

Laboratory 3:

FLOATING POINT ADDER/SUBTRACTOR

OBJECTIVES

- Getting to know how to describe a floating-point arithmetic, which could do add, subtract, and multiply operations.
- Design and implement digital circuits using FSM.
- Download the circuit into the FPGA chip and test its functionality.

PREPARATION FOR LAB 3

- Finish Pre Lab 3 at home.
- Students have to simulate all the exercises in Pre Lab 3 at home. All results (codes, waveform, RTL viewer, ...) have to be captured and submitted to instructors prior to the lab session.
If not, students will not participate in the lab and be considered absent this session.

REFERENCE



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Floating point numbers allow computers to perform operations on a wide range of numbers.

According to the IEEE standards, floating point numbers are of the form

$$(-1)^S * (1+F) * 2^E$$

S is the sign bit, which determines whether the number is positive or negative.

F – fraction – holds the significant bits of the floating point number.

E is the exponent that $(1+F)$ is raised to.

A 32 bit floating point number is standard, however for simplification, we will be using an 8 bit representation. We will have a sign bit, 3 bits for the exponent, and the remaining 4 bits will be devoted to the fraction. This will allow us to represent a resolution as small as $1/128$ and the smallest number we can represent is $1/8$. Eight-bit floating point numbers are not useful for performing extremely accurate calculations, but it does demonstrate the operation of a floating point adder.



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EXPERIMENT

Objective: Implement a floating point adder/subtractor using System Verilog description and download the circuit into the FPGA chip..

Requirement:

You are desired to design a floating-point adder/subtractor should perform correctly in the normal cases. Besides several pins needs to indicate some extreme cases:

- Zero detection: when the result is zero, zero detection pin will be 1.

Inputs	Operand 1	A[7:0]	8-bit normalized input
	Operand 2	B[7:0]	8-bit normalized input
	Selection	S	1-bit input, addition/subtraction selection
Outputs	Operation result	Result[7:0]	8-bit normalized output
	Zero detection	Z	1-bit output

Table 1: IO definition

Instruction:

Input A and B have 8 bits, in which the sign is represented by bit [7], the exponent value is represented by bit [6:4], and the remaining is for Fraction value. Output Result also need to be normalized as input signal.

The design have some sub-modules that perform floating point calculations:

- Identify which number is larger, which number is smaller.
- Identify the amount to right shift the operand which has smaller exponent.
- Right shift fraction value of the smaller operand to align decimal points.
- Calculate the two's complement of the shifted fraction, only needed in the case of subtraction or equivalent case (i.e. adding a negative number to a positive number).
- Add the two fractions together.
- Normalize the fraction and exponent value so it's back in floating point representation.
- Determine sign of the final value.
- Detect zero: the result is zero if the signs of A and B are different and there is no difference in the fraction and exponent.



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1. Create a new Quartus project for your circuit.
2. Use switches as inputs, LEDRs as outputs.
3. Compile your project. Download the circuit into the FPGA chip and test its functionality.

Check: Your report has to show two results:

The Code:

```
module Exponent(
input [2:0] Exp_A, Exp_B,
output [2:0] Bigger_exp,
output [3:0] Exp_diff
);

assign Exp_diff = Exp_A - Exp_B;

always_comb begin
    if (Exp_diff[3] == 0)
        Bigger_exp <= Exp_A;
    else
        Bigger_exp <= Exp_B;
end

endmodule

module add_sub_fract(
input Sign_A, Sign_B, S,
input [5:0] Shifted_fract, SixBitBigger_fract,
output [5:0] Mag_fract
);

logic Same_sign;

assign Same_sign = Sign_A ~^ Sign_B;

always_comb begin
    if (S == 1) begin
        if (Same_sign == 1)
            Mag_fract <= SixBitBigger_fract - Shifted_fract;
        else
            Mag_fract <= SixBitBigger_fract + Shifted_fract;
        end
    else begin
        if (Same_sign == 1)
            Mag_fract <= SixBitBigger_fract + Shifted_fract;
```



