Exercises

Introduction to Linear Models: ANOVAs, Multiple Regression and ANCOVA

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Exercise 1: Clinical trials

A clinical trial was conducted to study the effect the levels of a drug on some measure of well-being (called SCORE in this case). Both male and female subjects were randomly choosen for the study and then randomly assigned to to either a low or a high DOSE treatment.

To read this data, directly from the web, into an object called drugTrials, do the following in R:

```
drugTrials <- read.csv("https://git.io/Jew2T")</pre>
```

Make sure the data is read in correctly. If it is read correctly, there should be 48 rows and 4 columns (we don't need the first column which is unique ID for each individual).

- 1.) Perform some exploratory analysis on the data set and answer the following questions: (a) Do you think the SCOREs are different between genders? (b) are SCORES different between differend doses of the drug? (c) is there an interaction between GENDER and DOSE? (d) is this data set balanced (i.e. equal observations across all subgroups)?
- 2.) Carry out a two way ANOVA with interaction on this data set and answer the following questions (a) Is the interaction effect signficant? (b) are any of the main effects signficant? (c) if the interaction is signficant can you still easily interpret the results for any significant main effects?
- 3.) Carry out the appropriate Tukey Post-hoc tests and examine the results. do they contradict your interpretation of 2(c)?
- 4.) Evaluate the assumptions of the anova model for the drug trial data? Are there any assumptions violated? Which one might be the most problematic?

Exercise 2: The Diet Experiment

This data for this study comes from an experiment in which people were put on one of three diets to encourage weight gain. Additionally the diets were trialled in three different countries.

To read this data, directly from the web, into an object called dietData, do the following in R:

```
dietData <- read.csv("https://git.io/JewFx")</pre>
```

Make sure the data is read in correctly. If it is read correctly, there should be 27 rows and 3 columns.

- 1.) Perform some exploratory analysis on the data set and answer the following questions: (a) Do you think the different diets are equally effective for weight gain? (b) How do you think country of origin might influence weight gain? (d) is this data set balanced (i.e. equal observations across all subgroups)?
- 2.) Carry out a two way ANOVA with interaction and Tukey post-hoc tests to determine which diet is most effective for weight gain? Is there a single answer to the previous question? Why or why not?
- 3.) Evaluate the assumptions of the anova model for the drug trial data? Are there any assumptions violated? Which one might be the most problematic?

4.) Visualize your results as interaction plot (as in the lecture slides), make sure to provide standard errors for means of all subgroups.

Exercise 3: Swiss Fertility data

For the follow exercise we will use a built-in data set in R. To load the dataset, type the following in R data(swiss)

Briefly this data includes a standardized fertility measure from 47 french-speaking provinces in Switzerland from 1888. It also includes 5 socio-economic indicators of the provinces as well. For further details type help(swiss). All variables have been scaled to a numerical continuous scale.

We would like to understand what influence, if any, the 5 socio-economic factors have on fertility.

- 1. Use the pairs() function to draw scatterplots of all 6 variables with one another: (a) Which variables seem most correlated with Fertility (b) Which variables seem highly correlated with one another? (c) Which variable would you choose to model changes in fertility?
- 2. Use the following code to fit all 5 variables as the explanatory variables for fertility and the save the fit in 'fit1:

```
fit1 <-lm(Fertility ~ . , data = swiss)</pre>
```

Call summary() on the saved model. Are all the slopes/coefficients significant? Are there any results surprising based on your plots from (1) above?

- 3. Use the vif() function from the car package, on fit1 to find the variable that leads to the most variance inflation. Fit a new linear model that omits this variable but retains the other 4 variables, save this model as fit2. Perform a nested likelihood ratio to test which model fit1 or fit2 is more appropriate. Note if the car package is not installed, you will have to install it yourself.
- 4. Repeat the process above to find the variable that leads to the most variance inflation in fit2. Fit a new linear model that omits this variable but retains the other 3 variables, save this model as fit3. Perform a nested likelihood ratio to test which model fit1, fit2 or fit3 is more appropriate.
- 5. For the best fitting model from (4) check all the assumptions of the multiple linear regression model. Do any of them seem particularly problematic?

Exercise 4: Stickleback Association Study