

# Team notebook

December 12, 2015

## Contents

<b>1 DS</b>	<b>1</b>
1.1 LazySegtree . . . . .	1
1.2 PersistentSegtree . . . . .	1
1.3 TreapBst . . . . .	2
1.4 TreapIntervalTree . . . . .	2
<b>2 Geometry</b>	<b>3</b>
2.1 ConvexHull . . . . .	3
2.2 GeometryTemplate . . . . .	3
<b>3 Graphs</b>	<b>5</b>
3.1 AuxillaryTree . . . . .	5
3.2 BCC . . . . .	6
3.3 BridgeTree . . . . .	7
3.4 CentroidDecomposition . . . . .	7
3.5 Dinics . . . . .	8
3.6 HLD . . . . .	9
3.7 HopcroftKarp . . . . .	9
3.8 Hungarian . . . . .	10
3.9 MinCostMaxFlow . . . . .	11
3.10 SCC . . . . .	12
<b>4 Math</b>	<b>12</b>
4.1 ExtendedGCD . . . . .	12
4.2 FFT . . . . .	13
4.3 MatrixDeterModP . . . . .	14
4.4 MatrixInverse . . . . .	14
4.5 MatrixRank . . . . .	14
4.6 MillerRabin . . . . .	15
4.7 QuadraticResidue . . . . .	15

4.8 Simplex . . . . .	16
4.9 nCrLarge . . . . .	16

<b>5 String</b>	<b>17</b>
5.1 KMP . . . . .	17
5.2 SuffixArray . . . . .	17
5.3 ZAlgo . . . . .	18
<b>6 Theory</b>	<b>19</b>
<b>7 template</b>	<b>19</b>

## 1 DS

### 1.1 LazySegtree

---

//to be coded

---

### 1.2 PersistentSegtree

---

```
const int N = int(1e5)+10;
const int MX = int(2e9)+10;
const int LOGN = 60;
int L[N*LOGN],R[N*LOGN],ST[N*LOGN],blen,root[N],A[N];
//sparse persistent-segment tree
//stores range sum. initially full range is 0
int update(int pos,int add,int l,int r,int id){
    if(l>pos || r<=pos)return id;
    int ID = ++blen;
    if(l==r-1){
```

```

        ST[ID]=ST[id]+add;
        return ID;
    }
    int m=l+(r-1)/2;
    L[ID]=update(pos,add,l,m,L[id]);
    R[ID]=update(pos,add,m,r,R[id]);
    ST[ID]=ST[L[ID]]+ST[R[ID]];
    return ID;
}
root[0]=++blen;
for(int i=1;i<=n;i++)
    root[i]=update(A[i],1,0,MX,root[i-1]);

```

---

### 1.3 TreapBst

```

#include<bits/stdc++.h>
using namespace std;
typedef struct node{
    int val,prior,size;
    struct node *l,*r;
}node;
typedef node* pnode;
int sz(pnode t){
    return t?t->size:0;
}
void upd_sz(pnode t){
    if(t)t->size = sz(t->l)+1+sz(t->r);
}
void split(pnode t,pnode &l,pnode &r,int key){
    if(!t)l=r=NULL;
    else if(t->val<=key)split(t->r,t->r,r,key),l=t; //elem=key comes in l
    else split(t->l,l,t->l,key),r=t;
    upd_sz(t);
}
void merge(pnode &t,pnode l,pnode r){
    if(!l || !r)t=l?l:r;
    else if(l->prior > r->prior)merge(l->r,l->r,r),t=l;
    else merge(r->l,l,r->l),t=r;
    upd_sz(t);
}
void insert(pnode &t,pnode it){
    if(!t) t=it;

```

```

        else if(it->prior>t->prior)split(t,it->l,it->r,it->val),t=it;
        else insert(t->val<it->val?t->r:t->l,it);
        upd_sz(t);
    }
    void erase(pnode &t,int key){
        if(!t)return;
        else if(t->val==key){pnode temp=t;merge(t,t->l,t->r);free(temp);}
        else erase(t->val<key?t->r:t->l,key);
        upd_sz(t);
    }
    void unite (pnode &t,pnode l, pnode r) {
        if (!l || !r) return void(t = l ? l : r);
        if (l->prior < r->prior) swap (l, r);
        pnode lt, rt;
        split (r,lt, rt,l->val);
        unite (l->l,l->l, lt);
        unite (l->r,l->r, rt);
        t=l;upd_sz(t);
    }
    pnode init(int val){
        pnode ret = (pnode)malloc(sizeof(node));
        ret->val=val;ret->size=1;ret->prior=rand();ret->l=ret->r=NULL;
        return ret;
    }
    insert(init(x),head);

```

---

### 1.4 TreapIntervalTree

```

#include<bits/stdc++.h>
using namespace std;
typedef struct node{
    int prior,size;
    int val; //value stored in the array
    int sum; //whatever info you want to maintain in segtree for each node
    int lazy; //whatever lazy update you want to do
    struct node *l,*r;
}node;
typedef node* pnode;
int sz(pnode t){
    return t?t->size:0;
}
void upd_sz(pnode t){

```

```

        if(t)t->size=sz(t->l)+1+sz(t->r);
    }
    void lazy(pnode t){
        if(!t || !t->lazy)return;
        t->val+=t->lazy;//operation of lazy
        t->sum+=t->lazy*sz(t);
        if(t->l)t->l->lazy+=t->lazy;//propagate lazy
        if(t->r)t->r->lazy+=t->lazy;
        t->lazy=0;
    }
    void reset(pnode t){
        if(t)t->sum = t->val;//no need to reset lazy coz when we call this
        lazy would itself be propagated
    }
    void combine(pnode& t,pnode l,pnode r){//combining two ranges of segtree
        if(!l || !r)return void(t = l?l:r);
        t->sum = l->sum + r->sum;
    }
    void operation(pnode t){//operation of segtree
        if(!t)return;
        reset(t);//reset the value of current node assuming it now
        represents a single element of the array
        lazy(t->l);lazy(t->r);//imp:propagate lazy before combining
        t->l,t->r;
        combine(t,t->l,t);
        combine(t,t->r);
    }
    void split(pnode t,pnode &l,pnode &r,int pos,int add=0){
        if(!t)return void(l=r=NULL);
        lazy(t);
        int curr_pos = add + sz(t->l);
        if(curr_pos<=pos)//element at pos goes to left subtree(l)
            split(t->r,t->r,r,pos,curr_pos+1),l=t;
        else split(t->l,l,t->l,pos,add),r=t;
        upd_sz(t);
        operation(t);
    }
    void merge(pnode &t,pnode l,pnode
    r){//l->leftarray,r->rightarray,t->resulting array
        lazy(l);lazy(r);
        if(!l || !r) t = l?l:r;
        else if(l->prior>r->prior)merge(l->r,l->r,r),t=l;
        else merge(r->l,l,r->l),t=r;
        upd_sz(t);
        operation(t);
    }

