第4章 線性規劃問題求解法:單行法

題目 4.4-5 (a) (b)

4.4-5.

(a) Set $x_1 = x_2 = x_3 = 0$.

$$(0) Z - 2x_1 - 4x_2 - 3x_3 = 0$$

(1)
$$x_1 + 3x_2 + 2x_3 + x_4 = 80 \Rightarrow x_4 = 80$$

$$(2) 3x_1 + 4x_2 + 2x_3 + x_5 = 60 \Rightarrow x_5 = 60$$

(3)
$$2x_1 + x_2 + 2x_3 + x_6 = 40 \Rightarrow x_6 = 40$$

Optimality Test: The coefficients of all nonbasic variables are negative, so the solution (0,0,0,80,60,40) is not optimal.

Choose x_2 as the entering basic variable, since it has the largest coefficient.

(1)
$$x_1 + 3x_2 + 2x_3 + x_4 = 80 \Rightarrow x_4 = 80 - 3x_2 \Rightarrow x_2 \le 26.67$$

(2)
$$3x_1 + 4x_2 + 2x_3 + x_5 = 60 \Rightarrow x_5 = 60 - 4x_2 \Rightarrow x_2 \le 15 \leftarrow \text{minimum}$$

(3)
$$2x_1 + x_2 + 2x_3 + x_6 = 40 \Rightarrow x_6 = 40 - x_2 \Rightarrow x_2 \le 40$$

We choose x_5 as the leaving basic variable. Set $x_1 = x_5 = x_3 = 0$.

$$(0) Z + x_1 - x_3 + x_5 = 60$$

(1)
$$-1.25x_1 + 0.5x_3 + x_4 - 0.75x_5 = 35 \Rightarrow x_4 = 35$$

(2)
$$0.75x_1 + x_2 + 0.5x_3 - 0.25x_5 = 15 \Rightarrow x_2 = 15$$

(3)
$$1.25x_1 + 1.5x_3 - 0.25x_5 + x_6 = 25 \Rightarrow x_6 = 25$$

Optimality Test: The coefficient of x_3 is negative, so the solution (0, 15, 0, 35, 0, 25) is not optimal.

Let x_3 be the entering basic variable.

(1)
$$-1.25x_1 + 0.5x_3 + x_4 - 0.75x_5 = 35 \Rightarrow x_4 = 35 - 0.5x_3 \Rightarrow x_3 \le 70$$

(2)
$$0.75x_1 + x_2 + 0.5x_3 + 0.25x_5 = 15 \Rightarrow x_2 = 15 - 0.5x_3 \Rightarrow x_3 \le 30$$

(3)
$$1.25x_1 + 1.5x_3 - 0.25x_5 + x_6 = 25 \Rightarrow x_6 = 25 - 1.5x_3 \Rightarrow x_3 \le 16.67 \leftarrow \min$$

We choose x_6 as the leaving basic variable. Set $x_1 = x_5 = x_6 = 0$.

$$(0) Z + 1.83x_1 + 0.83x_5 + 0.67x_6 = 76.67$$

(1)
$$-1.67x_1 + x_4 - 0.67x_5 - 0.33x_6 = 26.67 \Rightarrow x_4 = 26.67$$

(2)
$$0.33x_1 + x_2 + 0.33x_5 - 0.33x_6 = 6.67 \Rightarrow x_2 = 6.67$$

(3)
$$0.83x_1 + x_3 - 0.17x_5 + 0.67x_6 = 16.67 \Rightarrow x_3 = 16.67$$

Optimality Test: All of the coefficients are positive, so the solution (0, 6.67, 16.67, 26.67, 0, 0) is optimal. $Z^* = 76.67$.

(b) O	ptimal solution:	(x_1^*, x_2^*, x_3^*)) = (0	, 6.67	, 16.67) and Z^*	= 76.67
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Bas Eq			Coefficient of						
Var No	Ζ	X1	X2	ХЗ	X4	Х5	Х6		side
	_								
Z 0	1	-2	-4	-3	0	0	0		0
X4 1	0	1	3	2	1	0	0		80
X5 2	0	3	4 *	2	0	1	0		60
X6 3	0	2	1	2	0	0	1		40

Bas Eq			Co		Right			
Var No	Ζl	Х1	X2	ХЗ	X4	Х5	Х6	side
	I_							l
Z 0	1	1	0	-1	0	1	0	60
X4 1	0 -	1.25	0	0.5	1 -	0.75	0	35
X2 2	0 0	0.75	1	0.5	0	0.25	0	15
X6 3	0 3	1.25	0	1.5*	0 -	0.25	1	25

