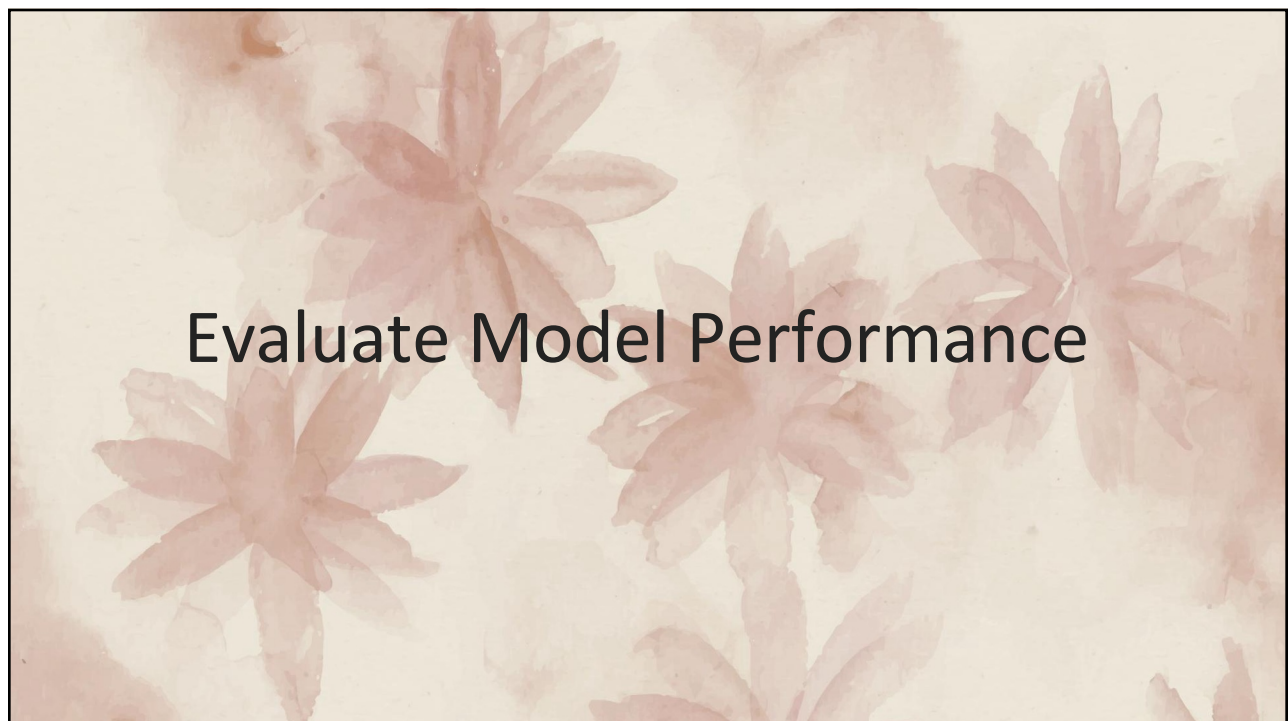


1



2

## Evaluating the performance of classification models

- Popular criteria
  - Accuracy (misclassification) rate: % of correct classifications
  - Confusion matrix
  - Lift curve/ROC curve
- Other evaluation criteria
  - Speed and scalability
  - Interpretability
  - Robustness

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### Accuracy (Misclassification) rate

- Accuracy rate =  $\frac{\text{Number of correct classifications}}{\text{Number of instances in dataset}}$ ;  $= (9320 + 205)/10000 = 95.25\%$
- *Misclassification rate* =  $1 - \text{Accuracy Rate} = (128 + 347)/10000 = 4.75\%$

		<i>True default status</i>		
		No	Yes	Total
<i>Predicted default status</i>	No	9320	128	9448
	Yes	347	205	552
Total		9667	333	10000

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## Confusion Matrix

- A **confusion matrix** records the source of error:

- **Type I error: False positives**
- **Type II error: False negatives**

**Actual  
class**

		<b>Predicted class</b>	
		Positive	Negative
<b>Actual class</b>	Positive	True positive	False negative
	Negative	False positive	True negative

- Suppose 950 mails are sent out
- What is the accuracy rate?