```

```

    }
    pnode init(int val){
        pnode ret = (pnode)malloc(sizeof(node));
        ret->prior=rand();ret->size=1;
        ret->val=val;
        ret->sum=val;ret->lazy=0;
        return ret;
    }
    int range_query(pnode t,int l,int r){//[l,r]
        pnode L,mid,R;
        split(t,L,mid,l-1);
        split(mid,t,R,r-1);//note: r-1!!
        int ans = t->sum;
        merge(mid,L,t);
        merge(t,mid,R);
        return ans;
    }
    void range_update(pnode t,int l,int r,int val){//[l,r]
        pnode L,mid,R;
        split(t,L,mid,l-1);
        split(mid,t,R,r-1);//note: r-1!!
        t->lazy+=val; //lazy_update
        merge(mid,L,t);
        merge(t,mid,R);
    }

```

## 2 Geometry

### 2.1 ConvexHull

---

//to be done

---

### 2.2 GeometryTemplate

---

```

//Tanuj Khattar
#include<bits/stdc++.h>

using namespace std;

typedef pair<int,int> II;

```

```

typedef vector< II > VII;
typedef vector<int> VI;
typedef vector< VI > VVI;
typedef long long int LL;
typedef unsigned long long int ULL;

#define PB push_back
#define MP make_pair
#define F first
#define S second
#define SZ(a) (int)(a.size())
#define ALL(a) a.begin(),a.end()
#define SET(a,b) memset(a,b,sizeof(a))
#define LET(x,a) __typeof(a) x(a)

#define rep(i, begin, end) for (__typeof(end) i = (begin) - ((begin) >
    (end)); i != (end) - ((begin) > (end)); i += 1 - 2 * ((begin) >
    (end)))
//Works for forward as well as backward iteration

#define gu getchar
#define pu putchar
#define si(n) scanf("%d",&n)
#define dout(n) printf("%d\n",n)
#define sll(n) scanf("%lld",&n)
#define lldout(n) printf("%lld\n",n)

#define DRT() int t; si(t); while(t--)

#define PLUSWRAP(index,n) index = (index+1)%n //index++;
    if(index>=n) index=0
#define MINUSWRAP(index,n) index = (index + n -1)%n //index--;
    if(index<0) index=n-1
#define ROUNDOFFINT(d) d = (int)((double)d + 0.5) //Round off d to
    nearest integer

#define FLUSHN while(gu()!='\n')
#define FLUSHS while(gu()!=' ')

#define TRACE

#ifdef TRACE
#define trace1(x) cerr << #x << ": " << x << endl;
#define trace2(x, y) cerr << #x << ": " << x << " | " << #y <<
    ": " << y << endl;

```

```

#define trace3(x, y, z) cerr << #x << ": " << x << " | " << #y <<
    ": " << y << " | " << #z << ": " << z << endl;
#define trace4(a, b, c, d) cerr << #a << ": " << a << " | " << #b <<
    ": " << b << " | " << #c << ": " << c << " | " << #d << ": " << d <<
    endl;
#define trace5(a, b, c, d, e) cerr << #a << ": " << a << " | " << #b <<
    ": " << b << " | " << #c << ": " << c << " | " << #d << ": " << d <<
    " | " << #e << ": " << e << endl;
#define trace6(a, b, c, d, e, f) cerr << #a << ": " << a << " | " << #b
    << ": " << b << " | " << #c << ": " << c << " | " << #d << ": " << d
    << " | " << #e << ": " << e << " | " << #f << ": " << f << endl;

#else

#define trace1(x)
#define trace2(x, y)
#define trace3(x, y, z)
#define trace4(a, b, c, d)
#define trace5(a, b, c, d, e)
#define trace6(a, b, c, d, e, f)

#endif

//FILE *fin = freopen("in","r",stdin);
//FILE *fout = freopen("out","w",stdout);

const double EPS = 1e-9;
const double PI = 22.0/7.0;
double DEG_to_RAD(double theta)
{
    return ((theta*PI)/180.0);
}
//***** Point *****
class point{
public:
    double x,y;
    point(){x=0;y=0;}
    point(double _x,double _y) : x(_x),y(_y){}
    bool operator < (point other) const
    {
        if(fabs(x - other.x)>EPS)
            return x<other.x;
        return y<other.y;
    }
    bool operator == (point other) const

```

```

        {
            return ((fabs(x - other.x)<EPS) && (fabs(y -
                other.y)<EPS));
        }
};

double dist(point p1,point p2){
    return hypot(p1.x-p2.x,p1.y-p2.y);
}

//rotate p by theta "degrees" counter clockwise wrt origin (0,0)
point rotate(point p,double theta){
    double rad = DEG_to_RAD(theta);
    return point(p.x*cos(rad) - p.y*sin(rad) , p.x*sin(rad) +
        p.y*cos(rad));
}

// ***** LINE *****

// We represent it as ax+by+c=0 where b = 1 always. i.e. a/b x + y + c/b
=0 or y = -a/b x + (-c/b) or y = (-A)x + (-C)

class line{
public :
    double a,b,c;
    line(point p1,point p2)
    {
        if(fabs(p1.x-p2.x)<EPS) //vertical line
        {
            a = 1.0;
            b = 0.0;
            c = -p1.x;
        }
        else
        {
            a = -(double)(p2.y-p1.y)/(p2.x-p1.x);
            b = 1;
            c = -(p1.y + a*p1.x);
        }
    }
};

bool areParallel(line l1,line l2)
{
    return ((fabs(l1.a-l2.a)<EPS) && (fabs(l1.b-l2.b)<EPS));
}

bool areSame(line l1,line l2)
{

```

```

        return (areParallel(l1,l2) && (fabs(l1.c-l2.c)<EPS));
    }
bool areIntersect(line l1,line l2,point &p)
{
    if(areParallel(l1,l2)) return false;

    //solve system of 2 linear algebraic equations with 2 unknowns
    p.x = (l2.b*l1.c - l1.b*l2.c)/(l2.a*l1.b - l1.a*l2.b);
    //special case for vertical line to avoid division by zero.
    if(fabs(l1.b)>EPS)
        p.y = -(l1.a*p.x + l1.c);
    else
        p.y = -(l2.a*p.x + l2.c);

    return true;
}

int main()
{

    return 0;
}

