Networks of Violence and Civilian Targeting During Civil Conflict

Abstract

Increasingly, scholarship demonstrates that armed groups' decision to kill civilians is a political, strategic choice. Most examinations of this choice assume a simple environment where the main conflict is between a government and a unified opposition. Yet, we know that civil conflicts are more complicated than this and often involve three or more actors. Using an innovative computational model, we investigate the strategic incentives for victimization in a complex multi-actor conflict environment that incorporates civilian behavior. We find that more dense strategic environments – where conflict between any two actors is more likely – lead to higher rates of civilian victimization, irrespective of the overall intensity of conflict. We test this hypothesis in multi-actor civil conflicts using ACLED to generate measures of both conflict intensity and network density. Empirical analysis supports our model's finding that more dense strategic environments are associated with a higher level of violence against the civilian population.

Introduction

Why do armed groups victimize civilians during civil conflicts? For years, political scientists considered the violent targeting of unarmed civilians "irrational, random, or the result of hatreds between ethnic groups." (Valentino, 2014, see summary on p. 91). More recently, however, a consistent body of research shows that violence against civilians is in fact a highly rational and well-coordinated strategy used by armed groups to gain resources, territory, or to achieve broad military and political goals (Condra and Shapiro, 2012; Berman and Matanock, 2015; Stanton, 2016). Under many of these strategic frameworks, information and competition plays a critical role in armed groups' choice to victimize. Groups who target civilians are disadvantaged because civilian targeting produces incentives for civilians to share information with a group's rivals. Consequently, armed groups must weigh the potential costs of targeting civilians, such as losing supporters and control of information, against the so-called benefits, such as punishing rival constituencies and gaining territory.

Despite the meaningful implications of this strategic framework for both policy-makers and civilian populations, prior approaches predominantly rest on the assumption that civil wars and intrastate conflicts are defined by violence between governments and a unified opposition, even with recent calls for more disaggregated research (Raleigh, 2012). An increase in empirical event data on intrastate conflicts over time now confirm what policy experts and qualitative analysts have often reported, that conflicts are typically not dyadic in nature Dowd (2015). Instead, conflicts are driven by the intense fragmentation and competiton across multiple warring parties (Christia, 2012). In Nigeria, multiple armed groups proliferate in the southern Niger Delta region alone, competing over oil resources and interethnic rivalries (Obi, 2009). The northeast region of Nigeria is shaped by Boko Haram's insurgent violence, which by 2013 had led to the

development of both government tasks forces and local vigilante groups fighting for territory (Mustapha, 2014). In the Democratic Republic of Congo, where conflict dynamics have taken a toll on civilian life, event data reports at least 20 armed actors in 2001 and upwards of over 50 ten years later, by 2011.¹

To further illustrate this point, we show the number of active armed groups per country case for each year of the ACLED data in Figure 1. The data clearly show that the majority of intrastate conflicts² are much more complex than a war between the government and a single mobilized armed challenger. The data also reveal that highly complex conflicts where a country has 10 or more active armed groups in a given year are on the rise in recent years. ³

¹According to ACLED. For a deeper understanding of dominant conflict narratives and summaries of the DRC case see (Autesserre, 2012).

²We broadly define 'intrastate conflict' as violence by organized political groups within the borders of a state.

³In this graph, we make a few important decisions that necessarily decrease the reported number of total actors over time. We consolidate government actors into one group, such as different branches of the military, and we remove actors with vague name labels such as 'unidentified' or 'opposition' group labels.

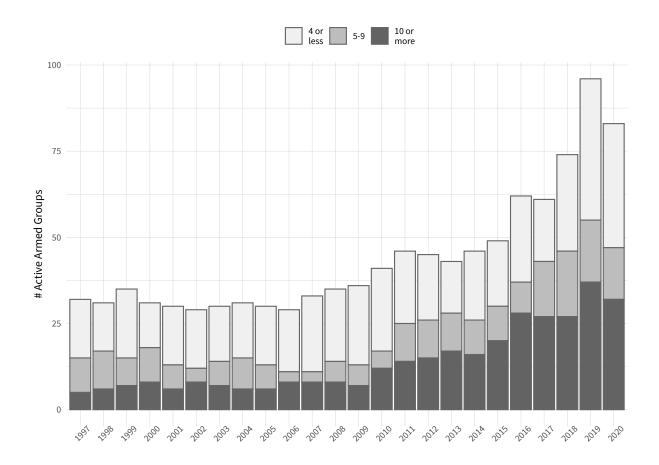


Figure 1: Number of total active armed groups in each country case across conflicts in ACLED from 1997 to 2020. Dark grey represents armed conflicts with 1-4 active armed groups, light grey represents armed conflicts with 5-9 active armed groups, and white represents armed conflicts with 10 or more armed groups.

How does such complexity effect civilian welfare? To understand the risk to civilian life during the course of war, we need to better understand the logic of victimization in multi-actor settings. A natural starting point is to apply existing strategic victimization theories to multi-actor conflicts. Doing so results in two plausible conclusions. First, in a traditional dyadic conflict, civilians might have to face tradeoffs between groups that treat civilians well and those whose political aims civilians support (see Lyall, Blair and Imai 2013). In a multi-actor environment, however, we can expect to observe more competition for civilian support between an array of ideologically motivated armed groups.

Civilians, in these settings, are more likely to identify, and consequently support, groups that both treat civilians well and are ideologically attractive. If this relationship holds, we would then expect to observe armed groups refrain from victimization in contexts where they fight against many ideologically similar armed groups in order to win civilian support.

Alternatively, one could also argue that in a traditional dyadic civil war the sides are clear, and civilians can always seek redress from the opposition [government] following victimization by the government [opposition]. In a more dense strategic environment, we would then observe shifting alliances and multilateral conflicts. In this context, civilians will have no guarantee that the group they support will target rival groups who committed violence against civilians, instead of an unrelated third party. Hence, we would expect that civilians are less likely to punish perpetrators of victimization and thus suffer higher levels of victimization in these contexts.

Both of these scenarios are drawn from the literature on civilian victimization and plausibly follow what we know about network structure in civil conflict. Given the complexity of civil conflict networks and what they entail for civilian victimization, we require a principled way of generating network hypotheses, rather than simply choosing a story that fits our empirical results. To do so, we develop a formal, computational model to better investigate the link between network structure and victimization. This allows us to posit a set of assumptions about actors' incentives and possible actions, and discern how these assumptions affect our outcome of interest.

In addition to network complexity, we incorporate another layer of behavior into our study. Preexisting work tends to overlook the role that civilians' own choices might play in affecting the strategic logic of armed groups (Dorff, 2019). Modern day warfare is fought on battlegrounds shaped by civilian behavior and their willingness to support armed actors. The interactive nature of conflict, wherein civilians assess their likeli-

hood of survival by balancing the risks and benefits of supporting armed groups, is a fundamental feature of conflict. Unpacking the intricate relationship between civilians, their experience with violence, and armed actors has been a growing trend in conflict and peace studies with an emphasis on rebel governance (Mampilly, 2012; Arjona, 2016), civilian victimization (Eck and Hultman, 2007; Wood, 2014), civilian displacement (Steele, 2011), and civilian organization and resistance (Kaplan, 2013; Arjona, 2017; Dorff and Braithwaite, 2018; Masullo, 2020). Our study contributes to recent scholarship on both sides of the civilian victimization puzzle by directly addressing the strategic implications of multi-actor armed conflicts and their relationship to civilian behavior during war.

