



information as pixel-level or region-based labels, they still have practical utility.

### C. FEDERATED LEARNING

**Federated Learning (FL) is a machine learning approach that enables multiple clients or devices to train a shared model collaboratively without sharing their raw data.** It addresses privacy concerns by decentralizing the data, thus maintaining data security and confidentiality.

### D. SEMI-SUPERVISED LEARNING TECHNIQUE

Semi-Supervised learning is a machine learning algorithm representing the intermediate ground between supervised and unsupervised learning algorithms. It uses a combination of labeled and unlabeled datasets during the training period **where the model is trained on the labeled data first and then used to predict labels for the unlabeled data, which is then incorporated into the training process.**

## II. PROBLEM STATEMENT AND MOTIVATION

For a fully-supervised semantic segmentation model, the ideal scenario is, we can collect the pixel-level annotated images as much as possible. this scenario is almost infeasible due to the following three reasons:

- 1) The strict sharing protocol of sensitive patient information between medical institutions.
- 2) High pixel-level annotation cost.
- 3) Expert knowledge usually required for annotating medical images is much more demanding and difficult to obtain.

Clients participating in FL may have different labeling budgets. Therefore, there may be a wide range of inter-client variations in label availability. Weak labels are easier to acquire and thus more broadly available compared to pixel-level ones.

## III. CHALLENGES

In practice, there can be various types of weak labels. Effectively utilizing the information from these weakly-labeled data with varying levels of label strengths as well as unlabeled data, especially for clients without pixel-level labeled data, would be highly beneficial for improving the federated model's robustness while preventing training instability.

**However, given less informative training data, ensuring that the local model updates from clients without pixel-level labels, e.g., weakly-labeled and unlabeled clients positively contribute to the federated model remains a challenge.**

## IV. EXISTING RELATED WORK AND ITS LIMITATIONS

- 1) For the inter-client variations, FL has been combined with domain adaptation [1] [2], to learn a more generalizable federated model.

### Limitations-

These existing work do not consider the variation in

supervision availability which is often observed in clinical practice.

- 2) Some semi-supervised federated learning methods attempt to utilize the unlabeled data in addition to pixel-level labeled images in training. [3]

### Limitations-

These existing work do not make any use of the other weakly-labeled images.

## V. METHODOLOGY AND IMPLEMENTATION APPROACH

To fully utilize every level of labels available at any client, FedMix addresses the challenge through:

- 1) Pseudo Label Generation and Selection (Sample Refine). [4]
- 2) Adaptive Aggregation for Federated Model Update (Aggregate).

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### Algorithm 1: Pseudocode of FedMix

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input      :  $\bar{D}$ : the set of training data
parameter:  $\beta, \lambda$ : hyperparameters for adaptive aggregation
               $T$ : maximum federated training rounds
               $\epsilon$ : threshold for dynamic sample selection
output    :  $\theta_{\xi 1}^T$ : parameters of  $F_1$ 
               $\theta_{\xi 2}^T$ : parameters of  $F_2$ 