Bas Eq		Coe	fficie		Right		
Var No Z	X1	X2	ХЗ	X4	Х5	Х6	side
Z 0 1 1.	833	0	0	0 0.	.833	0.667	76.67
X4 1 0 -1	67	0	0	1 -(0.67	-0.33	26.67
X2 2 0 0.	333	1	0	0 0.	.333	-0.33	6.667
X3 3 0 0.	833	0	1	0 -(17	0.667	16.67

題目 4.4-6 (a) (b)

4.4-6.

(a) Optimal Solution: $(x_1^*, x_2^*, x_3^*) = (0, \frac{4}{3}, \frac{4}{3})$ and $Z^* = 14\frac{2}{3}$

```
5 X<sub>2</sub>-
1 X<sub>2</sub>+
0) z-
            3 X1-
                                    6 X3+
                                                0 X4+
                                                            0 X5+
                                                                        0 X6+
                                                                                    0 X_7 = 0
            2 X<sub>1</sub>+
1)
                                    1 X3+
                                                1 X4+
                                                            0 X5+
                                                                        0 X<sub>6</sub>+
                                                                                   0 X_7 = 4
2)
            1 X1+
                        2 X2+
                                    1 X 1+
                                                0 X4+
                                                            1 X5+
                                                                        0 X6+
                                                                                   0 X_7 = 4
3)
            1 X<sub>1+</sub>
                        1 X2+
                                    2 X2+
                                                            0 X5+
                                                0 X4+
                                                                       1 X<sub>6</sub>+
                                                                                   0 X_7 = 4
4)
            1 X<sub>1</sub>+
                                    1 X3+
                        1 X2+
                                                0 X4+
                                                            0 X5+
                                                                        0 X6+
                                                                                   1 X_7 = 3
```

 $x_1 \ge 0$, $x_2 \ge 0$, $x_3 \ge 0$, $x_4 \ge 0$, $x_5 \ge 0$, $x_6 \ge 0$, $x_7 \ge 0$.

```
0 X<sub>1</sub>- 2 X<sub>2</sub>+
1.5 X<sub>1</sub>+ 0.5 X<sub>2</sub>+
0) Z+
                                0 X3+
                     2 X2+
                                           0 X4+
                                                     0 X5+ 3 X6+
                                                                           0 X_7 = 12
1)
                                0 X3+
                                           1 X4+
                                                   0 X5- 0.5 X6+
1 X5- 0.5 X6+
                                                                           0 X_7 = 2
2)
        0.5 X1+ 1.5 X2+
                                0 X3+
                                           0 X4+
                                                                           0 X_7 = 2
3)
        0.5 X1+ 0.5 X2
                                1 X3+
                                           0 X4+
                                                      0 X5+ 0.5 X6+
                                                                           0 X_7 = 2
4)
        0.5 X1+ 0.5 X2+
                                0 X3+
                                           0 X4+
                                                      0 X5- 0.5 X6+
                                                                           1 X_7 = 1
```

 $x_1 \ge 0$, $x_2 \ge 0$, $x_3 \ge 0$, $x_4 \ge 0$, $x_5 \ge 0$, $x_6 \ge 0$, $x_7 \ge 0$.

```
0) Z+0.67 X<sub>1</sub>+
                      0 X<sub>2</sub>+
                                  0 X3+
                                             0 X4+1.33 X5+2.33 X6+
                                                                               0 X_7 = 14.6667
1) 1.333 X<sub>1</sub>+
                      0 X<sub>2</sub>+
                                  0 X3+
                                             1 X4-0.33 X5-0.33 X6+
                                                                               0 X_7 = 1.33333
     0.333 X<sub>1</sub>+
                      1 X2+
2)
                                  0 X3+
                                             0 X4+0.67 X5-0.33 X6+
                                                                             0 X_7 = 1.33333
3)
     0.333 X<sub>1</sub>+
                      0 X<sub>2</sub>+
                                  1 X3+
                                             0 X<sub>4</sub>-0.33 X<sub>5</sub>+0.67 X<sub>6</sub>+
                                                                             0 X_7 = 1.33333
    0.333 X<sub>1</sub>+
                      0 X2+
                                  0 X3+
                                             0 X4-0.33 X5-0.33 X6+
                                                                             1 X_7 = 0.33333
```

 $x_1 \ge 0$, $x_2 \ge 0$, $x_3 \ge 0$, $x_4 \ge 0$, $x_5 \ge 0$, $x_6 \ge 0$, $x_7 \ge 0$.