We investigate the strategic incentives for civilian victimization in a complex multiactor conflict environment using an innovative computational model. Our model's key
finding is that a more dense conflict network—one in which any two actors are more
likely to fight—leads to more civilian victimization *irrespective* of the overall level of violence or the number of armed groups. This implies that, from a civilian perspective, a
setting with multiple moderately violent rival groups presents a situation that is *more*dangerous than an equally violent setting in which there is only one, extremely violent
group. This finding is counter-intuitive because it reveals that civilian casualties are
not just a function of total levels of violence in a conflict, but are a function of network
density. Below, we provide a compelling explanation of these insights from our computational model. We then investigate the relationship between network density and
civilian victimization empirically and find support for our models' predictions.

Civilian Victimization During War

Extant research into the underlying logic of civilian victimization has focused on key characteristics of armed groups, such as a group's fighting capability (Wood, 2010), re-

source base (Azam and Hoeffler, 2002*a*) and external support (Salehyan, Siroky and Wood, 2015). Yet, these studies also acknowledge that an armed actor's decision to victimize civilians is conditional on the conflict landscape at large, wherein the decisions of armed groups are informed by the actions of both rival armed challengers and the civilian population. As (Wood, 2010, p. 612) explains, "Unraveling these dynamics is particularly important if scholars wish to fully understand the dense web of interactions that guide insurgent's decisions to use violence." We draw on the intuition that the networked dynamics of armed groups influence violence against civilians to support each turn of our modeling decisions described below.

Model Environment

In this model, a country is composed of territories, filled with two types of actors: civilians and armed groups. Armed groups represent both rebel groups and governments. The main difference between the government and rebel actors is that at the start of the game the government controls more territory than non-state actors. In general, armed groups' primary motivation is to gain territory containing resources that can be mobilized (Kalyvas, 2006), where resources in our game are represented by civilians. Failing this, actors prefer that territory is held by groups with similar preferences.

The other main actors in this model are civilians. Civilians are primarily motivated by their personal safety; their secondary motivation is ideological. The inclusion of civilian preferences follows research on rebel-civilian relationships that underscores civilian agency in conflict areas (Mampilly, 2012; Kasfir, 2015; Arjona, 2017). Holding all else constant, civilians would prefer that their territory is held by groups with similar political preferences. When political preferences align, even if weakly, all actors experience the benefits of political stability and resource sharing.

Actor Overview

In our model, we characterize armed groups using two variables, a measure of their ideal point (x_i) on a one-dimensional preference space (bounded between 0 and 1), and a measure of how ideological they are $(\phi_i \in [0,1])$. Groups that are more ideological benefit (suffer) from having other groups with similar (dissimilar) preferences controlling territory, and thus have less (more) motivation to fight them.⁴ Civilians are also characterized by their ideal point (η_i) , but whereas the ideal points of armed groups are public, armed groups cannot directly observe the preferences of the civilian population. We define the distance between any two groups as:

$$D(a,b) = ||z_a - z_b|| (1)$$

where $z_a=x_a$ if a is an armed group. If a is a civilian, $z_a=\eta_a$. In particular, we define the ideological benefit that armed group i gets from changes to group j's utility as:

$$\alpha_{i,j} = 2\phi_i * (.5 - D(i,j))$$
 (2)

We use $2\phi_i$ so that a group that is both maximally ideological ($\phi_i=1$) and extreme ($x_i=0$ or 1) will be indifferent between a gain for themselves, and a loss for a group at the other end of the spectrum.

In this game, armed groups draw resources from the civilian mobilization. This "instrumentalist" perspective follows from research conceptualizing victimization as a strategic choice shaped by the desire to control resources and territory while capturing

⁴We treat the government actor as moderately ideological, because in most cases a government will not allow a strong challenger to hold territory simply because they have politically congenial views, but they would still prefer to attack more ideologically distant groups.

civilian support and undermining support for opponent groups (Wood, 2014).⁵ To extract resources, armed groups try to mobilize support from the civilian population and gain more resources as support increases. Furthermore, when the territory that civilians inhabit is under attack from another armed actor, civilians can choose to support the attacking group in order to increase that group's likelihood of victory.

Each actor makes two potential choices: (1) armed groups can choose to attack other armed groups in order to conquer additional territory, and gain more resources; and (2) armed groups can victimize civilians in territory they control. Civilians choose whether to support an armed group in their territory, and which group to support. In addition, civilians can choose to flee from one territory to another in search of a more congenial (or less indiscriminately violent) armed group.

When an armed actor attacks another territory, each group in the territory has a probability of winning based on their share of spatially weighted resources. To calculate resources, we need to understand the extent to which civilians support the armed groups. Each supporter of the group gives the total possible resources (normalized to 1). Conversely, because a non-supporter of the group requires effort to coerce into yielding resources, the armed group only captures ψ resources (where $0 < \psi < 1$). Finally, if a civilian supporter is in one of the territories where the conflict is taking place, and they support one of the opposing armed groups, that civilian will actually reduce the resources available to the group that controls the territory by k (where 0 < k < 1). This civilian-armed group nexus follows previous scholarship on the incentives for civilian abuse which argues that both governments and non-state actors target the popu-

⁵A modification of the game would be to allow for groups to have natural resources or foreign support which depends on territorial control but not civilian support (Ross, 2004; Salehyan, Gleditsch and Cunningham, 2011).

lation in order to gain support or shift support away from their opponent (Valentino, 2014; Azam and Hoeffler, 2002*b*; Kalyvas, 2006; Wood, 2010).

If the attacking group wins, they take control of the territory, and in any case, resources are lost and civilians casualities occur in all territories that are the source or target of an attack.⁶ When a group is deciding which territory to attack, they compare all their neighboring territories, and choose to attack the one that gives the biggest difference in utility between fighting in a battle, and the status quo if they were to refrain from attacking.

Decision to Victimize

Armed groups can also choose to victimize civilians in territories they control. These groups' ability to be selective relies on their access to resources and trustworthy information, as in Kalyvas (2006). The probability of successful victimization (targeting a non-supporter) is a non-linear function of support in a territory. This probability is a combination of the probability of successful victimization given information, and with no information. On the one hand access to information increases as support increases (Lyall, Shiraito and Imai, 2015), on the other hand, in the absence of information, the armed groups will victimize at random, and the more supporters they have, the more likely they are target a supporter. We define the probability of successful victimization by group i in territory q (denoted ζ_{iq}) 7 as:

$$1 - \zeta_{iq} \equiv \epsilon(\frac{n_{\text{supp},i,q}}{n_{\text{civilians},i,q}}) + (\frac{n_{\text{civilians},i,q} - n_{\text{supp},i,q}}{n_{\text{civilians},i,q}}(\frac{n_{\text{supp},i,q}}{n_{\text{civilians},i,q}})) \tag{3}$$

⁶Losses in the attacking territory represent civilians who were mobilized and died in the fighting.

⁷An exception here is when they have either universal support, or no support. In the first case, the decision rule prohibits them from victimizing. In the second case, there is no risk of unintentionally targeting a supporter since there are no supporters to target.

Where $n_{\text{supp},i,q}$ is the number of supporters of group i in territory q, and $n_{\text{civilians},i,q}$ is the total number of civilians in territory q. The first term here is the probability (ϵ) of unsuccessful victimization given information times the probability of receiving information. The second term is the probability of unsuccessful victimization (the proportion of supporters in the territory) given no information times the probability of not receiving information. In this model selective violence is effective at coercing civilians into giving support, whereas indiscriminate violence (targeting ones' own supporters) is counterproductive. When an actor targets a supporter, the range of ideologies that will provide support to the actor shrinks (since the safety provided by supporting the actor is illusory) and when they target a non-supporter, the range of ideologies grow.⁸

Civilian Preferences

When civilians choose whether or not to support an armed group, they do so with knowledge of the risk of violence. In particular, if the territory is not the site of a battle, civilian's decision for who to support is based on their expectation of who other civilians will support. This is because if they believe other civilians will support the incumbent power in a region, it becomes more effective to "go along" with it in order to avoid the risk of violence.