```

## 3 Graphs

### 3.1 AuxillaryTree

```

//Q[]: array containing k nodes of auxillary tree
//arr[] : arrival time of nodes
//anc(p,u) : returns true if p is ancestor of u
//VI tree[N] : final auxillary tree with O(k) nodes
bool cmp(int u,int v){
    return arr[u]<arr[v];
}

int create_tree(){//return root of tree
    set<int> S;//get distinct nodes
    for(int i=0;i<k;i++)
        S.insert(Q[i]);

    k=0;
    for(auto it=S.begin();it!=S.end();it++)

```

```

        Q[k++] = *it;
    sort(Q, Q+k, cmp);
    int kk = k; // number of distinct initial nodes
    // add lca of adjacent pairs
    for(int i=0; i<kk-1; i++){
        int x = lca(Q[i], Q[i+1]);
        if(S.count(x)) continue;
        Q[k++] = x;
        S.insert(x);
    }
    sort(Q, Q+k, cmp);
    stack<int> s;
    s.push(Q[0]);
    for(int i=1; i<k; i++){
        while(!anc(s.top(), Q[i])) s.pop();
        tree[s.top()].PB(Q[i]);
        tree[Q[i]].PB(s.top());
        s.push(Q[i]);
    }
    return Q[0];
}

```

## 3.2 BCC

```

const int N = int(2e5) + 10;
VI g[N], tree[N]; // graph is stored in edge list form
int U[N], V[N], vis[N], numComp, compNo[N], arr[N], t;
stack<int> S;
bool isArtic[N];
set<int> compNodes[N]; // contains indexes of nodes in i'th BCC
// compNo[i] : if node i (original graph) is an articulation point, then
//              corresponding Ci in block tree
//              else the Bi in the tree where the node lies
int dfs(int u, int p){
    arr[u] = t++; vis[u] = 1;
    int dbe = arr[u], dfsChild = 0;
    for(int i=0; i<SZ(g[u]); i++){
        int e = g[u][i], w = (U[e]==u?V[e]:U[e]);
        if(!vis[w]){
            S.push(e); dfsChild++;
            int wbe = dfs(w, u); // Back edge coming from w;
            dbe = min(dbe, wbe);
            if((arr[u]==0 && dfsChild>1) || (wbe >= arr[u] && arr[u]>0)){

```

```

                // u is an articulation vertex "wrt" to the subtree of w .
                isArtic[u] = true;
            }
            if(compNo[u]==-1){
                compNo[u] = numComp;
                compNodes[numComp].insert(u);
                numComp++;
                compNodes[numComp].insert(u);
            }
            while(S.top()!=e){
                compNodes[numComp].insert(U[S.top()]);
                compNodes[numComp].insert(V[S.top()]);
                S.pop();
            }
            compNodes[numComp].insert(U[S.top()]);
            compNodes[numComp].insert(V[S.top()]);
            S.pop();
            for(set<int>::iterator
                it=compNodes[numComp].begin(); it!=compNodes[numComp].end(); it++){
                if(isArtic[*it]){
                    tree[numComp].PB(compNo[*it]);
                    tree[compNo[*it]].PB(numComp);
                }
                else
                    compNo[*it] = numComp;
                numComp++;
            }
        }
    }
    else if(w!=p && arr[w]<dbe) {
        dbe = min(dbe, arr[w]);
        S.push(e);
    }
}
return dbe;
}

void buildTree(int n)
{
    SET(compNo, -1); SET(vis, 0);
    for(int i=0; i<n; i++){
        if(vis[i]) continue;
        t=0; dfs(i, i);
        if(!S.empty()){
            while(!S.empty()){
                compNodes[numComp].insert(U[S.top()]);
                compNodes[numComp].insert(V[S.top()]);

```

```

    S.pop();
}
for(set<int>::iterator it =
    compNodes[numComp].begin(); it!=compNodes[numComp].end(); it++)
    if(isArtic[*it]){
        tree[numComp].PB(compNo[*it]);
        tree[compNo[*it]].PB(numComp);
    }
    else
        compNo[*it]=numComp;
    numComp++;
}
}
//buildTree(n);//builds the block cut tree;

```

---

### 3.3 BridgeTree

```

VI tree[N],graph[N]; //edge list representation of graph
int U[M],V[M],vis[N],arr[N],T,cmpno;
bool isbridge[M]; // if i'th edge is a bridge edge or not
queue<int> Q[N];
int adj(int u,int e){
    return U[e]==u?V[e]:U[e];
}
int dfs0(int u,int edge){ //mark bridges
    vis[u]=1;arr[u]=T++;
    int dbe = arr[u];
    for(int i=0;i<SZ(graph[u]);i++){
        int e = graph[u][i];
        int w = adj(u,e);
        if(!vis[w])dbe = min(dbe,dfs0(w,e));
        else if(e!=edge)dbe = min(dbe,arr[w]);
    }
    if(dbe == arr[u] && edge!=-1)isbridge[edge]=true;
    return dbe;
}
void dfs1(int v){ //Build the bridge tree
    int currcmp = cmpno;
    Q[currcmp].push(v);vis[v]=1;
    while(!Q[currcmp].empty()){
        int u = Q[currcmp].front();
        Q[currcmp].pop();
    }
}

```

```

for(int i=0;i<SZ(graph[u]);i++){
    int e = graph[u][i];
    int w = adj(u,e);
    if(vis[w])continue;
    if(isbridge[e]){
        cmpno++;
        tree[currcmp].push_back(cmpno);
        tree[cmpno].push_back(currcmp);
        dfs1(w);
    }
    else{
        Q[currcmp].push(w);
        vis[w]=1;
    }
}
}
}

```

---

### 3.4 CentroidDecomposition

```

set<int> g[N];int sub[N];
//decompose
int nn;
void dfs1(int u,int p){
    sub[u]=1;nn++;
    for(auto it=g[u].begin();it!=g[u].end();it++){
        if(*it!=p){
            dfs1(*it,u);
            sub[u]+=sub[*it];
        }
    }
}
int dfs2(int u,int p){
    for(auto it=g[u].begin();it!=g[u].end();it++){
        if(*it!=p && sub[*it]>nn/2)
            return dfs2(*it,u);
    }
    return u;
}
void decompose(int root,int p){
    nn=0;
    dfs1(root,root);
    int centroid = dfs2(root,root);
    if(p!=-1)p=centroid;
    //fuck the centroid here :)
}

