



Biomedical Imaging

Magnetic Resonance Imaging

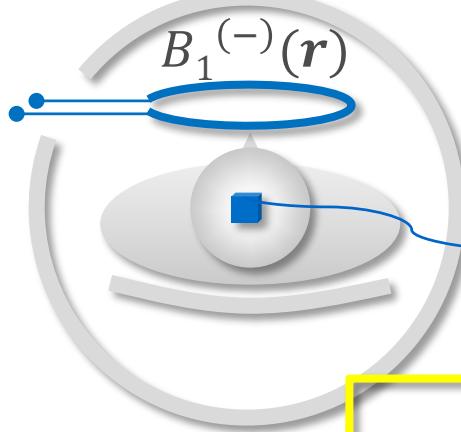
Sebastian Kozerke, Klaas Pruessmann

Institute for Biomedical Engineering
University and ETH Zurich

Signal and noise

Signal-to-noise ratio

Signal

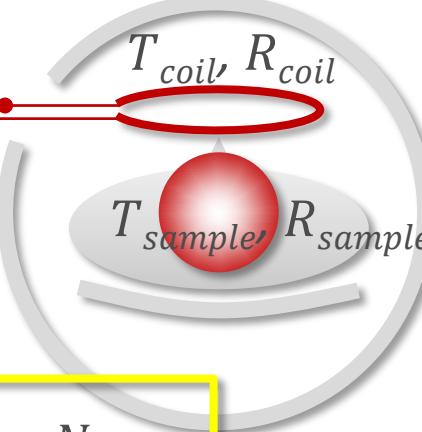


U_{signal}

$B_1^{(-)}(\mathbf{r})$

$M_{xy}(\mathbf{r})$

Noise



U_{noise}

T_{coil}, R_{coil}

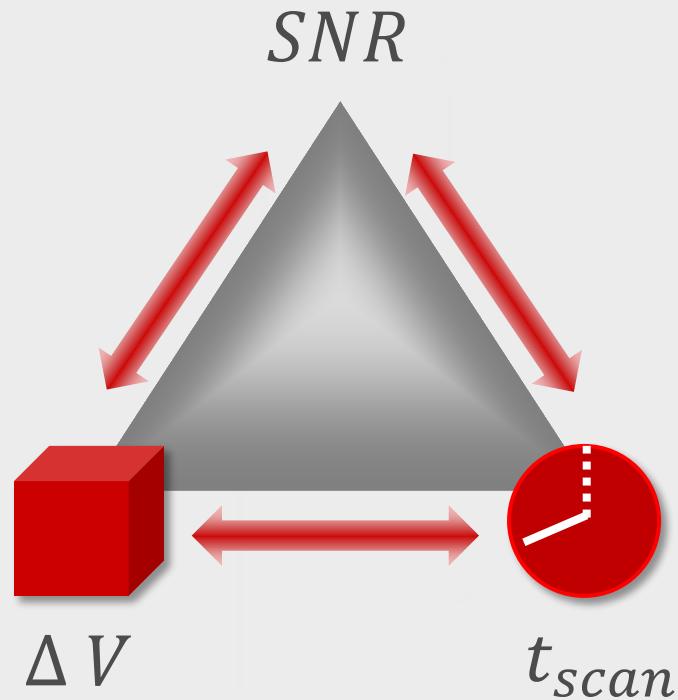
T_{sample}, R_{sample}

$t_{acq} \propto BW^{-1}$

$t_{scan} \propto N_{avg}$

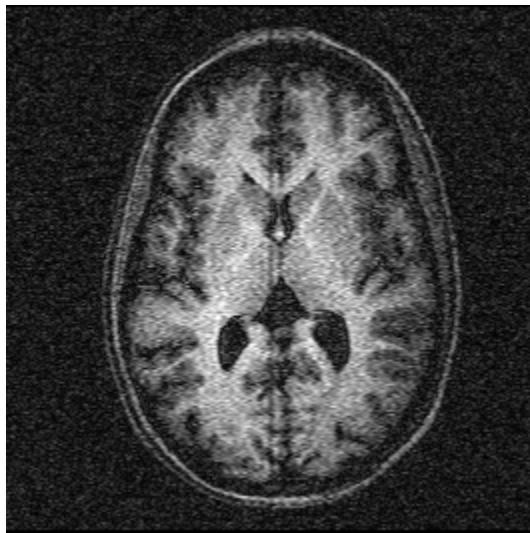
$$SNR = \frac{U_{signal}}{\sigma(U_{noise})} = \frac{\omega B_1^{(-)}(\mathbf{r}) M_{xy}(\mathbf{r}) \Delta V}{\sqrt{4\kappa_B BW(T_{sample}R_{sample} + T_{coil}R_{coil})} \sqrt{N_{avg}}}$$

$$SNR \propto \Delta V \sqrt{t_{scan}}$$



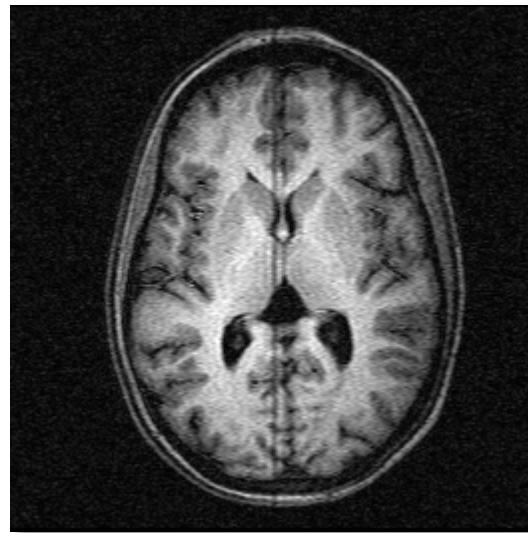
SNR – Speed – Image quality

SNR = 8



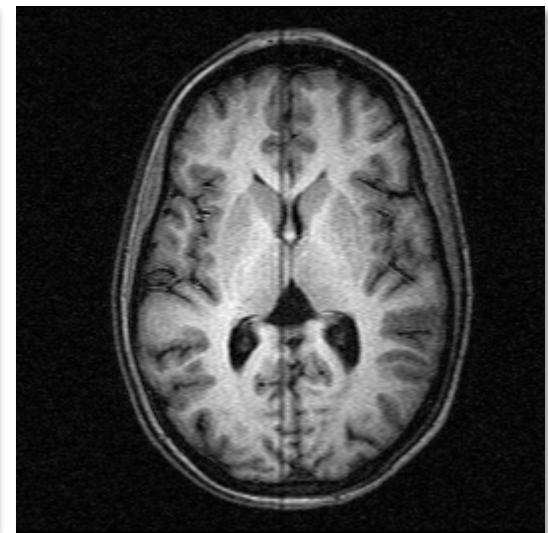
$N_{avg} = 1$
3 sec

SNR = 16



$N_{avg} = 4$
12 sec

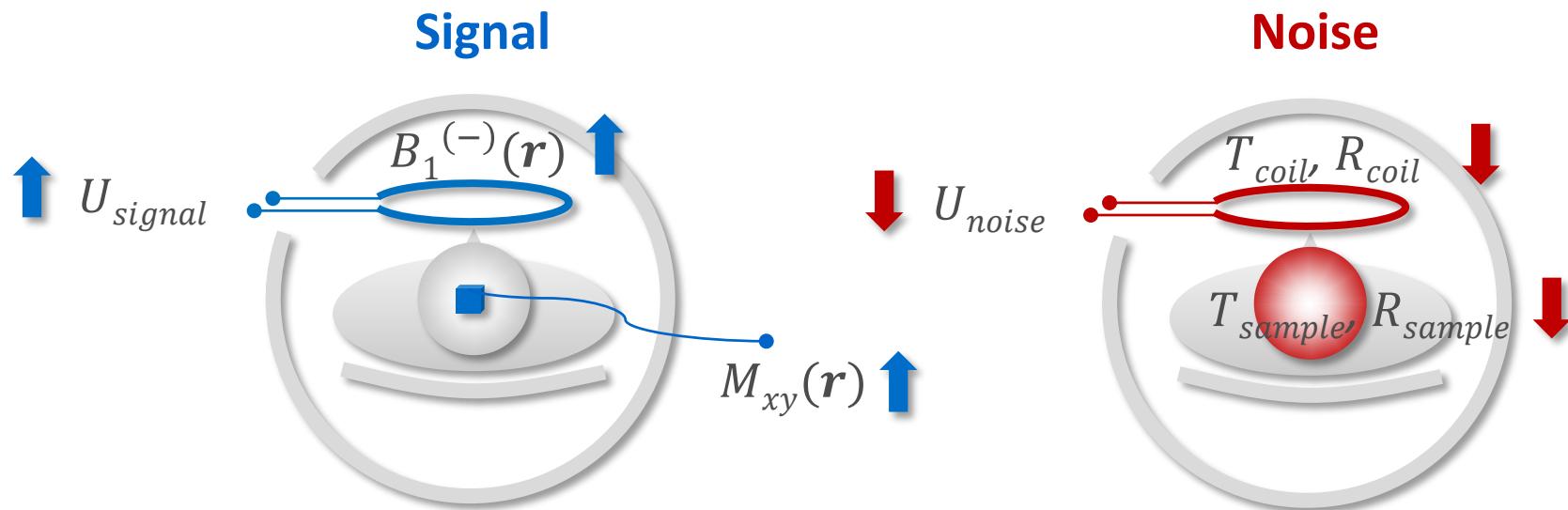
SNR = 23



$N_{avg} = 8$
24 sec

Signal and noise

Increasing SNR efficiency



Increase signal voltage

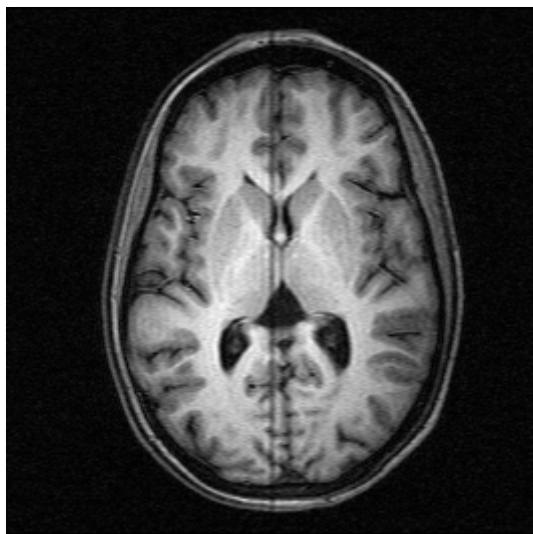
- Increase $B_1^{(-)}(r)$
- Increase magnetization $M_{xy}(r)$
- Increase frequency ω

Reduce noise voltage

- Minimize sample losses R_{sample}
- Minimize coil temperature T_{coil}
- Reduce coil resistance R_{coil}

Spatial resolution

MR imaging

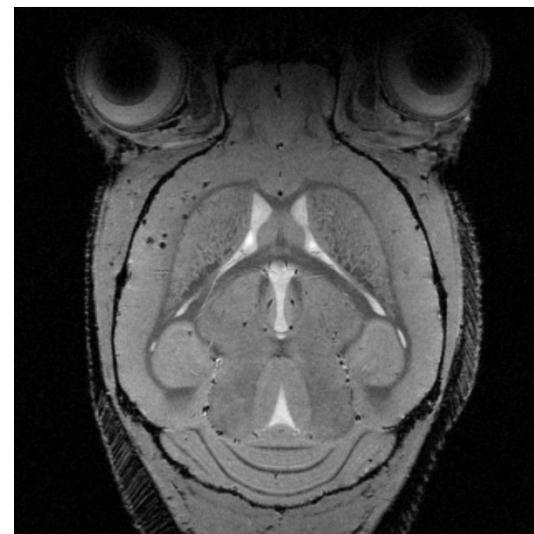


$0.7 \times 0.7 \times 2 \text{ mm}^3$, 1 min



$3 \cdot 10^{19}$ water molecules/voxel

MR microscopy



$50 \times 50 \times 200 \mu\text{m}^3$, 1 min

0.0005 mm^3 •

$1.5 \cdot 10^{16}$ water molecules/voxel

2000

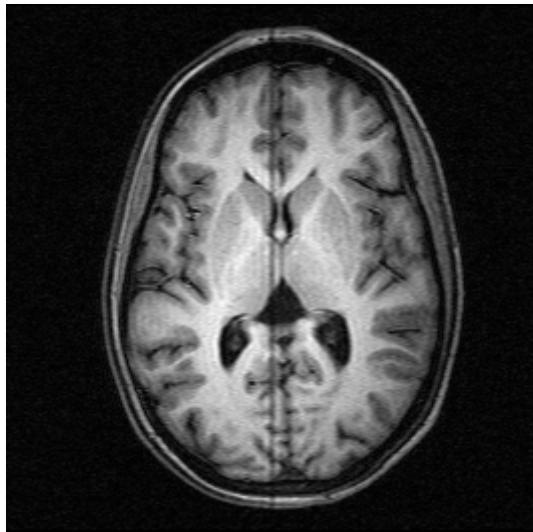
:

1

Signal and noise

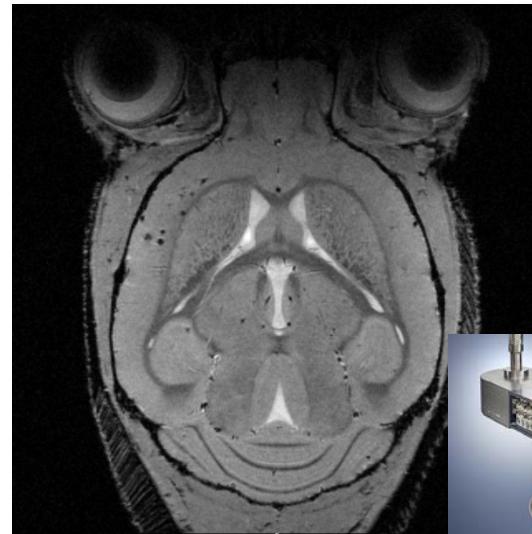
Maximizing signal-to-noise

MR imaging



0.7x0.7x2 mm³

MR microscopy



50x50x200 µm³ CryoProbe

Field B_0 3.0 Tesla

Frequency ω 128 MHz

Sensitivity S 20 cm coil

Coil temp T_{coil} 300 K

9.4 Tesla

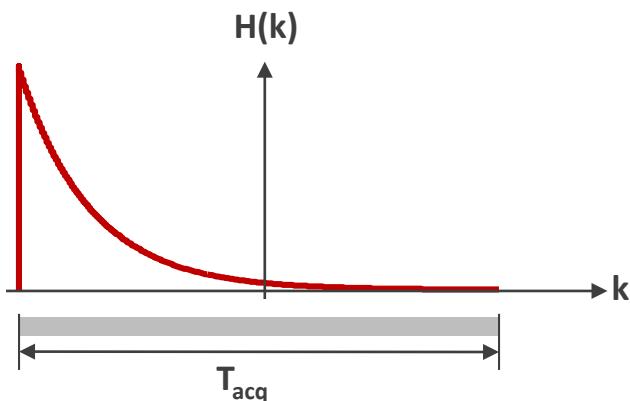
400 MHz

1 cm coil

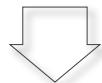
30 K

Resolution limits

Relaxation

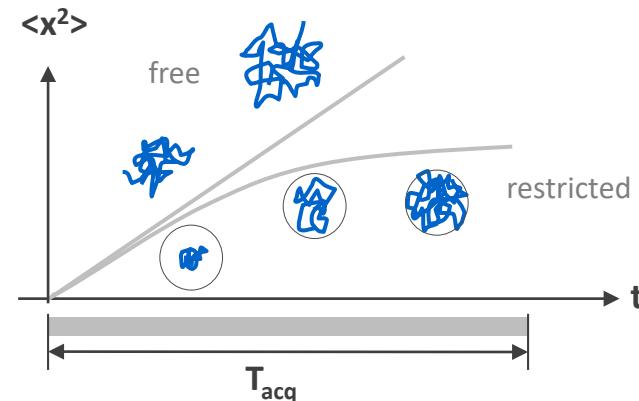


$$H(k) = \text{rect}\left(\frac{k}{2k_{max}}\right) e^{-t/T_2^*}$$

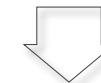


$$\Delta x \geq \frac{\pi}{\gamma G_{max} T_2^*}$$

Diffusion



$$\langle \Delta x^2 \rangle = 6DT_{acq}$$

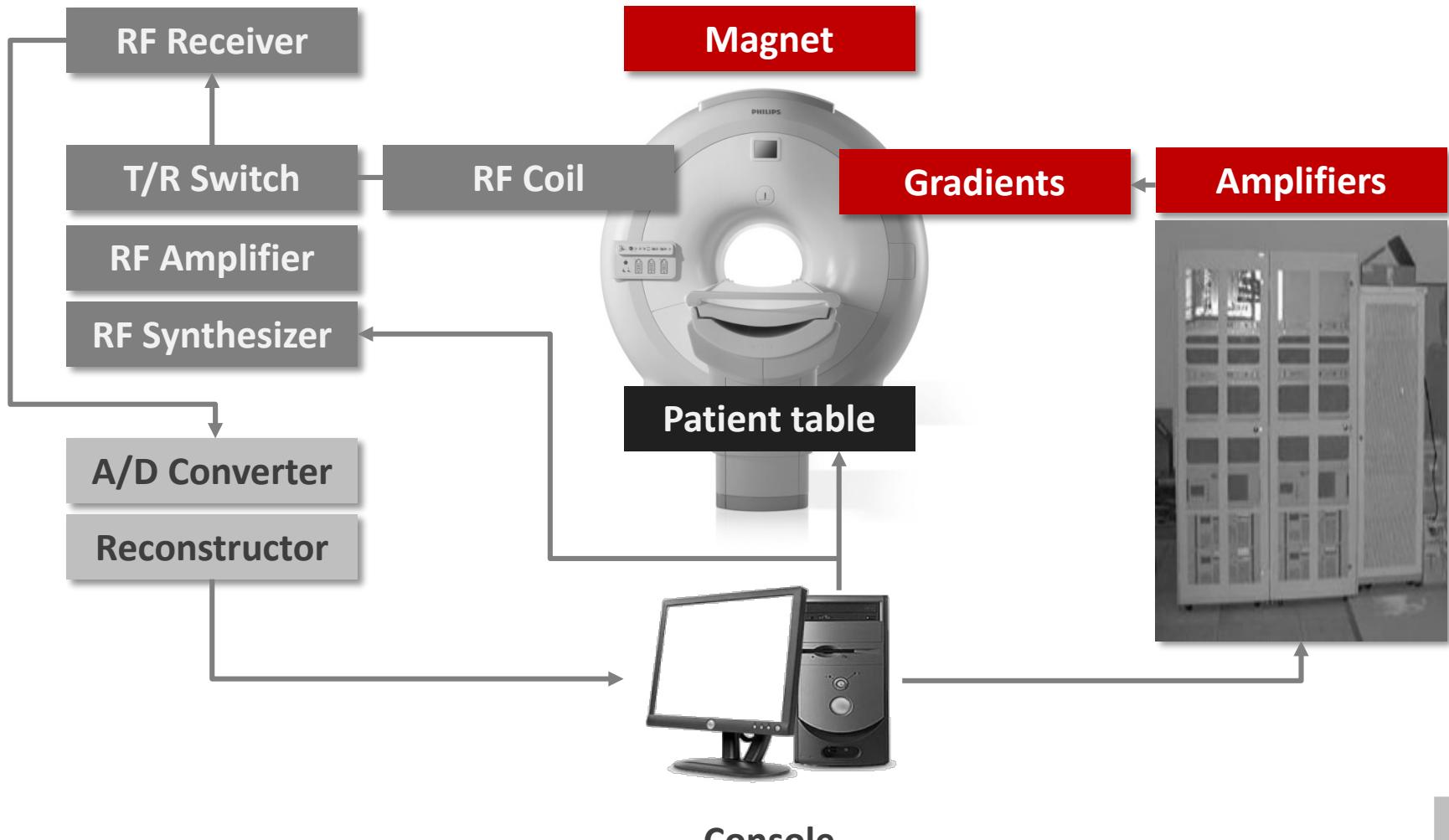


$$D = 1 \cdot 10^{-3} \frac{\text{mm}^2}{\text{s}}$$

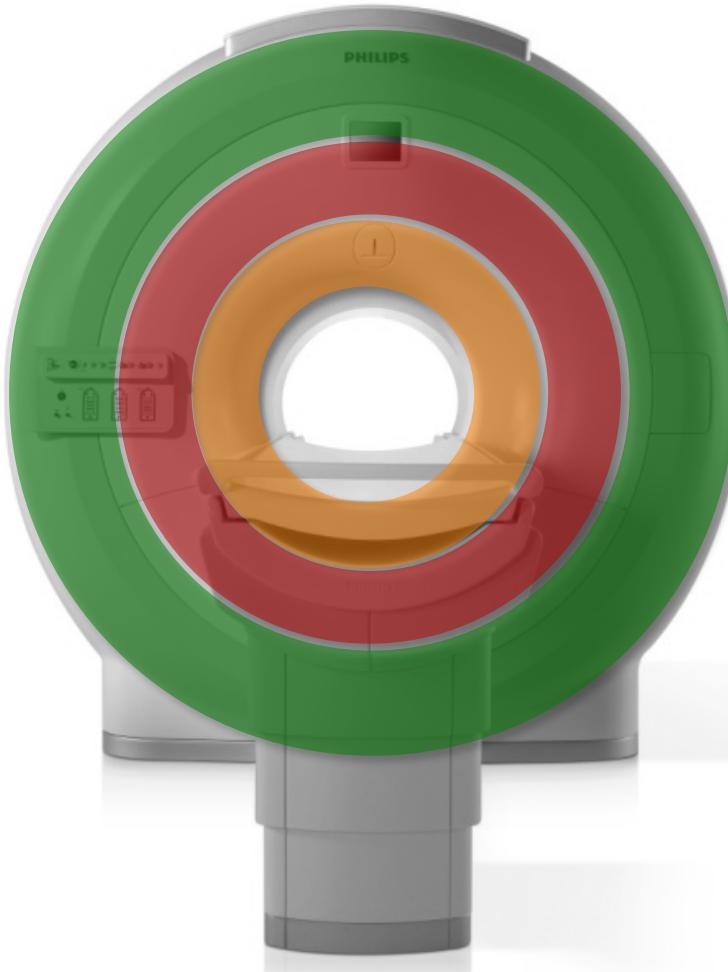
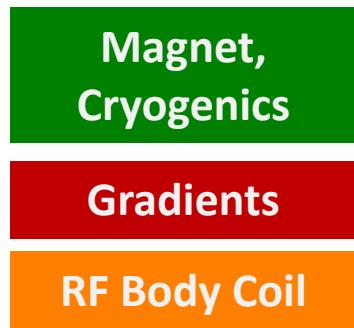
$$T_{acq} = 10 \text{ ms} \Rightarrow \Delta x \geq 8 \mu\text{m}$$