Civilians are assumed to support the incumbent with a probability that is based on their ideological proximity to the group. Civilians will then support the group if their ideological distance, modified by the effect of past victimizations, is less than half of the expected number of other supporters of the armed group.⁹ If a territory is the site of a battle, the calculations for civilians change. Now civilians seek to trade off

⁸Fjelde and Hultman (2014) show that that the number of civilians targeted by armed groups (government and non-state alike) is higher in areas populated by the enemy's ethnic constituency.

⁹All else equal, civilians will support a maximally close group regardless of the number of other supporters. If a civilian is half the preference space away, then she will only support the armed group if they

between ideological distance and the chance a group will triumph. In particular, civilians choose to support the group that has the greatest product of ideological proximity and expected probability of victory. When civilians decide whether to remain in a territory they are not simply looking for the best armed actor controlling a territory, they are also often paying serious material costs in order to relocate. Thus, the decision to flee begins with a high threshold in the model and becomes more plausible over the course of the conflict.

Sequential Order of Events

We depict the main stages of the game in Figures 2 and 3. In these graphics, territories are represented by rectangles, rectangle size is determined by its civilian population. Territories of the same color are held by the same armed group. The beginning stages of the game are shown in row 1, Figure 2. In row 2 (left panel), we illustrate an armed groups' choice to attack in a given territory (if any). Civilians are arranged in the territory based on their ideological preferences (row 2, right panel); this graphic also shows civilians' decision to support an armed actor. The outcomes for both armed actor and civilian decisions are in the final row. In Figure 3 we depict how a third actor represented in this conflict environment would choose to victimize civilians. This actor's calculus depends on both whether an attack is likely, as well as the possible consequences of victimization. Below, we discuss the specific decision rules for each group in the graphic.

(o) Genesis of Country and Actors

We begin by generating all of the relevant actors and territories. We first generate a number of territories that is at least as large as the number of armed actors in the game. The territories are connected via a random adjacency matrix that we define such that

are supported by the rest of the population, or if they have a history of very effective victimization.

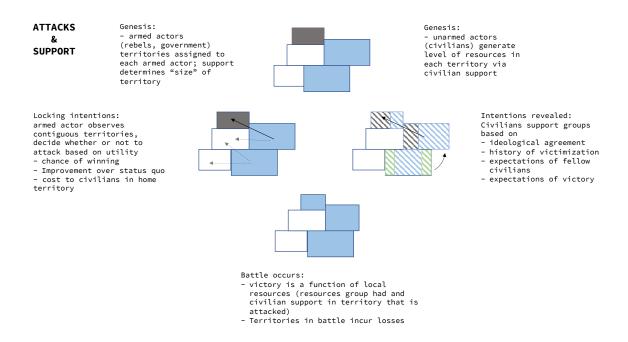


Figure 2: Graphic illustrating the choice of an armed actor to attack, and the choice of civilians to support the actor or not. Rectangles represent territory, with its size based on the size of the civilian population. For the solid colors, color represents the group controlling the territory. The arrows illustrate the potential territories this group can attack. A solid arrow indicates the actual choice. The diagonal lines represent the civilian population in each territory, ordered by ideology. In the two territories that are part of the battle, civilians choose between two combatants; in the other territory, the civilians choose between supporting the blue group or supporting no one. Based on the resources from civilian support, the battle concludes with blue group's victory.

CIVILIAN VICTIMIZATION

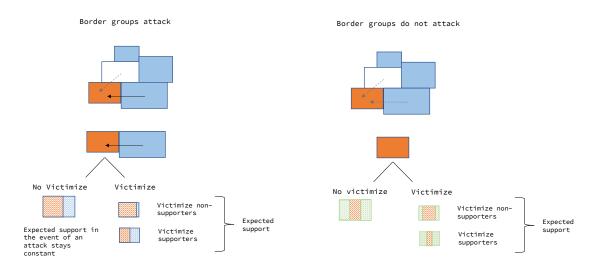


Figure 3: Graphic illustrating the choice of an armed actor to victimize civilians. The orange group first determines whether any of their neighbors are likely to attack. If they are likely to attack, the orange group decides whether to victimize to maximize their support and chance of winning in a battle, if they choose not to victimize, they do so to maximize the resources they gain from the territory. Victimizing can either succeed (in killing a non-supporter) or fail (and indiscriminately kill a supporter) based on both levels of support in the territory and random chance. If it succeeds, the ideological range of support for the incumbent group increases, if it fails, the range contracts.

no territory is totally isolated. We then generate some number of armed actors, each with a random ideal point (x_i) and level of ideology (ϕ_i) . Each armed actor is assigned a territory, and the remaining territories are given to the last group, the government.¹⁰ We then generate the number of civilians in each territory, each with a random ideal point (η_i) . With this foundation, we are ready to begin the game.

(1) Armed groups choose which territories to invade

When an armed actor attacks another territory, each group involved in the territory has a probability of winning based on their share of spatially weighted resources. In particular, we call the local resources of group i in territory L:

$$\Gamma_{i,L} = \sum_{l} \delta^{d_{l,L}} (n_{s,i,l} + \psi n_{ns,i,l} - k n_{o,i,l})$$
 (4)

where δ is the spatial discount factor – how much less useful distant resources are than proximate ones – and $d_{l,L}$ is the distance from region l to L. $n_{s,i,l}$ denotes the number of supporters of group i in territory l and $n_{ns,i,l}$ are non-supporters of i in l. $n_{o,i,l}$ are the number of opponents of group i in territory l as long as territory l is part of the "battlefield" – the set of territories that are either the source or the target of the battle in question. Finally, ψ and k are the resources you get from non supporters, and those you lose from supporters of your opponent respectively.

For each group in the battle, the probability of winning is:

$$p_{i,L} \equiv P(i \text{ wins in territory L}) = \frac{\Gamma_{i,L}}{\sum_{j} \Gamma_{j,L}}$$
 (5)

where a group's probability of winning in territory (L) is determined by the group's local resources within the territory relative to the sum of all combatant's local resources

¹⁰We also define the government with an extreme ideal point $x_i=0$, and as non-ideological $\phi_i=0$.

in the same territory. Next, a group decides which territory to attack by looking at all territories they border, and compares their utility for attacking that territory compared to doing nothing. In particular, for each territory q, they look at:

$$U_i(q|G) = \sum_{g \in G} E(p_{g,L}|G))\alpha_{i,j}(R_q - c)$$
(6)

where G are the groups already committed to battle within a territory, R is the number of civilians within a territory, c is the cost of war. We include the expectation here because at the time of the decision, civilian support is unknown, or armed groups estimate their likelihood of victory using either their prior beliefs about the distribution of civilian preferences, or the past actions taken by civilians in a territory towards a particular armed group. Specifically, the potential attacker assesses how much utility they will gain from attacking a territory compared to how satisfied they will be if they do nothing. For comparison, the utility for group i of the status quo in territory q, held by group j is:

$$U_i(j \text{ controls } q) = \alpha_{j,i} R_q$$
 (7)

The difference between these two factors is the payoff for attacking a given territory. Groups choose to attack in a territory where there will be the biggest payoff from attacking compared to the status quo (or if none of these are positive, they attack nowhere). This decision is illustrated in Figure 2.

(2) Civilians choose whether to support armed groups

Civilians' decisions are conditioned not just on the characteristics of armed actors, but on the behavior of other civilians. When civilians choose who to support, they

¹¹We will determine this in Equations 9 and 10 in the next stage.