```

```

for(auto it=g[centroid].begin();it!=g[centroid].end();it++)
{
    g[*it].erase(centroid);
    decompose(*it,centroid);
}
g[centroid].clear();
}

```

### 3.5 Dinics

```

// INPUT:
// - graph, constructed using AddEdge()
// - source and sink
// OUTPUT:
// - maximum flow value
// - To obtain actual flow values, look at edges with capacity > 0
// (zero capacity edges are residual edges).
struct Edge {
    int from, to, cap, flow, index;
    Edge(int from, int to, int cap, int flow, int index) :
        from(from), to(to), cap(cap), flow(flow), index(index) {}
    LL rcap() { return cap - flow; }
};

struct Dinic {
    int N;
    vector<vector<Edge> > G;
    vector<vector<Edge *> > Lf;
    vector<int> layer;
    vector<int> Q;
    Dinic(int N) : N(N), G(N), Q(N) {}
    void AddEdge(int from, int to, int cap) {
        if (from == to) return;
        G[from].push_back(Edge(from, to, cap, 0, G[to].size()));
        G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
    }
    LL BlockingFlow(int s, int t) {
        layer.clear(); layer.resize(N, -1);
        layer[s] = 0;
        Lf.clear(); Lf.resize(N);
        int head = 0, tail = 0;
        Q[tail++] = s;
        while (head < tail) {
            int x = Q[head++];

```

```

for (int i = 0; i < G[x].size(); i++) {
    Edge &e = G[x][i]; if (e.rcap() <= 0) continue;
    if (layer[e.to] == -1) {
        layer[e.to] = layer[e.from] + 1;
        Q[tail++] = e.to;
    }
    if (layer[e.to] > layer[e.from]) {
        Lf[e.from].push_back(&e);
    }
}
}

if (layer[t] == -1) return 0;
LL totflow = 0;
vector<Edge *> P;
while (!Lf[s].empty()) {
    int curr = P.empty() ? s : P.back()->to;
    if (curr == t) { // Augment
        LL amt = P.front()->rcap();
        for (int i = 0; i < P.size(); ++i) {
            amt = min(amt, P[i]->rcap());
        }
        totflow += amt;
        for (int i = P.size() - 1; i >= 0; --i) {
            P[i]->flow += amt;
            G[P[i]->to][P[i]->index].flow -= amt;
            if (P[i]->rcap() <= 0) {
                Lf[P[i]->from].pop_back();
                P.resize(i);
            }
        }
    } else if (Lf[curr].empty()) { // Retreat
        P.pop_back();
        for (int i = 0; i < N; ++i)
            for (int j = 0; j < Lf[i].size(); ++j)
                if (Lf[i][j]->to == curr)
                    Lf[i].erase(Lf[i].begin() + j);
    } else { // Advance
        P.push_back(Lf[curr].back());
    }
}

return totflow;
}

LL GetMaxFlow(int s, int t) {
    LL totflow = 0;
    while (LL flow = BlockingFlow(s, t))

```



```

    totflow += flow;
    return totflow;
}
};

```

---

### 3.6 HLD

```

VI g[N];
int U[N], V[N], W[N]; //edge list graph.graph is 1-based.
int
    DP[LOGN][N], chainParent[N], chainHead[N], blen, chainNo[N], pos[N], sub[N], nchain, level[N]
int baseArray[N], ST[4*N]; //for segtree
int adj(int u, int e)
{
    return U[e]==u?V[e]:U[e];
}
void HLD(int u, int ee)
{
    baseArray[blen]=W[ee];
    pos[u]=blen; blen++;
    chainNo[u]=nchain;
    int sc=-1, mx=0;
    for(int i=0; i<SZ(g[u]); i++)
    {
        int e = g[u][i];
        if(e==ee) continue;
        int w = adj(u, e);
        if(sub[w]>mx)
            sc = e, mx = sub[w];
    }
    if(sc==-1) return;
    HLD(adj(u, sc), sc);
    for(int i=0; i<SZ(g[u]); i++)
    {
        int e = g[u][i];
        if(e==ee || e==sc) continue;
        int w = adj(u, e);
        nchain++; chainParent[nchain]=u; chainHead[nchain]=w;
        HLD(w, e);
    }
}
void dfs(int u, int ee)
{

```

```

    sub[u]=1;
    for(int i=0; i<SZ(g[u]); i++)
        if(g[u][i]!=ee)
        {
            int w = adj(u, g[u][i]);
            level[w]=level[u]+1; DP[0][w]=u;
            dfs(w, g[u][i]);
            sub[u]+=sub[w];
        }
}
void preprocess()
{
    //hang the tree
    DP[0][1]=1; dfs(1, 0);
    //HLD
    chainHead[nchain]=chainParent[nchain]=1;
    HLD(1, 0);
    //LCA & segtree :)
}

```

---

### 3.7 HopcroftKarp

```

const int MAXN1 = 50000;
const int MAXN2 = 50000;
const int MAXM = 150000;
int n1, n2, edges, last[MAXN1], prev[MAXM], head[MAXM];
int matching[MAXN2], dist[MAXN1], Q[MAXN1];
bool used[MAXN1], vis[MAXN1];
//init : takes no of vertices on left and right
//addEdge(u,v) : node u on left and v on right(0-based)
void init(int _n1, int _n2) {
    n1 = _n1;
    n2 = _n2;
    edges = 0;
    fill(last, last + n1, -1);
}
void addEdge(int u, int v) {
    head[edges] = v;
    prev[edges] = last[u];
    last[u] = edges++;
}
void bfs() {
    fill(dist, dist + n1, -1);

```

```

int sizeQ = 0;
for (int u = 0; u < n1; ++u) {
    if (!used[u]) {
        Q[sizeQ++] = u;
        dist[u] = 0;
    }
}
for (int i = 0; i < sizeQ; i++) {
    int u1 = Q[i];
    for (int e = last[u1]; e >= 0; e = prev[e]) {
        int u2 = matching[head[e]];
        if (u2 >= 0 && dist[u2] < 0) {
            dist[u2] = dist[u1] + 1;
            Q[sizeQ++] = u2;
        }
    }
}
}

bool dfs(int u1) {
    vis[u1] = true;
    for (int e = last[u1]; e >= 0; e = prev[e]) {
        int v = head[e];
        int u2 = matching[v];
        if (u2 < 0 || !vis[u2] && dist[u2] == dist[u1] + 1 && dfs(u2)) {
            matching[v] = u1;
            used[u1] = true;
            return true;
        }
    }
    return false;
}

int maxMatching() {
    fill(used, used + n1, false);
    fill(matching, matching + n2, -1);
    for (int res = 0; ;) {
        bfs();
        fill(vis, vis + n1, false);
        int f = 0;
        for (int u = 0; u < n1; ++u)
            if (!used[u] && dfs(u))
                ++f;
        if (!f)
            return res;
        res += f;
    }
}