(b) Optimal Solution: $(x_1^*, x_2^*, x_3^*) = (0, \frac{4}{2}, \frac{4}{2})$ and $Z^* = 14\frac{2}{2}$

(b) Optimal Solution. $(x_1, x_2, x_3) = (0, 3, 3)$ and $z = 14_3$											
Bas	Eq				Coef	ficient	of			Right	
Var	No	Z	X1	X2	Х3	X4	X5	X6	X7	Side	
Z	0	1	-3	-5 _	-6	0	0	0	0	0	
X4	1	0	2	1	1	1	0	0	0	4	
x_5	2	0	1	2	1	0	1	0	0_	4	
Х6	3	0	1	1	2	0	0	1	0	4	
X7	4	0	1	1	1	0	0	0	1	3	
Bas	l Ec	1			Coef	ficient	of			Right	
Var			X ₁	X2	Х3	X4	X5	Х6	X7	Side	
70.2	1	_									
\mathbf{z}	0	1	0	-2	0	0	0	3	0	12	
X4	1	٥	1.5	0.5	0_	1	0	-0.5	0_	2	
X5		0	0.5	1.5	0_	0	1	-0.5	0	2	
ХЗ		0	0.5	0.5	1	0	0	0.5	0	2	
Х7	4	0	0.5	0.5	0	0	0	-0.5	1	1	
Bas	Eσ				Coeff	icient	of		- 1	Right	
Var		z	X ₁	X ₂	Х3	X4	X5	X6	X7	Side	
Z	0	1	0.6667	0	0	0 1	.3333 2	2.3333	0	14.6667	
X4	1	0	1.3333	0	0	1 -	0.333 -	0.333	0	1.33333	
x_2	2	0	0.3333	1	0		.6667 -		0	1.33333	
хз	3	0	0.3333	0	1			.6667	0	1.33333	
X7	4	0	0.3333	0	0	0 -	0.333 -	0.333	1	0.33333	

題目 4.6-2 (a) (b) (c) (d) (e) (f)

4.6-2.

(a) - (b) Initial artificial BF solution: $(0,0,0,0,300,300)\,$

Bas	Eq	Right							
Var	No	Z	x ₁	X2	Хз	X4	X ₅	X ₆	Side
			-10M	-4M	-5M	-7M			
Z	0	1	-4	-2	-3	- 5	0	0	-600M
<u>x</u> 5	1	0	2	3	4	2	1	0	300
$\bar{\mathbf{x}}_{6}$	2	0	. 8	1	1	. 5	0	1	300

Bas	Eq	Ĺ			Right				
Var	No	Z	X ₁	Х2	Хз	X4	X ₅	X ₆	Side
				-2.75M	-3.75M	-0.75M		1.25M	-225M
Z	0	1	0	-1.5	-2.5	-2.5	0	+0.5	+150
$\frac{z}{x_5}$	1	0	0	2.75	3.75	0.75	1	-0.25	225
x_1	2	0	1	0.125	0.125	0.625	0	0.125	37.5

Bas	Eq		Right						
Bas <u>V</u> ar	No	Z	Х1	X ₂	_ X ₃	X4		\bar{x}_6	Side
							1M	1M	
Z	0	1	0	0.3333	0	-2	+0.667	+0.333	300
ХЗ	1	0	0	0.7333	1	0.2	0.2667	-0.067	60
x_1	2	0	1	0.0333	0	0.6	-0.033	0.1333	30

Bas	Eq		Right						
Var	No	2	X ₁	Х2	х3	X4	X ₅	\bar{x}_6	Side
							1M	1M	
Z	0	1	3.3333	0.4444	0	0	+0.556	+0.778	400
Хз	1	0	-0.333	0.7222	1			-0.111	
Z X3 X4	2	0	1.6667	0.0556	0	1	-0.056	0.2222	50

Optimal Solution: $(x_1^\ast, x_2^\ast, x_3^\ast, x_4^\ast) = (0, 0, 50, 50)$ and $Z^\ast = 400$

(c) - (d) - (e) - (f) Initial artificial BF solution: (0,0,0,0,300,300)