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```
        else
            Mag_fract <= SixBitBigger_fract - Shifted_fract;
        end

    end

endmodule

module Exp_Fract(
    input [5:0] Mag_fract,
    input [2:0] Bigger_exp,
    output [3:0] Result_fract,
    output [2:0] Result_exp,
    output OV
);

always_ff begin
    if (Mag_fract[5] == 1) begin
        if (Bigger_exp <= 6) begin
            Result_exp <= Bigger_exp + 1;
            Result_fract <= Mag_fract[4:1];
            OV <= 1'b0;
        end
        else begin
            OV <= 1'b1;
            Result_exp <= 3'b111;
            Result_fract <= 4'b1111;
        end
    end
    else if (Mag_fract[4] == 1) begin
        Result_exp <= Bigger_exp;
        Result_fract <= Mag_fract[3:0];
        OV <= 1'b0;
    end
    else if (Mag_fract[3] == 1) begin
        if (Bigger_exp >= 1) begin
            Result_exp <= Bigger_exp - 1;
            Result_fract <= {Mag_fract[2:0], 1'b0};
            OV <= 1'b0;
        end
        else begin
            OV <= 1'b1;
            Result_exp <= 3'b111;
            Result_fract <= 4'b1111;
        end
    end
end
```



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```

end
else if (Mag_fract[2] == 1) begin
    if (Bigger_exp >= 2) begin
        Result_exp <= Bigger_exp - 2;
        Result_fract <= {Mag_fract[1:0], 2'b0};
        OV <= 1'b0;
    end
    else begin
        OV <= 1'b1;
        Result_exp <= 3'b111;
        Result_fract <= 4'b1111;
    end
end
else if (Mag_fract[1] == 1) begin
    if (Bigger_exp >= 3) begin
        Result_exp <= Bigger_exp - 3;
        Result_fract <= {Mag_fract[0], 3'b0};
        OV <= 1'b0;
    end
    else begin
        OV <= 1'b1;
        Result_exp <= 3'b111;
        Result_fract <= 4'b1111;
    end
end
else if (Mag_fract[0] == 1) begin
    if (Bigger_exp >= 4) begin
        Result_exp <= Bigger_exp - 4;
        Result_fract <= 4'b0;
        OV <= 1'b0;
    end
    else begin
        OV <= 1'b1;
        Result_exp <= 3'b111;
        Result_fract <= 4'b1111;
    end
end
else OV <= 1'b0;
end

endmodule

```

```

module Exponent(
input [2:0] Exp_A, Exp_B,

```



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```
output [2:0] Bigger_exp,
output [3:0] Exp_diff
);

assign Exp_diff = Exp_A - Exp_B;

always_comb begin
    if (Exp_diff[3] == 0)
        Bigger_exp <= Exp_A;
    else
        Bigger_exp <= Exp_B;
end

endmodule

module Fraction(
input [3:0] Fract_A, Fract_B, Exp_diff,
output [3:0] Bigger_fract, Smaller_fract
);

logic [3:0] Fract_diff;
assign Fract_diff = Fract_A - Fract_B;

always_comb begin
    if (Exp_diff == 0) begin                //Exp_A = Exp_B
        if (Fract_diff[3] == 0) begin
            Bigger_fract <= Fract_A;
            Smaller_fract <= Fract_B;
        end
        else begin
            Bigger_fract <= Fract_B;
            Smaller_fract <= Fract_A;
        end
    end

    else begin                            //Exp_A <> Exp_B
        if (Exp_diff[3] == 0) begin
            Bigger_fract <= Fract_A;
            Smaller_fract <= Fract_B;
        end
        else begin
            Bigger_fract <= Fract_B;
            Smaller_fract <= Fract_A;
        end
    end
end
```



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```
end
end

endmodule

module Result(
input [7:0] A, B,
input Result_sign, S,
input [2:0] Result_exp,
input [3:0] Result_fract,
output Z,
output [7:0] Result
);

always_comb begin
    if (A[6:0] == B[6:0] && A[7] != B[7] && S == 0) begin
        Z <= 1'b1;
        Result <= '0;
    end
    else begin
        Z <= 1'b0;
        Result <= {Result_sign, Result_exp, Result_fract};
    end
end

endmodule

module Shift(
input logic [3:0] Smaller_fract, Exp_diff,
output logic [5:0] Shifted_fract
);

logic [3:0] Shift_amount;
logic [4:0] Lead1;

always_comb begin
    if (Exp_diff[3] == 0)
        Shift_amount = Exp_diff;
    else
        Shift_amount = -Exp_diff;
end

assign Lead1 = {1'b1, Smaller_fract};
assign Shifted_fract = Lead1 >> Shift_amount;
```



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```
endmodule
```

```
module Sign(  
input [2:0] Exp_A, Exp_B,  
input [3:0] Fract_A, Fract_B,  
input Sign_A, Sign_B,  
output Result_sign  
);
```

```
always_comb begin
```

```
    if (Exp_A == Exp_B) begin
```

```
        if (Fract_B > Fract_A) Result_sign <= Sign_B;
```

```
        else Result_sign <= Sign_A;
```

```
    end
```

```
    else begin
```

```
        if (Exp_B > Exp_A) Result_sign <= Sign_B;
```

```
        else Result_sign <= Sign_A;
```

```
    end
```

```
end
```

```
endmodule
```

```
module lab3_lan2(  
input S,  
input [7:0] A, B,  
output [7:0] Result,  
output OV,  
output Z  
);
```

