Fall (2024) S. Alghunaim

- Basics operations and statements
- Vectors
- Plotting
- Matrices

### **Outline**

- Basics operations and statements
- Vectors
- Plotting
- Matrices

#### **Basic commands**

MATLAB is a computer program that provides the user with a convenient environment for numerical computations and programming

- When MATLAB is ready to accept instructions, a command prompt (>>) is displayed in the command window
- scalar addition, subtraction, multiplication, division, and exponentiation can be computed using the symbols +, -, \*, / and ^, for example:

```
>> 2+2
ans = 4
```

MATLAB automatically assigns the answer to a variable, ans; example:

```
>> ans*2
ans = 8
```

• assignment of values to variables can be done using equal sign; example:

```
\Rightarrow a=2.23 a = 2.2300
```

creates a variable named "a" with value equal to 2.23 and displays result

- result can be suppressed by terminating the command line with semicolon (;)
- text after (%) on same line are treated as comments and ignored
   >> a=4; create variable 'a' with value 4 without displaying result
- you can type several commands on same line by separating them with commas or semicolons; if you separate them with commas, they will be displayed
   >> a = 4, A = 6; x = 1;
- e is used for powers of ten (e.g.,  $10^2$  can be found using 1e2 or 10^2)
- MATLAB predefines the variables
  - $pi = \pi$ -  $i = j = \sqrt{-1}$  (imaginary number)
  - Inf = ∞ and NaN means not a number
  - for example, we can create a complex number

>> x=pi+2i x = 3.1416 + 2i

a = 4

 MATLAB displays four decimal points; for additional precision, use format long; we can switch back using format short

- clear command deletes all objects from the workspace
- clear followed by the names of the variables removes specific variables; e.g.,
   clear a %removes the variable 'a' from the workspace
- clc command clears the command window
- save command, followed by the desired filename, saves the workspace to a file, which has the .mat extension
- load command followed by the filename is used to load the data and objects contained in a MATLAB data file (.mat file)
- in the command window, pressing the up or down arrow key scrolls through previous commands and redisplays them at the command prompt
  - typing the first few characters and then pressing the arrow keys scrolls through the previous commands that start with the same characters
  - the arrow keys allow command sequences to be repeated without retyping

### **Built-in functions**

| function       | command  |
|----------------|----------|
| $\sqrt{x}$     | sqrt(x)  |
| $e^x$          | exp(x)   |
| $\sin(x)$      | sin(x)   |
| $\cos(x)$      | cos(x)   |
| tan(x)         | tan(x)   |
| $\tan^{-1}(x)$ | atan(x)  |
| $\log_{10} x$  | log10(x) |
| $\ln x$        | log(x)   |

### **Complex numbers**

| command  | meaning                |
|----------|------------------------|
| real(x)  | real part of $x$       |
| imag(x)  | imaginary part of $x$  |
| abs(x)   | absolute value of x    |
| angle(x) | phase of $x$ in rad/s  |
| conj(x)  | complex conjugate of x |

(for list of functions type help elfun)

# Rounding and remainder

| command  | meaning                                   |
|----------|---|
| round(x) | rounds to nearest integer                 |
| fix(x)   | rounds to nearest integer towards zero    |
| floor(x) | rounds down (towards negative infinity)   |
| ceil(x)  | rounds up (towards positive infinity)     |
| mod(x,y) | modulus (signed remainder after division) |
| rem(x,y) | remainder after division                  |

### Example

```
>> x = 2.3 - 4.7*i;
>> round(x);  % results in (2 - 5i)
>> fix(x);  % results in (2 - 4i)
>> floor(x);  % results in (2 - 5i)
>> ceil(x);  % results in (3 - 4i)
```

# **Strings**

 character strings can be represented by enclosing the strings within single quotation marks; for example

```
>> f = 'Miles';
>> s = 'Davis';
```

• we can concatenate (i.e., paste together) strings as in

```
>> x = [f s]
x =
Miles Davis
```

- str2num(s) converts string s to a number
- num2str(n) converts number n to a string

# Relational operations

a relational operator compares two items and indicates whether a condition is true

| relational ope | erator | meaning                  |
|----------------|--------|--------------------------|
| <              |        | less than                |
| >              |        | greater than             |
| <=             |        | less than or equal to    |
| >=             |        | greater than or equal to |
| ==             |        | equal to                 |
| ~=             |        | not equal to             |

- if true, a logical true (1) is returned; else, a logical false (0) is returned
- for example

```
>> 1>2
ans =
logical
0
```

# **Logical operations**

| logical operator | meaning          |
|------------------|------------------|
| &                | logical AND      |
| 1                | logical OR       |
| ~                | logical negation |

- relational operators can be combined using logical operators
- for example, we can test the condition 0 < t < 1 using