Phase 1:

Bas	coefficient of										
Var		Z	Х1	Х2	Х3	Х4	X ₅	\bar{x}_6	Right Side		
Z	0	1	-10	-4	-5	-7	0	0	-600		
<u>X</u> 5	1	0	2	3	4	2	1	0	300		
$\bar{\mathbf{x}}_{6}$	2	0	8	1	1	5	0	1	300		

Bas	Eq	Coefficient of									
Var		_ Z	X1	Х2	Х3	X4	Χ̈́5	x ₆	Side		
<u>z</u>	0	1	0	-2.75	-3.75	-0.75	0	1.25	-225		
<u>Z</u> X5	1	0	0	2.75	3.75	0.75	1	-0.25	225		
x_1	2	0	1	0.125	0.125	0.625	0	0.125	37.5		

Bas	Eq			Coefficient of							
Var	No	2	x ₁	X2	Х3	X4	X ₅	X ₆	Side		
-											
Z	0	1	0	Ò	0	0	1	1	0		
Х3	1	0	0	0.7333	1	0.2	0.2667	-0.067	60		
Z X3 X1	2	0	1	0.0333	0		-0.033		30		

Phase 2:

		Right		
x ₁	Coeffici X2	X3	X4	Side
0	0.7333	0	-2 0.2	300 60
		0 0.3333	0 0.3333 0 0 0.7333 1	0 0.3333 0 -2 0 0.7333 1 0.2

Bas	_		Coefficient of							
Var	No	Z	X ₁	x ₂	Х3	X4	Right Side			
z X3	0		3.3333 -0.333		0	0	400 50			
X4.	2		1.6667		0	1	50			

Optimal Solution: $(x_1^\ast, x_2^\ast, x_3^\ast, x_4^\ast) = (0, 0, 50, 50)$ and $Z^\ast = 400$

題目 4.6-7 (a) (b) (c) (d) (e) (f)

4.6-7. (a) Initial artificial BF solution: (0,0,0,0,20,50)

Bas	Eq		Right						
Bas Var	No	Z	X1	X2	Х́З	X4	\bar{x}_5	- X ₆	Side
	П		-3M	-2M	-2M				
Z	0	1	-2	-5	-3	1M	0	0	-70M
<u>x</u> 5	1	0	1	-2	1	-1	1	0	20
X6	2	0	2	4	1	0	0	1	50

(b) Optimal Solution: $(x_1^\ast, x_2^\ast, x_3^\ast) = (0, 0, 50)$ and $Z^\ast = 150$

Bas Eq	Coefficient of								
Var		Z	X1	X2	Х3	X4	X ₅	\bar{x}_{6}	Side
				-8M	1M	-2M	3M		-10M
z	0	1	. 0	-9	-1	-2	+2	0	+40
v.	1	0	1 [-2	1	-1	1	0	20
<u>⊼</u> 1 X6	2	0	0	8	-1	2	-2	1	10

Bas	Eal		Right						
Var		Z	X1	X2	Х3	X4	X ₅	\bar{x}_6	Side
		10.00					1M	1M	
Z	0	1	0	0	-2.125	0.25	-0.25	+1.125	51.25
x_1	1	0	1	0	0.75	-0.5	0.5	0.25	22.5
\mathbf{x}_{2}	2	0	0	1	-0.125	0.25	-0.25	0.125	1.25

Bas	Eal	Coefficient of								
Var	No	Z	X1	X2	Хз	X4	X5	\bar{x}_{6}	Side	
							1M	1M	984	
z	ol	1	2.8333	0	0	-1.167	+1.167	+1.833	115	
Хa	1	0	1.3333	0	1	-0.667	0.6667	0.3333_	30	
z x ₃ x ₂	2	0	0.1667	1	0	0.1667	-0.167	0.1667	5	

Bas Eq				Right					
Var		Z	X1	X2	Хз	X ₄	X ₅	\bar{x}_6	Side
		_						1M	
z	اه	1	4	7	0	0	1M	+3	150
X3	1	0	2	4	1	0	0	1	50
X4	2	Ō	1	6	0	1	-1	1	30

(c) Initial artificial BF solution: (0, 0, 0, 0, 20, 50)

Phase 1:

Bas	Eq				Coeffic	ient of			Right
Var	No	Z	х1	x ₂	Х3	X4	X ₅	<u>x</u> 6	Right Side
<u>z</u>	0	1	-3	-2	-2	1	0_	0	-70
$\bar{\mathbf{x}}_{5}$	1	0	1	-2	1	-1	1	0	20
X5 X6	2	0	2	4	1	0	0	1	50

(d)

Bas			Coefficient of								
Var	No	Z	X ₁	Х2	Х3	X4	X ₅	X ₆	Right Side		
z <u>X</u> 1 X6	0	1	0	-8 -2	1 1	-2 -1	3 1	0	-10 20		
X61	2	0	0	. 8		2	-2	1	10		

Bas			Coefficient of								
Var	No	Z	х1	_x ₂	Х3	X4	X ₅	<u>x</u> 6	Right Side		
z x ₁ x ₂	0 1 2	0	0 1 0	0 0 1	0 0.75 -0.125	0 -0.5 0.25	1 0.5 -0.25	0.25 0.125	0 22.5 1.25		

(e) - (f) Optimal Solution: $(x_1^*, x_2^*, x_3^*) = (0, 0, 50)$ and $Z^* = 150$

Phase 2:

Bas	Eq	L			Right		
Var		Z	X1	X ₂	Х3	X4	Side
z	0	1	0	0	-2.125	0.25	51.25
x_1	1	0	1	0	0.75	-0.5	22.5
X ₂	2	0	0	1	-0.125	0.25	1.25
Bas	ا	i	,	rooffic	ient of		Right
	_						
Var	No	Z	X1	x ₂	Х3	X4	Side
z	0	1	2.8333	0	0	-1.167	115
Х3	1	٥	1.3333	0	1	-0.667	30
Xo	2		0.1667	1	0	0.1667	5

Bas	Εσ	l	Co	Right			
Bas Var	No	Z	X ₁	Х2	Хз	Х4	Side
Z X3	0 1	1 0	4 2	7 4	0 1	0 0 1	150 50 30

題目 4.6-9 (a) (b)

4.6-9.

(a) Optimal Solution: $(x_1^\ast, x_2^\ast, x_3^\ast) = (0, 15, 15)$ and $Z^\ast = 90$

Bas	Eq		Coefficient of								
Var	No	Z	X1	X2	Х3	X4	X ₅	X ₆	Side		
			-5M	-4M	-8M						
Z	0	1	+3	+2	+4	1M	0	0	-180M		
<u>z</u> X5 X6	1	0	2	1	3_	0	1	0	60		
\bar{x}_6	2	0	3	3	5	-1	0	1	120		
,				_					1		
Bas	Εq				oeffici	ent of			Right		
Var	No	Z	X ₁	X2	Х3	X4	X5	Х6	Side		
			0.333M ·	-1.33M		2.	667M		-20M		
Z	0	1	+0.333	-0.667	0	1M -1	.333	0	-80		
<u>X</u> 3	1	0	0.6667	0.3333	1	0 0.	3333	0	20		
<u>x</u> 3	2	0	-0.333	1.3333	0	-1 -1	.667	1	20		

Bas	Eq	L		Right					
Var	No	Z	X1	x ₂	Х3	X4	X ₅	X ₆	Side
							1M	1M	
Z	0	1	0.5	0	0	0.5	-0.5	-0.5	-90
z x3	1	0	0.75	0	1	0.25	0.75	-0.25	15
x ₂	2	0	-0.25	1	0	-0.75	-1.25	0.75	15

(b) Optimal Solution: $(x_1^*, x_2^*, x_3^*) = (0, 15, 15)$ and $Z^* = 90$

Phase 1:

Bas	Eal	Coefficient of									
Var	No	Z	X ₁	X ₂	Х3	X4	X ₅	х6_	Side		
		1	-5	-4	-8	1 _	0	0	-180		
Ž-	Ĭĭ	ō	2	1	3	0	1	0	60		
X5 X6	2	ŏ	3	3	5	-1	0	1	120		

Bas	Eal		Coefficient of							
Var		13.	32,	Ya	Ya_	X4 X5	X6	Side		
z <u>X</u> 3 X6	0	1 0	0.3333	-1.333 0.3333	0 1	1 2.6667 0 0.3333	0 0 1	-20 20 20		

Bas	Eal		Coefficient of								
Var	No	z	x ₁	x ₂	Х3_	X4	X ₅	X ₆	Side		
z X3 X2	0 1 2	1 0	-3e-20 0.75 -0.25	0 0 1	0 1 0	0 0.25 -0.75	1 0.75 -1.25	1 -0.25 0.75	0 15 15		