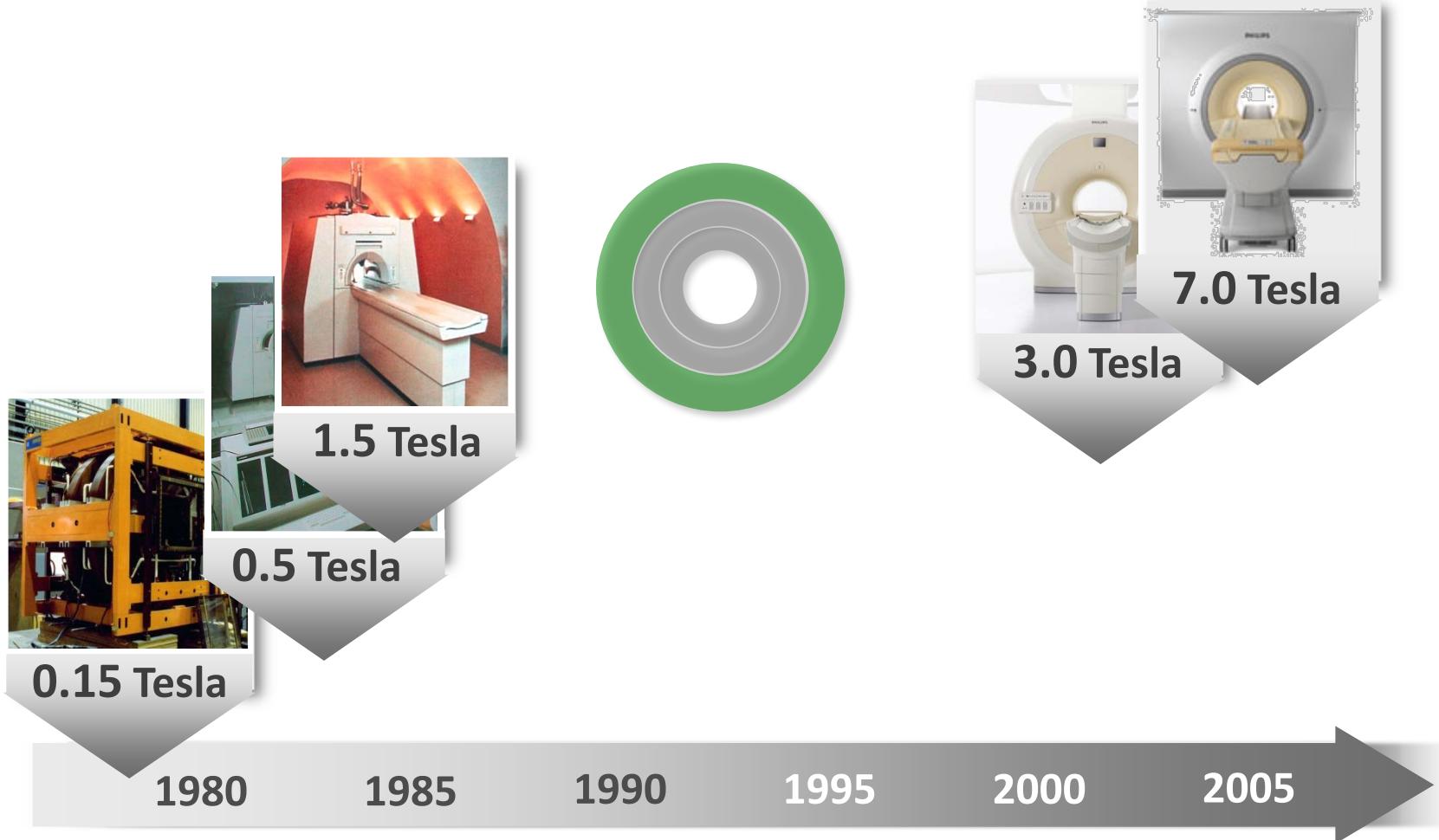
Magnetic Resonance Hardware



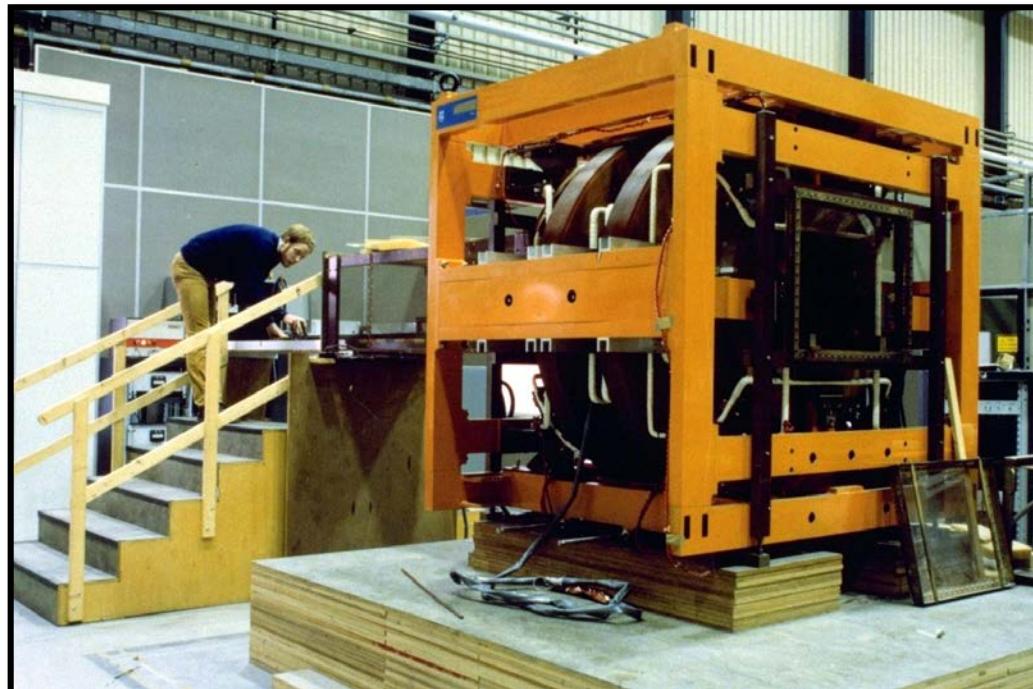
Magnetic Resonance Hardware



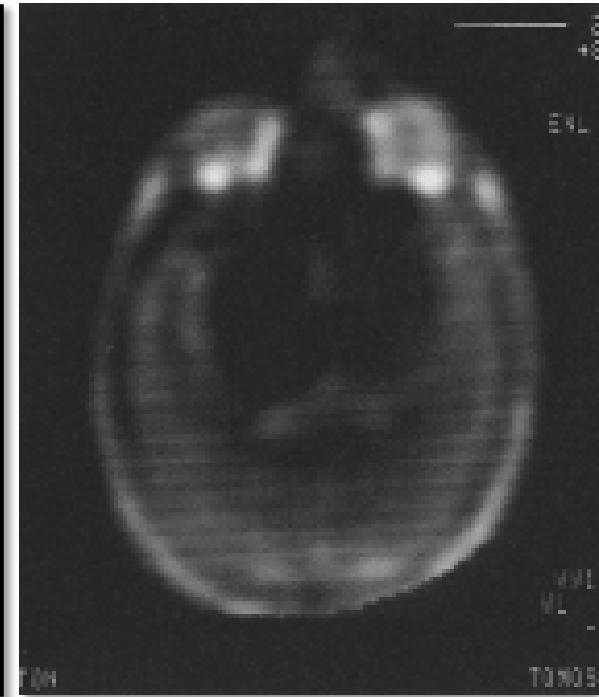
Magnet



Magnet



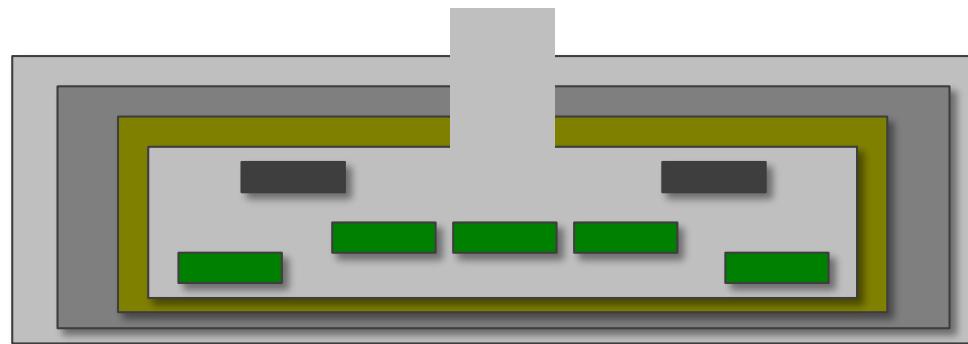
0.15 Tesla, resistive magnet (50 kW)



**First human image (in Europe)
December 3, 1980**

Superconducting Magnets

Cryo-Pump



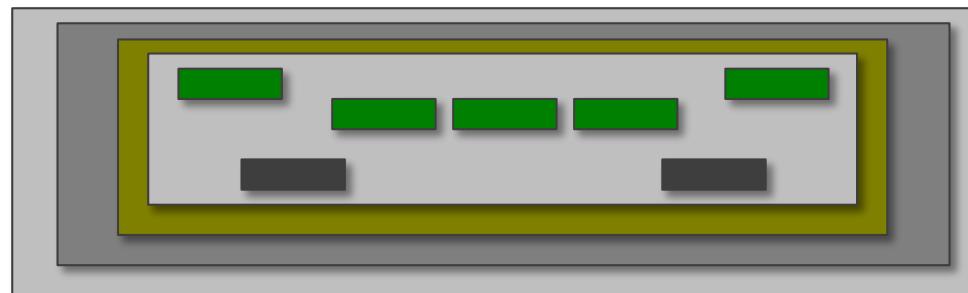
70K Shield

20K Shield

Liquid Helium

Field Coils

Shield Coils



Niobium-Titanium

Magnet



1.0 Tesla vertical field

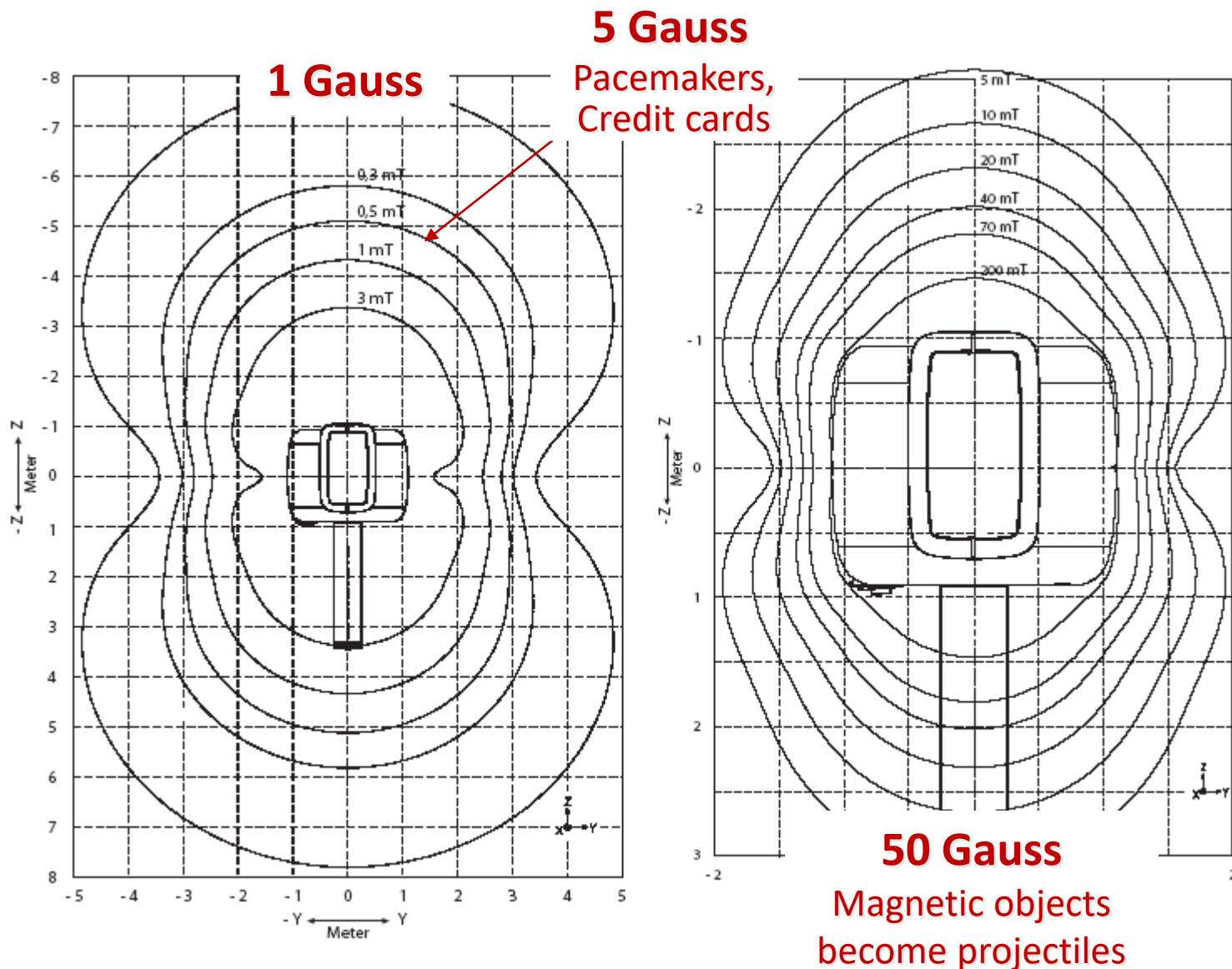


3.0 Tesla horizontal field

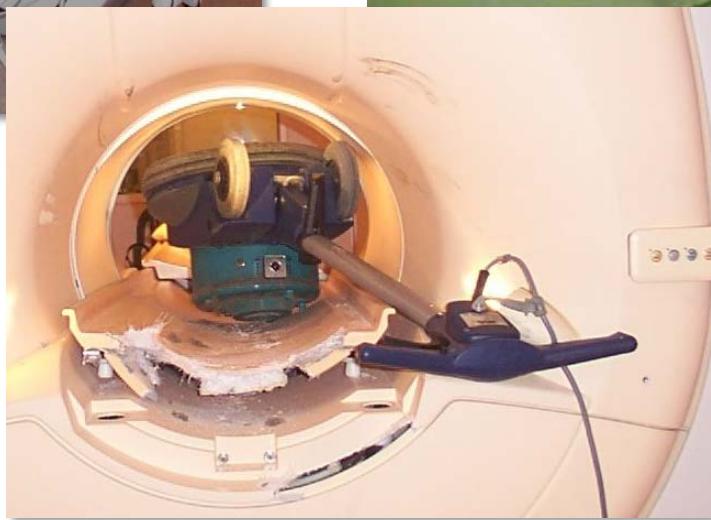
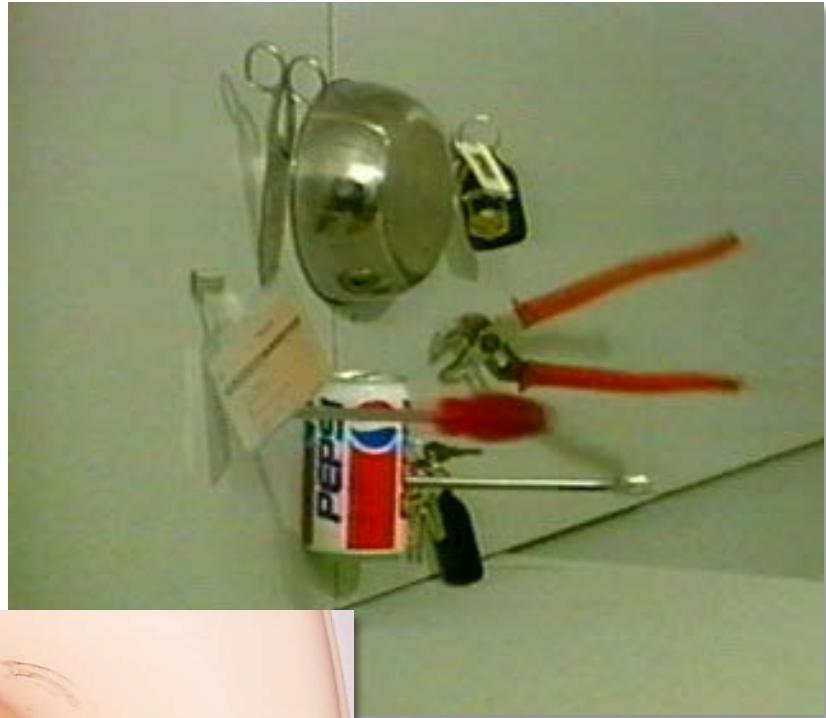
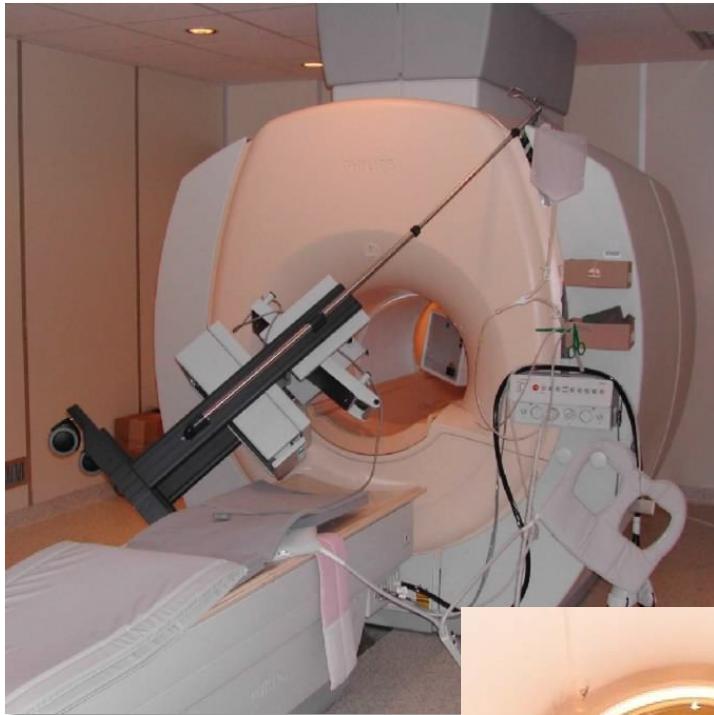
Magnet