¹²This is admittedly difficult to observe, but the assumption holds in the broader literature on col-

assume that other civilians will make support decisions probabilistically based on their proximity to armed groups, such that:

$$E(P(\text{Civilian I supports Group } i)) \equiv \max(\min(1 - D(i, l) + v\chi_j, 1), 0)$$
 (8)

Civilians that are ideologically close to the armed group are assumed to be highly likely to support them and civilians that are very far from the armed group will be much less likely to support them. Here χ_i is the net discriminacy of victimization by group i, which decreases when they victimize a supporter and v is the penalty for indiscriminately victimizing civilians. If a group has a history of killing supporters, all civilians are perceived as less likely to support the group.

Civilian behavior is also conditioned on the actions of armed groups in the territory and battle occurrence, as determined in the previous stage. If no battle is taking place in territory q, civilian l will support an armed group i if:

$$\frac{E(\bar{n}_{s,i,q})}{2} > D(i,l) + v\chi_i \tag{9}$$

where the expected number of supporters is calculated as discussed in Equation 8.

On the other hand, when a battle is taking place in a territory q, civilian h will support group g such that:

$$\operatorname{argmax}_{(g \in G)} E(p_{g,q}) (1 - D(g,h) + v\chi_g)$$
 (10)

It is worth highlighting here that $E(p_{g,q})$ is determined by using beliefs from Equation 8 to calculate the values in Equations 4 and 5. Civilians try to meet both their goals by

lective action. Larson et al. (2019) show how protest participation is driven by network relations; Steele (2017) describes how civilians' decision to leave their community is interdependent across individuals.

choosing the group that gives them the best combination of plausibly winning the battle and ideologically congruence.

(3) Battles take place and winners are determined

This occurs as discussed above in Equation 5, in each territory involved in the battle, \emph{c} civilians at random are removed.

(4) Armed groups choose which territories to victimize.

Armed groups first determine if each territory is at risk of an attack next period. This means a group i will evaluate, for each neighbor j and territory they control q, whether:

$$\alpha_{i,i}R_q < E(p_{i,q})\alpha_{j,i}(R_q - c) + E(p_{j,q})(R_q - c)$$
 (11)

Note that these are the same utilities from Equation 6 and 7. In any territory where this is true for all neighbors j, the armed group will victimize to maximize their potential of winning in a future period. If it is not true, they will victimize in order to maximize resources in a future period.

Armed groups believe that the proportion of the preference space made by their supporters is $s \equiv \frac{x_{s,i,q}}{n_{ns_i,q}+n_{s,i,q}}+v\chi_i$. The proportion believed to be composed by non-supporters is of course 1-s. If the territory is not at risk of attack, the group will victimize if:

$$\zeta_q(\frac{v(1-c)n_{ns,i,q-1}}{(1-s)}-c)-(1-\zeta_q)(\frac{v(1-c)n_{s,i,q-1}}{s}-1)>0 \tag{12}$$

Here $\frac{(vn_{ns,i,q-1})}{1-s}$ is the expected number of non-supporters coerced to support the armed group in the event of selective victimization, (1-c) is the benefit of coercing non-supporters into support, and $\frac{(vn_{s,i,q-1})}{s}$ are the number of supporters pushed to non-support in the event of indiscriminate victimization. In addition, victimization has a direct effect of either killing a supporter or a non-supporter.

When considering whether to victimize in a territory at risk of an attack, the armed group needs to separate civilians into potential supporters of the attacker and non-supporters. Their belief is that the division for support for groups i and j, defined such that $x_i > x_j$ is that a civilian, f, will support group i if:

$$\eta_f > x_i E(p_{i,q}) + x_j E(p_{j,q}) \equiv \lambda_q$$
 (13)

This, combined with their beliefs about the distribution of supporters and non-supporters, allows an armed group to estimate the number of supporters both for themselves and the attacking group, as well as the range of preferences occupied by each group which are of length λ_q and $1-\lambda_q$ respectively. They then victimize if:

$$\zeta_q \frac{v(1+k)E(n_{o,i,q})}{\lambda_k} + k) - (1-\zeta_q)(\frac{v(1+k)E(n_{s,i,q})}{(1-\lambda_k)} + 1) > 0$$
(14)

Similar to the case where there is no risk of battle, this is the net effect of victimization on local resources, which is the probability of gaining new supporters and the negative effect of civilian death on resources. The tradeoffs for the armed group in each of these cases is illustrated in Figure 3.

(5) Civilians Choose to Flee

After victimization civilians choose whether or not to flee from a territory into an adjacent territory. Civilian k will choose to flee a territory controlled by group i for a territory controlled by group j if these territories are contiguous and:

$$D(i,l) + v\chi_i < e^{3-t3/T}D(j,l) + v\chi_j$$
(15)

The exponential decay function is such that in the first turn of a game (t) another group needs to be at least e^3 times better than the incumbent in a civilians territory

for the civilian to move, but by the final turn of the game (T) the group will move to whichever territory has a more congenial incumbent.¹³

(6) Game Iterates

Stages 1-6 will continue until one of three end conditions are met: a) the government controls all the territories, b) the government controls no territories, c) the game reaches the predetermined turn limit and ends in a stalemate.

Hypotheses

As we model it, the decision for armed groups to victimize civilians is a strategic action. Armed groups target civilians to help extract resources from the population and to increase their likelihood of prevailing in expected conflicts with other groups. Civilians likewise act strategically to minimize their personal likelihood of being killed by armed groups. Thus, to understand when and where civilian victimization is likely to take place, we need to evaluate the strategic environment.

To do this, we conceptualize the overall strategic environment as a social network, wherein the nodes in this network are armed groups, and the edges are battles between these groups. Density measures the number of edges (or connections) proportional to the total number of possible edges. To understand the strategic environment, we illustrate three ideal types of conflict networks in Figure 4. In each network the number of battles (edge thickness) and the number of actors (nodes) stay the same, but the distribution of these events change across actors. Our conceptual illustration demonstrates that even though the number of actors and battles are constant across all three networks, the third network exhibits the highest density.

 $^{^{13}}$ Second, in each territory, there will be new civilians added to the game based on the global growth rate parameter G (rounded down to the nearest integer).

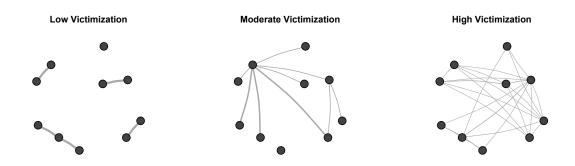


Figure 4: Conceptual networks demonstrate the expected relationship between density and civilian victimization. The number of conflictual events and the number of actors stay constant, while the distribution of these events between actors changes in each example.

The first type of conflict network is the sparse network. Here, conflict occurs between a few distinct dyads. In this network, the strategic decision to victimize civilians is simple – victimization takes place if the coercive effect (causing more non-supporters to begrudgingly support the group in charge) outweighs the resources that could be mobilized from non-supporters. In this environment, while there may be some initial low levels of victimization, we will pretty quickly approach an equilibrium where most civilians support the groups in control of their territory, and no victimization occurs. Intrastate conflict in Chad during the hearly 2000s might reflect this network structure, where conflict was largely split between a sparse number of warring rebel groups in the north and the south.

A second stylized network we might observe is a polarized network. In this type of network, we have two clustered groups of actors where actors' interactions are with groups in the other cluster. For example, in many civil conflicts, a number of different separatist groups fight the central government but do not fighting each-other. This layout would be especially likely if we see ideologically oriented groups that cluster at two points on the spectrum. Here, some territories that groups control will be at risk of

attack, and so these groups will have incentive to victimize civilians not just to coerce them into support, but also to avoid the risk of civilians supporting an attacking group. This will lead to a moderate level of victimization in these border territories. That being said, victimization should only be moderate, because many territories will not be at risk of attack.