```

```

}

```

### 3.8 Hungarian

```

// Min cost bipartite matching via shortest augmenting paths
// In practice, it solves 1000x1000 problems in around 1
// second.
// cost[i][j] = cost for pairing left node i with right node j
// Lmate[i] = index of right node that left node i pairs with
// Rmate[j] = index of left node that right node j pairs with
// The values in cost[i][j] may be positive or negative. To perform
// maximization, simply negate the cost[][] matrix.
typedef vector<double> VD;
typedef vector<VD> VVD;
double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
    int n = int(cost.size());
    // construct dual feasible solution
    VD u(n);
    VD v(n);
    for (int i = 0; i < n; i++) {
        u[i] = cost[i][0];
        for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);
    }
    for (int j = 0; j < n; j++) {
        v[j] = cost[0][j] - u[0];
        for (int i = 1; i < n; i++) v[j] = min(v[j], cost[i][j] - u[i]);
    }
    // construct primal solution satisfying complementary slackness
    Lmate = VI(n, -1);
    Rmate = VI(n, -1);
    int mated = 0;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if (Rmate[j] != -1) continue;
            if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
                Lmate[i] = j;
                Rmate[j] = i;
                mated++;
                break;
            }
        }
    }
}
}
}
VD dist(n);

```

```

VI dad(n), seen(n);
// repeat until primal solution is feasible
while (mated < n) {
    // find an unmatched left node
    int s = 0;
    while (Lmate[s] != -1) s++;
    // initialize Dijkstra
    fill(dad.begin(), dad.end(), -1);
    fill(seen.begin(), seen.end(), 0);
    for (int k = 0; k < n; k++)
        dist[k] = cost[s][k] - u[s] - v[k];
    int j = 0;
    while (true) {
        // find closest
        j = -1;
        for (int k = 0; k < n; k++) {
            if (seen[k]) continue;
            if (j == -1 || dist[k] < dist[j]) j = k;
        }
        seen[j] = 1;
        // termination condition
        if (Rmate[j] == -1) break;
        // relax neighbors
        const int i = Rmate[j];
        for (int k = 0; k < n; k++) {
            if (seen[k]) continue;
            const double new_dist = dist[j] + cost[i][k] - u[i] - v[k];
            if (dist[k] > new_dist) {
                dist[k] = new_dist;
                dad[k] = j;
            }
        }
    }
    // update dual variables
    for (int k = 0; k < n; k++) {
        if (k == j || !seen[k]) continue;
        const int i = Rmate[k];
        v[k] += dist[k] - dist[j];
        u[i] -= dist[k] - dist[j];
    }
    u[s] += dist[j];
    // augment along path
    while (dad[j] >= 0) {
        const int d = dad[j];
        Rmate[j] = Rmate[d];

```

```

        Lmate[Rmate[j]] = j;
        j = d;
    }
    Rmate[j] = s;
    Lmate[s] = j;
    mated++;
}
double value = 0;
for (int i = 0; i < n; i++)
    value += cost[i][Lmate[i]];
return value;
}

```

### 3.9 MinCostMaxFlow

```

//INPUT:
// - graph, constructed using AddEdge()
// - source
// - sink
// OUTPUT:
// - (maximum flow value, minimum cost value(can be double)
// - To obtain the actual flow, look at positive values only.
const LL INF = numeric_limits<LL>::max() / 4;
struct MinCostMaxFlow {
    int N;
    vector<vector<LL>> cap, flow, cost;
    VI found;
    vector<LL> dist, pi, width;
    VII dad;
    MinCostMaxFlow(int N) :
        N(N), cap(N, vector<LL>(N)), flow(N, vector<LL>(N)), cost(N,
            vector<LL>(N)),
        found(N), dist(N), pi(N), width(N), dad(N) {}
    void AddEdge(int from, int to, LL cap, LL cost) {
        this->cap[from][to] = cap;
        this->cost[from][to] = cost;
    }
    void Relax(int s, int k, LL cap, LL cost, int dir) {
        LL val = dist[s] + pi[s] - pi[k] + cost;
        if (cap && val < dist[k]) {
            dist[k] = val;
            dad[k] = make_pair(s, dir);
            width[k] = min(cap, width[s]);

```

```

    }
}
LL Dijkstra(int s, int t) {
    fill(found.begin(), found.end(), false);
    fill(dist.begin(), dist.end(), INF);
    fill(width.begin(), width.end(), 0);
    dist[s] = 0;
    width[s] = INF;
    while (s != -1) {
        int best = -1;
        found[s] = true;
        for (int k = 0; k < N; k++) {
            if (found[k]) continue;
            Relax(s, k, cap[s][k] - flow[s][k], cost[s][k], 1);
            Relax(s, k, flow[k][s], -cost[k][s], -1);
            if (best == -1 || dist[k] < dist[best]) best = k;
        }
        s = best;
    }
    for (int k = 0; k < N; k++)
        pi[k] = min(pi[k] + dist[k], INF);
    return width[t];
}
pair<LL, LL> GetMaxFlow(int s, int t) {
    LL totflow = 0, totcost = 0;
    while (LL amt = Dijkstra(s, t)) {
        totflow += amt;
        for (int x = t; x != s; x = dad[x].first) {
            if (dad[x].second == 1) {
                flow[dad[x].first][x] += amt;
                totcost += amt * cost[dad[x].first][x];
            } else {
                flow[x][dad[x].first] -= amt;
                totcost -= amt * cost[x][dad[x].first];
            }
        }
    }
    return make_pair(totflow, totcost);
}
};

```

### 3.10 SCC

```

VI order, component;
int vis[N];
//g:graph,rg:reverse graph
void dfs1(int u){
    vis[u] = 1;
    for(int i=0;i<SZ(g[u]);i++)
        if(!vis[g[u][i]])
            dfs1(g[u][i]);

    order.PB(v);
}
void dfs2(int u) {
    vis[u] = 1;
    component.push_back (u);
    for(int i=0;i<SZ(rg[u]);i++)
        if (!vis[rg[u][i]])
            dfs2(rg[u][i]);
}
//main
SET(vis,0);
for (int i=0;i<n;i++)
    if(!vis[i])
        dfs1 (i);

SET(vis,0);
for (int i=0; i<n; ++i) {
    int u = order[n-1-i];
    if (!vis[u]) {
        dfs2 (u);
        component.clear();
    }
}