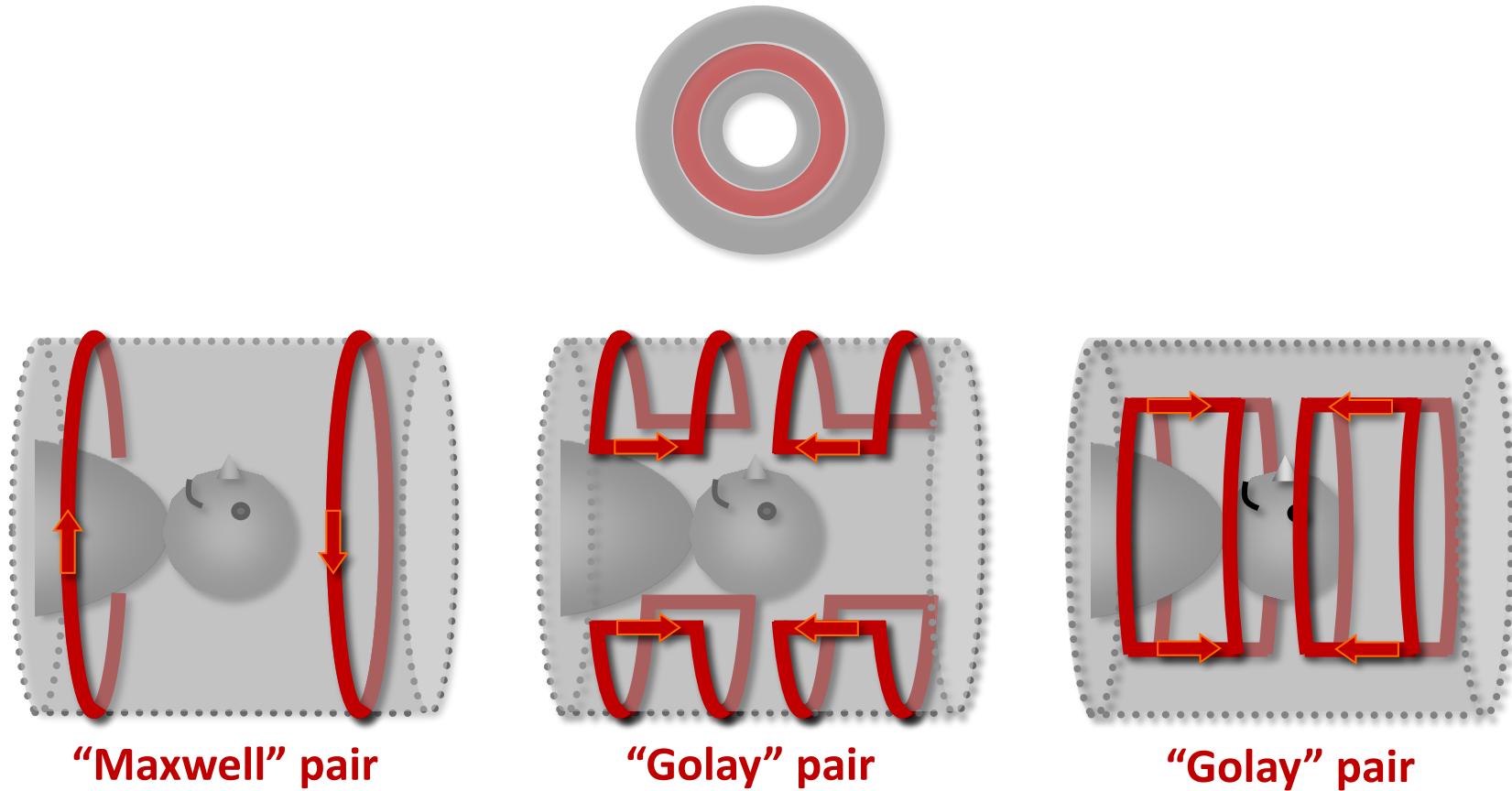
Magnet stray field



Magnetic stray field hazards

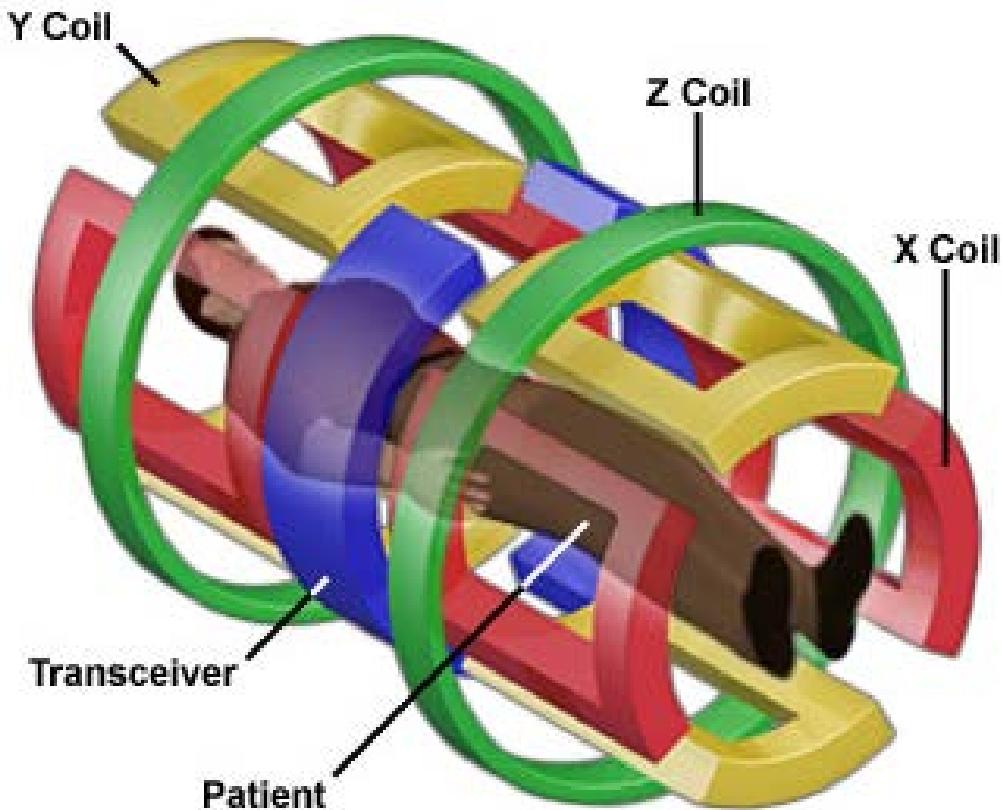


Gradients



Gradients

Basic Design

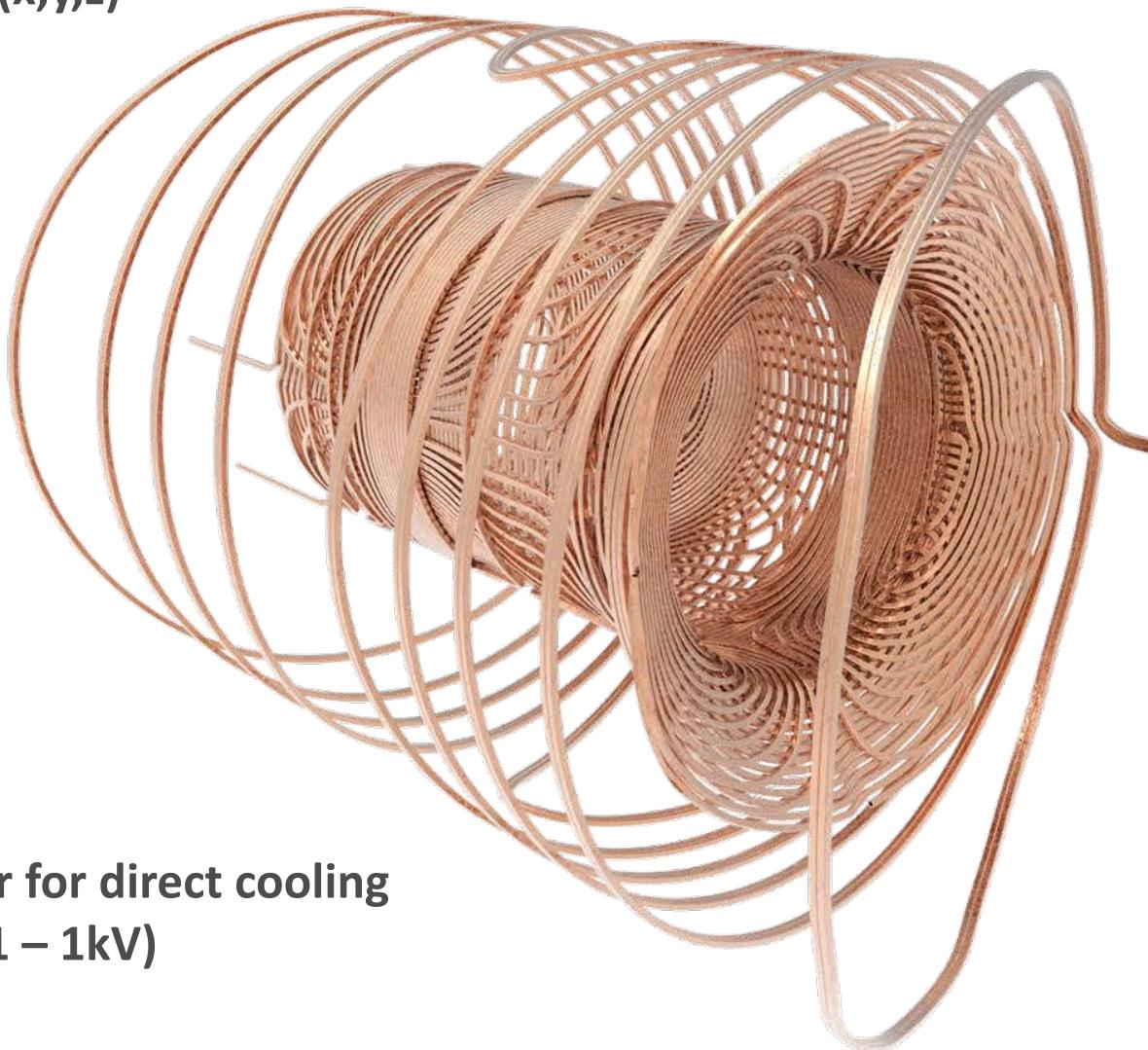


Gradients

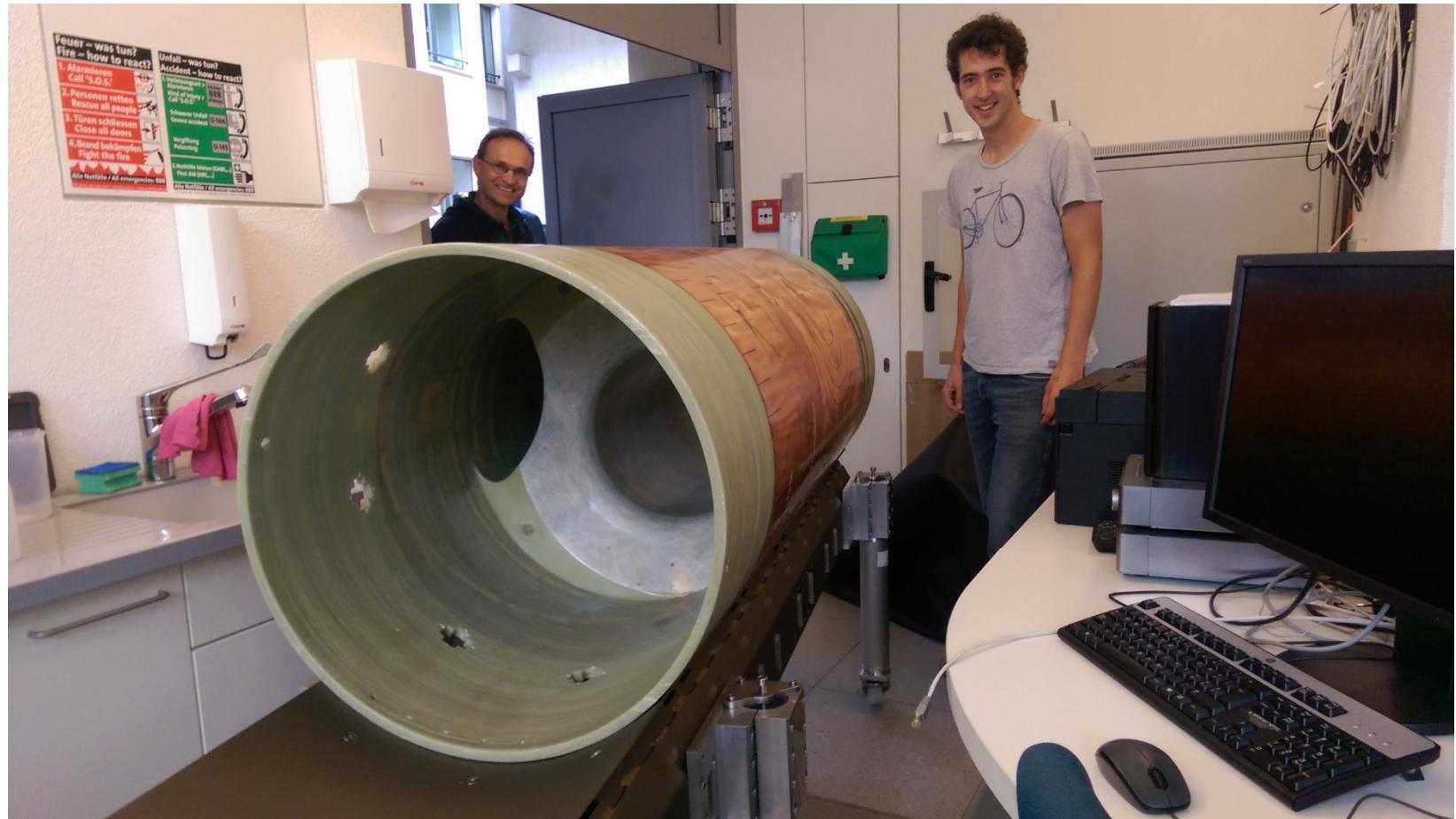
Advanced Design (x,y,z)

shield windings

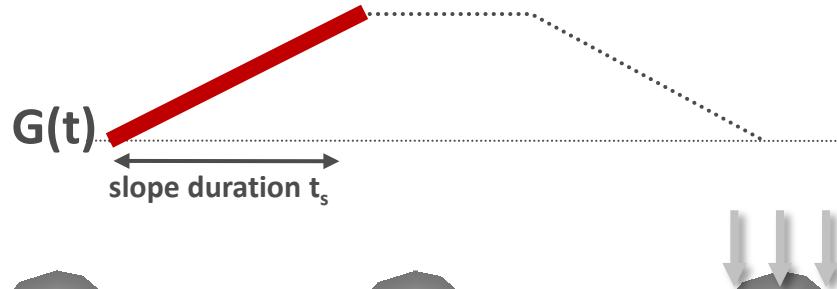
**hollow conductor for direct cooling
(100 - 1000 A, 0.1 – 1kV)**



Gradients

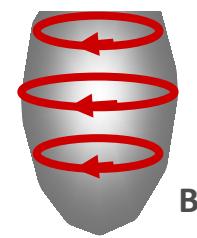
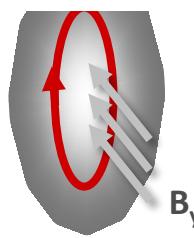
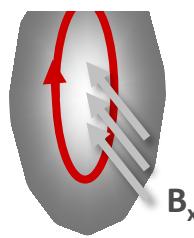


Peripheral nerve stimulation



Membrane depolarization of peripheral nerve cells...

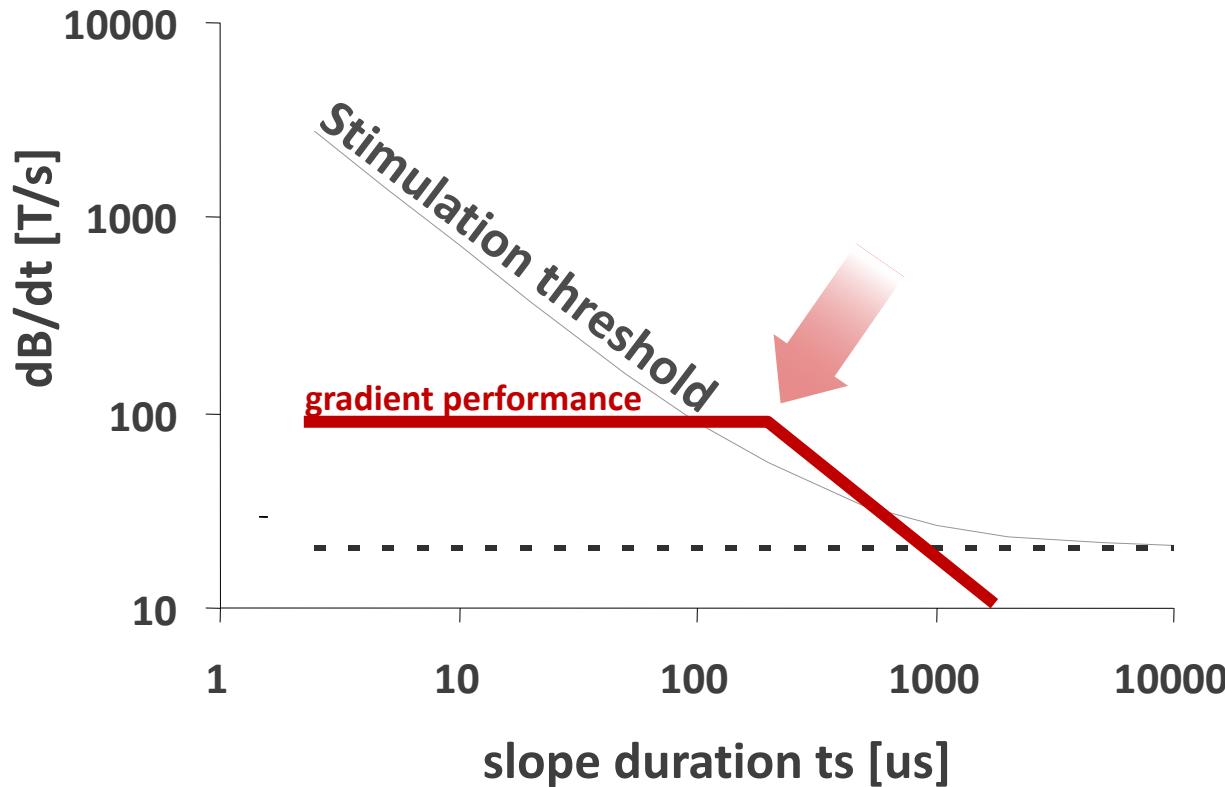
(threshold of cardiac muscle stimulation factor 80 greater)



$$\sqrt{\sum \left(w \frac{\partial B}{\partial t} \right)^2} < 20 \frac{T}{s} \left(1 + \frac{0.36ms}{t_s} \right)$$

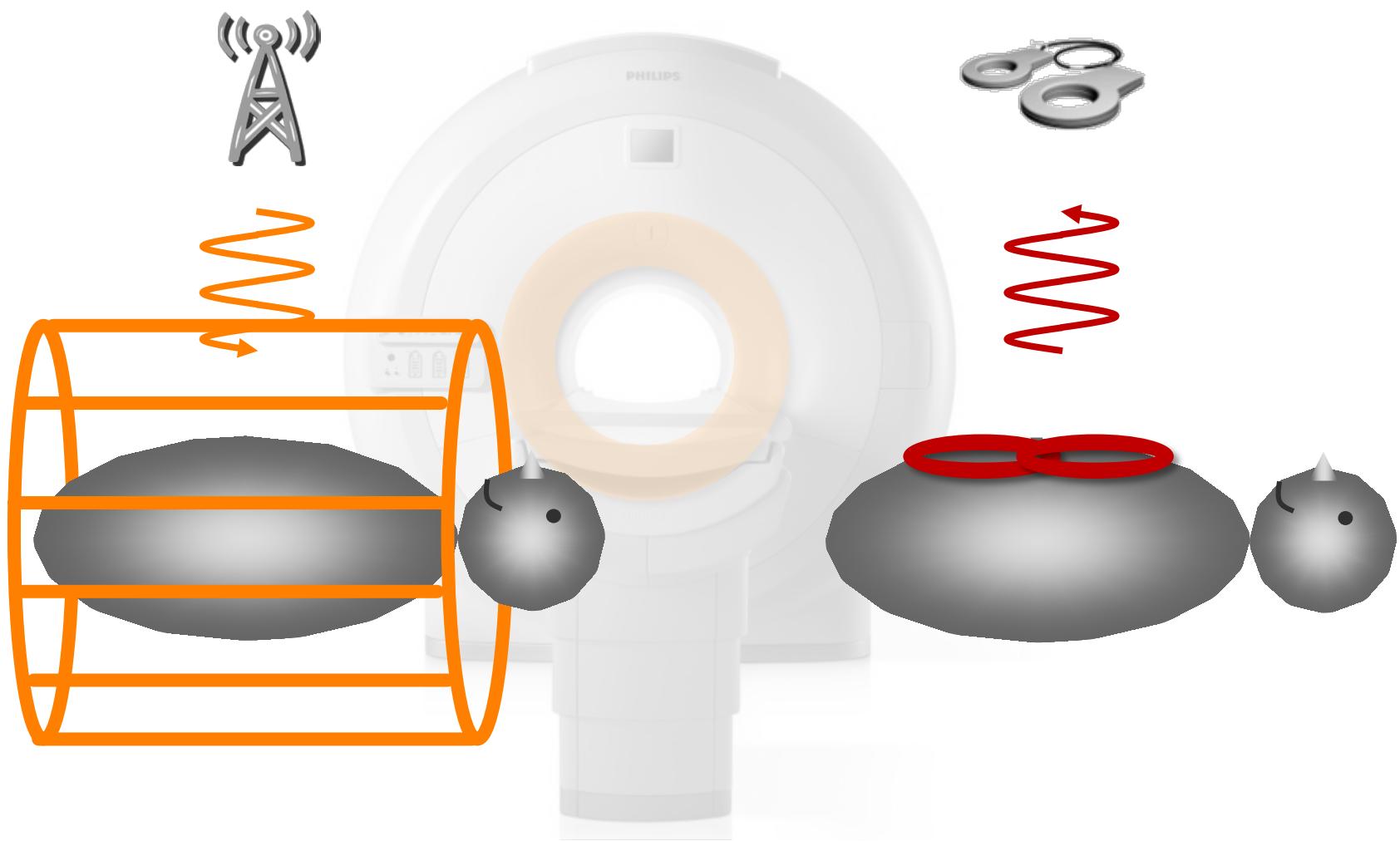
Safety limit IEC 2002

Peripheral nerve stimulation



40 cm off-centre, max grad strength: **40mT/m**, min slope dur: **200us, G_x, G_y, G_z active**

RF coils



Summary

- **Superconducting, shielded magnets (0.5-7.0 Tesla)**
- **Magnetic stray field poses potential hazards (projectiles)**
- **Magnetic material not permitted within stray field**
- **Nerve stimulation threshold** constrains gradient fields
- **Body coil to transmit, surface coils to receive**

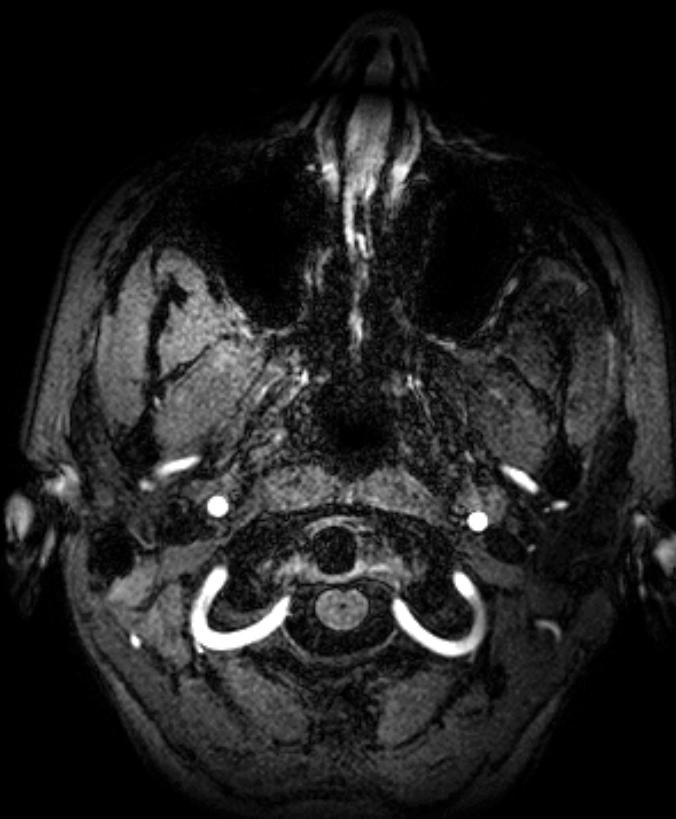
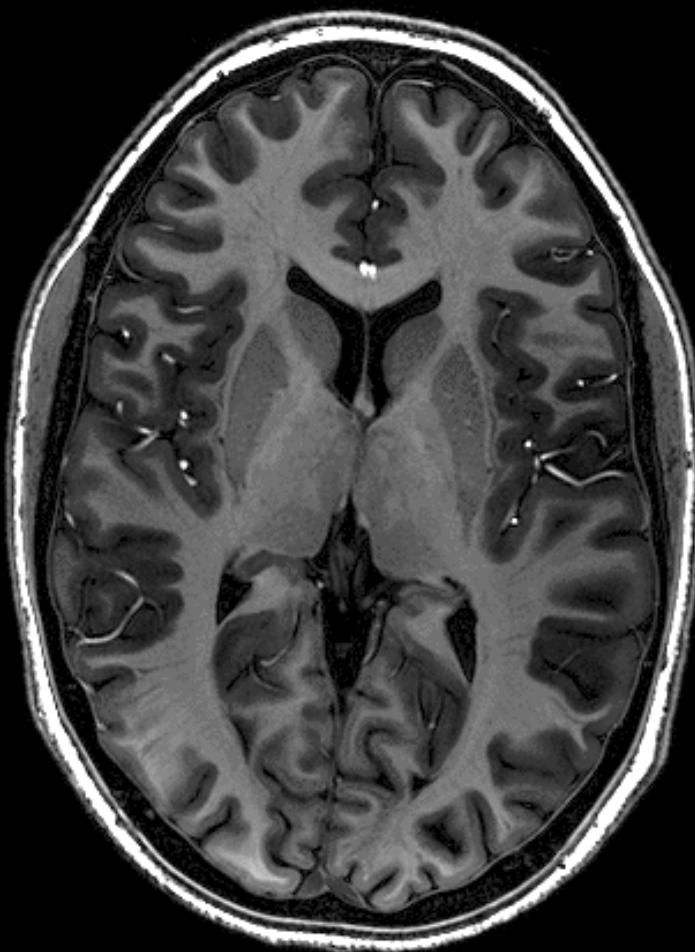
Anatomical Imaging

