

Evaluate Model Performance

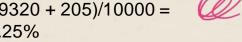
Evaluating the performance of classification models

- Popular criteria
 - Accuracy (misclassification) rate: % of correct classifications
 - Confusion matrix
 - Lift curve/ROC curve
- Other evaluation criteria
 - Speed and scalability
 - Interpretability
 - Robustness



Accuracy (Misclassification) rate

• Accuracy rate = $\frac{\text{Number of correct classifications}}{\text{Number of instances in dataset}}$; = $\frac{(9320 + 205)/10000}{95.25\%}$



• $Misclassification\ rate = 1 - Accuracy\ Rate = (128 + 347)/10000 = 4.75\%$

		True d	default	t status	
		No	Yes	Total	
Predicted	No	9320	128	9448	
$default\ status$	Yes	347	205	552	
	Total	9667/	333	(10000)	





Confusion Matrix

• A **confusion matrix** records the source of error:

Type I error: False positives

• Type II error: False negatives

Actual class

	Predicted class		
	Positive Negative		
Positive	True positive	False negative	
Negative	False positive	True negative	

• Suppose 950 mails are sent out

• What is the accuracy rate?

Predicted class

Actual class

	Respond	Do not respond
Respond	250	40
Do not Respond	10	650

Confusion Matrix - Evaluation

 Below shows the performance of two classifiers. Which one is better based on accuracy?

Model 1 - Predicted class

Actual class

	Respond	Do not respond		
Respond	5	5		
Do not Respond	40	950		

- Accuracy = (5+950)/1000 = 95.5%
- Misclassification rate = 4.5%

Model 2 - Predicted class

Actual class

	Respond	Do not respond
Respond	10	0
Do not Respond	90	900

- Accuracy= 91%?
- Misclassification rate = 9%?



• Suppose cost of mailing to a non-responder is \$1, and (net) lost revenue of not mailing to a responder is \$20.

Now from cost perspective, which classifier is better?

Model 1 - Predicted class

Actual class

	Respond		Do not respond	
Respond	5		5	
Do not Respond	40		950	

Model 2 - Predicted class

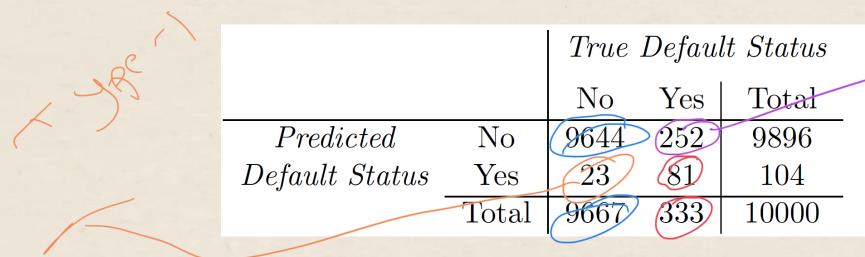
Actual class

	Respond	Do not respond
Respond	10	0
Do not Respond	90	900

• Cost = 0 * 20 + 90 *1 = 90



The credit card default



- What is Type I error rate? 23 What is Type II error rate? 252
- As a credit card company, which type of error would it like to avoid more? Type II error is more important.
- Sensitivity: the proportion of all positives that are correctly identified as positives True positive rate 81/333 =
- **Specificity**: the proportion of all negatives that are correctly identified as negatives True negative rate 9644/9667 =

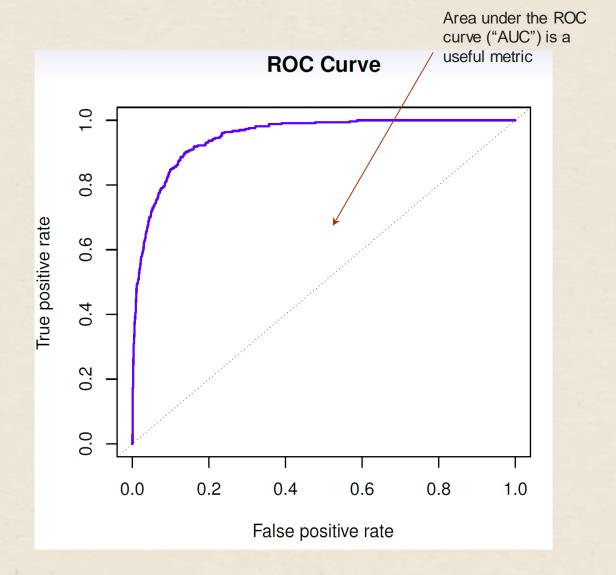
The credit card default

		True default status		
		No	Yes	Total
$\overline{Predicted}$	No	9,432	138	9,570
$default\ status$	Yes	235	195	430
	Total	9,667	333	10,000

- We adjust the threshold probability from 0.5 to 0.2
- Sensitivity increases
- It comes at a cost of decreasing specificity and slightly increasing error rate
- There is a trade-off between sensitivity and specificity

ROC curve

- ROC curve depicts the trade-off between
 Sensitivity vs Specificity
- It displays two types of errors for all possible thresholds
- False positive rate: 1 specificity
- The overall performance is given by the area under the curve: the larger the better
- An ideal ROC curve will hug the top left corner





Takeaways

- Discriminant analysis: models and assumptions
 - o LDA
 - o QDA
 - Naïve Bayes
- The comparison between them
- Evaluate performance of different methods
 - Accuracy rate
 - Confusion matrix
 - ROC curve