#### If statements

• if statements execute commands if a certain condition is met

```
if condition
statements
else
statments
end
```

• **example:** set x = 5 if a > 0 and x = 100 otherwise

```
>> a = 15;
>> if a > 0,
    x = 5;
    else
    x = 100
    end
```

### For loop

• for statements loop a specific number of times, and keep track of iteration index

```
for index = values
statements
end
```

• example: determine the product of all prime numbers between 1 and 20

```
>> result = 1;
>> for n = 1:20 % iterate over 'n' from 1 to 20
   if isprime(n) % built-in function
   result = result*n;
   end
   end
```

# While loop

while statements loop as long as a condition remains true

```
while expression statements end
```

**example:** find the first integer n for which factorial(n) is a 100-digit number

```
n = 1;
nFact = 1;
while nFact < 1e100
n = n + 1;
nFact = nFact * n;
end</pre>
```

# **Anonymous function**

an *anonymous function* provides a symbolic representation of a function defined in terms of MATLAB operators, functions, or other anonymous functions

**Example:** we can define  $f(t) = e^{-t} \cos(2\pi t)$  as

```
>> f = Q(t) \exp(-t)*\cos(2*pi*t);
```

- symbol @ identifies the expression as an anonymous function
- parentheses following @ symbol are used to identify variables (input arguments)
- f(t) can be evaluated simply by passing the input values of interest
   t = 0; f(t)

```
>> t = 0; f(t ans = 1
```

# **Example: piecewise functions**

• the unit step function

$$u(t) = \begin{cases} 1 & t \ge 0 \\ 0 & t < 0 \end{cases}$$

can be created using the command

$$y = 0(t) 1.0*(t>=0);$$

the function

$$f(t) = \begin{cases} 1 & 0 \le t \le 2\\ -t & -1 \le t < 0 \end{cases}$$

can be created using the command

>> f = 
$$@(t) 1.0*((t>=0)&(t<=2))-t*((t<0)&(t>=-1));$$

#### **Functions M-files**

- script M-files file is a series of commands saved on a file that can be run at once
- function M-files can accept input arguments as well as return outputs
- a function M-file is identical to a script M-file except for the first line
- the general form of the first line is function [outputs] = filename(inputs)
- an M-file is executed by simply typing the filename (without the .m extension)

### Example

#### M-file content

```
function [f1] = myfirsfunx(x)
% input x, output f1
f1 = sin(pi*x); % Calculate function f1
end
```

#### **Execute function M-file**

```
>> x = 2; % Define the input argument
>> [y] = myfirstfunc(x); % Output value is returned to y
```

### **Outline**

- Basics operations and statements
- Vectors
- Plotting
- Matrices

#### **Vectors**

vector arrays are created using square brackets and semicolon

• we can create the row vector  $x = [1 \ 2 \ 3]$  by the command

>> 
$$x = [1 \ 2 \ 3]$$
  
 $x = 2 \ 0 \ 3$ 

• we can create the column vector  $y = \begin{bmatrix} -1 \\ -2 \\ -3 \end{bmatrix}$  using the command

(conjugate) transpose of a vector can be found using apostrophe

-3

# Vector indexing and operations

### Vector indexing

- the nth element of x can be extracted using x(n)
- we can use indexing to get a slice of a vector; for example, x(98:100) gives a vector (x(98),x(99),x(100))
- end command automatically references the final index of an array; for example,

```
>> x(end-9:end) % extract final 10 values of vector x
```

we can concatenate vectors to create a larger vector

```
>> a=[1;2];b=[1;1];c=[-1;-1]
>> d=[a;b;c]; % create concatenated vector
```

### **Vector operations**

- vector addition and subtraction are carried out using the commands +, -
- element-by-element operations are computed using (.\*, ./,.^); example:

```
>> u=[1 2 3]; v=[-1 -2 -3];
>> w=u.*v
w = -1 -5 -9
```

### **Basic vector commands**

| command                      | meaning   |
|------------------------------|---|
| a:b:c                        | vector with elements between a and c with increments b      |
|                              | (command a:c assumes increment of 1)                        |
| <pre>linspace(x1,x2,n)</pre> | n-vector from x1 to x2 with equal spacing (x2-x1)/(n-1)     |
| logspace(x1,x2,n)            | $n$ -vector from $10^{x1}$ to $10^{x2}$ logarithmic spacing |
| sum(x)                       | sums the elements of a vector x                             |
| prod(x)                      | return products of entries x                                |
| max(x)                       | return max value in x                                       |
| min(x)                       | return min value in x                                       |
| sort(x)                      | sorts elements in ascending order                           |
| ones(1,n)/zeros(1,n)         | row $n$ -vector of all ones/zeros                           |
| ones(n,1)/zeros(n,1)         | column <i>n</i> -vector of all ones/zeros                   |
| length(x)                    | returns the length of the vector x                          |
| x'y rr dot(x,y)              | return inner (dot) product between vectors $x$ and $y$      |
| norm(x)                      | return the 2-norm of vector x                               |