Overview



Human MRI at 7 Tesla

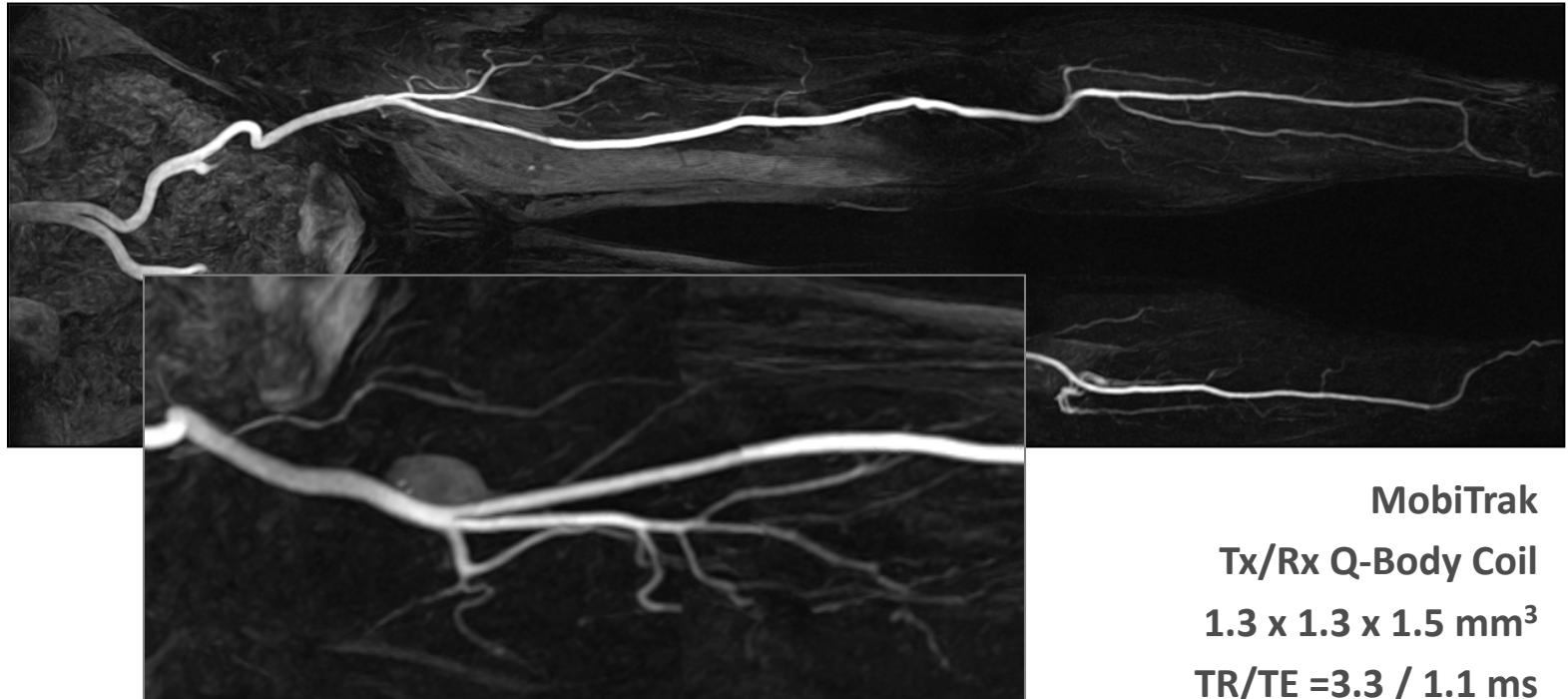
T_1 - weighted brain anatomy



Angiography



Extremities



MobiTrak

Tx/Rx Q-Body Coil

$1.3 \times 1.3 \times 1.5 \text{ mm}^3$

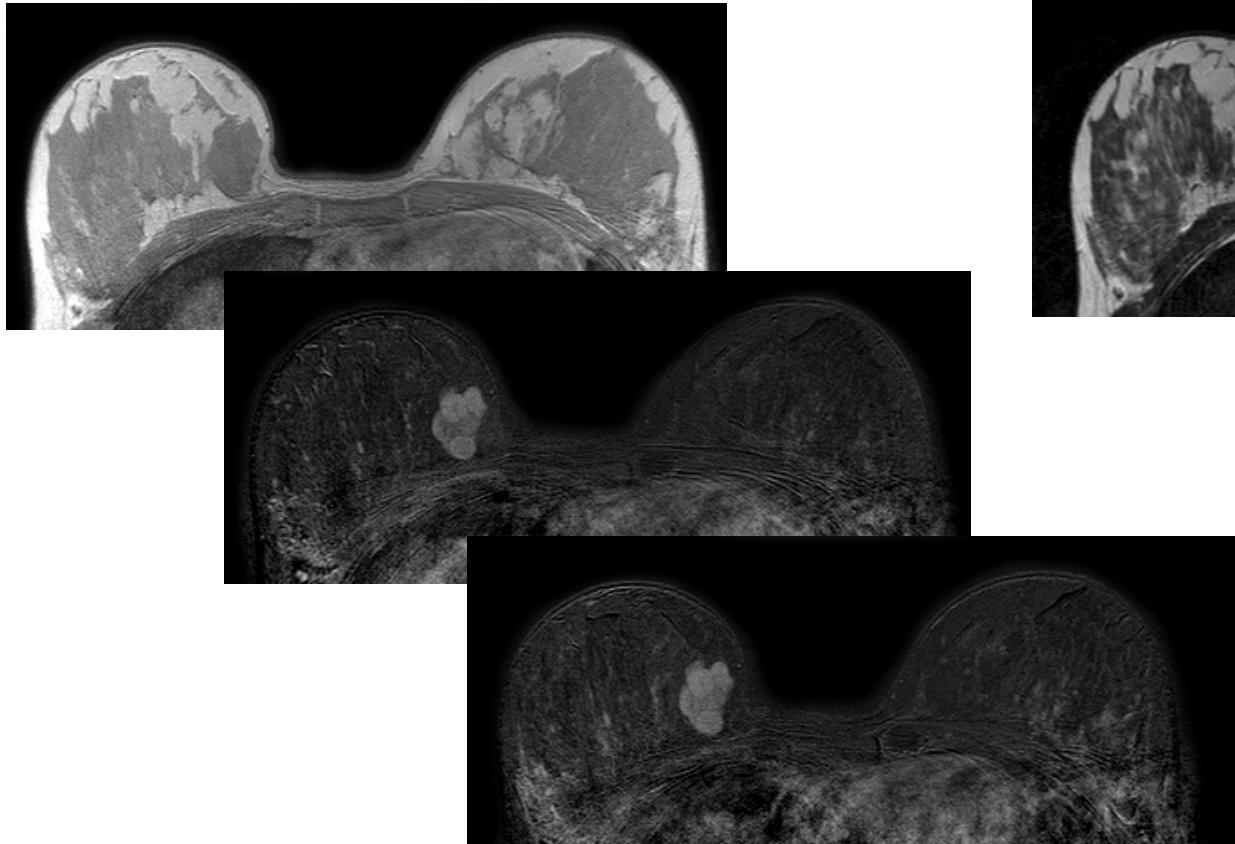
TR/TE = 3.3 / 1.1 ms

2:07 min

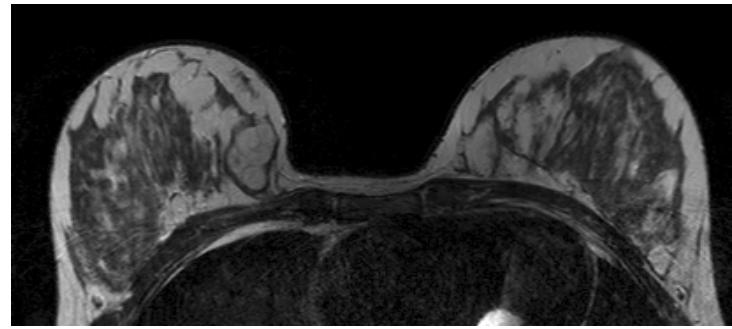
Courtesy: Dept. of Radiology, University of Bonn, Germany

Breast imaging

3D Gradient Echo, $0.7 \times 0.7 \times 2.5 \text{ mm}^3$

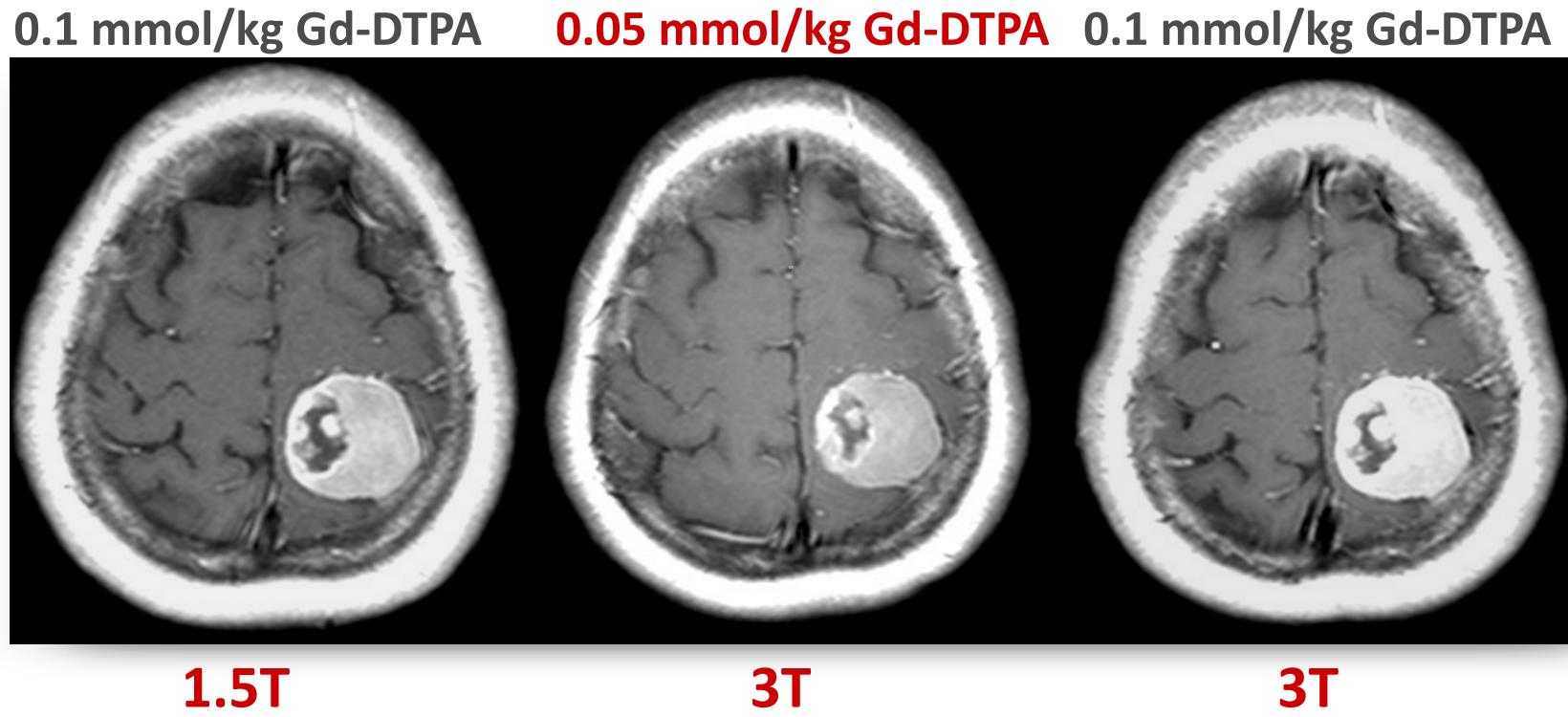


Spin Echo, $0.7 \times 0.7 \times 2.5 \text{ mm}^3$



Courtesy: Dr. C. Kuhl, Dept. of Radiology, University of Bonn, Germany

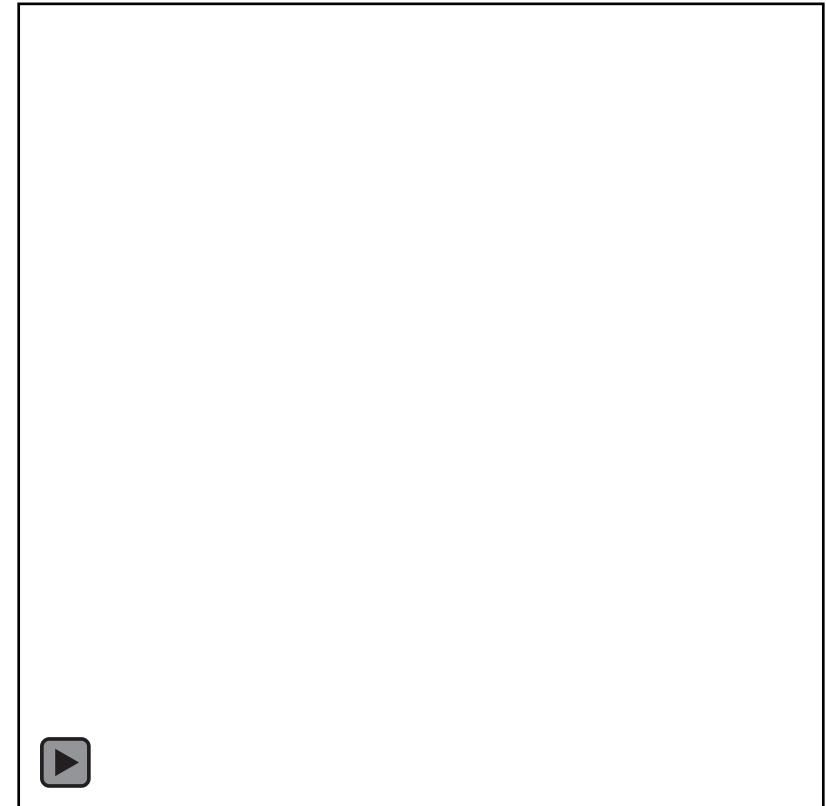
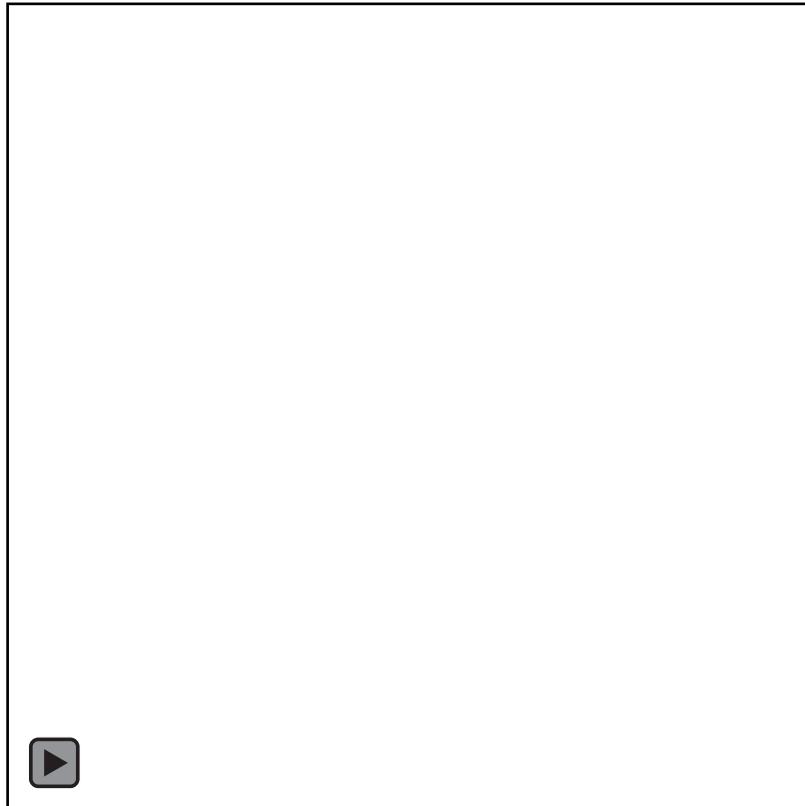
Contrast-enhanced imaging



Willinek WA et al.: Neuroimag Clin N Am 2006; 16: 217-228

Time-resolved cardiac imaging

Image each heart phase separately, ECG-triggered



Angiography

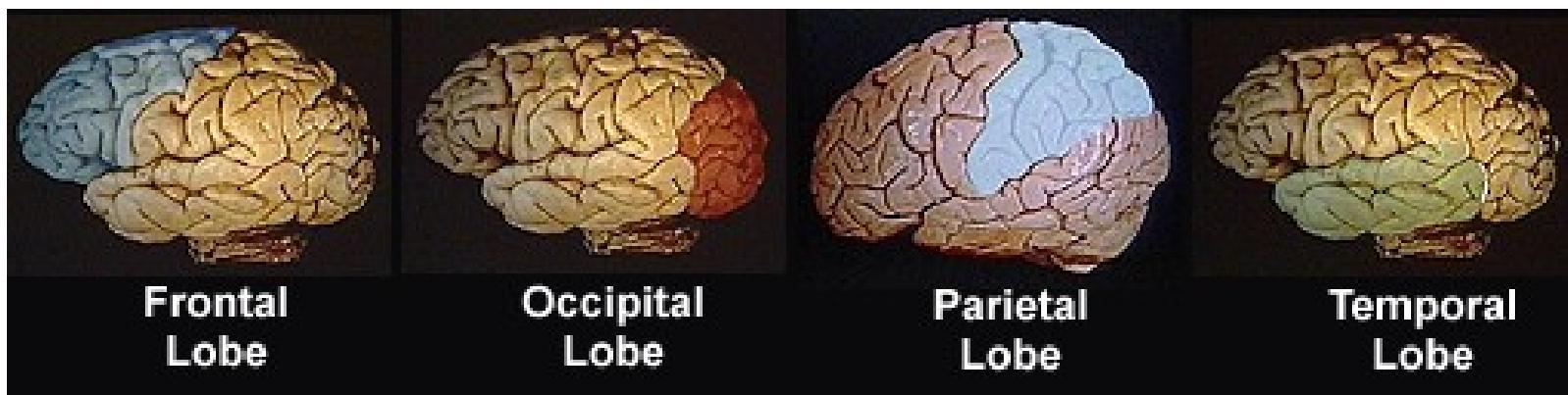


Functional Imaging

Functional Magnetic Resonance Imaging - fMRI

reasoning, planning,
parts of speech,
movement (motor cortex),
emotions,
problem-solving

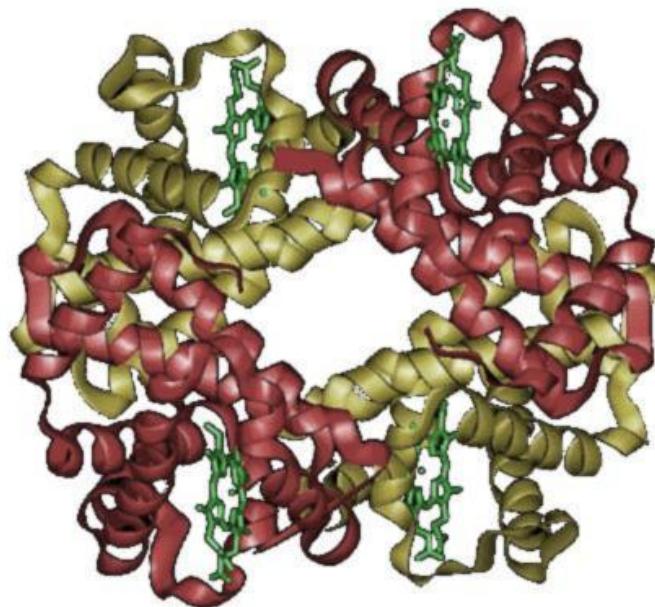
perception of stimuli
related to touch,
pressure, temperature,
pain



aspects of
vision

perception/recognition of
auditory stimuli (hearing),
memory (hippocampus)

Hemoglobin – “the molecule to breathe with”

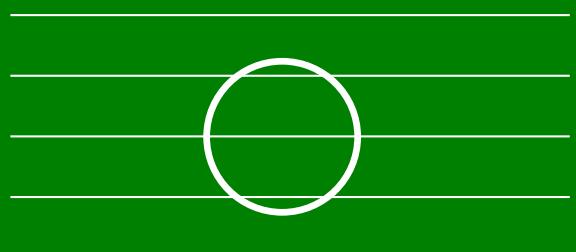


Hemoglobin (Hgb):

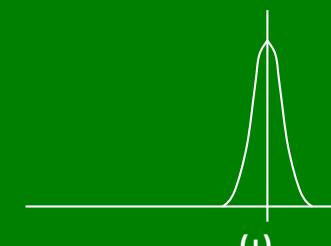
- four globin chains
- each globin chain contains a heme group
- at center of each heme group is an iron atom (Fe^{2+})
- each heme group can attach an oxygen atom (O_2)
- oxy-Hb is diamagnetic
- deoxy-Hb is paramagnetic

fMRI – principles

oxy-hemoglobin: diamagnetic

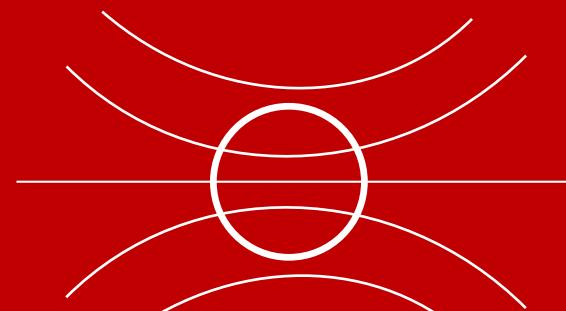


magnetic flux

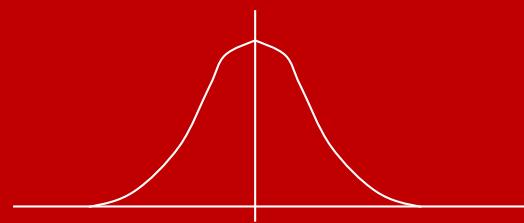


sharp resonance-frequency
long T_2^*

deoxy-hemoglobin: paramagnetic

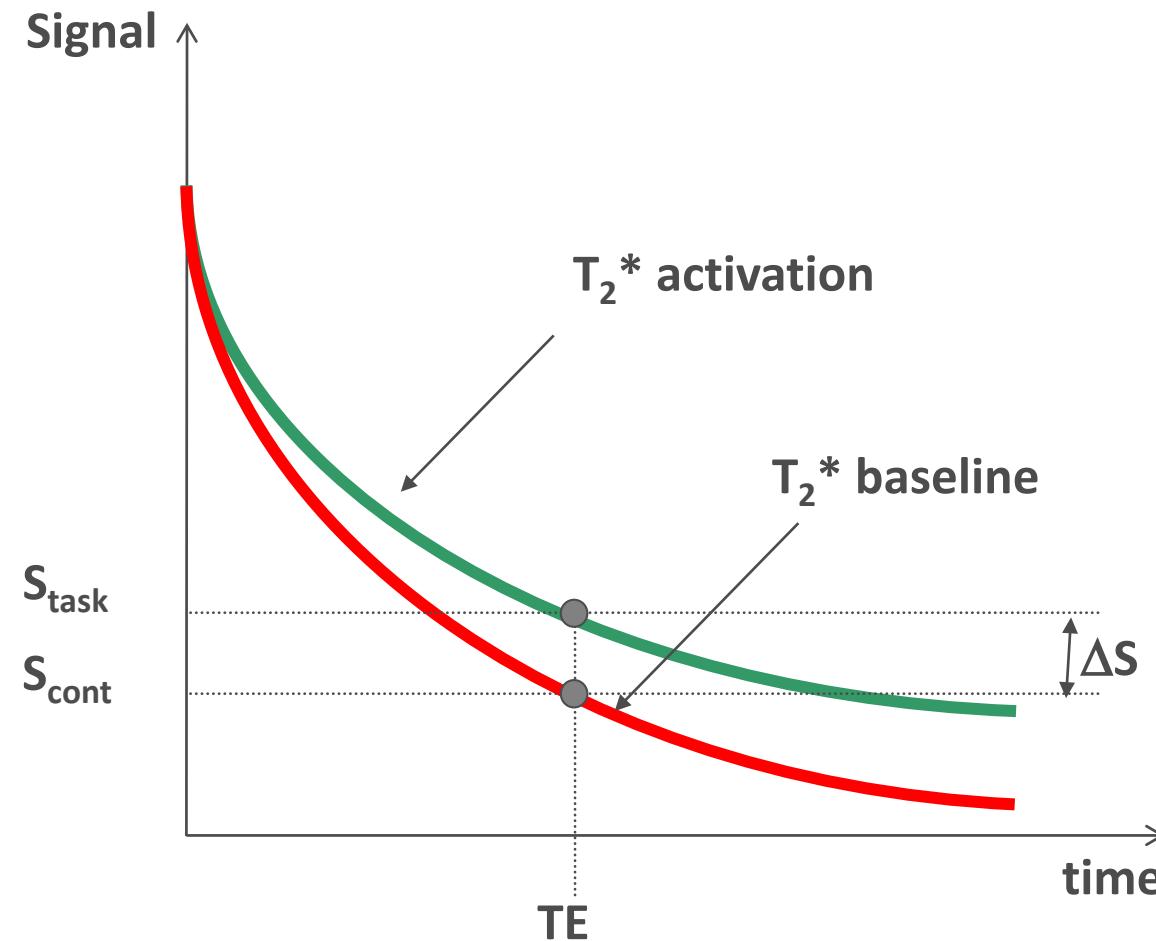


magnetic field locally disturbed



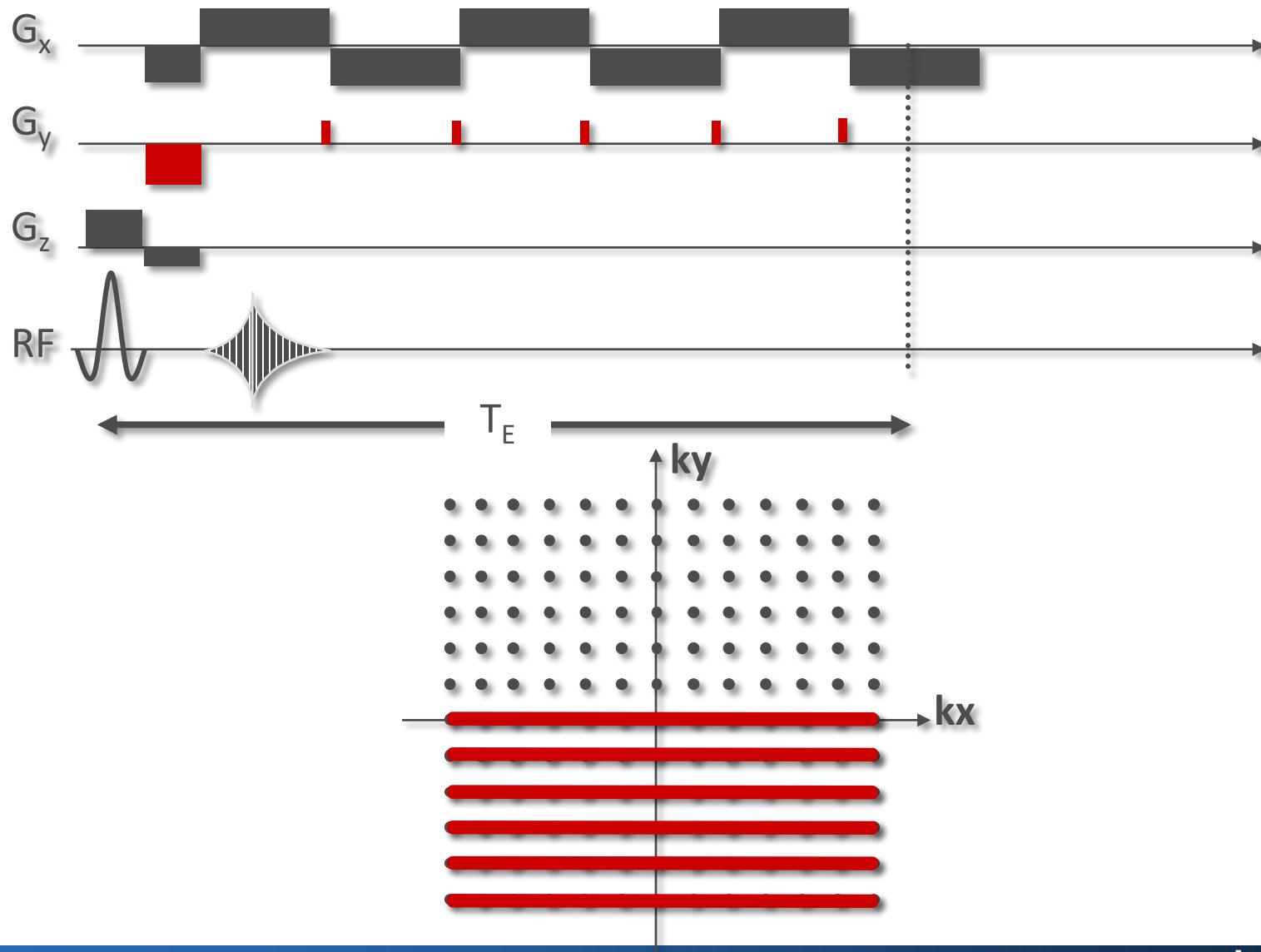
distribution of resonance frequencies
short T_2^*