```

## 4 Math

### 4.1 ExtendedGCD

```

LL coeffA, coeffB, G;
void extGcd(LL a, LL b){
    if( b == 0 ){
        G = a;
        coeffA = 1; coeffB = 0;
    }
    else{

```

```

    extGcd(b, a % b);
    coeffA -= coeffB * (a/b);
    swap(coeffA, coeffB);
}
}
/* If this system { x = r1 mod m1 ; x = r2 mod m2 }
 * has a solution, this methods returns the
 * smallest non negative solution.
 * If there is no solution, -1 is returned.*/
LL congruence( LL r1, LL m1, LL r2, LL m2){
    extGcd(m1,m2);
    if( (r1 - r2) % G != 0) return -1;
    LL M = m1 * m2 / G;
    // Solution exists and is unique on LCM(m1,m2) = M
    LL K = ( r2 - r1) / G;
    LL ans = ((K * m1 * coeffA) + r1) % M;
    //Note that K * (m1*coeffA + m2*coeffB) = r2-r1
    if( ans < 0) ans += M;
    return ans;
}

```

## 4.2 FFT

```

namespace FFT {
#define fore(i, a, b) for(int i = (int)(a); i <= (int)(b); ++i)
#define forn(i, n) for(int i = 0; i < (int)(n); ++i)
    typedef long double ld;
    struct base {
        typedef double T; T re, im;
        base() :re(0), im(0) {}
        base(T re) :re(re), im(0) {}
        base(T re, T im) :re(re), im(im) {}
        base operator + (const base& o) const { return base(re +
            o.re, im + o.im); }
        base operator - (const base& o) const { return base(re -
            o.re, im - o.im); }
        base operator * (const base& o) const { return base(re *
            o.re - im * o.im, re * o.im + im * o.re); }
        base operator * (ld k) const { return base(re * k, im * k)
            ;}
        base conj() const { return base(re, -im); }
    };
    const int N = 21;
}

```

```

const int MAXN = (1<<N);
base w[MAXN], f1[MAXN];
int rev[MAXN];
void build_rev(int k) {
    static int rk = -1;
    if( k == rk )return ; rk = k;
    for(int i=1; i<=(1<<k); i++){
        int j = rev[i-1], t = k-1;
        while(t >= 0 && ((j>>t)&1)){j ^= 1<<t; --t;}
        if(t >= 0){j ^= 1<<t; --t;}
        rev[i] = j;
    }
}
void fft(base *a, int k) {
    build_rev(k); int n = 1<<k;
    forn(i, n) if( rev[i] > i ) swap(a[i], a[rev[i]]);
    for(int l = 2, ll = 1; l <= n; l += l, ll += ll) {
        if( w[ll].re == 0 && w[ll].im == 0 ) {
            ld angle = M_PI / ll;
            base ww( cosl(angle), sinl(angle) );
            if( ll > 1 ) for(int j = 0; j < ll; ++j) {
                if( j & 1 ) w[ll + j] = w[(ll+j)/2] *
                    ww;
                else w[ll + j] = w[(ll+j)/2];
            } else w[ll] = base(1, 0);
        }
        for(int i = 0; i < n; i += l) forn(j, ll) {
            base v = a[i + j], u = a[i + j + ll] * w[ll
                + j];
            a[i + j] = v + u; a[i + j + ll] = v - u;
        }
    }
}
VI mul(const VI& a, const VI& b) {
    int k = 1;
    while( (1<<k) < (SZ(a) + SZ(b)) ) ++k;
    int n = (1<<k);
    for(int i=0; i<n; i++) f1[i] = base(0,0);
    for(int i=0; i<SZ(a); i++) f1[i] = f1[i]+base(a[i], 0);
    for(int i=0; i<SZ(b); i++) f1[i] = f1[i]+base(0, b[i]);
    fft(f1, k);
    for(int i=1; i<=1+n/2; i++){
        base p = f1[i] + f1[(n-i)%n].conj();
        base _q = f1[(n-i)%n] - f1[i].conj();
        base q(_q.im, _q.re);
    }
}

```

```

        f1[i] = (p * q) * 0.25;
        if(i>0) f1[(n - i)] = f1[i].conj();
    }
    for(int i=0;i<n;i++)f1[i] = f1[i].conj();
    fft(f1, k);
    VI r(SZ(a) + SZ(b));
    for(int i=0;i<SZ(r);i++){
        r[i] = LL (f1[i].re / n + 0.5);
    }
    /*Uncomment for multiplication of two numbers
    int carry = 0;
    for (int i=0; i<SZ(r); ++i) {
        r[i] += carry; carry = r[i] / 10;
        r[i] %= 10;
    }
    */
    return r;
}
} // end of FFT namespace

```

---

### 4.3 MatrixDeterModP

---

### 4.4 MatrixInverse

---

### 4.5 MatrixRank

---

```

//Mobius_Treap
#include<bits/stdc++.h>

using namespace std;

typedef pair<int,int> II;
typedef vector< II > VII;
typedef vector<int> VI;
typedef vector< VI > VVI;
typedef long long int LL;

```

```

#define PB push_back
#define MP make_pair
#define F first
#define S second
#define SZ(a) (int)(a.size())
#define ALL(a) a.begin(),a.end()
#define SET(a,b) memset(a,b,sizeof(a))

#define si(n) scanf("%d",&n)
#define dout(n) printf("%d\n",n)
#define sll(n) scanf("%lld",&n)
#define lldout(n) printf("%lld\n",n)
#define fast_io ios_base::sync_with_stdio(false);cin.tie(NULL)

#define TRACE

#ifdef TRACE
#define trace(...) __f(#__VA_ARGS__, __VA_ARGS__)
template <typename Arg1>
void __f(const char* name, Arg1&& arg1){
    cerr << name << " : " << arg1 << std::endl;
}
template <typename Arg1, typename... Args>
void __f(const char* names, Arg1&& arg1, Args&&... args){
    const char* comma = strchr(names + 1, ',');cerr.write(names, comma
        - names) << " : " << arg1<<" | ";__f(comma+1, args...);
}
#else
#define trace(...)
#endif

//FILE *fin = freopen("in","r",stdin);
//FILE *fout = freopen("out","w",stdout);

int main()
{

    return 0;
}