#### **Functions of vectors**

- common built in functions operates elementwise on vectors and matrices
- example: to compute  $\sqrt{x}$  for all values (1, 2, ..., 100), we can use >> x = 1:100; y=sqrt(x);
- vectors can be used to represent points of a function f over some interval
- for example, we can represent  $f = \sin(2\pi 10t + \pi/6)$  over  $0 \le t \le 2$  using >> t = linspace(0,2,500); %500 points between 0 and 2 >> f =  $\sin(2*pi*10*t+pi/6)$
- indexing in Matlab starts from 1
- for example, the value of f(t) at t=0 is the first element of the vector f(1)

# **Example**

$$x = \begin{bmatrix} 1 & 4 & -2 & (3-j2) \end{bmatrix}$$
$$y = \begin{bmatrix} -3 & (5+j7) & 6 & 2 \end{bmatrix}$$

### use Matlab to compute

- (a) x + y
- (b) inner product  $x^*y$
- (c) mean or average  $avg(x) = (1/4) \sum_{k=1}^{4} x(k)$
- (d) average energy  $E_x = (1/4) \sum_{k=1}^{4} |x(k)|^2$
- (e) variance  $var(x) = (1/4) \sum_{k=1}^{4} |x(k) avg(x)|^2$

#### Solution:

```
(a) >> x = [1 \ 4 \ -2 \ 3-2*i];
   y = [-3 5+7*i 6 2];
   >> sum_xy = x + y;
(b) \Rightarrow dot_xy = dot(x,y);
   >> dot_xy = x*y'; % alternative computation
(c) >> mean_x = sum(x)/length(y);
   >> mean_x = mean(x); % alternative computation
(d) >> avg_x = sum(x.*conj(x))/length(x);
   >> avg_x = sum(x*x')/length(x); % alternative computation
   >> avg_x = norm(x)^2/length(x); % alternative computation
   >> avg_x = mean(abs(x).^2); % alternative computation
(e) >> z=x-mean(x);
   >> var_x = sum(z.*conj(z))/length(x);
   >> var_x = sum(z*z'))/length(x); % alternative computation
   >> var_x = mean(|z|.^2); % alternative computation
```

### **Outline**

- Basics operations and statements
- Vectors
- Plotting
- Matrices

#### Plot commands

| command       | meaning                                       |
|---------------|---|
| plot(x,y)     | Plots the vector x versus the vector y        |
| semilogx(x,y) | The x-axis is log10; the y-axis is linear     |
| semilogy(x,y) | The x-axis is linear; the y-axis is log10.    |
| loglog(x,y)   | Creates a plot with log10 scales on both axes |

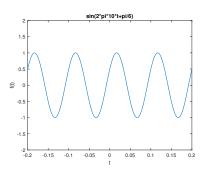
there are also several other 2D graphical functions in MATLAB including

```
stem, bar, hist, polar, stairs,...
```

- · clf command clears the current figure window
- axis equal command ensures that the scale used for the horizontal axis is equal to the scale used for the vertical axis
- we can add labels, change axis range, plot color,...etc

#### Plot command

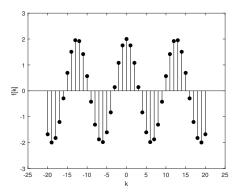
```
>> t = linspace(-0.2,0.2,500);
>> f = sin(2*pi*10*t+pi/6);
>> plot(t,f);
>> axis([-0.2 0.2 -2 2]) % plot range
>> xlabel('t'); ylabel('f(t)'); % label the x and y axis
>> title('sin(2*pi*10*t+pi/6)'); %label the title
```



#### Stem command

the stem command can be used to plot f[k] against discrete k

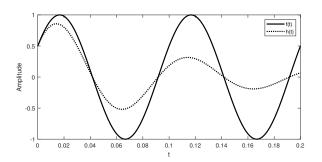
```
>> k = -20:20;
>> f = 2*cos(0.5*k);
>> stem(k,f,,k,'filled'); %'k' for black and filled circle
>> xlabel('k'); ylabel('f[k]');
>> axis([-25 25 -3 3])
```



### Multiple curves

plot command can accommodates multiple curves

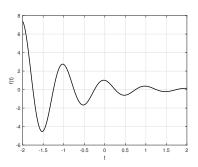
```
>> t = linspace(0,0.2,500);
>> f = sin(2*pi*10*t+pi/6);
>> g = exp(-10*t);
>> h = f.*g;
>> plot(t,f,'-k',t,h,':k','linewidth',2);
>> xlabel('t'); ylabel('Amplitude');
>> legend('f(t)','h(t)');
```