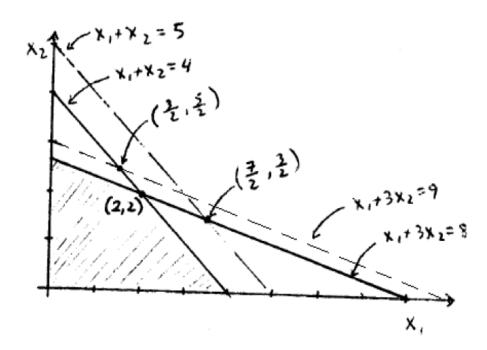
Phase 2:

Bas	Eq	L	C	Right			
Var		Z	x ₁	X ₂	Х3	X4	Side
z	0	1	0.5	0	0	0.5	-90 15
X3 X2	7	lä	0.75	0 1	0	-0.75	15

題目 4.7-2 (a) (b) (c) (d)

4.7-2.

(a)



Constraint (1):
$$x_1 + 3x_2 \le 8$$
: $x_1 + 3x_2 = 8 \Rightarrow x_1 = x_2 = 2$ and $Z = 6$

$$x_1 + 3x_2 = 9 \Rightarrow x_1 = 3/2, x_2 = 5/2 \text{ and } Z = 13/2$$

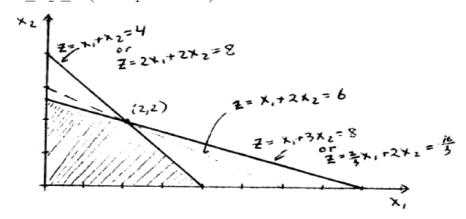
$$\Delta Z = 13/2 - 6 = 1/2 = y_1^*$$
Constraint (2): $x_1 + x_2 \le 4$: $x_1 + x_2 = 4 \Rightarrow x_1 = x_2 = 2$ and $Z = 6$

$$x_1 + x_2 = 5 \Rightarrow x_1 = 7/2, x_2 = 3/2 \text{ and } Z = 13/2$$

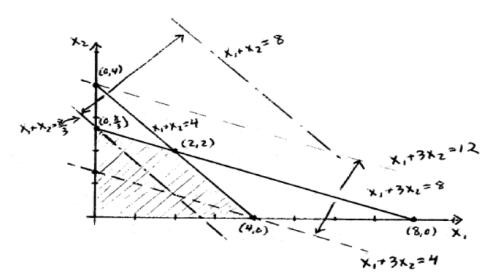
$$\Delta Z = 13/2 - 6 = 1/2 = y_2^*$$

(b) From (a), we see that the right-hand sides $b_1 = 8$ and $b_2 = 4$ are sensitive parameters. The graph in part (a) shows that both constraints are active (binding) at the optimal solution, so all the coefficients $a_{11} = 1$, $a_{12} = 3$, $a_{21} = 1$, and $a_{22} = 1$ are sensitive parameters, too. As will be seen in (c), the objective coefficients $c_1 = 1$ and $c_2 = 2$ are not sensitive parameters.

(c) Observe that the optimal solution remains the same for $2/3 \le c_1 \le 2$ (with $c_2 = 2$ fixed) and $1 \le c_2 \le 3$ (with $c_1 = 1$ fixed)



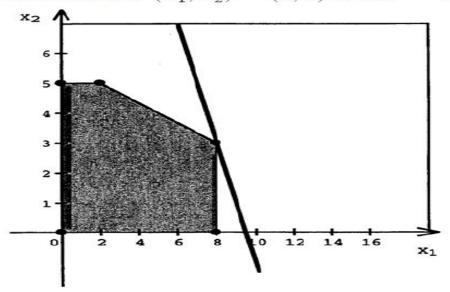
(d) The dashed lines "- - " in the graph below suggest that the CP solution ranges from (4,0) to (0,4) when $4 \le b_1 \le 12$. Outside this range, the CP solution becomes infeasible. The dashed lines "- · -" represent the second constraint for different right-hand side values. They suggest that the CP solution ranges from (0,8/3) to (0,8) when $8/3 \le b_2 \le 8$. Hence, the allowable ranges are $4 \le b_1 \le 12$ and $8/3 \le b_2 \le 8$.