```

---

## 4.6 MillerRabin

```
/* this function calculates (a*b)%c taking into account that a*b might
overflow */
long long mulmod(long long a,long long b,long long c){
    long long x = 0,y=a%c;
    while(b > 0){
        if(b%2 == 1)x = (x+y)%c;
        y = (y*2)%c;
        b /= 2;
    }
    return x%c;
}
/* Miller-Rabin primality test, iteration signifies the accuracy of the
test */
bool Miller(long long p,int iteration){
    if(p<2){
        return false;
    }
    if(p!=2 && p%2==0){
        return false;
    }
    long long s=p-1;
    while(s%2==0)s/=2;
    for(int i=0;i<iteration;i++){
        long long a=rand()%(p-1)+1,temp=s;
        long long mod=power(a,temp,p);
        while(temp!=p-1 && mod!=1 && mod!=p-1){
            mod=mulmod(mod,mod,p);
            temp *= 2;
        }
        if(mod!=p-1 && temp%2==0){
            return false;
        }
    }
    return true;
}
```

## 4.7 QuadraticResidue

```
#include<iostream>
#include<cstdio>
#include<algorithm>
```

```
#define M(x) ((x)%p)
using namespace std;
typedef long long int ll;
ll p;
ll pwm(ll v,int in)
{
    ll x=v;v=1;
    while(in>0)
    {
        if((in&1)==1)
            v=M(v*x);
        in=(in>>1);
        x=M(x*x);
    }
    return v;
}
ll sqrt(ll a)
{
    ll r=0,s=p-1,n,m,x,b,g,coff,t;
    if(pwm(a,((p-1)>>1))==p-1)
        return -1;
    while((s&1)==0){ //generating s and r///
        s=(s>>1);
        r++;
    }
    for(ll i=2;i<p;i++)
        if(pwm(i,((p-1)>>1))==p-1){ //finding n//
            n=i;
            break;
        }
    b=pwm(a,s);
    g=pwm(n,s);
    x=pwm(a,((s+1)>>1));
    while(r>0)
    {
        t=b;
        for(m=0;m<r;m++){
            if(M(t)==1)
                break;
            t=M(t*t);
        }
        if(m>0)
        {
            coff=pwm(g,(1<<(r-(m+1))));
            x=M(x*coff);
        }
    }
}
```

```

        g=M(coff*coff);
        b=M(b*g);
    }
    r=m;
}
return x;
}

////////////////////////////////////////
//note do not use this variable again///
void ren(ll &a,ll &b,ll q)
{
    ll temp;
    temp=b;
    b=(a-(b*q));
    a=temp;
}
ll gcd(ll a,ll b)
{
    ll olds=1,s=0,t=1,oldt=0;
    ll q;
    while(b!=0)
    {
        q=a/b;
        ren(a,b,q);
        ren(olds,s,q);
        ren(oldt,t,q);
        oldt=M(oldt);
    }
    return oldt;
}
int main()
{
    ll a,q,test,b,c,sqr1,sqr2,ans1,ans2,oldt;
    scanf("%lld",&test);
    while(test--)
    {
        scanf("%lld %lld %lld %lld",&a,&b,&c,&p);
        if(p==2){
            int cnt=0;
            if(M(a+b+c)==0) cnt+=2;
            if(c==0) cnt++;
            if(cnt==3) printf("2 0 1\n");
            else if(cnt==1) printf("1 0\n");

```

```

            else if(cnt==2) printf("1 1\n");
            else printf("0\n ");
            continue;
        }
        q=M(b*b)-M(4*a*c)+p);
        if(b==0 && c==0){
            printf("1 0\n");
            continue;
        }
        if(q==0)
            sqr1=0;
        else
            sqr1=sqrt(q);
        sqr2=p-sqr1;
        if(sqr1==-1){
            printf("0\n");
            continue;
        }
        //          printf("%lld %lld\n",sqr1,sqr2);
        oldt=gcd(p,M(2*a));
        if(oldt<0)
            oldt+=p*((oldt/p)+1);
        oldt=M(oldt);
        //          printf("%lld\n",oldt);
        ans1=M(oldt*M(sqr1+p-b));
        ans2=M(oldt*M(sqr2+p-b));
        if(ans1<ans2)
            printf("2 %lld %lld\n",ans1,ans2);
        else if(ans2<ans1)
            printf("2 %lld %lld\n",ans2,ans1);
        else
            printf("1 %lld\n",ans1);
    }
    return 0;
}

```

---

## 4.8 Simplex

---

## 4.9 nCrLarge



---

```

const int MOD = int(1e6) + 3;
long long invert_mod(long long k, long long m){
    if(m == 0) return(k == 1 || k == -1) ? k : 0;
    if(m < 0) m = -m;
    k %= m;
    if(k < 0) k += m;
    int neg = 1;
    long long p1 = 1, p2 = 0, k1 = k, m1 = m, q, r, temp;
    while(k1 > 0) {
        q = m1 / k1; r = m1 % k1;
        temp = q*p1 + p2;
        p2 = p1; p1 = temp;
        m1 = k1; k1 = r;
        neg = !neg;
    }
    return neg ? m - p2 : p2;
}
// Preconditions: 0 <= k <= n; p > 1 prime
long long choose_mod_one(long long n, long long k, long long p){
    // For small k, no recursion is necessary
    if (k < p) return choose_mod_two(n,k,p);
    long long q_n, r_n, q_k, r_k, choose;
    q_n = n / p; r_n = n % p;
    q_k = k / p; r_k = k % p;
    choose = choose_mod_two(r_n, r_k, p);
    // If the exponent of p in choose(n,k) isn't determined to be 0
    // before the calculation gets serious, short-cut here:
    /* if (choose == 0) return 0; */
    choose *= choose_mod_one(q_n, q_k, p);
    return choose % p;
}
// Preconditions: 0 <= k <= min(n,p-1); p > 1 prime
long long choose_mod_two(long long n, long long k, long long p){
    // reduce n modulo p
    n %= p;
    if (n < k) return 0;
    if (k == 0 || k == n) return 1;
    // Now 0 < k < n, save a bit of work if k > n/2
    if (k > n/2) k = n-k;
    // calculate numerator and denominator modulo p
    long long num = n, den = 1;
    for(n = n-1; k > 1; --n, --k){
        num = (num * n) % p;
        den = (den * k) % p;
    }