fMRI – contrast

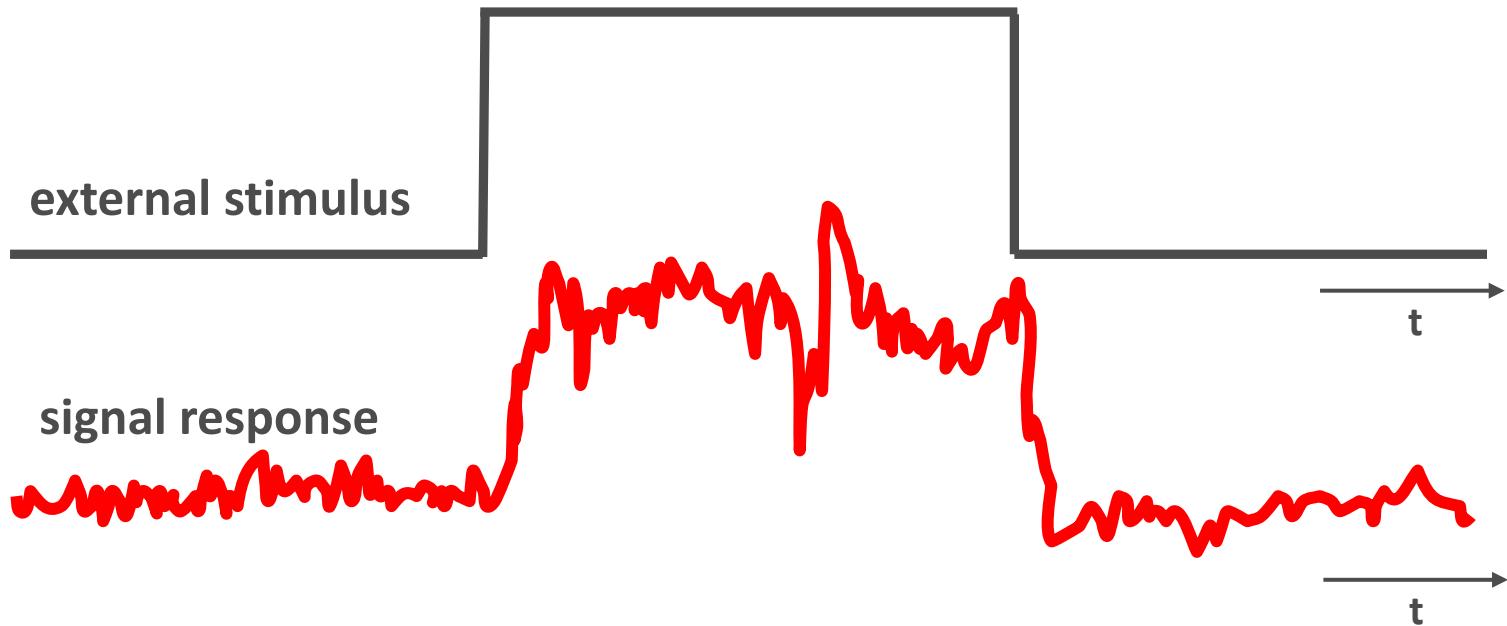


Signal change very small: 0.3-5%

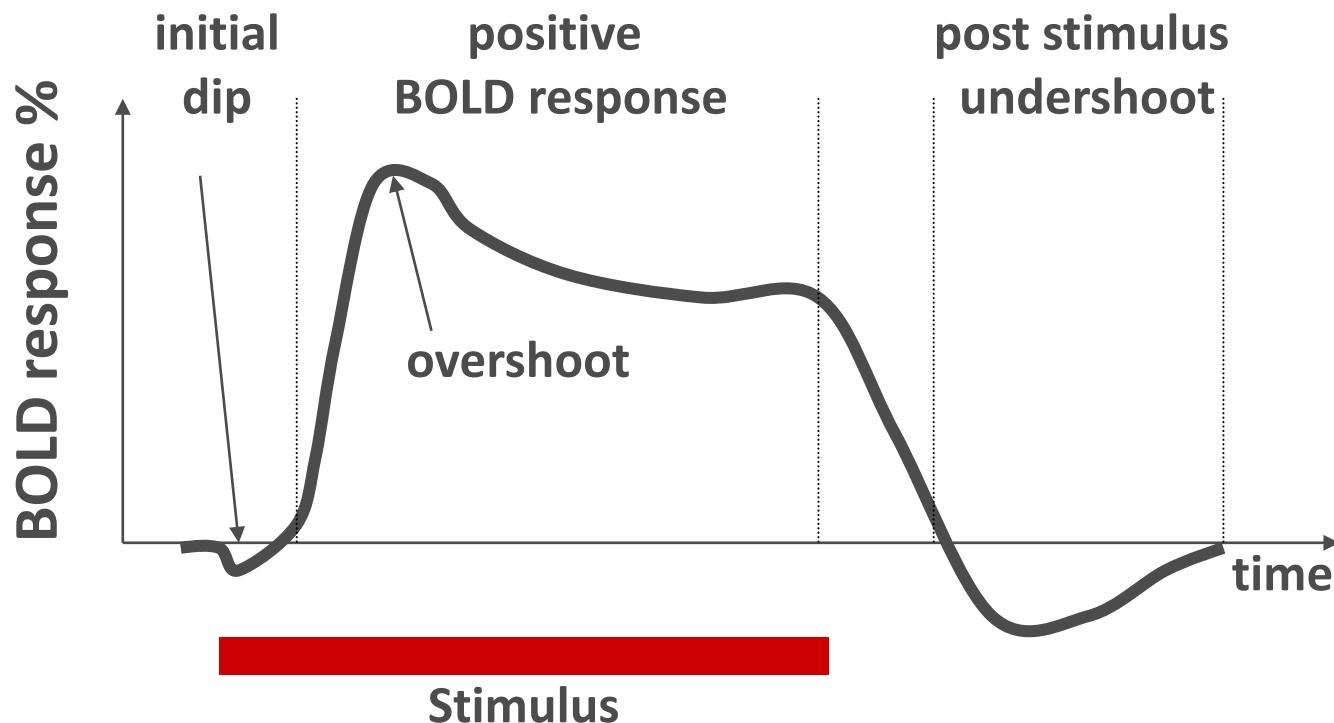
fMRI – echo planar imaging (EPI)



fMRI – stimulation

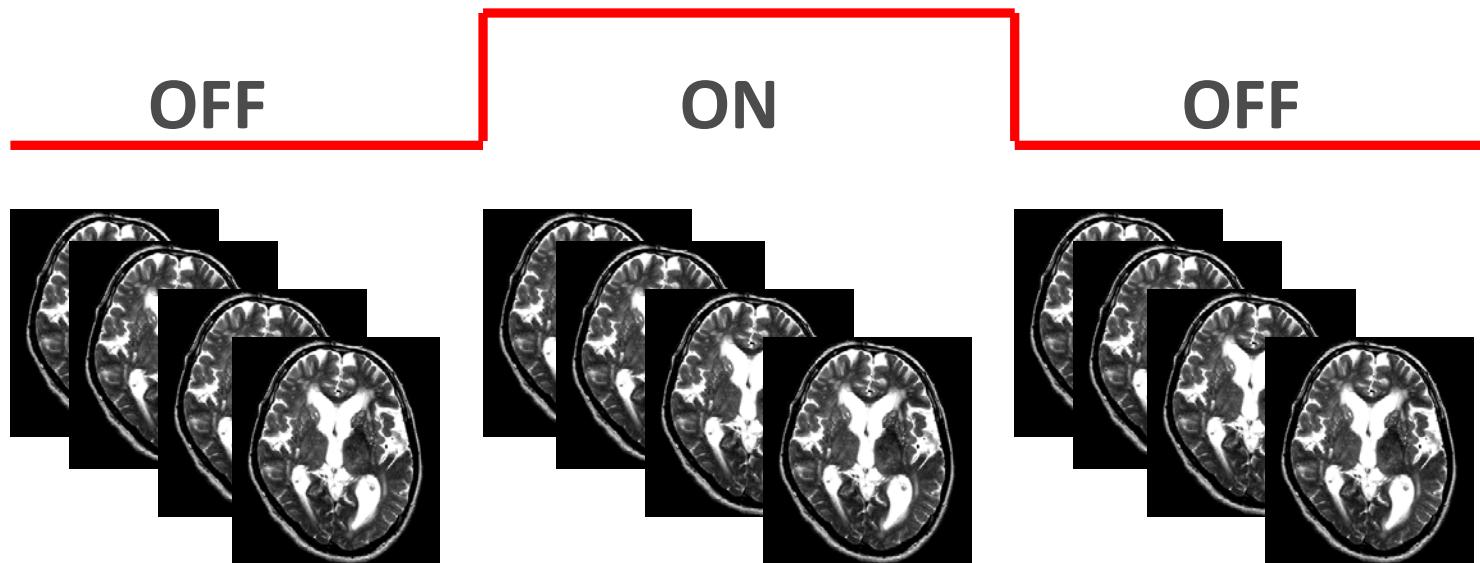


fMRI – temporal BOLD response

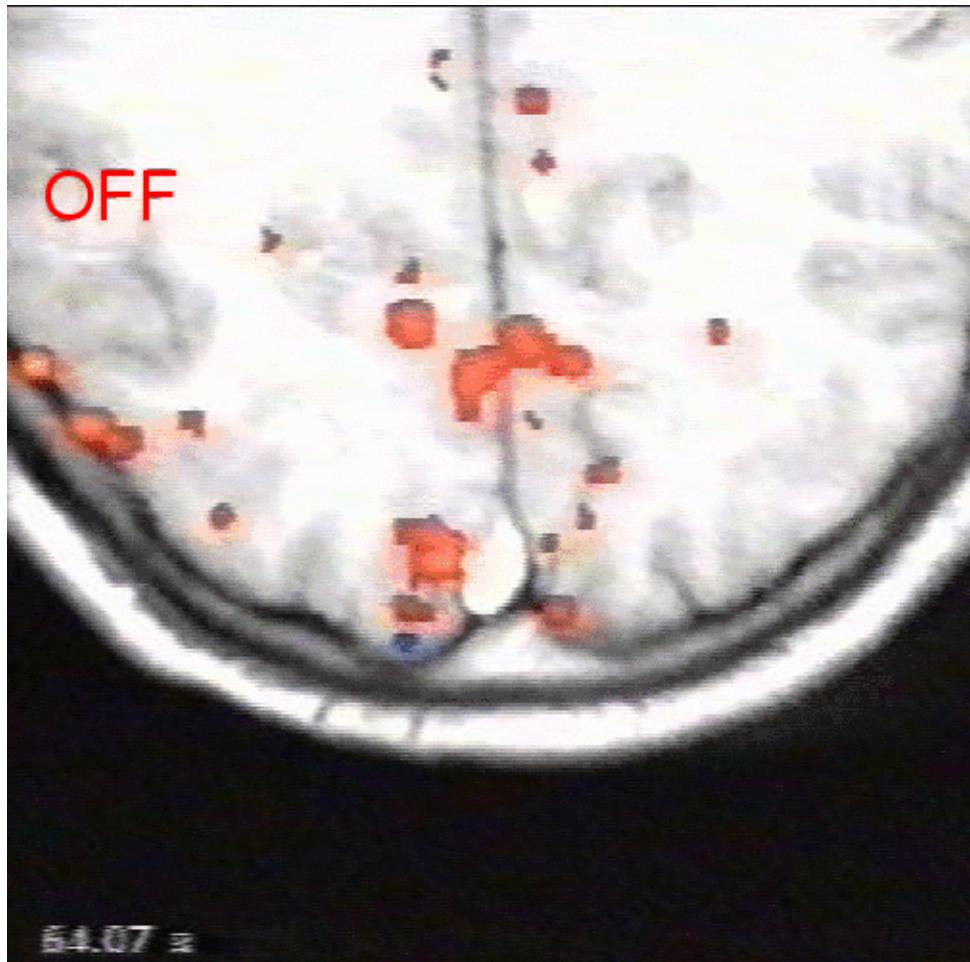


fMRI – post-processing

Measurement of slice images before, during and after stimulation

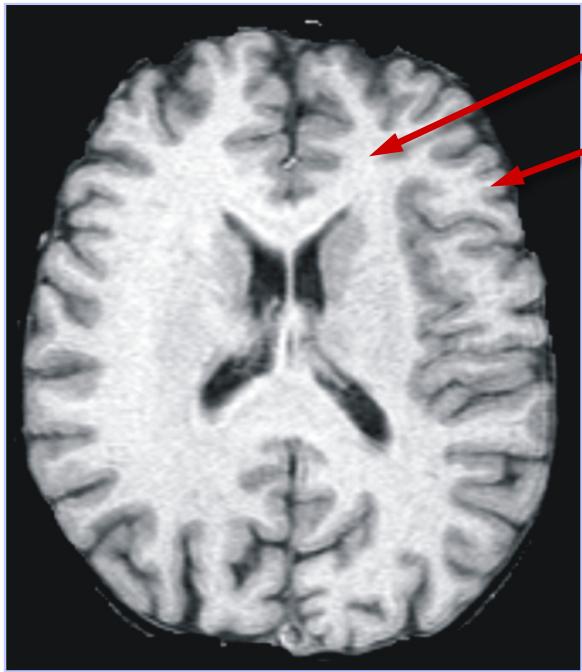


fMRI – visual stimulation



- **Blood oxygenation level dependent (BOLD) contrast**
- **BOLD signal** is relative and very weak
- **Image intensity changes** are due to several effects
- **Series of activation/deactivation** for statistical power