The final stylized network is the complex network. This conflict network functions as a Hobbesian war of all against all, where each armed group is ready to attack each other armed group. In these cases, the dynamics that led to victimization in the polarized network are intensified. Almost all territories are at risk of an attack, and they are at risk of an attack from multiple sources leading to even stronger incentives towards victimization, since even if victimization is counterproductive against some opponents, it will be beneficial against others. In this case, there would also likely be a fluid control of territory and frequent changes in ruling groups, which generates even more incentives for violence against civilians. Some of the most intractable and dynamic conflicts-like the modern wars in Somalia- are likely to exhibit this network structure.

To determine the macro-level effects of the micro-actions described above, we run a simulation analysis with 10,000 separate conflict scenarios. In each scenario, we chose parameters at random and record three main network statistics – the number of armed groups in the network, the overall level of violence in the network, and the density of the conflict network. We also capture the frequency of civilian victimization in each run of the game. Returning to our three stylized networks in Figure 4, all three networks have the same level of violence, but the sparse network would have both a low density, and the full network would be most dense, but does not have a higher level of conflict than the polarized network or the sparse network.

To estimate the effect that our three network statistics have in relation to civilian victimization, we employ a negative binomial regression with fixed effects on the con-

flict scenarios. We depict the results of this analysis in Figure 5.¹⁴ Here we can see that even when controlling for the level of violence between armed groups and the number of actors, more dense conflict networks had both a higher likelihood and frequency of civilian victimization.¹⁵ This finding generates our main hypothesis for empirical investigation.

Hypothesis: Even when controlling for the overall level of violence, a more dense conflict network leads to higher levels of civilian victimization.

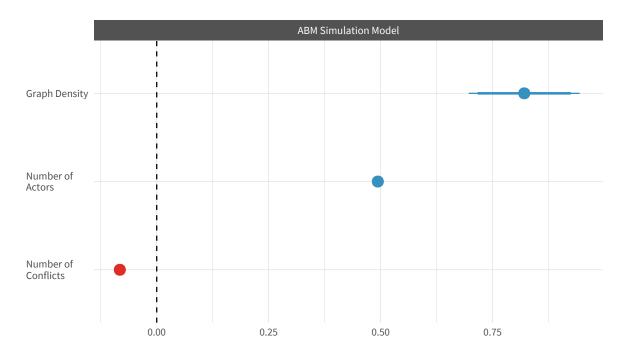


Figure 5: Analysis of determinants of victimization in computational model. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

¹⁴Results are similar when we estimate via random effects as well.

¹⁵It is worth noting here that in the ABM, victimization both refers to the overall number of civilians killed strategically by armed groups and the number of incidents of victimization.

Empirical analysis

To investigate the implications of our computational model empirically, we utilize the Armed Conflict Location and Event Dataset (ACLED) dataset developed by Raleigh et al. (2010). Our first step is to calculate conflict network densities for countries experiencing intrastate conflict according to the *battles* data provided by ACLED. Our sample ranges from 1997 to 2020 and includes 45 countries.

only include cntries that have some data left in the adjacency matrix, min is three cntries need to have at least three years of data

For each country in our sample we construct a conflict adjacency matrix in which a value of one is recorded if there was a battle between armed groups. Given that untangling who initiated a particular battle can be difficult, the conflict adjacency matrices we construct are symmetric. The set of actors in these adjacency matrices include both rebel groups and government forces. We aggregate military and police forces from the same country into one government actor. Additionally, we exclude international actors such as peacekeepers, militaries from other countries, and peacekeepers from our analysis. Once we have generated our set of adjacency matrices for every country-year we then calculate the number of actors and the graph density of the conflict networks. We control for the overall level of violence by counting the number of battle events a country faces in a given year. Apart from the ACLED based data, we incorporate a number of other controls that have been argued to affect the level of civilian victimization at the country-year. These are depicted in Table 1.

Variable	Source	Last Year of Data		Base + Controls (1997-2018)	Base + Controls (1997-2012)	
Graph Density Number of Actors Number of Conflicts	Raleigh et al. (2010)	2020	Х	Х	Х	
Polity	Marshall et al. (2009)	2018		X	X	
Log(Population) Log(GDP per Capita)	World Bank Group (2016)	2019		X	X	
Excluded Population	Vogt et al. (2015)	2017		X	X	
Presence of Peacekeepers	Kathman (2013)	2012			X	
Rebel(s) Stronger than Govt. Rebel(s) Supported by Foreign Govt. Govt. Supported by Foreign Govt.	Cunningham et al. (2013)	2011			х	

Table 1: Summary of data used in our empirical analysis.

While the ACLED data is available from 1997 to 2020. The availability of other data sources varies notably, we list the last year of available data for each of the other variables. To maximize the size of the sample we can test for each dataset we run several models. First, we run a "Base" model that just includes the variables we derive from ACLED, which gives us a sample of 42 countries from 1997 to 2020. The next model we run includes polity, population, GDP per capita, and a measure of excluded population from the Ethnic Power Relations dataset (Cederman, Wimmer and Min, 2010). The sample for this model includes 38 countries and ranges from 1997 to 2018.

In the last model, we create a binary variable to indicate whether any peacekeepers were active in a given country year based on data from Kathman (2013). We also include controls from the Non-State Actor database for rebel strength relative to the government and whether rebel(s) or governments were receiving support from foreign countries (Cunningham, Gleditsch and Salehyan, 2013). The sample for the model ranges from 1997 to 2012 and includes 19 countries.

¹⁶We list the countries used to estimate each of the models in the Appendix.

Our dependent variable is a count of the number of civilians killed during a country-year. We retrieve this information from the "Violence against civilians" event type in the ACLED dataset. To model this, we utilize a negative binomial model with fixed effects for countries.¹⁷

We report the results for our models of civilian victimization in Figure 6 below.

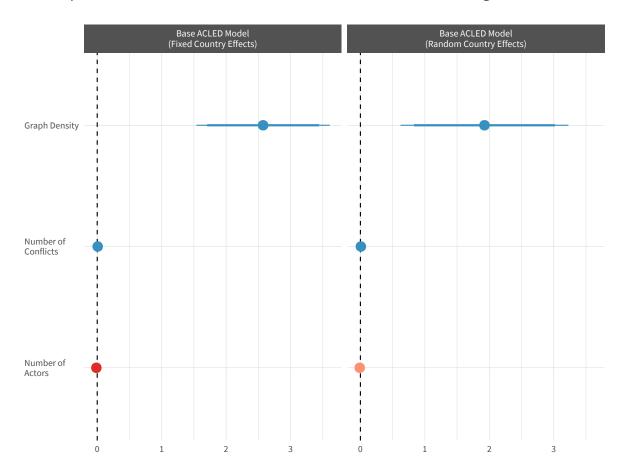


Figure 6: Regression results using Base specification that includes 42 countries from 1997 to 2020. The left panel visualizes coefficient estimates when using fixed effects on countries and the right random effects. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

In the left panel, we show results without using any of the controls. Within this

¹⁷Results are similar when using a random effects framework.

fixed effects framework, graph density has a notable effect on the level of civilian victimization observed in a country-year. Whereas simple counts of the number of actors involved in a conflict or the number of conflicts seem to be less meaningful in explaining levels of civilian victimization. In the right panel, we show that our findings are robust to a number of controls.¹⁸

¹⁸To deal with missingness in our sample, we employ a multiple imputation method developed by Hoff (2007) and shown to have comparable performance to alternatives such as AMELIA and MICE by Hollenbach (2014).