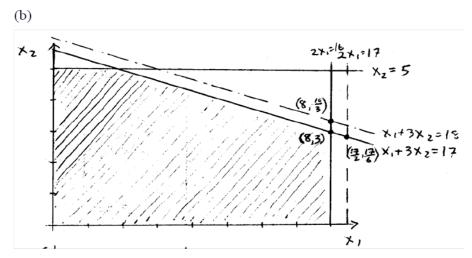
題目 4.7-3

4.7-3.

(a) Optimal Solution: $(x_1^*, x_2^*) = (8, 3)$ and $Z^* = 38$



Corner Point	Z
(8,3)	38*
(8,0)	32
(2,5)	18
(0,5)	10
(0,0)	O



Increasing resource 1 to 17 units increases Z to 4(8.5) + 2(2.83) = 39.67, so $\Delta Z = y_1^* = 1.67$.

Increasing resource 2 to 18 units increases Z to 4(8)+2(3.33)=38.33, so $\Delta Z=y_2^*=0.67$.

The third constraint is not binding, so $y_3^* = 0$.

(c) To increase Z by 15, resource 1 should be increased by $\frac{15}{y_1^*} = \frac{15}{1.67} \approx 9$. Solving the LP problem with resource 1 set to 16 + 9 = 25 returns the result Z = 53.

題目 4.7-4 (a) (b)

4.7-4.

(a) Optimal Solution: $(x_1^\ast, x_2^\ast, x_3^\ast) = (0.5, 0, 4.5)$ and $Z^\ast = 14$

Bas	Eq		Coefficient of								
Var		Z	х1	x ₂	Х3	Х4	X5	Х6	Right Side		
z	0	1	-1	7	-3	0	0	0	0		
Х4	1	0	2	1	-1	1	0	. 0	4		
X 5	2	0	4	-3	0	. 0	1	0	2		
x ₆	3	0	-3	2	1	0	0	1	3		

Bas	Eq		Coefficient of								
Var		Z	x ₁	X2	Х3	X4	X5	X6	Right Side		
Z X4	0	1	-10 -1	13 3	0	0	0	3	9		
X5	2	0	4	-3.	0	0	1	0	2		
x3	3	0	-3	2	1	0	0	1	3		

Bas	Eσ		Coefficient of								
Var		Z	Х1	х2	Хз	X4_	X5	Х6	Side		
z X4 X1 X3	0 1 2	1 0 0 0	0 0 1	5.5 2.25 -0.75 -0.25	0 0 0	0 1 0 0	2.5 0.25 0.25 0.75	3 1 0 1	14 7.5 0.5 4.5		

(b) The shadow prices for the three resources are given by the reduced costs (in the objective function) for the corresponding slack variables. These values are circled in the table above. The shadow prices for resources 1, 2 and 3 are 0, 2.5 and 3 respectively. They represent the rate at which the objective function value z increases as the corresponding resource is increased. For instance, increasing resource 3 by one unit increases Z by 3, provided that no other constraints cause any trouble.

題目 4.7-5(a) (b)

4.7-5.

(a) Optimal Solution: $(x_1^\ast, x_2^\ast, x_3^\ast) = (0,1,3)$ and $Z^\ast = 7$

Bas	Eq										
Var	No	Z	x ₁	x_2	Хз	Х4	X5	Х6	Right Side		
Z	0	1	-2	2 _		0	0	0	0		
X4	1	0	-1	1	1	1	0	0	4		
X5		0	2	1	1	0	1	0	2		
X6	3	0	1	1	3	0	0	1	12		

Bas	Eq		Coefficient of										
Var	No	Z	X ₁	Х2	Х3	X4	X ₅	Х6	Right Side				
z	0	1	4	-1	0	0	3	0	6				
x_4	1	0	-3	2	0	1	-1	0	2				
Хз	2	0	2	-1	1	0	1	0	2				
Х6	3	0	-5	4	0	0	-3	1	6				

Bas	Eq	Coefficient of							Right
Var	No	Z	Х1	x ₂	ХЗ	Х4	X5	Х6	Side
z x ₂ x ₃ x ₆	0 1 2 3	1 0 0 0	2.5 -1.5 0.5	0 1 0	0 0 1 0	0.5 0.5 0.5 -2	2.5 -0.5 0.5 -1	0 0 0	7 1 3 2

(b) The shadow prices are $y_1^*=0.5$, $y_2^*=2.5$ and $y_3^*=0$. They are the marginal values of resources 1, 2 and 3 respectively.