = TRUE,
boundaries = "periodic")
```

Arguments

pyr	a list containing arrays of complex coefficients for each level of the decomposition, produced by dtcwt(\dots , dec=TRUE).
fb1	the filter bank for the first level
fb2	the filter bank for all following levels

verbose if true, the function will say a few words while doing its thing.

boundaries how to handle the boundary conditions, should be the same as for the decompo-

sition.

Details

This function re-arranges the six complex daughter coefficients back into the four trees, convolves them with the synthesis wavelets and adds everything up to recover an image. For the near_sym_b and qshift_b filter banks, this reconstruction should be basically perfect. In the case of the the b_bp filters, non-negligible artifacts appear near +-45° edges.

Value

```
a real array of size 2N \times 2M where dim(pyr[[1]]) = (M,N,6).
```

Note

```
At present, only boundaries="periodic" actually works :(
```

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References

Selesnick, I.W., R.G. Baraniuk, and N.C. Kingsbury. "The Dual-Tree Complex Wavelet Transform." IEEE Signal Processing Magazine 22, no. 6 (November 2005): 123–51. https://doi.org/10.1109/MSP.2005.1550194.

See Also

dtcwt

Examples

```
py <- dtcwt( boys )
boys_i <- idtcwt( py )
image( boys - boys_i )</pre>
```

my_conv

Column-convolutions

Description

This function convolves the columns of a matrix mat with a filter fil.

Usage

```
my_conv(mat, fil, dec = TRUE, mode = "direct", odd = FALSE,
boundaries = "periodic")
```

Arguments

mat	a matrix
fil	the filter to convolve the columns with
dec	if TRUE, every second row is discarded after the convolution
mode	how to actually do the convolutions, must be either "direct" or "FFT" $$
odd	if TRUE, the first row is discarded, otherwise the second row is.
how	to handle the boundaries, does nothing if mode="FFT"

Details

This functions does all of the actual computations inside the wavelet transform. The direct mode uses filter(...) and can handle any field size you like. It is supposedly faster when the filters are short, i.e., in the decimated case. The FFT-version really only works when the input dimensions are whole powers of two and the filter is not longer than the columns of the matrix.

Value

a matrix with as many columns and either the same (dec=FALSE) or half (dec=TRUE) the number of rows as mat

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Examples

```
\label{local-conv} $$ dboysdy <- my\_conv( boys, c(-1,1), dec=FALSE ) $$ dboysdx <- t( my\_conv( t(boys), c(-1,1), dec=FALSE ) ) $$ par( mfrow=c(1,2) ) $$ image( dboysdx, col=gray.colors(32) ) $$ image( dboysdy, col=gray.colors(32) ) $$
```

uvplot

plot centre as vectors

Description

display the radial and angular component of the spectrum's centre as arrows.

Usage

```
uvplot(uv, z = NULL, col = "green", zcol = gray.colors(32, 0, 1), n = 42, f = 1, code = 0, length = 0.05)
```

Arguments

uv	array of dimension $\ \ nx\ x\ ny\ x\ 2$, containing the u- and v-component, result of cen2uv
z	image to show in the background, defaults to the absolute velocity
col	color of the arrows
zcol	color scale for the image
n	number of arrows in one direction
f	factor by which to enlarge the arrows
code	determines the type of arrow, passed to arrows()
length	length of the arrowhead in inches, does nothing if code=0

Details

The pivot of the arrows is at the location to which the u- and v-component belong. By default, no arrowhead is displayed (code=0) since the egdges deteted by the cdtwt have an orientation but no sign (SW and NE are equivalent). The default size of the arrows is such that a 'velocity' of 1 corresponds to 5

See Also

cen2uv

Examples

```
uv <- cen2uv( dt2cen( fld2dt( boys ) ) )
uvplot( uv, z=boys )</pre>
```

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