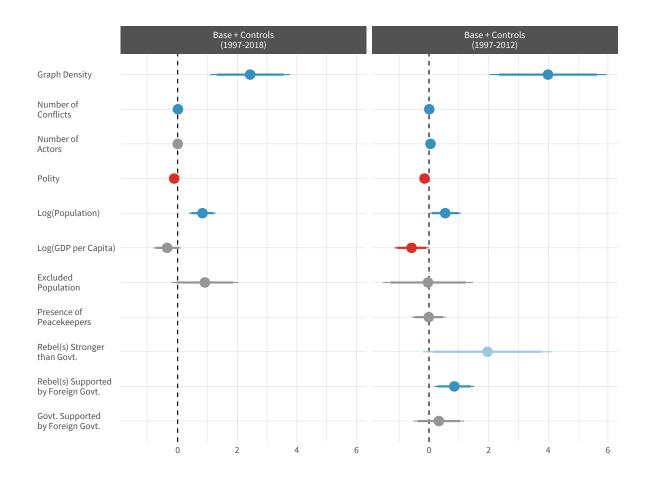


Figure 7: Regression results from multiply imputed datasets when pairing Base specification with controls using random effects for countries. Specification in the left panel includes 38 countries from 1997 to 2018 and the right includes 19 countries from 1997 to 2012. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

Discussion

We have shown that frequency of civilian victimization depends, in large part, on the strategic environment. If conflict between armed groups is rare, civilian victimization will similarly be rare; if conflict is polarized between two groups (for example a government and different opposition groups, or armed groups of two opposing religions or ethnicities) then there will be a moderate level of civilian victimization; if we have a conflict where any two conflict groups are likely to fight, then civilian victimization will be at

its highest. This result holds even when accounting for the number of belligerents and the total volume of fighting. There are two primary reasons for this pattern of victimization. First, groups are more likely to victimize civilians in a territory if that territory is at risk of an attack. Second, victimization is most common when groups are newly in control of territory, since a combination of past victimization, and civilians' choice to flee make territories more ideologically homogeneous and congruent with the ruling group over time. Both of these factors are at their most intense in dense conflict networks.

We test these dynamics in a cross-national analysis of multi-actor civil wars using ACLED data to construct conflict networks. We find a consistent positive effect of network density on civilian victimization even when controlling for other characteristics of the conflict network. Going forward, we aim to make a number of advances in both empirical and theoretical research. On the empirical side, we would like to investigate whether these results hold when using event data from other sources such as UCDP's GED data. Theoretically, we will investigate whether other empirical regularities concerning civilian victimization, like the tendency for more violent battles to increase the risk of victimization, are borne out in our model. We also plan to incorporate other important factors into our model, such as the ability for armed groups to endogenously enter and leave the model and the possibility that armed groups' reliance on foreign support or lootable goods influences patterns of victimization.

While this paper has focused on civilian victimization during civil conflicts, we believe it has wider implications. First, it shows the implications of moving from a relatively simple dyadic interaction or model to a more complex multi-actor model. We can see similar dynamics at play for example in the median voter theory, where the equilibrium breaks down in the presence of a third candidate (Patty et al., 2009) in coalition bargaining, where circumstances with only two major parties are trivial, and appropriately modeling and measuring negotiations with three or more parties is fraught (Laver,

De Marchi and Mutlu, 2011); and in the bargaining model of war, where the fundamental finding that war is irrational ceases to hold with more than two potential combatants (Gallop, 2017).

In sum, our study models the choice for armed groups to victimize civilians as a strategic one. Importantly, our findings have important implications for policymakers and the civilian population. We have shown that a conflict setting with multiple moderately violent rival groups presents a situation that is at least as risky as a setting in which there is only one, extremely violent group. Armed groups choose to victimize civilians to improve their ability to mobilize resources and to maximize their chances to defend themselves if their territory is attacked. Civilians can decide to provide or withhold support, as well as flee, out of self-preservation and to achieve ideological goals. Our study unites the strategic decision-making of both armed groups and civilians into a single multi-actor framework of civil war that reveals how actors' incentives change according to the network dimensions of their strategic environment.

References

- Arjona, Ana. 2016. Rebelocracy. Cambridge University Press.
- Arjona, Ana. 2017. "Civilian Cooperation and Non-Cooperation with Non-State Armed Groups: The Centrality of Obedience and Resistance." *Small Wars & Insurgencies* 28(4-5):755-778.
- Autesserre, Séverine. 2012. "Dangerous tales: Dominant narratives on the Congo and their unintended consequences." *African Affairs* 111(443):202–222.
- Azam, Jean-Paul and Anke Hoeffler. 2002a. "Violence against civilians in civil wars: looting or terror?" *Journal of Peace Research* 39(4):461–485.
- Azam, Jean-Paul and Anke Hoeffler. 2002b. "Violence against civilians in civil wars: Looting or terror?" *Journal of Peace Research* 39(4):461–485.
- Berman, Eli and Aila M. Matanock. 2015. "The Empiricists' Insurgency." *Annual Review of Political Science* 18:443–464.
- Cederman, Lars-Erik, Andreas Wimmer and Brian Min. 2010. "Why do ethnic groups rebel? New data and analysis." *World Politics* 62(1):87–119.
- Christia, Fotini. 2012. *Alliance formation in civil wars*. Cambridge University Press.
- Condra, Luke N. and Jacob N. Shapiro. 2012. "Who takes the blame? The strategic effects of collateral damage." *American Journal of Political Science* 56(1):167–187.
- Cunningham, David, Kristian Skrede Gleditsch and Idean Salehyan. 2013. "Non-State Actors in Civil Wars: A New Dataset." *Conflict Management and Peace Science* 30(5):516–531.
- Dorff, Cassy. 2019. "Violent and Nonviolent Resistance in Contexts of Prolonged Crisis: The Civilian Perspective." *Journal of Global Security Studies* 4(2):286–291.
- Dorff, Cassy and Jessica M. Braithwaite. 2018. "Fear of Nonviolent Organizing in Mexico's Criminal Conflict." *Journal of Global Security Studies* 3(3):271–284.
- Dowd, Caitriona. 2015. "Actor proliferation and the fragmentation of violent groups in conflict." *Research & Politics* 2(4):2053168015607891.
- Eck, Kristine and Lisa Hultman. 2007. "One-sided violence against civilians in war: Insights from new fatality data." *Journal of Peace Research* 44(2):233–246.
- Fjelde, Hanne and Lisa Hultman. 2014. "Weakening the enemy: A disaggregated study of violence against civilians in Africa." *Journal of Conflict Resolution* 58(7):1230–1257.

- Gallop, Max. 2017. "More Dangerous Than Dyads: How a Third Party Enables Rationalist Explanations for War." *Journal of Peace Research* .
- Hoff, Peter D. 2007. "Extending the Rank Likelihood for Semiparametric Copula Estimation." *Annals of Applied Statistics* 1(1):265–283.
- Hollenbach, Florian M. 2014. "Raising Robinhood: The Political Economy of Tax Capacity Investments in Authoritarian Regimes." Dissertation Chapter. http://sites.duke.edu/fmh3/research/.
- Kalyvas, Stathis. 2006. *The Logic of Violence in Civil War*. New York: Cambridge University Press.
- Kaplan, Oliver. 2013. "Protecting civilians in civil war The institution of the ATCC in Colombia." *Journal of Peace Research* 50(3):351–367.
- Kasfir, Nelson. 2015. "Rebel governance–constructing a field of inquiry: Definitions, scope, patterns, order, causes." *Rebel governance in civil war* pp. 21–46.
- Kathman, Jacob D. 2013. "United Nations peacekeeping personnel commitments, 1990–2011." Conflict Management and Peace Science 30(5):532–549.
- Larson, Jennifer M, Jonathan Nagler, Jonathan Ronen and Joshua A Tucker. 2019. "Social networks and protest participation: Evidence from 130 million Twitter users." *American Journal of Political Science* 63(3):690–705.
- Laver, Michael, Scott De Marchi and Hande Mutlu. 2011. "Negotiation in legislatures over government formation." *Public Choice* 147(3-4):285–304.
- Lyall, Jason, Graeme Blair and Kosuke Imai. 2013. "Explaining support for combatants during wartime: A survey experiment in Afghanistan." *American Political Science Review* 107(04):679–705.
- Lyall, Jason, Yuki Shiraito and Kosuke Imai. 2015. "Coethnic bias and wartime informing." *The Journal of Politics* 77(3):833–848.
- Mampilly, Zachariah Cherian. 2012. *Rebel rulers: Insurgent governance and civilian life during war*. Cornell University Press.
- Marshall, Monty G., Keith Jaggers and Ted Robert Gurr. 2009. "Polity IV Project: Political Regime Characteristics and Transition 1800-2007." CIDCM: University of Maryland, MD.
- Masullo, Juan. 2020. "Civilian Contention in Civil War: How Ideational Factors Shape Community Responses to Armed Groups." *Comparative Political Studies* p. 0010414020912285.