Anatomical connectivity

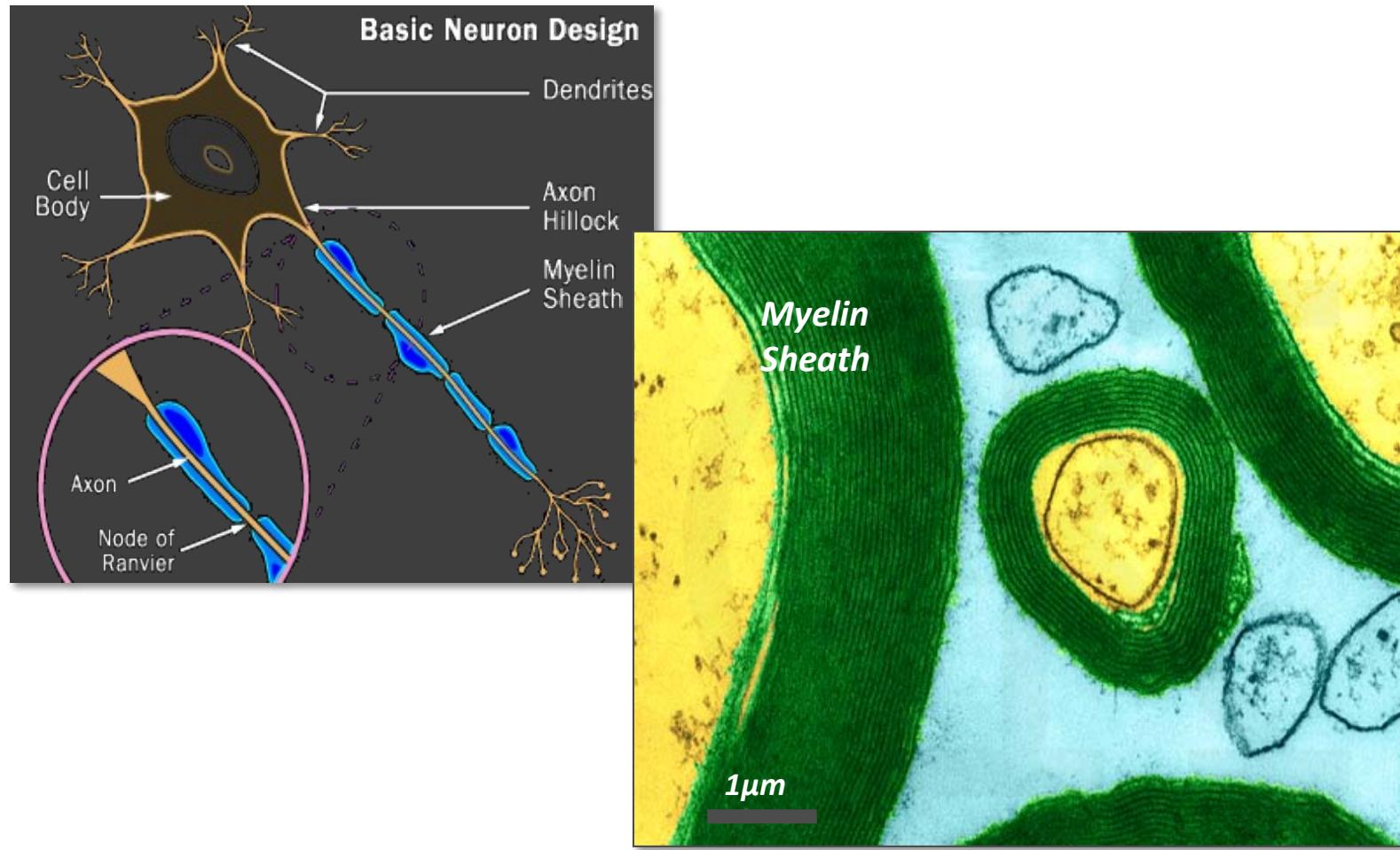


White brain matter

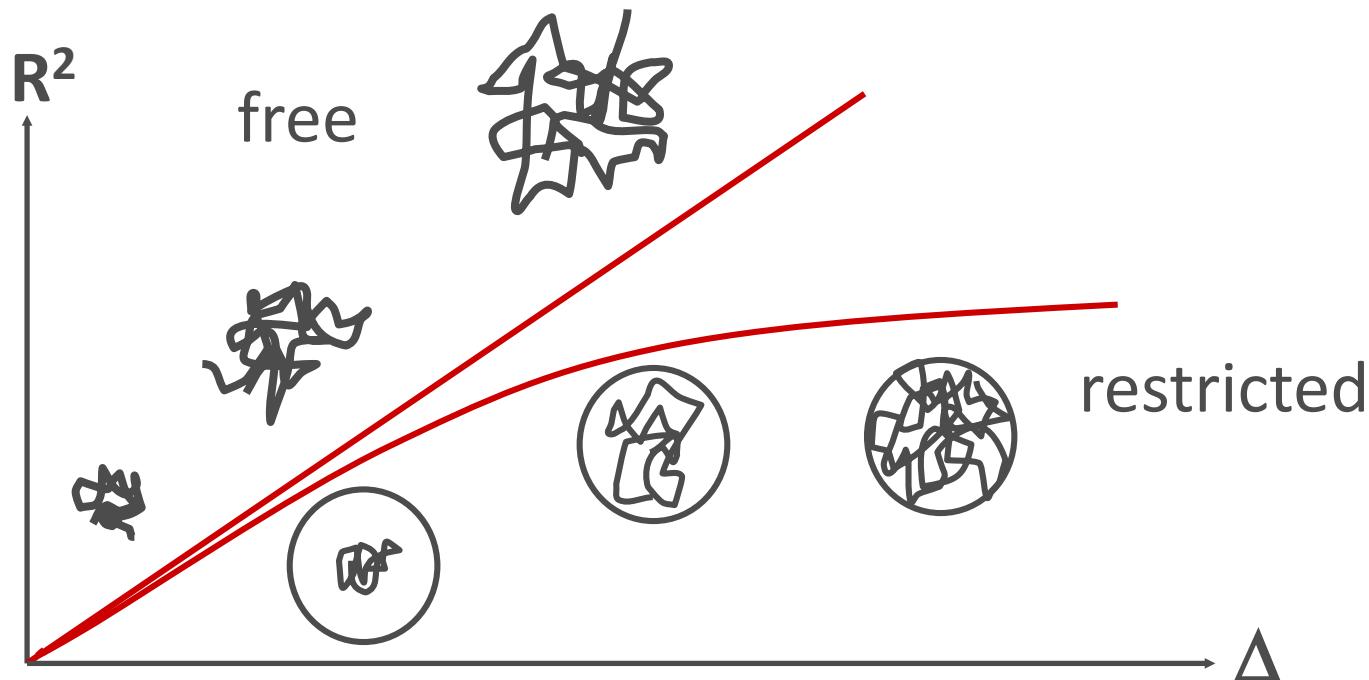
Gray brain matter



Axon



Self-Diffusion vs. Restricted Diffusion



$$R = \sqrt{2 \cdot D \cdot \Delta}$$

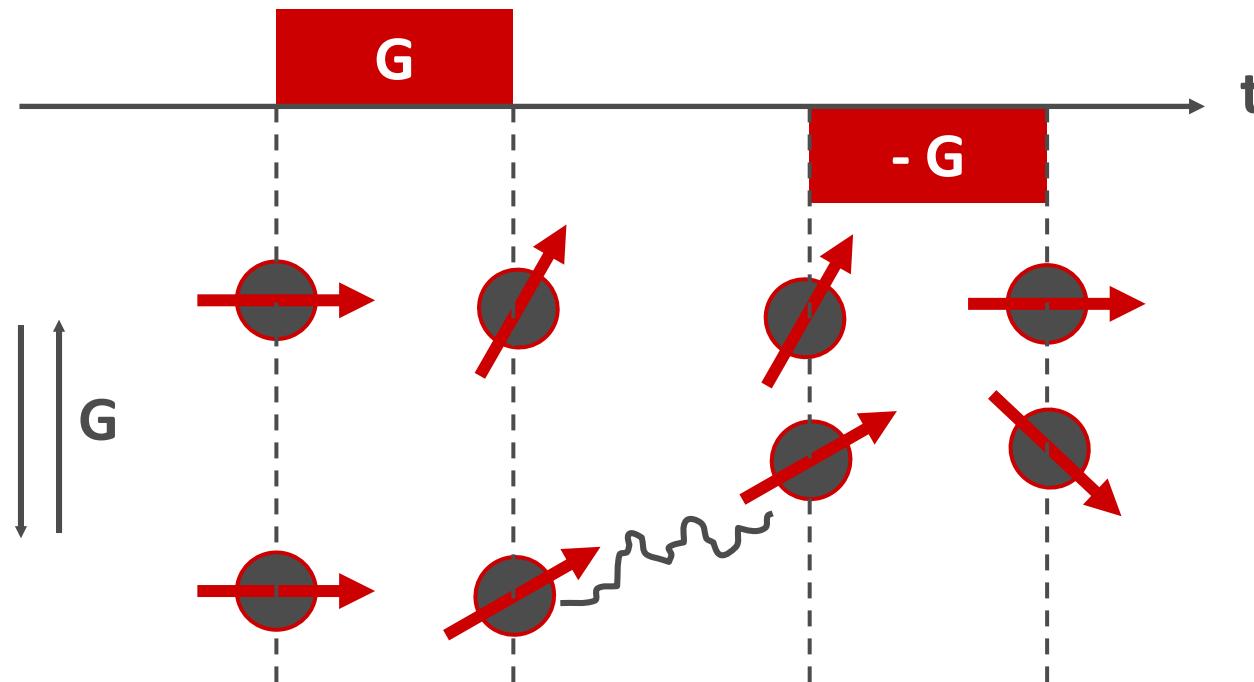
Diffusion coefficients

$$D = \frac{\langle \lambda \rangle \cdot \langle v \rangle}{6}$$

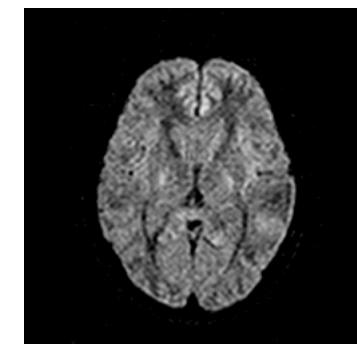
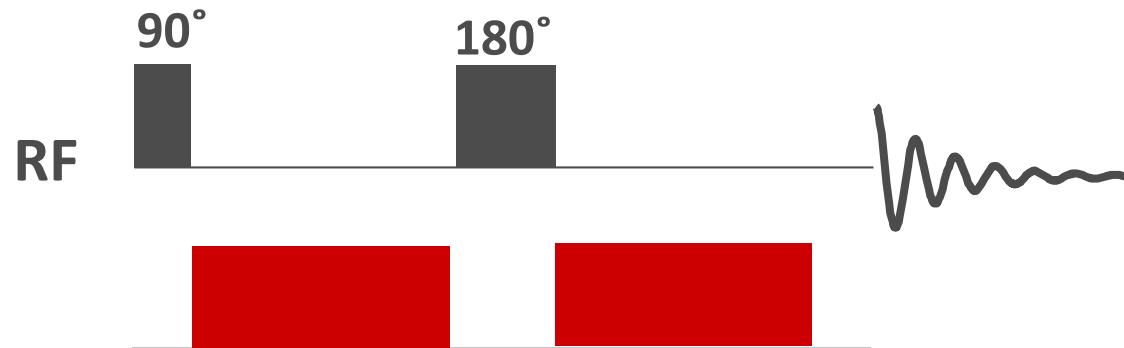
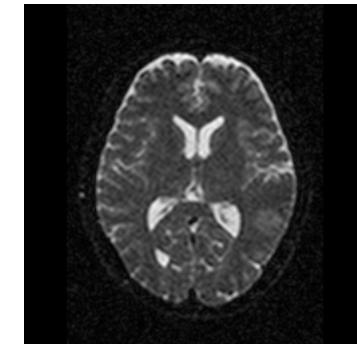
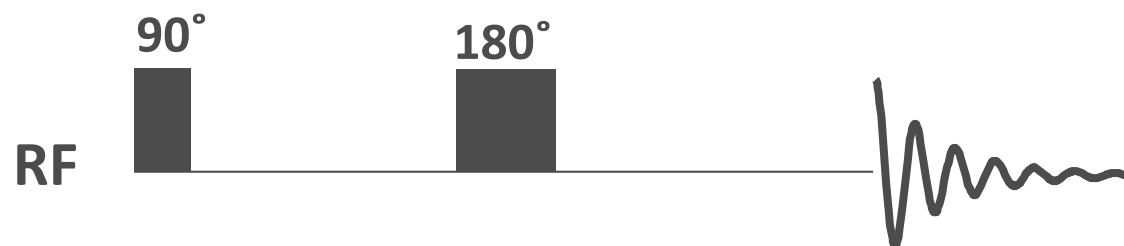
λ free path length
 v molecular velocity
D diffusion coefficient

Tissue	D [10 ⁻³ · mm ² /s]
Water T=22°C	2.0 – 2.5
Myocardium	0.2 – 0.7
White Matter	0.1 – 0.6
Gray Matter	0.8

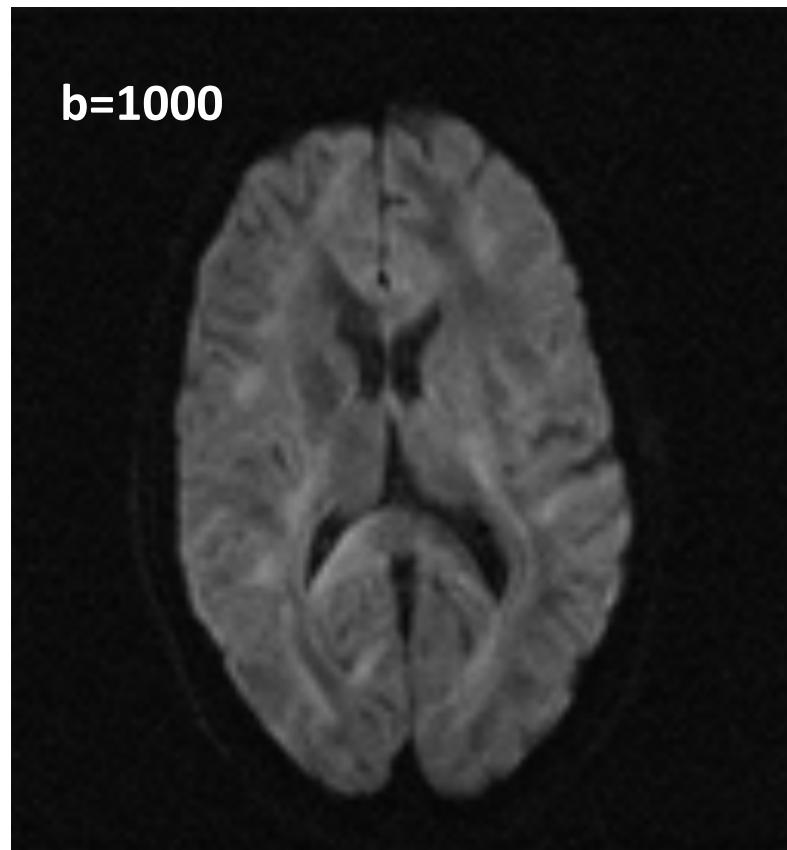
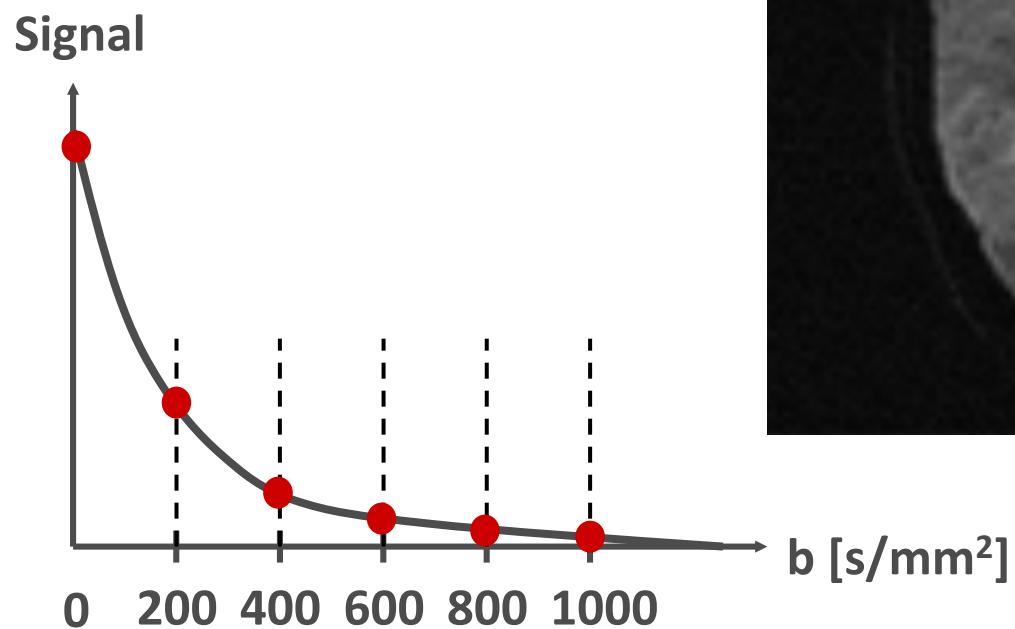
Diffusion weighting



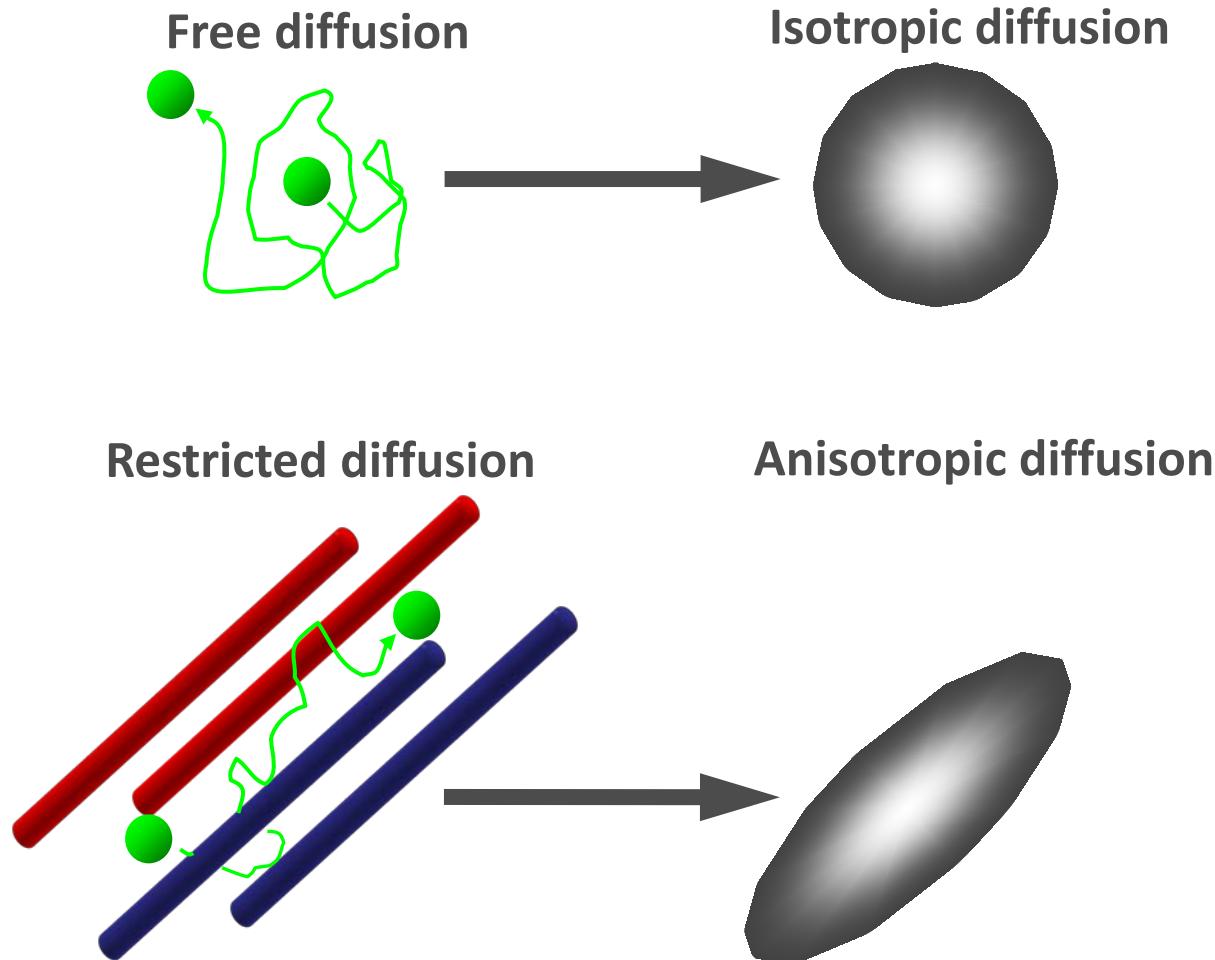
Diffusion weighted imaging (DWI)



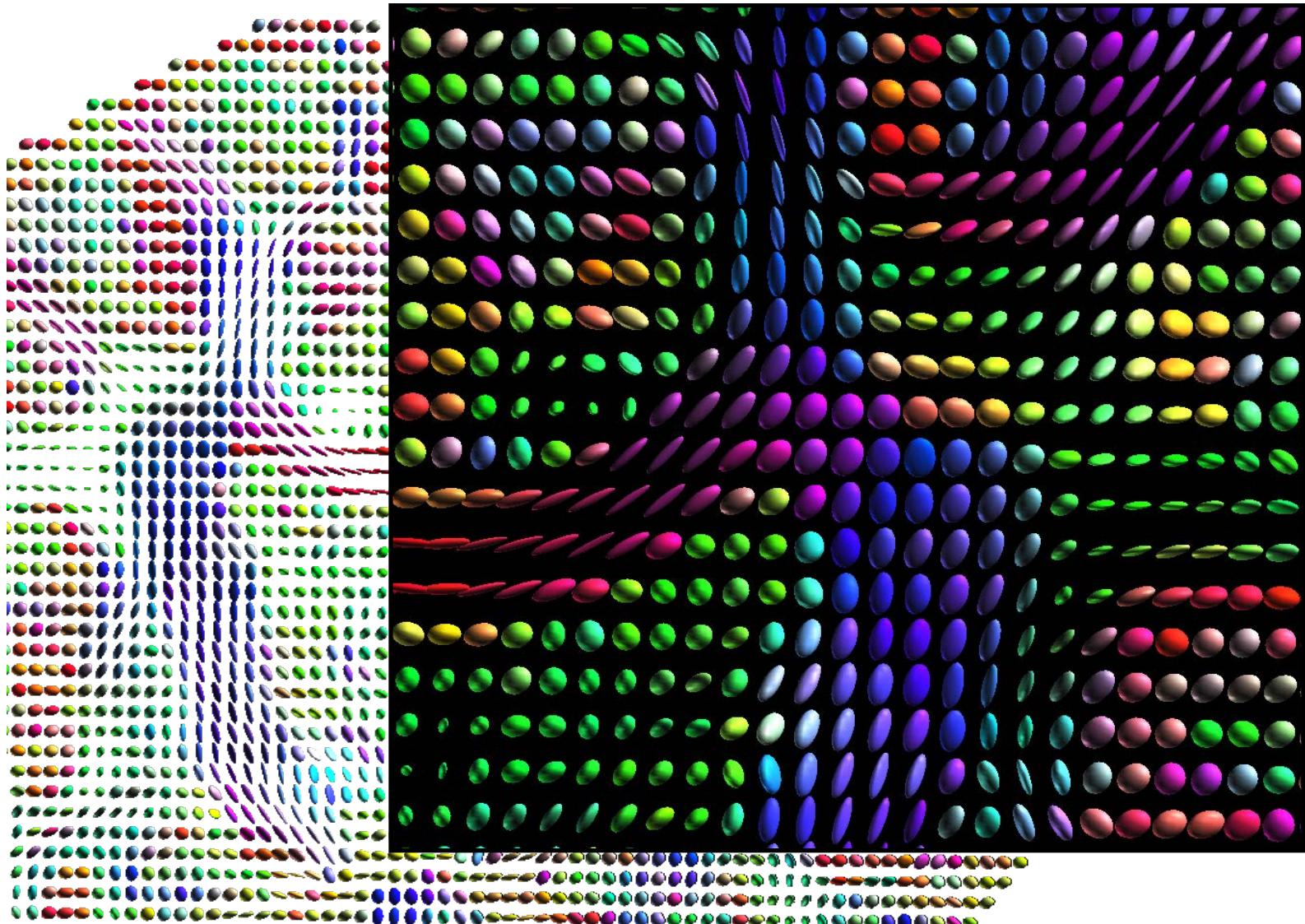
Diffusion weighted imaging



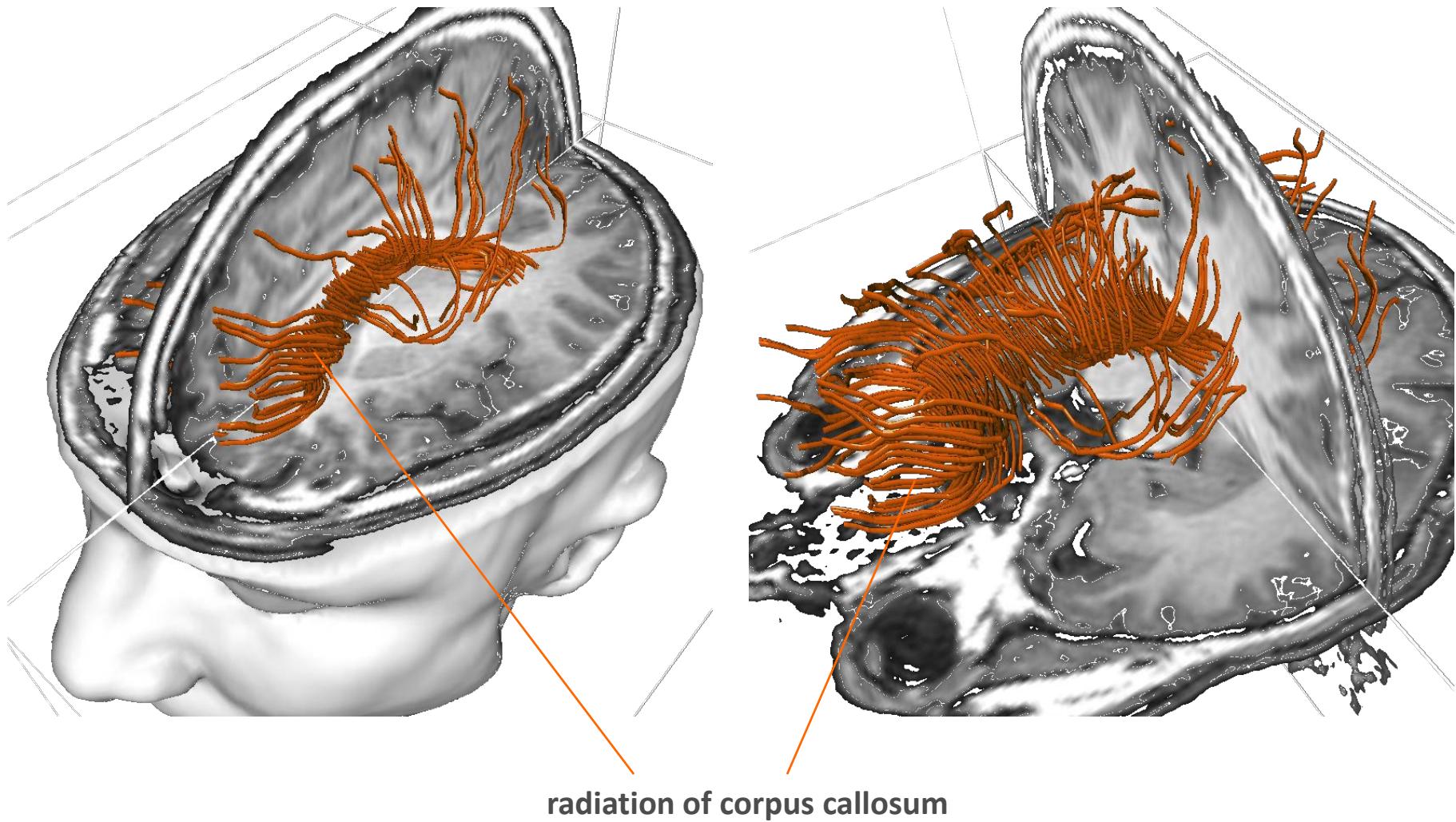
Diffusion Tensor Imaging (DTI)



Diffusion Tensor Imaging



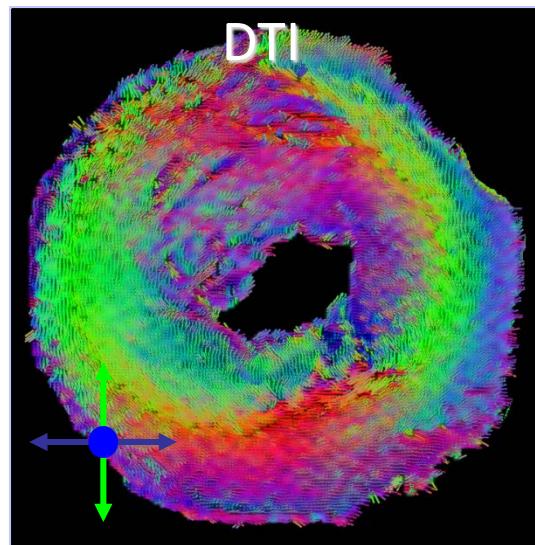
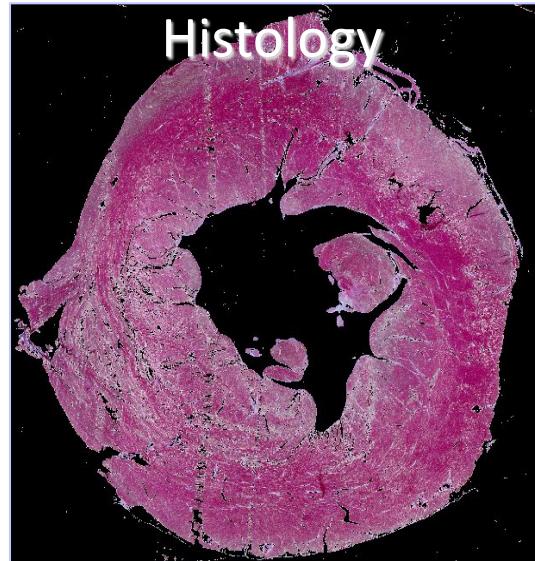
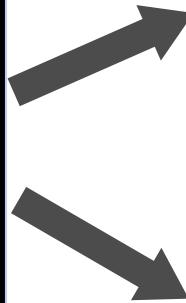
Fiber Tracking