```
    logic Sign_A, sign_B;  
    logic [2:0] Exp_A, Exp_B;  
    logic [3:0] Fract_A, Fract_B;  
    logic [2:0] Bigger_exp;  
    logic [3:0] Exp_diff;  
    logic [3:0] Bigger_fract, Smaller_fract;  
    logic [5:0] Shifted_fract;  
    logic [5:0] SixBitBigger_fract;  
    logic [5:0] Neg_Shifted_fract;  
    logic [5:0] Mag_fract;  
    logic [3:0] Result_fract;
```



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```
logic [2:0] Result_exp;
logic Result_sign;

assign Sign_A = A[7];
assign Exp_A = A[6:4];
assign Fract_A = A[3:0];
assign Sign_B = B[7];
assign Exp_B = B[6:4];
assign Fract_B = B[3:0];

Exponent
exponent(.Exp_A(Exp_A),.Exp_B(Exp_B),.Bigger_exp(Bigger_exp),.Exp_diff(Exp_diff));

Fraction
fraction(.Fract_A(Fract_A),.Fract_B(Fract_B),.Exp_diff(Exp_diff),.Bigger_fract(Bigger_fract),.Smaller_fract(Smaller_fract));

Shift shift(.Smaller_fract(Smaller_fract),.Exp_diff(Exp_diff),.Shifted_fract(Shifted_fract));

assign SixBitBigger_fract = {2'b01, Bigger_fract};
assign Neg_Shifted_fract = -Shifted_fract;

add_sub_fract
addsub(.Sign_A(Sign_A),.Sign_B(Sign_B),.S(S),.Shifted_fract(Shifted_fract),.SixBitBigger_fract
(SixBitBigger_fract),.Mag_fract(Mag_fract));

Exp_Fract
expfract(.Mag_fract(Mag_fract),.Bigger_exp(Bigger_exp),.Result_fract(Result_fract),.Result_exp
(Result_exp),.OV(OV));

Sign
sign(.Sign_A(Sign_A),.Sign_B(Sign_B),.Exp_A(Exp_A),.Exp_B(Exp_B),.Fract_A(Fract_A),.Fract_B(Fract_B),.Result_sign(Result_sign));

Result
result(.A(A),.B(B),.S(S),.Result_sign(Result_sign),.Result_exp(Result_exp),.Result_fract(Result_fract),.Result(Result),.Z(Z));

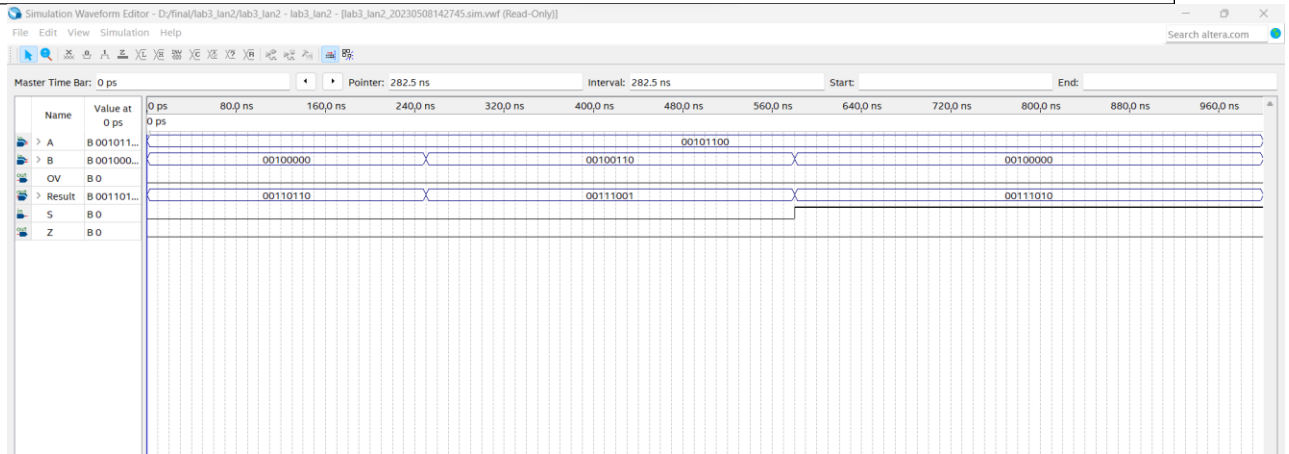
endmodule
```

- The waveform to prove the circuit works correctly.



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➤ The result of RTL viewer.