 $\theta_{\xi 1}^0, \theta_{\xi 2}^0 \leftarrow \text{initialize}()$ 
for  $t = 1 : T$  do
   $\bar{\mathcal{L}} = \{\}, \bar{\theta}_{\xi 1} = \{\}, \bar{\theta}_{\xi 2} = \{\}$ 
  for  $i = 1 : |\bar{D}|$  do
     $F_1, F_2 \leftarrow \text{Download}(\theta_{\xi 1}^{t-1}, \theta_{\xi 2}^{t-1})$ 
     $(X, Y) \leftarrow \bar{D}[i]$ 
     $Y_1, Y_2 \leftarrow F_1(X), F_2(X)$ 
     $(X, \hat{Y}_1, \hat{Y}_2) \leftarrow \text{Sample\&Refine}(X, Y_1, Y_2, Y, \epsilon)$ 
     $d_i \leftarrow (X, \hat{Y}_1, \hat{Y}_2)$ 
     $\Delta\theta_{\xi 1}^t, \Delta\theta_{\xi 2}^t, \mathcal{L}_i^t \leftarrow \text{Update}(F_1, F_2; d_i)$ 
     $\bar{\theta}_{\xi 1}.\text{add}(\Delta\theta_{\xi 1}^t), \bar{\theta}_{\xi 2}.\text{add}(\Delta\theta_{\xi 2}^t), \bar{\mathcal{L}}.\text{add}(\mathcal{L}_i^t)$ 
  end
   $\theta_{\xi 1}^t, \theta_{\xi 2}^t \leftarrow \text{Aggregate}(\bar{\theta}_{\xi 1}, \bar{\theta}_{\xi 2}, \bar{\mathcal{L}}; \beta, \lambda)$ 
end
return  $\theta_{\xi 1}^T$  and  $\theta_{\xi 2}^T$ 

```

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FIGURE 1: Pseudocode of FedMix

### A. TRAINING NOTATIONS

The collection of N clients' training data.

$$\bar{D} = [D_1, D_2, \dots, D_N]$$

Where, for a given client i

For pixel-level labeled data

$$D_i^L = [X, Y_{gt}]$$

unlabeled data

$$D_i^U = [X]$$

image-level class labeled data

$$D_i^{img} = [X, Y_{img}]$$

bounding box-level labeled data

$$D_i^{bbox} = [X, Y_{bbox}]$$

### B. PSEUDO LABEL GENERATION AND SELECTION (SAMPLE REFINE).

To utilize every available data and ensure reliable local model updates from clients without pixel-level labels, Authors have designed a novel unified framework using every level of the label to amplify and filter useful signals from pseudo supervision.

- FedMix utilizes consistency regularization - cross-pseudo supervision to generate pseudo labels, which are then dynamically filtered and refined before being used for training.
- The training image X is fed to the F1 and F2 models to generate pseudo labels Y1 and Y2, respectively. Y1 and Y2 are then refined, denoted as  $\hat{Y}^1$  and  $\hat{Y}^2$

### C. ADAPTIVE AGGREGATION FOR FEDERATED MODEL UPDATE (AGGREGATE)

- Each participating client updates the model locally with its training data  $D_i$ . Finally, the gradient update from each local client  $\nabla \theta_i^t$  is sent to the server to update the federated model's parameters by

$$\theta_\epsilon^t \leftarrow \theta_\epsilon^{t-1} + \sum_{i=1}^{|\bar{D}|} w_i \nabla \theta_i^t$$

Where  $w_i$  is the aggregation weight of each client, defined below

- $w_i$  is the aggregation weight of each client, defined below

$$c_i \leftarrow \frac{|D_i|}{\sum_{i=1}^{|\bar{D}|} |D_i|}, d_i \leftarrow \frac{(\mathcal{L}_i)^\beta}{\sum_{i=1}^{|\bar{D}|} (\mathcal{L}_i)^\beta}$$

$$w_i \leftarrow \frac{c_i + \lambda d_i}{\sum_{i=1}^{|\bar{D}|} c_i + \lambda d_i}$$

## VI. EXPERIMENTS AND RESULTS

For Experiments and Results, the Authors have used datasets from the breast ultrasound task, Skin tumor segmentation. Because of resource constraints, I used the Skin tumor segmentation task dataset. Results are reproduced for the HAM10K dataset with epoch value 60 where original epoch value was 300.

TABLE II: Statistics of the HAM10K dataset