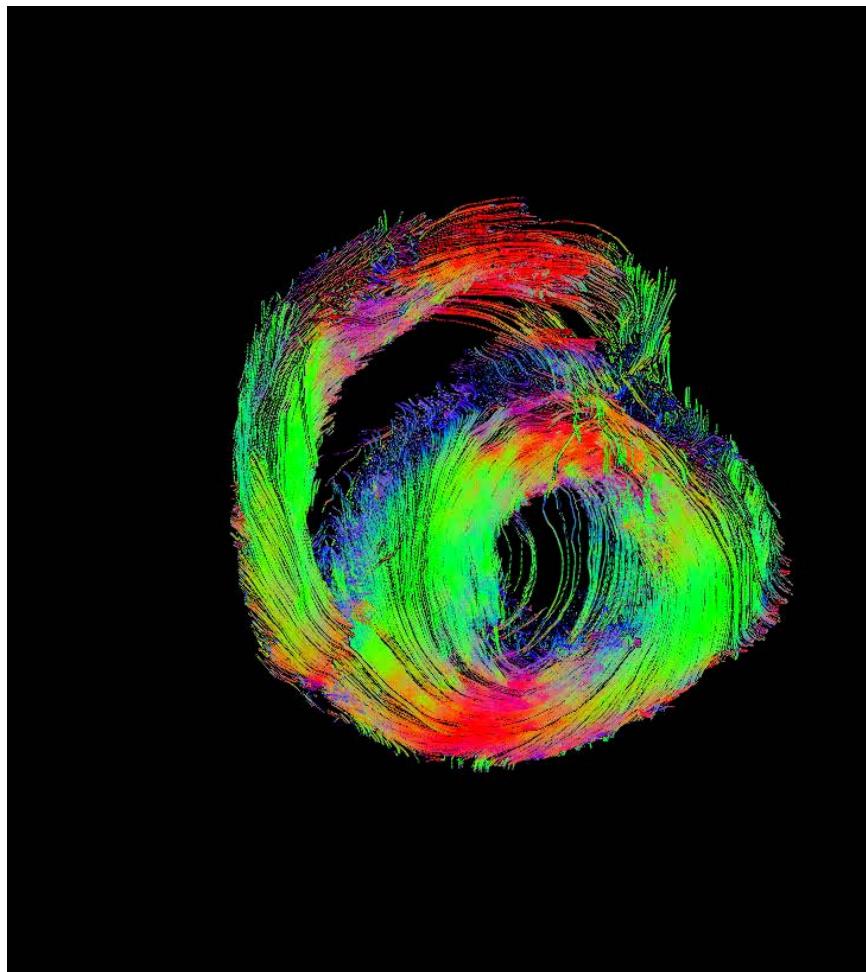
Pig heart (ex-vivo)



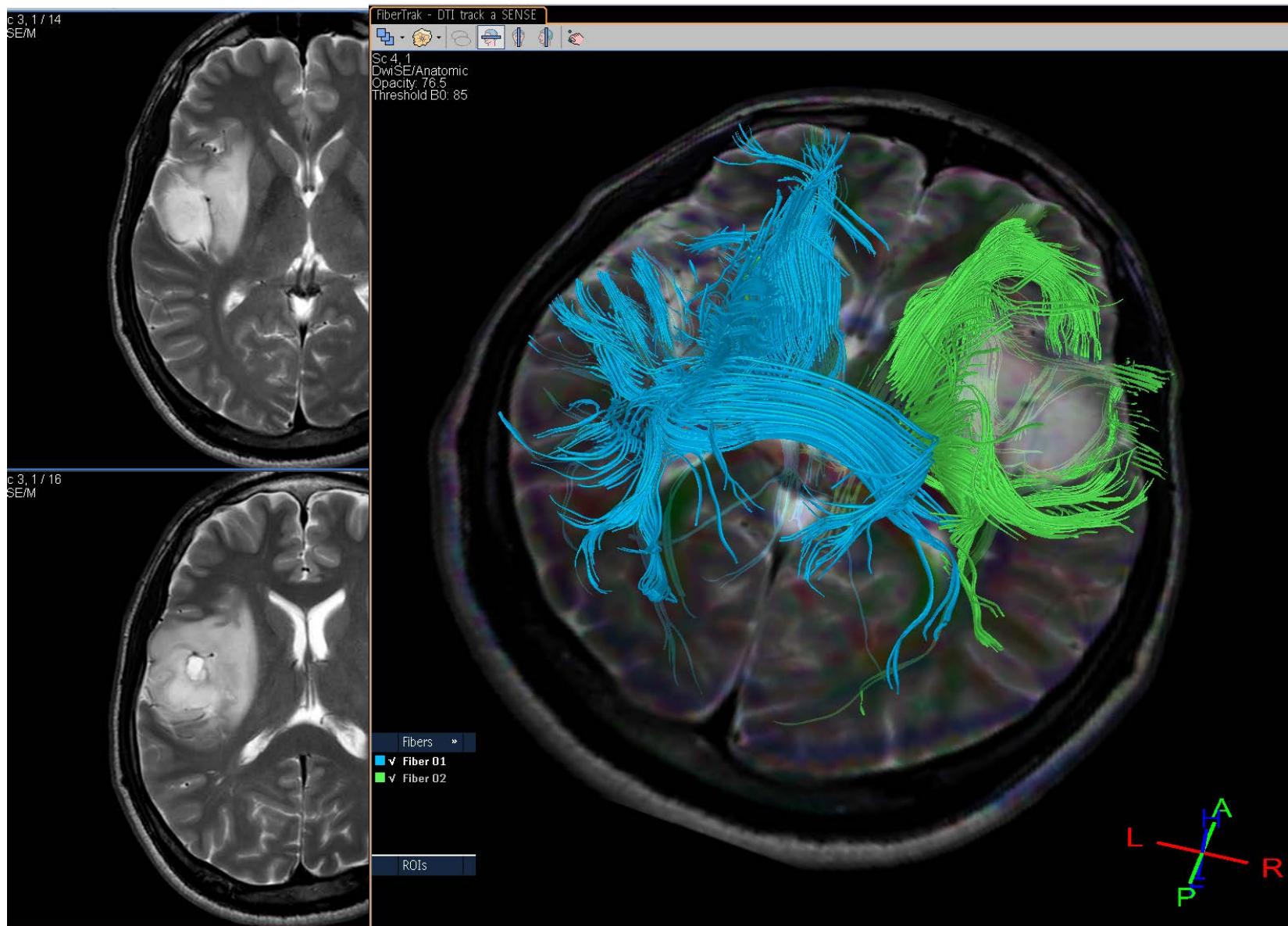
short axis heart slice



Diffusion Tensor Imaging (ex-vivo)



Tumor

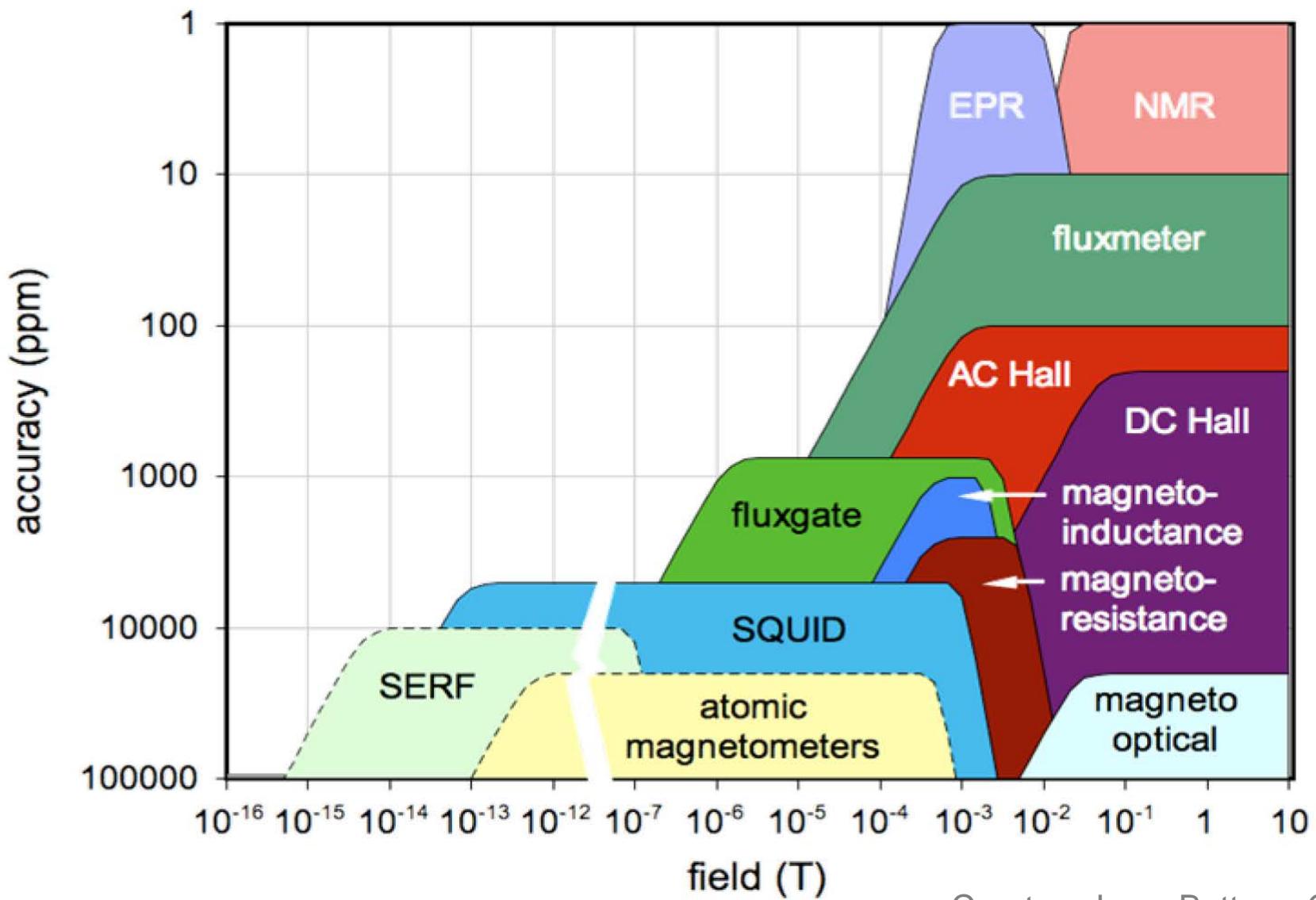


Summary

- **Water self-diffusion** constrained in different tissue types
- **Diffusion weighted imaging** to create diffusion contrast
- **Diffusion tensor imaging** to infer diffusion directions
- **Fiber tracking** to visualize paths of fiber bundles
- **Measurement very sensitive** to bulk motion of subject

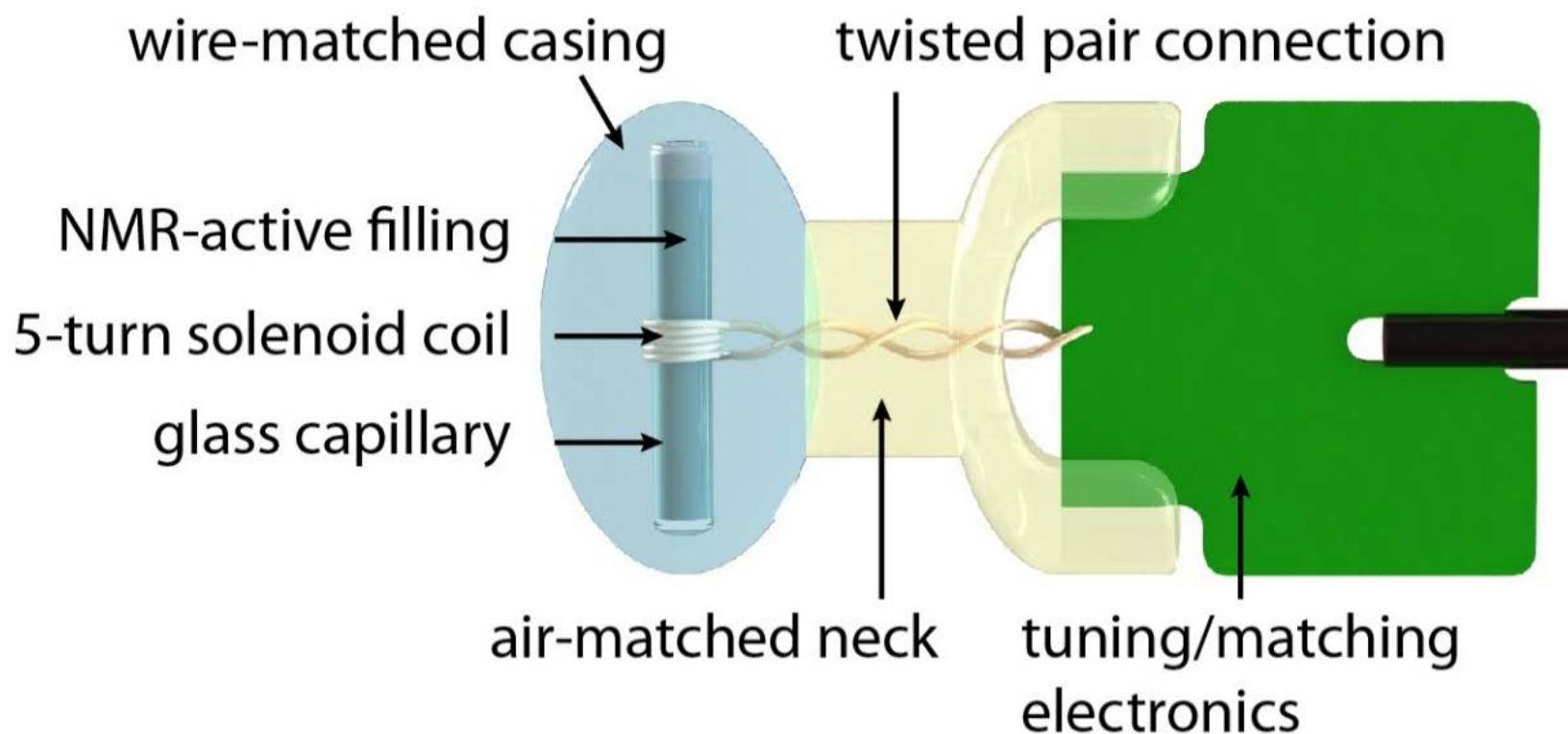
A peek into ongoing development...

Field Sensing for MRI

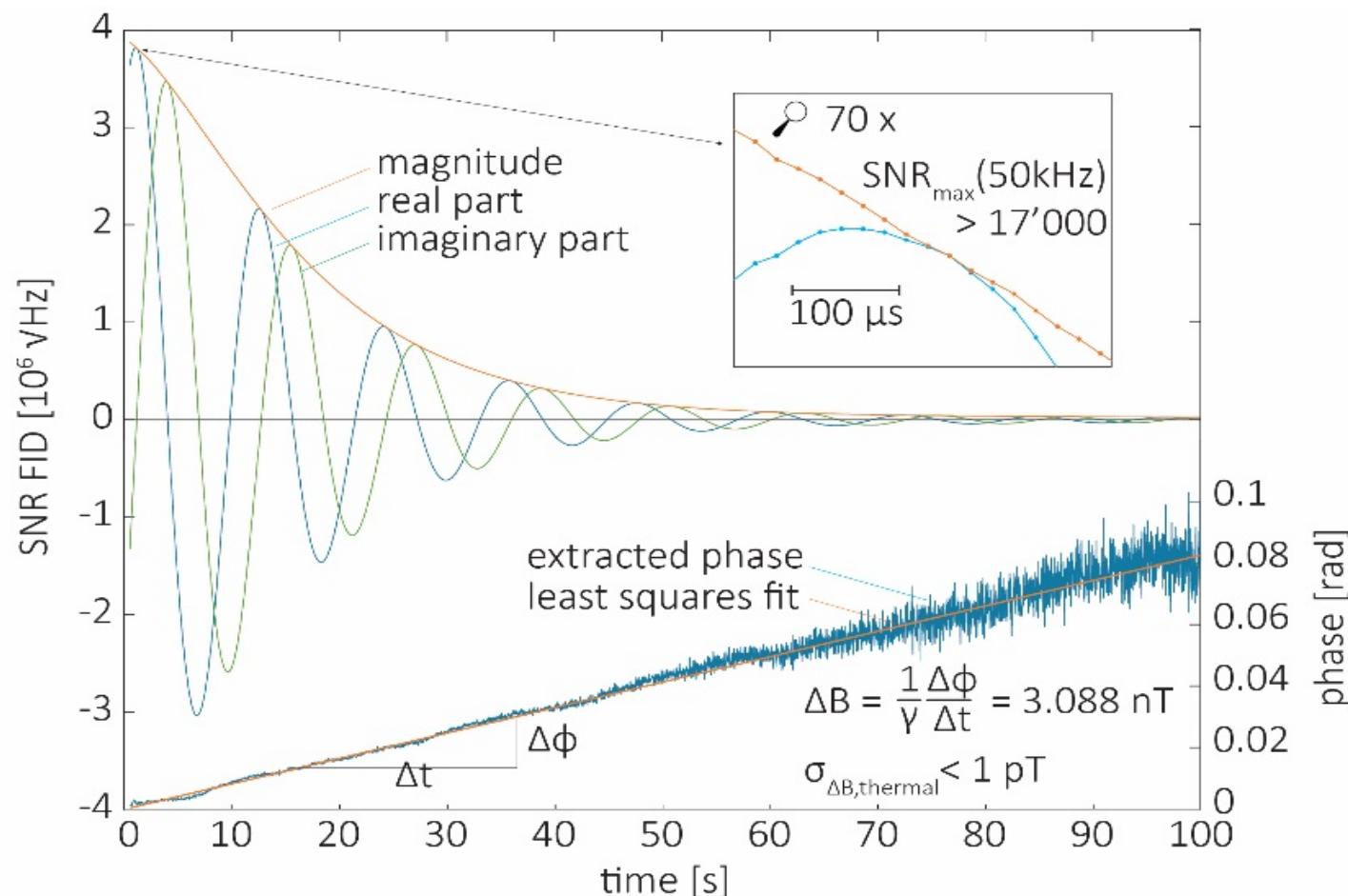


Courtesy Luca Bottura, CERN

NMR field probes

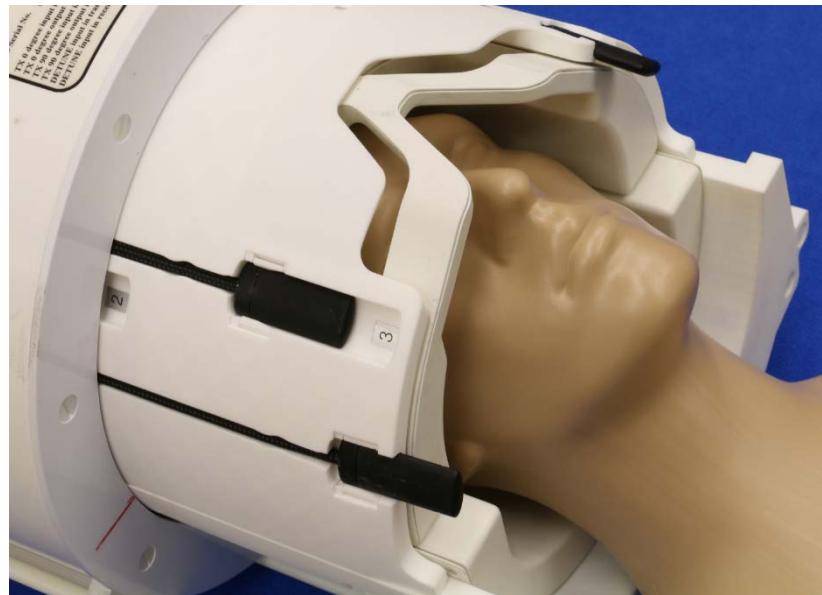


Sensing Performance



Phase noise: $0.23 \mu\text{rad} / \text{Hz}^{1/2}$ $\rightarrow \Delta B \approx 6 \text{ pT}$

Concurrent Field Sensing



3rd-order spherical harmonics

order	basis function $f(\mathbf{r})$
0	1
	X
1	Y
	Z
	XY
	ZY
2	$3Z^2 - (X^2 + Y^2 + Z^2)$
	XZ
	$X^2 - Y^2$
	$3X^2Y - Y^3$
	XYZ
3	$Y(5Z^2 - (X^2 + Y^2 + Z^2))$
	$5Z^3 - 3Z(X^2 + Y^2 + Z^2)$
	$X(5Z^2 - (X^2 + Y^2 + Z^2))$
	$X^2Z - Y^2Z$
	$X^3 - 3XY^2$

Fit spatiotemporal phase model:

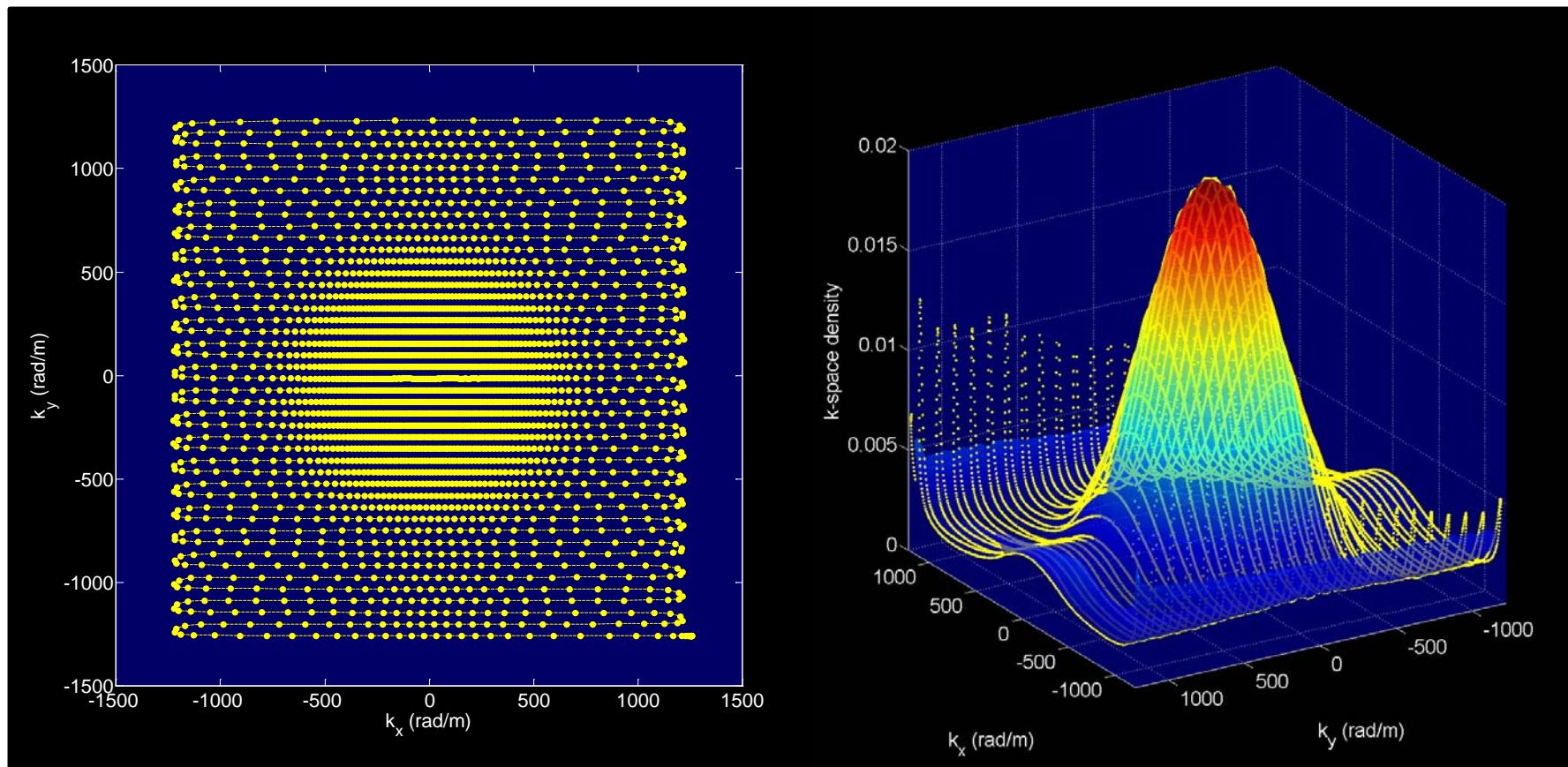
$$\varphi(\mathbf{r}, t) = \sum_i k_i(t) \cdot f(\mathbf{r})$$