**Actual  
class**

		<b>Predicted class</b>	
		Respond	Do not respond
<b>Actual class</b>	Respond	250	40
	Do not Respond	10	650

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## Confusion Matrix - Evaluation

- Below shows the performance of two classifiers. Which one is better based on accuracy?

**Model 1 - Predicted class**

		Respond	Do not respond
<b>Actual class</b>	Respond	5	5
	Do not Respond	40	950

- Accuracy =  $(5+950)/1000 = 95.5\%$
- Misclassification rate = 4.5%

**Model 2 - Predicted class**

		Respond	Do not respond
<b>Actual class</b>	Respond	10	0
	Do not Respond	90	900

- Accuracy = 91%?
- Misclassification rate = 9%?

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## Asymmetric costs of different types of errors

- Suppose cost of mailing to a non-responder is \$1, and (net) lost revenue of not mailing to a responder is \$20.

Now from cost perspective, which classifier is better?

Model 1 - Predicted class

Actual class	Predicted class	
	Respond	Do not respond
	Respond	Do not Respond
Respond	5	5
Do not Respond	40	950

$$\bullet \text{ Cost} = 5 \times 20 + 40 \times 1 = \$140$$

Model 2 - Predicted class

Actual class	Predicted class	
	Respond	Do not respond
	Respond	Do not Respond
Respond	10	0
Do not Respond	90	900

$$\bullet \text{ Cost} = 0 \times 20 + 90 \times 1 = 90$$

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## The credit card default

		True Default Status		
		No	Yes	Total
Predicted Default Status	No	9644	252	9896
	Yes	23	81	104
Total		9667	333	10000

- What is Type I error rate? - 23 What is Type II error rate? - 252
- As a credit card company, which type of error would it like to avoid more? Type II error is more important.
- Sensitivity:** the proportion of all positives that are correctly identified as positives - True positive rate –  $81/333 =$
- Specificity:** the proportion of all negatives that are correctly identified as negatives – True negative rate  $9644/9667 =$

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### The credit card default

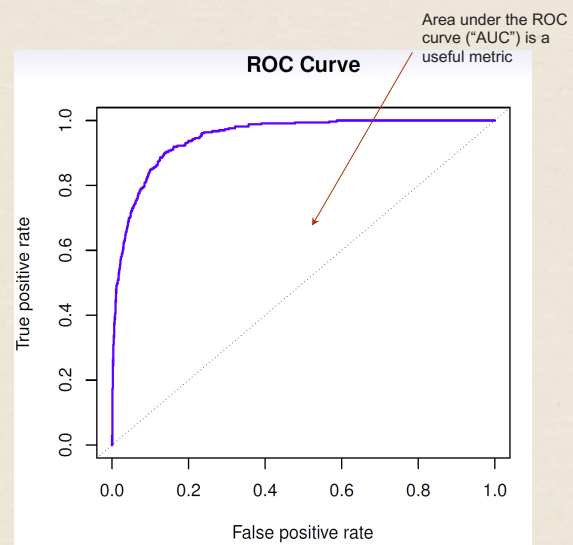
		<i>True default status</i>		
		No	Yes	Total
<i>Predicted default status</i>	No	9,432	138	9,570
	Yes	235	195	430
Total		9,667	333	10,000

- We adjust the threshold probability from 0.5 to 0.2
- Sensitivity increases
- It comes at a cost of decreasing specificity and slightly increasing error rate
- There is a trade-off between sensitivity and specificity

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### ROC curve

- ROC curve depicts the trade-off between **Sensitivity** vs **Specificity**
- It displays two types of errors for all possible thresholds
- False positive rate: **1 - specificity**
- The overall performance is given by the area under the curve: the larger the better
- An ideal ROC curve will hug the top left corner



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## Takeaways

- Discriminant analysis: models and assumptions
  - LDA
  - QDA
  - Naïve Bayes
- The comparison between them
- Evaluate performance of different methods
  - Accuracy rate
  - Confusion matrix
  - ROC curve