Site	Source	# Patients	# Images
Rosendahl	rosendahl	1552	2259
Vidir	modern	1695	3363
	old	278	439
	molemax	3954	3954

FIGURE 2: Statistics for HAM10K Dataset

Images from Rosendahl, Vidirodern, Vidir-old, and Vidir-molemax are represented by client1, client2, client3, and client4, respectively, and C3 owns the least amount of data, is selected as the client with pixel-level labels. The levels of labels on C1, C2, and C4 have been adjusted accordingly under different settings.

Original Results for 300 Epochs:-

Supervision	client1	client2	client3	client4
U,U,L,B	77.9±2.2	80.0±2.8	96.5±0.8	91.5±0.7

Reproduced results for 60 Epochs:-

Supervision	client1	client2	client3	client4
U,U,L,B	77.84	82.40	92.15	89.87

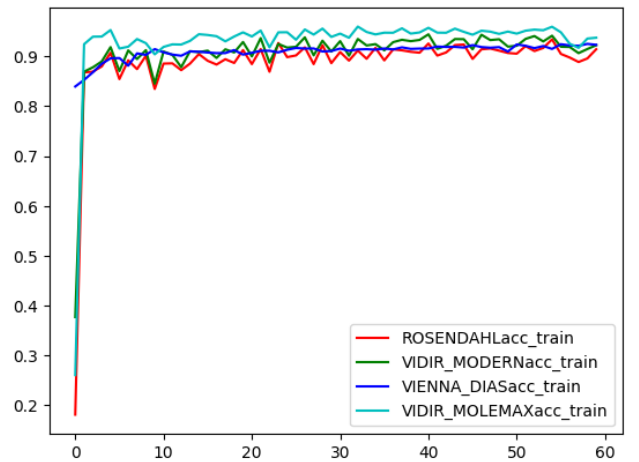


FIGURE 3: Train accuracy vs Epoch

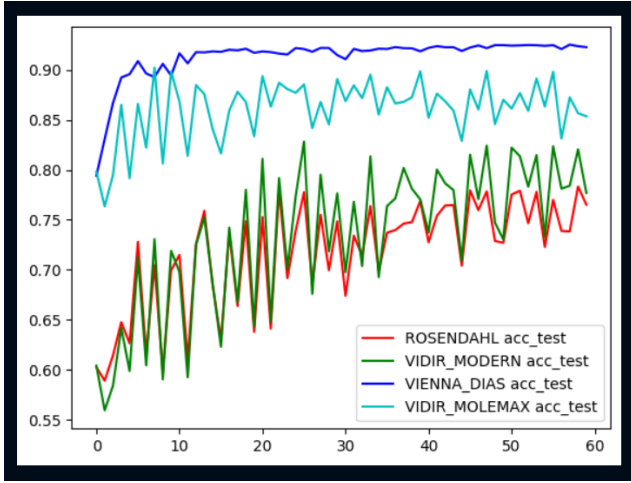


FIGURE 4: Test accuracy vs Epoch

## VII. NOVELTY

### A. PROBLEM STATEMENT

Suppose there are  $N$  clients, denoted  $c_1, \dots, c_N$ . Each client has local unlabelled dataset  $D_i$ . Our goal is to learn deep learning model for each client with the help of central server, where central server has labelled dataset. So, our aim is to utilize the labelled information available at central server side to train local client having unlabelled dataset with the help of model-constrastive loss.

### B. NETWORK ARCHITECTURE

The deep learning network has two components: a base encoder, an output decoder. Each client and central server has same architecture, specifically we are using UNET-3D as deep learning architecture. For ease of presentation, with model weight  $w$ , we use  $R_w()$  to denote the network before the output layer (i.e.,  $R_w(x)$  is the mapped representation vector of input  $x$  till the encoder part).

### C. IMPLEMENTATION DETAILS

At communication round  $t$ , suppose client  $c_i$  is conducting the local training on unlabelled dataset  $d_i$ . It receives the global model  $w^t$  from server and updates his model to  $w_i^t$  in the local train phase. For every input  $x$ , we extract the representation of  $x$  from the global model  $w^t$  i.e.,  $\text{serv} = R_{w^t}(x)$ , representation of  $x$  from the local client model of last round  $w_i^{t-1}$  i.e.,  $\text{past} = R_{w_i^{t-1}}(x)$ , and the representation of  $x$  from the local model being updated  $w_i^t$  i.e.,  $\text{present} = R_{w_i^t}(x)$ . Since the global model should be able to learn better representation with the help of labelled data, our goal is to decrease the distance between present and serv, and increase the distance between present and past.

so we define the model-constrastive loss as,

$$\mathcal{L}_{con} = -\log \frac{\exp(\text{sim}(\text{present}, \text{serv})/\tau)}{\exp(\text{sim}(\text{present}, \text{serv})/\tau) + \exp(\text{sim}(\text{present}, \text{past})/\tau)}$$

where  $\tau$  is temperature parameter.

same objective can be written as

$$\text{Loss} = \mathcal{L}_{con}(w_i^t; w_i^{t-1}; w^t; x)$$

### Algorithm 1

**Input:** Communication round  $T$ , number of clients  $N$ , Number of local epochs  $E$ , temperature  $\tau$ , learning rate  $\eta$

**Hyperparameter:**  $\beta, \lambda$  for FedMIX weighted average

**Output:** The final model  $w^T$