```

```

    }
    // Invert denominator modulo p
    den = invert_mod(den,p);
    return (num * den) % p;
}
long long factorial_exponent(long long n, long long p){
    long long ex = 0;
    do{
        n /= p;
        ex += n;
    }while(n > 0);
    return ex;
}
//returns nCk % p in O(p). n and k can be large.
long long choose_mod(long long n, long long k, long long p){
    // We deal with the trivial cases first
    if (k < 0 || n < k) return 0;
    if (k == 0 || k == n) return 1;
    // Now check whether choose(n,k) is divisible by p
    if (factorial_exponent(n) > factorial_exponent(k) +
        factorial_exponent(n-k)) return 0;
    // If it's not divisible, do the generic work
    return choose_mod_one(n,k,p);
}

```

---

## 5 String

### 5.1 KMP

---

```
// to be done
```

---

### 5.2 SuffixArray

---

```

//LCP[0][i] = length of LCP of SA[i] && SA[i+1] (sorted suffixes).
//RA[i][j] = Rank of suffix S[j...j+2^i] i.e. 2^j length substring
              starting at i.
//SA[i] = i'th Lexicographically smallest suffix's index.
int RA[LOGN][N], SA[N], tempSA[N], cnt[N], msb[N], LCP[LOGN][N];
void countingSort(int l, int k, int n){
    SET(cnt, 0);

```

```

for(int i=0;i<n;i++){
    int idx = i+k<n?RA[l][i+k]:0;
    cnt[idx]++;
}
int maxi = max(300,n);
for(int i=0,sum=0;i<maxi;i++){
    int t = cnt[i];
    cnt[i] = sum;
    sum+=t;
}
for(int i=0;i<n;i++){
    int idx = SA[i]+k<n?RA[l][SA[i]+k]:0;
    tempSA[cnt[idx]++]=SA[i];
}
for(int i=0;i<n;i++)
    SA[i]=tempSA[i];
}
void build_SA(string &s){
    int n = SZ(s);
    for(int i=0;i<n;i++)RA[0][i]=s[i];
    for(int i=0;i<n;i++)SA[i]=i;
    for(int i=0;i<LOGN-1;i++){
        int k = (1<<i);
        if(k>=n)break;
        countingSort(i,k,n);
        countingSort(i,0,n);
        int rank=0;
        RA[i+1][SA[0]]=rank;
        for(int j=1;j<n;j++){
            if(RA[i][SA[j]] == RA[i][SA[j-1]] &&
               RA[i][SA[j]+k]==RA[i][SA[j-1]+k])RA[i+1][SA[j]]=rank;
            else RA[i+1][SA[j]]=++rank;
        }
    }
}
void build_msb(){
    int mx=-1;
    for(int i=0;i<N;i++){
        if(i>=(1<<(mx+1)))mx++;
        msb[i]=mx;
    }
}
void build_LCP(string& s){
    int n =SZ(s);
    for(int i=0;i<n-1;i++){//Build the LCP array in O(NlogN)
        int x = SA[i],y=SA[i+1];

```

```

        int k,ret=0;
        for(k=LOGN-1;k>=0 && x<n && y<n;k--){
            if((1<<k)>=n)continue;
            if(RA[k][x]==RA[k][y])x+=1<<k,y+=1<<k,ret+=1<<k;
        }
        LCP[0][i]=ret;
    }
    LCP[0][n-1]=10*N;
    for(int i=1;i<LOGN;i++){//Build the O(1) RMQ structure in O(NlogN)
        int add = (1<<(i-1));
        if(add>=n)break; //small optimization
        for(int j=0;j<n;j++){
            if(j+add<n)LCP[i][j] = min(LCP[i-1][j],LCP[i-1][j+add]);
            else LCP[i][j] = LCP[i-1][j];
        }
    }
    int lcp(int x,int y){
        //O(1) LCP.x and y are indexes of the suffix in SUFFIX array...!!
        if(x==y)return 0;
        if(x>y)swap(x,y);y--;
        int idx = msb[y-x+1],sub = (1<<idx);
        return min(LCP[idx][x],LCP[idx][y-sub+1]);
    }
    bool equal(int i,int j,int p,int q){
        if(j-i!=q-p)return false;
        int idx = msb[j-i+1],sub = (1<<idx);
        return RA[idx][i]==RA[idx][p] && RA[idx][j-sub+1]==RA[idx][q-sub+1];
    }
    //Note : Do not forget to add a terminating '$'

```

### 5.3 ZAlgo

```

//compute Z array
int L=0,R=0;
for(int i = 1; i < n; i++) {
    if (i > R) {
        L = R = i;
        while (R < n && s[R-L] == s[R]) R++;
        z[i] = R-L; R--;
    } else {
        int k = i-L;
        if (z[k] < R-i+1) z[i] = z[k];
        else {

```

```

    L = i;
    while (R < n && s[R-L] == s[R]) R++;
    z[i] = R-L; R--;
}
}
}
//usage
int maxz = 0, res = 0;
for (int i = 1; i < n; i++) {
    if (z[i] == n-i && maxz >= n-i) { res = n-i; break; }
    maxz = max(maxz, z[i]);
}

```

---

## 6 Theory

## 7 template

```

//Mobius_Treap
#include<bits/stdc++.h>

using namespace std;

typedef pair<int,int> II;
typedef vector< II > VII;
typedef vector<int> VI;
typedef vector< VI > VVI;
typedef long long int LL;

#define PB push_back
#define MP make_pair
#define F first
#define S second
#define SZ(a) (int)(a.size())
#define ALL(a) a.begin(),a.end()
#define SET(a,b) memset(a,b,sizeof(a))

#define si(n) scanf("%d",&n)
#define dout(n) printf("%d\n",n)
#define sll(n) scanf("%lld",&n)
#define lldout(n) printf("%lld\n",n)
#define fast_io ios_base::sync_with_stdio(false);cin.tie(NULL)

```

```

#define TRACE

#ifdef TRACE
#define trace(...) __f(#__VA_ARGS__, __VA_ARGS__)
template <typename Arg1>
void __f(const char* name, Arg1&& arg1){
    cerr << name << " : " << arg1 << std::endl;
}
template <typename Arg1, typename... Args>
void __f(const char* names, Arg1&& arg1, Args&&... args){
    const char* comma = strchr(names + 1, ',');cerr.write(names, comma
        - names) << " : " << arg1<<" | ";__f(comma+1, args...);
}
#else
#define trace(...)
#endif

//FILE *fin = freopen("in","r",stdin);
//FILE *fout = freopen("out","w",stdout);

int main()
{

    return 0;
}

```

---