- Mustapha, Abdul Raufu. 2014. "Understanding Boko Haram." *Sects & Social Disorder: Muslim Identities & Conflict in Northern Nigeria, Ed. by AR Mustapha* pp. 147–198.
- Obi, Cyril. 2009. "Nigeria's Niger Delta: Understanding the complex drivers of violent oil-related conflict." *Africa Development* 34(2).
- Patty, John W., James M. Snyder, M. Ting et al. 2009. "Two's company, three's an equilibrium: Strategic voting and multicandidate elections." *Quarterly Journal of Political Science* 4(3):251–278.
- Raleigh, Clionadh. 2012. "Violence against civilians: A disaggregated analysis." *International Interactions* 38(4):462–481.
- Raleigh, Clionadh, Andrew Linke, Håvard Hegre and Joakim Karlsen. 2010. "Introducing ACLED: An Armed Conflict Location and Event Dataset Special Data Feature." *Journal of Peace Research* 47(5):651–660.
- Ross, Michael. 2004. "How Do Natural Resources Influence Civil War? Evidence from Thirteen Cases." *International Organization* 58(1):35–67.
- Salehyan, I., K.S. Gleditsch and D. Cunningham. 2011. "Explaining external support for insurgent groups." *International Organization* 65(04):709–744.
- Salehyan, Idean, David Siroky and Reed Wood. 2015. "External rebel sponsorship and civilian abuse: A principal-agent analysis of wartime atrocities." *International Organization* 68(3):633–661.
- Stanton, Jessica A. 2016. *Violence and restraint in civil war: Civilian targeting in the shadow of international law.* Cambridge University Press.
- Steele, Abbey. 2011. "Electing Displacement: Political Cleansing in Apartado, Colombia." *Journal of Conflict Resolution* 55(3):423–445.
- Steele, Abbey. 2017. *Democracy and Displacement in Colombia's Civil War*. Cornell University Press.
- Valentino, Benjamin A. 2014. "Why we kill: The political science of political violence against civilians." *Annual Review of Political Science* 17:89–103.
- Vogt, Manuel, Nils-Christian Bormann, Seraina Rüegger, Lars-Erik Cederman, Philipp Hunziker and Luc Girardin. 2015. "Integrating Data on Ethnicity, Geography, and Conflict: The Ethnic Power Relations Data Set Family." *Journal of Conflict Resolution* 59(7):1327–1342.
- Wood, Reed M. 2010. "Rebel capability and strategic violence against civilians." *Journal of Peace Research* 47(5):601–614.

Wood, Reed M. 2014. "From loss to looting? Battlefield costs and rebel incentives for violence." *International Organization* 68(4):979–999.

World Bank Group. 2016. World Development Indicators 2016. World Bank Publications.

ABM Random Effects Regression

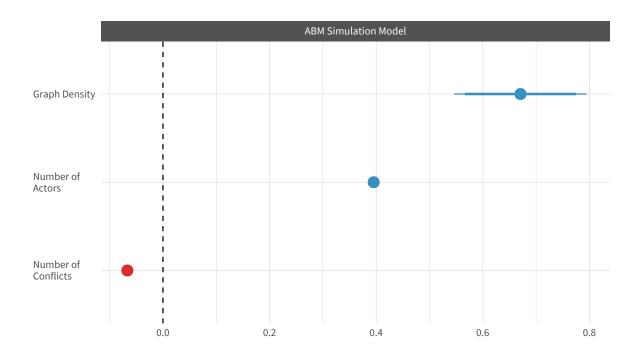


Figure A1: Analysis of determinants of victimization in computational model. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

Countries in the Sample

Table A1 list the countries that we are able to include based on data availability in each of our models. The "Base" model includes 42 countries, the "Base + Controls (1997-2018)" includes 38, and the "Base + Controls (1997-2012)" includes 19.

		Base + Controls	Base + Controls	
	Base	(1997-2018)	(1997-2012)	
Algeria	Х	X	X	
Angola	Χ	Χ	Χ	
Benin	Χ	Χ		
Burkina Faso	X	Χ		
Burundi	Χ	Χ	Χ	
Cameroon	Χ	Χ		
Central African Republic	Χ	Χ	Χ	
Chad	Χ	Χ	Χ	
Congo, Republic Of	Χ	Χ	Χ	
Congo, The Democratic Republic Of	Χ	Χ	Χ	
Cote D'ivoire	Χ	Χ	Χ	
Egypt	Χ	Χ	Χ	
Eritrea	Χ	Χ		
Ethiopia	Χ	X	Χ	
Gambia	Χ			
Ghana	Χ	X		
Guinea	Χ	X	Χ	
Guinea-Bissau	Χ	Χ		
Kenya	Χ	X		
Liberia	Χ	Χ	Χ	
Libyan Arab Jamahiriya	Χ	Χ		
Madagascar	Χ	Χ		
Mali	Χ	Χ	Χ	
Mauritania	Χ	X		
Morocco	Χ			
Mozambique	Χ	Χ		
Namibia	Χ			
Niger	Χ	Χ		
Nigeria	Χ	Χ	Χ	
Rwanda	Χ	Χ	X	
Senegal	Χ	X	X	
Sierra Leone	Χ	Χ	Χ	
Somalia	Χ			
South Africa	Χ	X		
South Sudan	Χ	X		
Sudan	Χ	X	X	
Tanzania, United Republic Of	Χ	X		
Togo	Χ	X		
Tunisia	Χ	X		
Uganda	Χ	X	X	
Zambia	Χ	X		
Zimbabwe	Х	X		

Table A1: List of countries in each model, "X" indicates country was included.

Descriptive Statistics

Below we show descriptive statistics for each of the variables underlying our models.

Base Model

	N	Min.	Median	Mean	Max.	Std. Dev.
Civ. Victimization	638	0	35	291.53	9337	753.8
Graph Density	638	0	0.1	0.15	0.67	0.15
Num. Actors	638	3	8	20.17	168	28.18
Num. Conflicts	638	1	23.5	90.77	1534	182.09

Table A2: Descriptive statistics for variables in Base model.

Base + Controls (1997-2018)

	N	Min.	Median	Mean	Max.	Std. Dev.
Civ. Victimization	544	0	27	301.55	9337	800.65
Graph Density	544	0	0.1	0.15	0.67	0.15
Num. Actors	544	3	8	17.25	148	21.55
Num. Conflicts	544	1	21	69.24	1185	114.22
Polity	543	4	11	12.36	20	4.47
Log(Pop.)	542	13.94	16.74	16.75	19.07	0.99
Log(GDP Cap.)	536	5.23	6.74	6.85	9.4	0.87
Excl. Pop.	543	0	0.09	0.19	0.85	0.25

Table A3: Descriptive statistics for variables in Base + Controls (1997-2018) model.