```

1: for  $t \leftarrow 1$  to  $T$  do
2:    $w^t$  server weight at  $t$  time
3:   for  $i \leftarrow 1$  to  $N$  do
4:      $w_i^t \leftarrow w^t$ 
5:     for  $i \leftarrow 1$  to  $E$  do
6:        $\text{clientDataLength.append}(\text{length}(D_i))$ 
7:       for each batch  $b = \{x\}$  of  $D_i$  do
8:          $\text{serv} = R_{w^t}(x)$ 
9:          $\text{output} = R_{w_i^t}(x)$ 
10:         $\text{past} = R_{w_i^{t-1}}(x)$ 
11:         $\text{loss}_i =$ 
12:           $\mu * \text{constrastiveLoss}(\text{past}, \text{output}, \text{serv})$ 
13:         $w_i^t \leftarrow w_i^t - \eta \nabla \text{loss}_i$ 
14:      end for
15:    end for
16:     $\text{loss.append}(\text{loss}_i^\beta)$ 
17:     $\text{localWeight.append}(w_i^t)$ 
18:  end for
19:   $w^{t+1} =$ 
20:     $\text{aggregate}(\text{loss}, \text{localWeight}, \text{clientDataLength}, \lambda)$ 
21: end for
```

The overall federated learning algorithm is shown in algorithm1. In each communication round server sends the global model to the clients, receives the local model from the parties, and updates the global model using weighted averaging fed-MIX. In local training each client uses stochastic gradient descent to update the weight which later be send to global model.

After the training of each local client, we are using fedMIX weighted averaging for calculating the final weight  $w^{t+1}$  which will be later send to the server.

FedMix presents a novel adaptive aggregation as explained in section V-C, unlike FedAVG, FedMix also consider the loss of each client with the dataset length for calculating the weightage given to each local client weight. FedMix aims to alleviate the training instability which may arise from naively aggregating local client model updates. The weight of each client is determined according to its data quantity and quality (inferred from training loss). In this way, more

reliable clients will be assigned with higher weights, leading to better convergence.

Integration of FedMIX weighted averaging is explained in algorithm2

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**Algorithm 2**  $\text{aggregate}(loss, localWeight, clientDataLength, \lambda)$

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```

1: denominatorDI =  $sum(loss)$ 
2:  $d = []$ 
3: for  $\mathcal{L}_i$  in  $Loss$  do
4:    $d.append(\mathcal{L}_i / denominatorDI)$ 
5: end for
6: denominatorCI =  $sum(clientDataLength)$ 
7:  $c = []$ 
8: for  $d_i$  in  $clientDataLength$  do
9:    $c.append(d_i / denominatorCI)$ 
10: end for
11:  $fedmix = []$ 
12: for  $i \leftarrow 1 \text{ to } N$  do
13:    $fedmix.append(c[i] + \lambda * d[i])$ 
14: end for
15: denominatorWI =  $sum(fedmix)$ 
16:  $w = []$ 
17: for  $n_i$  in  $fedmix$  do
18:    $w.append(n_i / denominatorWI)$ 
19: end for
20: for  $i \leftarrow 1 \text{ to } N$  do
21:    $localWeight[i] = localWeight[i] * w[i]$ 
22: end for
23:  $w^{t+1} = sum(localWeight)$ 
24: return  $w^{t+1}$ 

```

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for the calculation of  $w_i$  for particular local client, we will first calculate the  $c_i$  which will consider the dataset length of local client which is under consideration, then we will calculate  $d_i$ , which will consider the training loss of localclient client which is under consideration, and then finally we will calculate the  $w_i$  based on  $d_i$  and  $c_i$ .

$\lambda$  and  $\beta$  are hyper-parameters to tune, impacting the degree of reliance on different clients. **Thus, adaptive weight assignment according to training loss not only prioritizes learning from more informative clients.**

## REFERENCES

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