# Plotting using anonymous functions

we can use anonymous functions for potting

```
>> f = @(t) exp(-t).*cos(2*pi*t);
>> t = (-2:0.01:2);
>> plot(t,f(t),'k','linewidth',1.4);
>> xlabel('t'); ylabel('f(t)');
>> grid; % adds grid lines
```



### Example

```
plot f(t) = e^{-t}u(t) over -1 \le t \le 3:

>> u = @(t) 1.0*(t>0);

>> f = @(t) \exp(-t).*u(t);

>> t = -1:0.0001:3;

>> subplot(2,1,1) % create multiple graphs in one figure

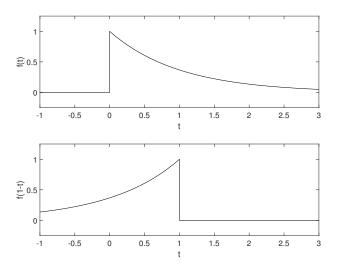
>> plot(t,f(t),'k')

>> axis([-1 3 -0.25 1.25]);

>> xlabel('t'); ylabel('f(t)');
```

we can also evaluate a function by passing it an expression; this makes it very convenient to evaluate expressions such as f(1-t), for example:

```
>> subplot(2,1,2)
>> plot(t,f(1-t),'k')
>> axis([-1 3 -0.25 1.25]);
>> xlabel('t'); ylabel('f(1-t)');
```



### **Outline**

- Basics operations and statements
- Vectors
- Plotting
- Matrices

### **Matrices**

matrices can be created similar to vectors using square brackets and semicolon

• we can create the  $3 \times 4$  matrix  $A = \begin{bmatrix} 2 & 3 \\ 4 & 5 \\ 0 & 6 \end{bmatrix}$  by the command

• (conjugate) transpose of a matrix can be found using apostrophe

>> A' ans = 2 4 0 3 5 6

# Matrix indexing

- element (k, l) of matrix A can be extracted using A(k,1)
- subblocks of A can be extracted using indexing; for example

```
>> A = [1 2 3;
0 4 5;
0 0 6];
>>A(1:2,2:3)
ans = 2 3
4 5
A(2,:) selects all column elements along the second row
>> A(2,:)
ans = 0 4 5
```

we can concatenate arrays to create larger arrays; for example

```
>> a = [1;0;0]; B = [2 3;4 5;0 6]
>> C = [a B]
C = 1 2 3
0 4 5
0 0 6
```

• repmat command replicate objects; for example

### **Matrix operations**

- matrix addition and multiplications are carried out using the commands +, -, \*
- matrix power can be found using ^ (e.g., A^3)
- element-by-element operations are computed using .\*, ./,.^
- passing a matrix into a function computes the function element-wise

**Linear equation:** we can solve Ax=b using inv(A)\*b; or by backlash operator (left division),

 $x=A\b$ 

which is more computationally efficient

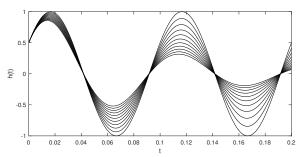
# **Basic matrix commands**

| command                  | meaning  |
|--------------------------|--|
| sum(A)                   | returns a row vector containing the sum of each column |
| sum(A,2)                 | returns a column vector containing the sum of each row |
| <pre>sum(A,"all")</pre>  | returns the sum of all elements of A                   |
| prod(A)                  | returns a row vector containing the sum of each column |
| <pre>max(A)/min(A)</pre> | return max/min value in A                              |
| eye(m)                   | $m \times m$ identity matrix                           |
| ones(m,n)/zeros(m,n)     | $m \times n$ matrix of all ones/zeros                  |
| diag(x)                  | creates diagonal matrix with diagonal elements x       |
| length(A)                | returns the length of the largest array dimension in A |
| size(A)                  | returns the size of the array A                        |
| det(A)                   | determinant of a square matrix A                       |
| inv(A)                   | inverse of a square matrix A                           |
| eig(A)                   | computes eigenvalues and eigenvectors of A             |
| rank(A)                  | computes rank of A                                     |
| norm(A)                  | return the 2-norm of A                                 |
| <pre>norm(A,"fro")</pre> | return the Frobenius norm of A                         |

# Family of curves

matrices can be used to create a family of curves

```
>> alpha = (0:10);
>> t = (0:0.001:0.2)'; %defined as column vector
>> T = repmat(t,1,11); %matrix T, columns t repeated 11 times
>> H = exp(-T*diag(alpha)).*sin(2*pi*10*T+pi/6);
>> plot(t,H,'k'); xlabel('t'); ylabel('h(t)');
```



 $h_{\alpha}(t) = e^{-\alpha t} \sin(2\pi 10t + \pi/6)$  for  $\alpha = [0, 1, ..., 10]$