Base + Controls (1997-2012)

	Ν	Min.	Median	Mean	Max.	Std. Dev.
Civ. Victimization	240	0	58.5	408.86	9337	964.97
Graph Density	240	0	0.1	0.15	0.67	0.15
Num. Actors	240	3	8	16.32	105	17.52
Num. Conflicts	240	1	44	74.9	1185	107.97
Polity	240	4	11	11.24	19	4.06
Log(Pop.)	240	14.59	16.67	16.69	18.91	1.09
Log(GDP Cap.)	236	5.23	6.52	6.66	8.42	0.87
Excl. Pop.	240	0	0.24	0.28	0.85	0.28
Peacekeepers	240	0	0	0.3	1	0.46
Reb. Stronger Govt.	149	0	0	0.02	1	0.12
Reb. Supp. by Foreign Govt.	149	0	0.5	0.43	1	0.4
Govt. Supp. by Foreign Govt.	149	0	1	0.66	1	0.46

Table A4: Descriptive statistics for variables in Base + Controls (1997-2012) model.

Fixed Effect Regression Results when Including Controls

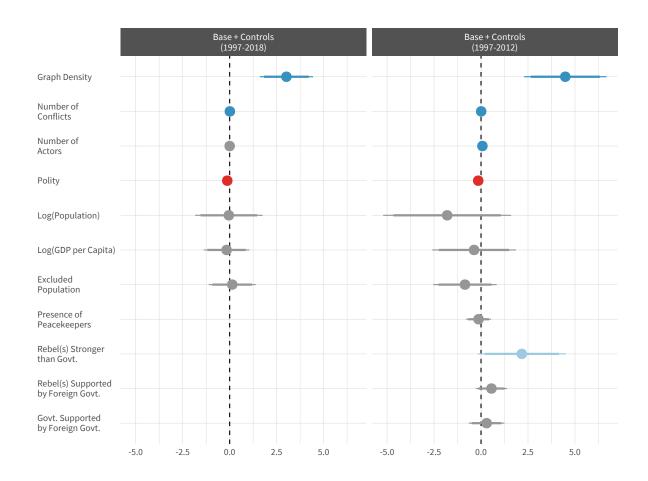


Figure A2: Regression results from multiply imputed datasets when pairing Base specification with controls using fixed effects for countries. Specification in the left panel includes 38 countries from 1997 to 2018 and the right includes 19 countries from 1997 to 2012. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

Results without Multiple Imputation

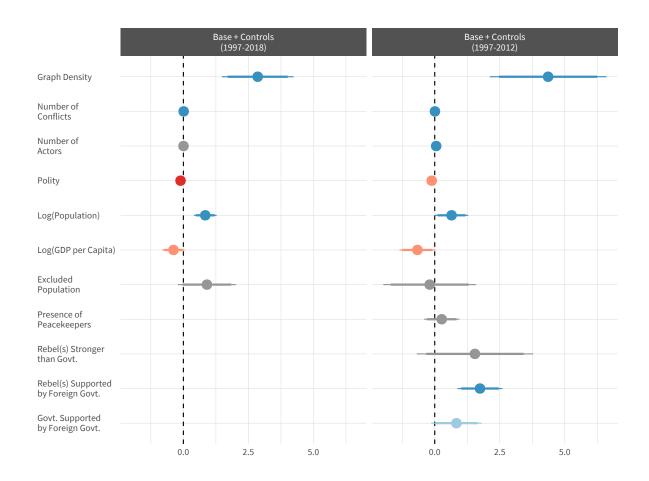


Figure A3: Regression results from unimputed data when pairing Base specification with controls using random effects for countries. Specification in the left panel includes 38 countries from 1997 to 2018 and the right includes 19 countries from 1997 to 2012. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

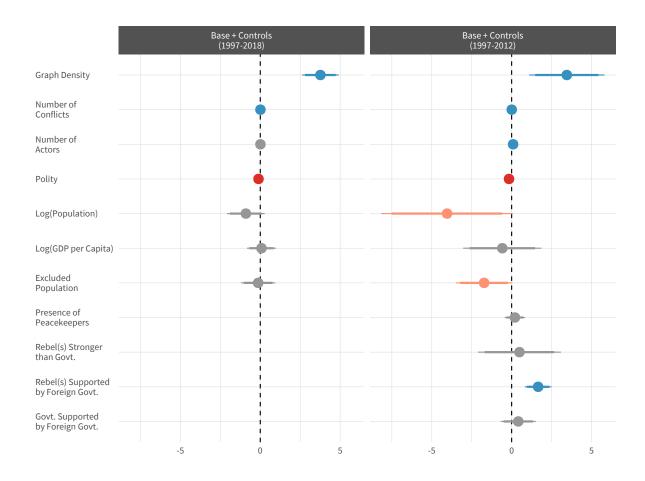


Figure A4: Regression results from unimputed data when pairing Base specification with controls using fixed effects for countries. Specification in the left panel includes 38 countries from 1997 to 2018 and the right includes 19 countries from 1997 to 2012. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

Results using Various Thresholds to Include Countries

In the Base results presented in Figure 6 of the manuscript, the underlying sample had a requirement that a country must have at least three observations to be included in our analysis. This led to a sample of 42 countries from 1997 to 2020. Here we modify this three observation minimum to test the robustness of our results. The first row in Figure A5 depicts our results when we employ no miminum and the second row when we employ a five observation minimum per country. The former criterion leads to a sample of 45 countries and the latter 39. Our results in terms of graph density are robust to any of these minimum country observation requirements.

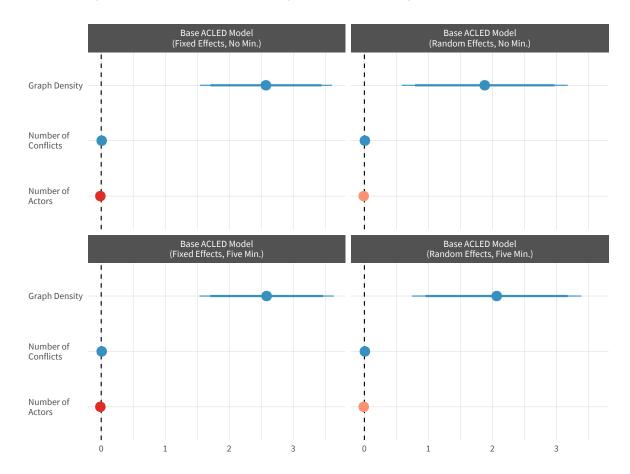


Figure A5: Regression results from unimputed data on Base specification when using various thresholds to include countries and estimations via fixed or random effects. Specification in the left panel includes 38 countries from 1997 to 2018 and the right includes 19 countries from 1997 to 2012. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.

Sensitivity of Results to Dropping Countries

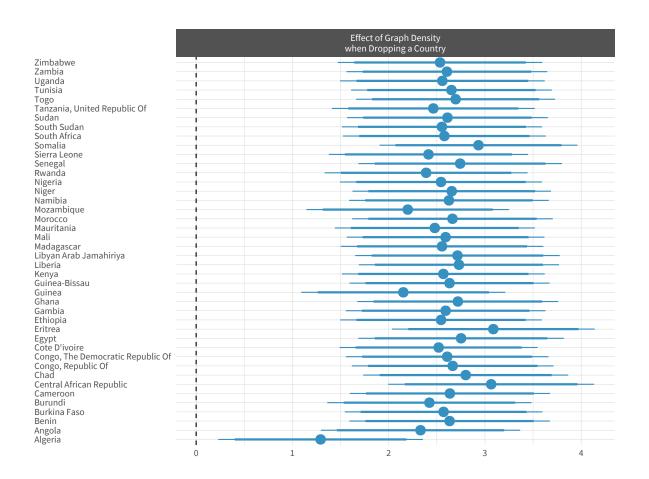


Figure A6: Effect of Graph Density in Base specification when dropping a country on the y-axis. Points represent average value of parameters, thicker line the 90% confidence interval, and thinner line the 95%. Darker shade of red or blue indicates significance at 95% interval, lighter at 90%.