Field expansion: $\frac{d}{dt} k_i(t)$

Matched-Filter Acquisition for BOLD fMRI

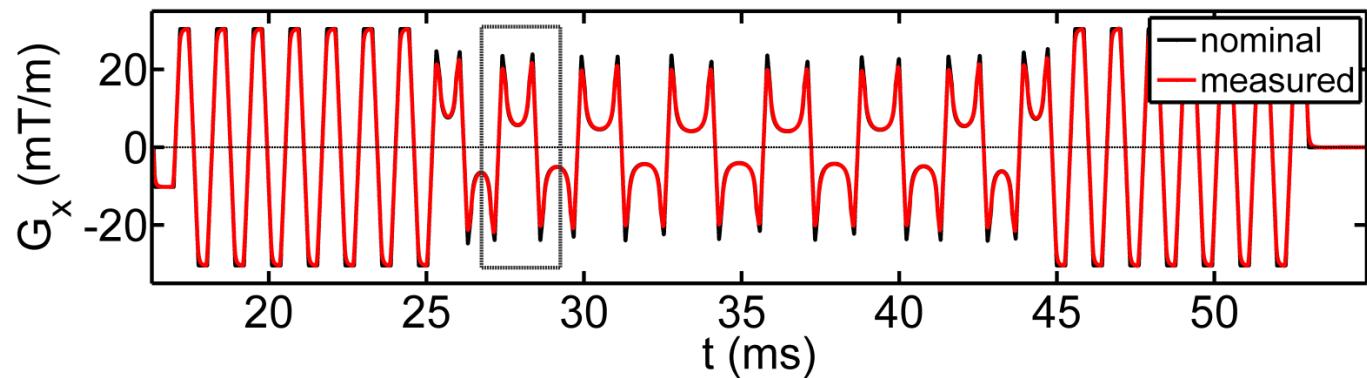
BOLD analysis often based on Gaussian statistics → k-space filtering / smoothing

For optimal SNR yield: **Distribution of AQ time should match the k-space filter**



Magnetic Field Sensing & Control

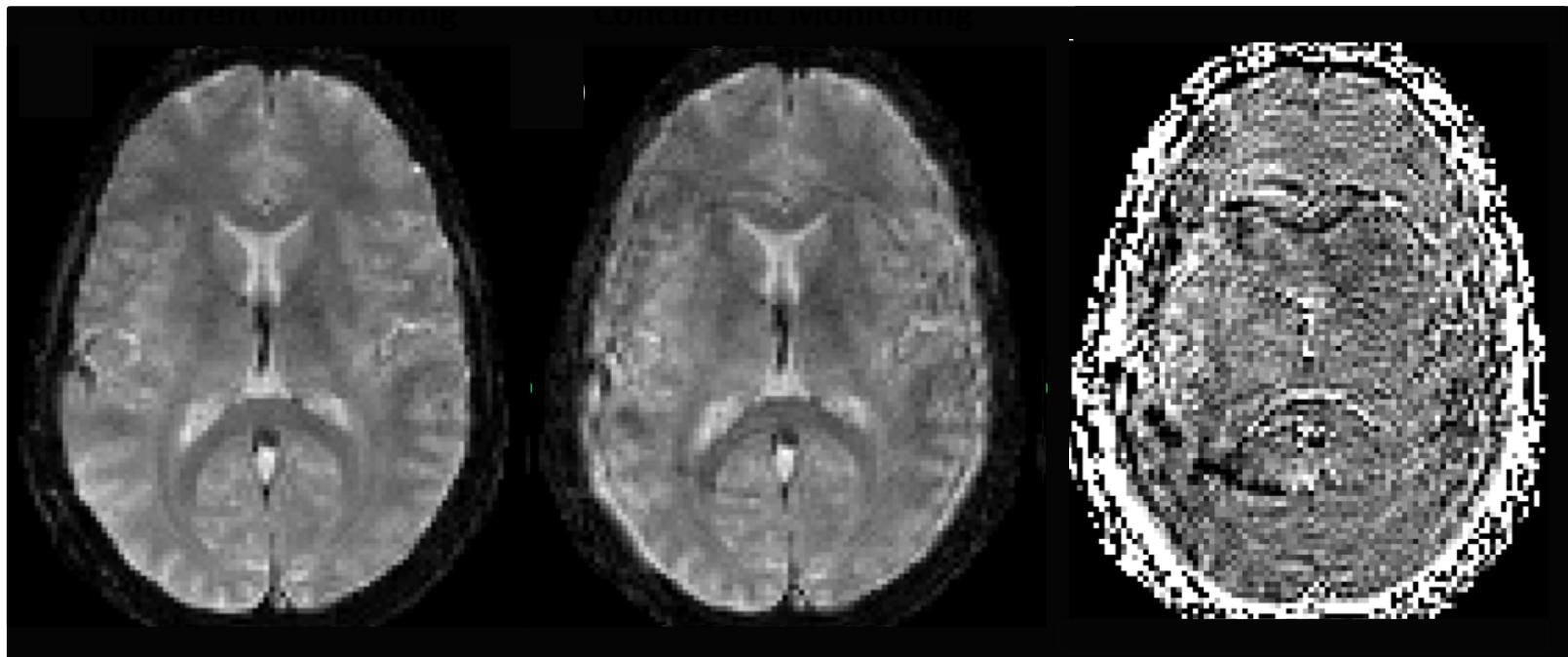
Rapid readout:
41 msec



Field monitoring

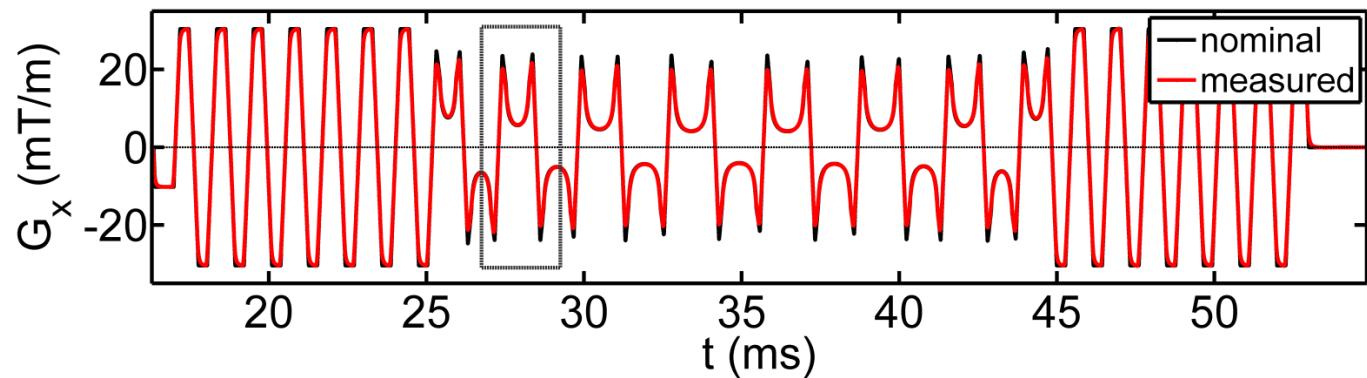
Nominal evolution

Difference

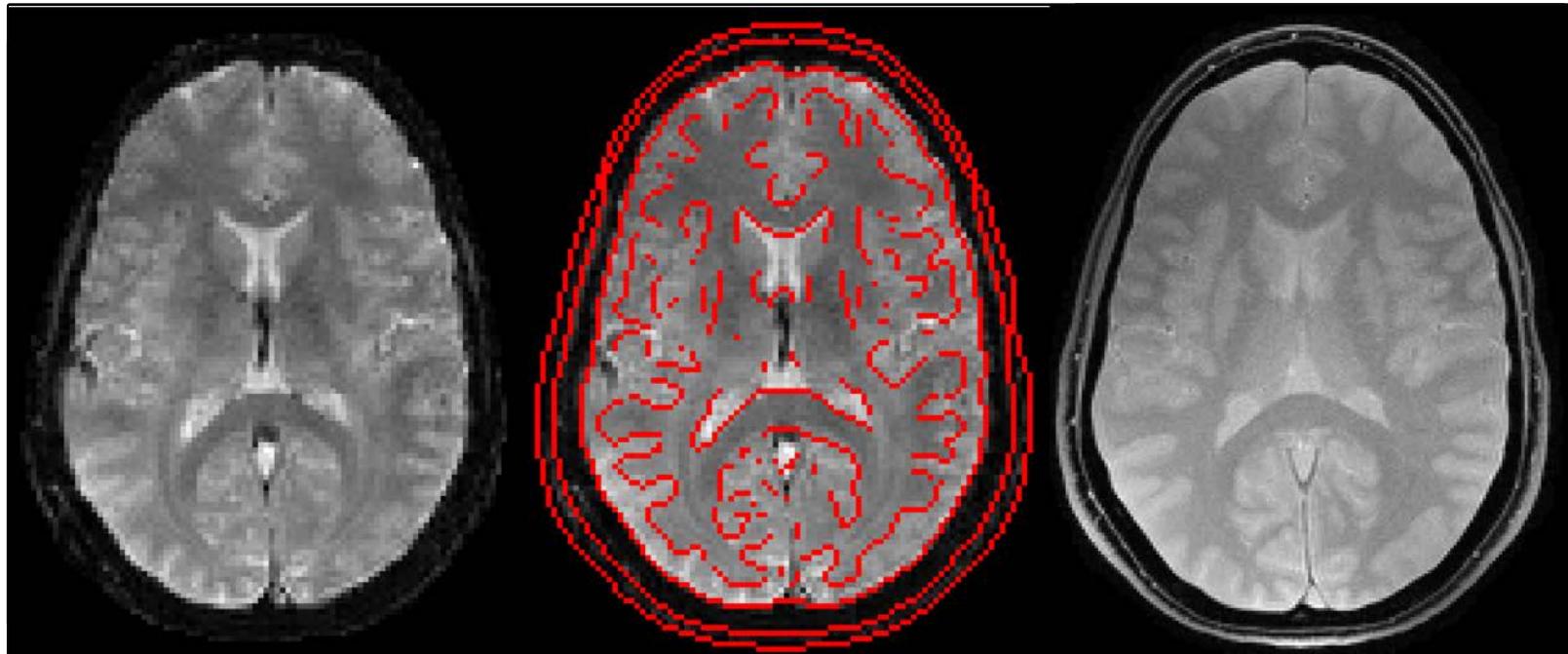


Magnetic Field Sensing & Control

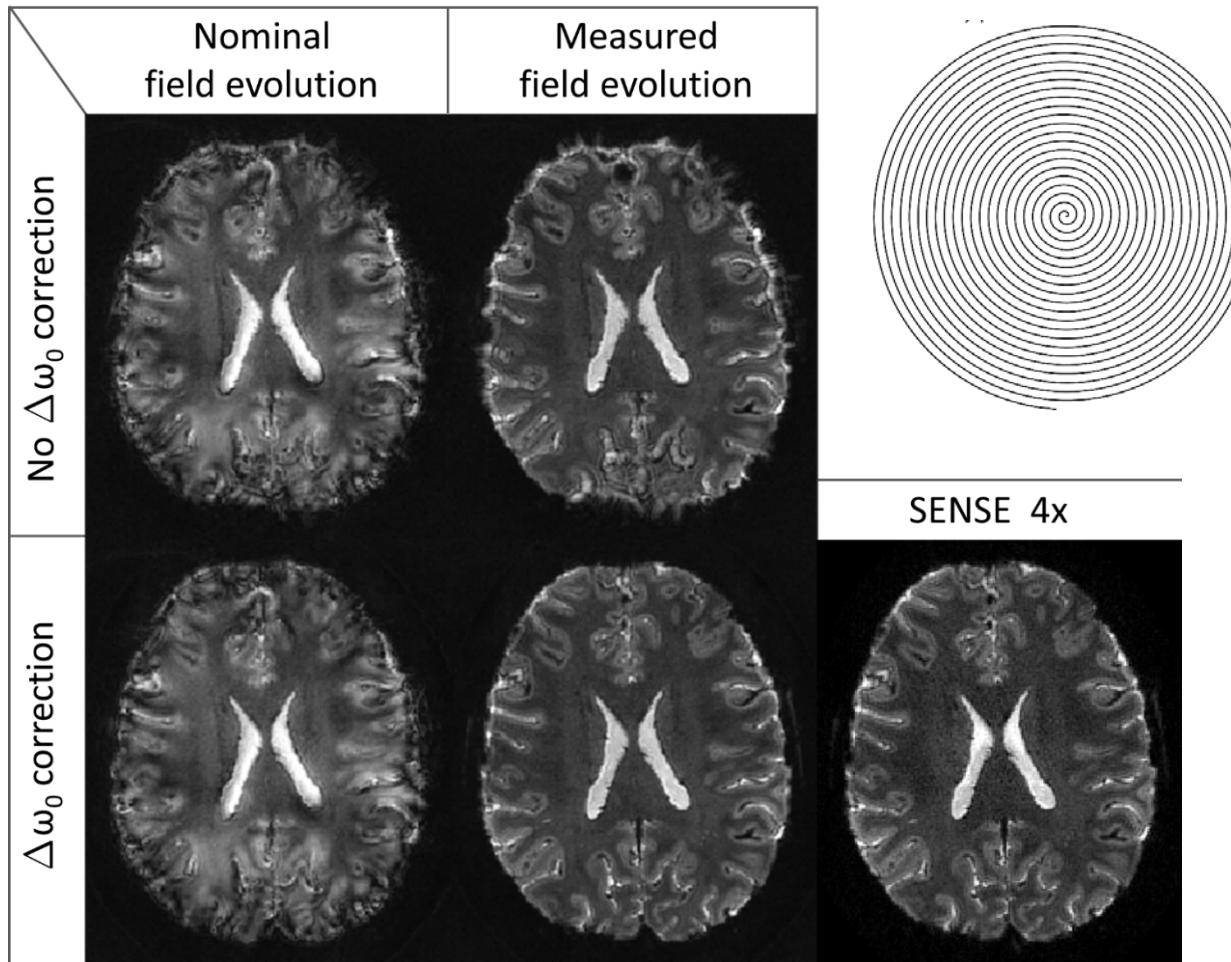
Rapid readout:
41 msec



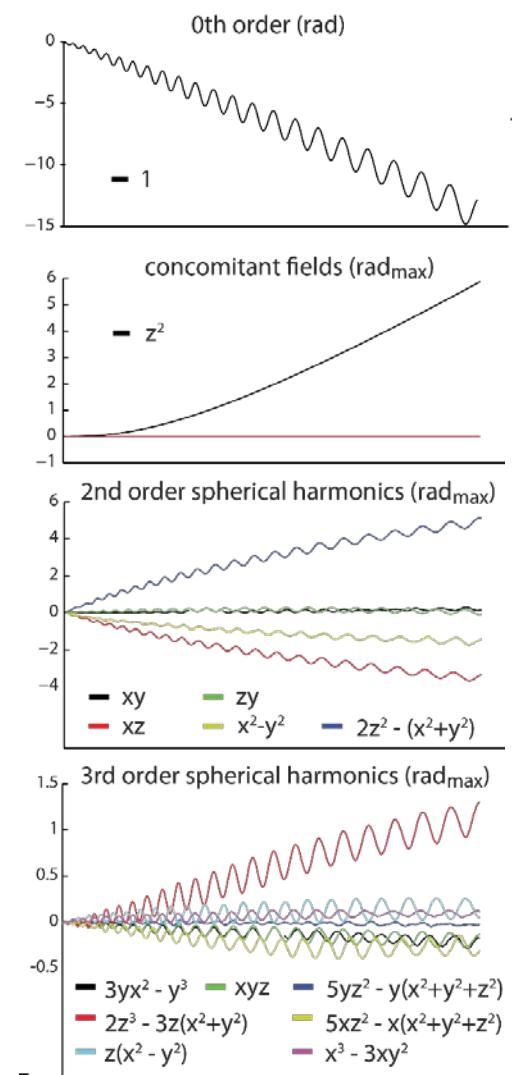
Field monitoring enforces consistent geometry:



Single-Shot Spiral Imaging at 7T

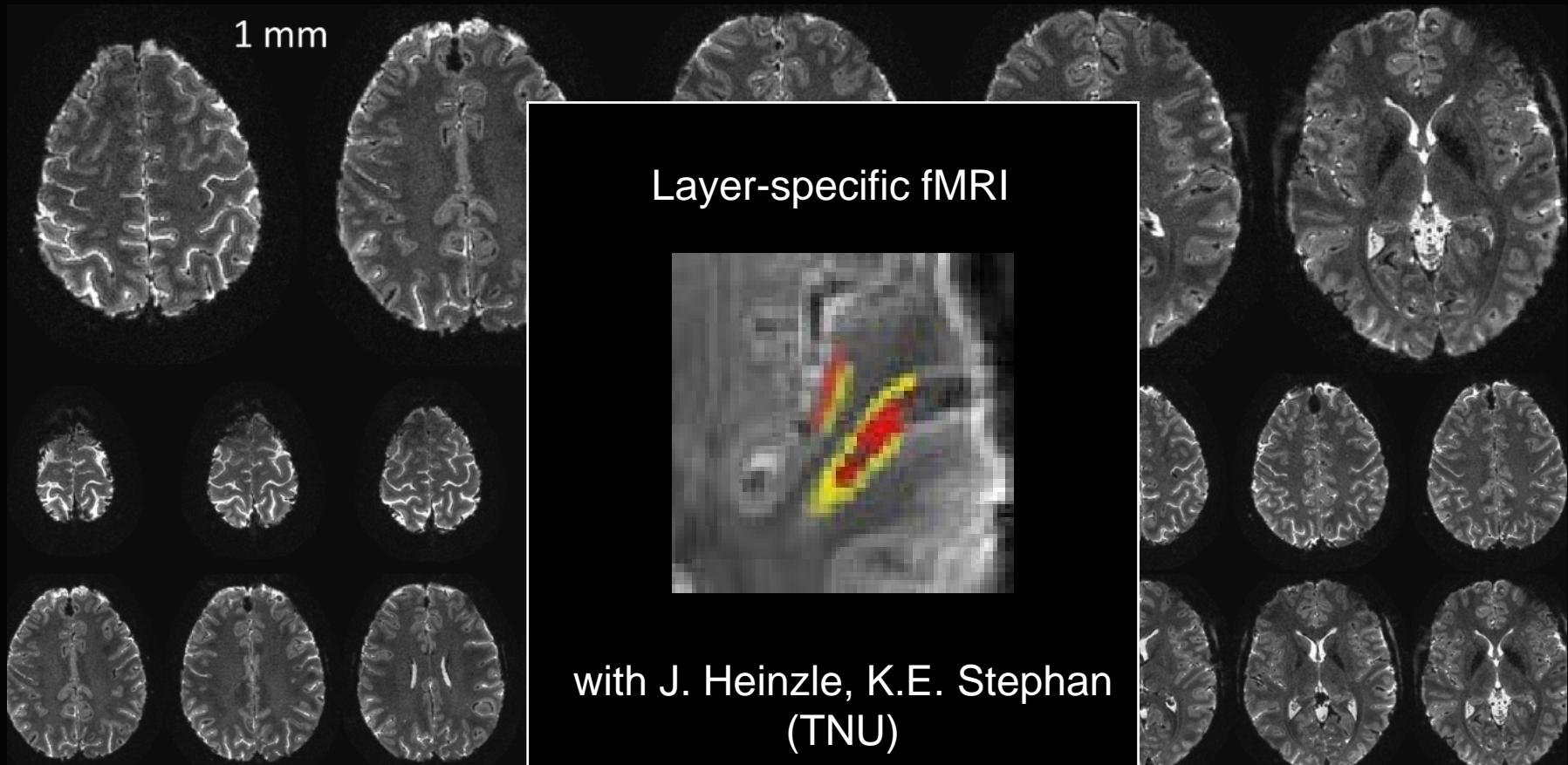


M. Engel et al., MRM (2018)



Single-Shot Spirals

7 T, $\Delta x = 800 \mu\text{m}$, TE = 25 ms, AQ = 58 ms



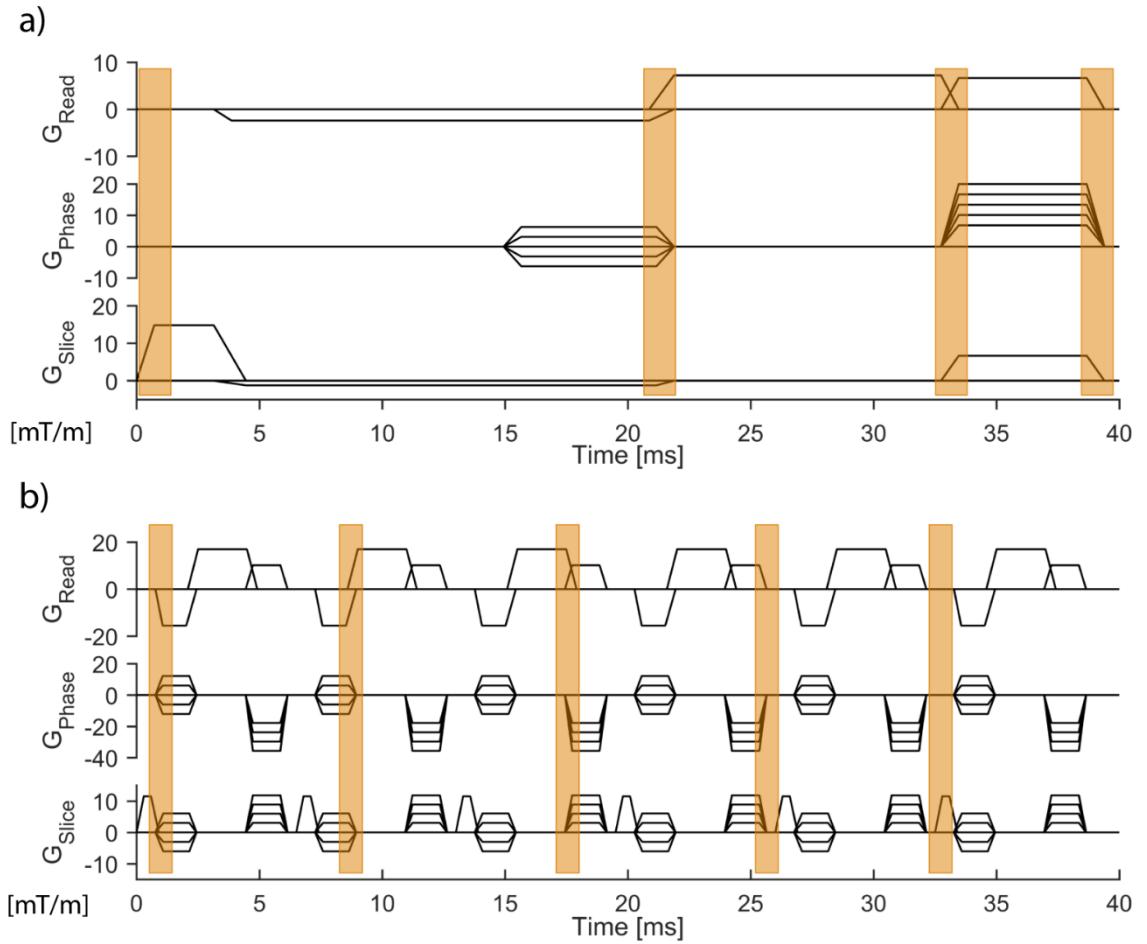
with J. Heinze, K.E. Stephan
(TNU)

M. Engel, L. Kasper

Motion Tracking and Correction

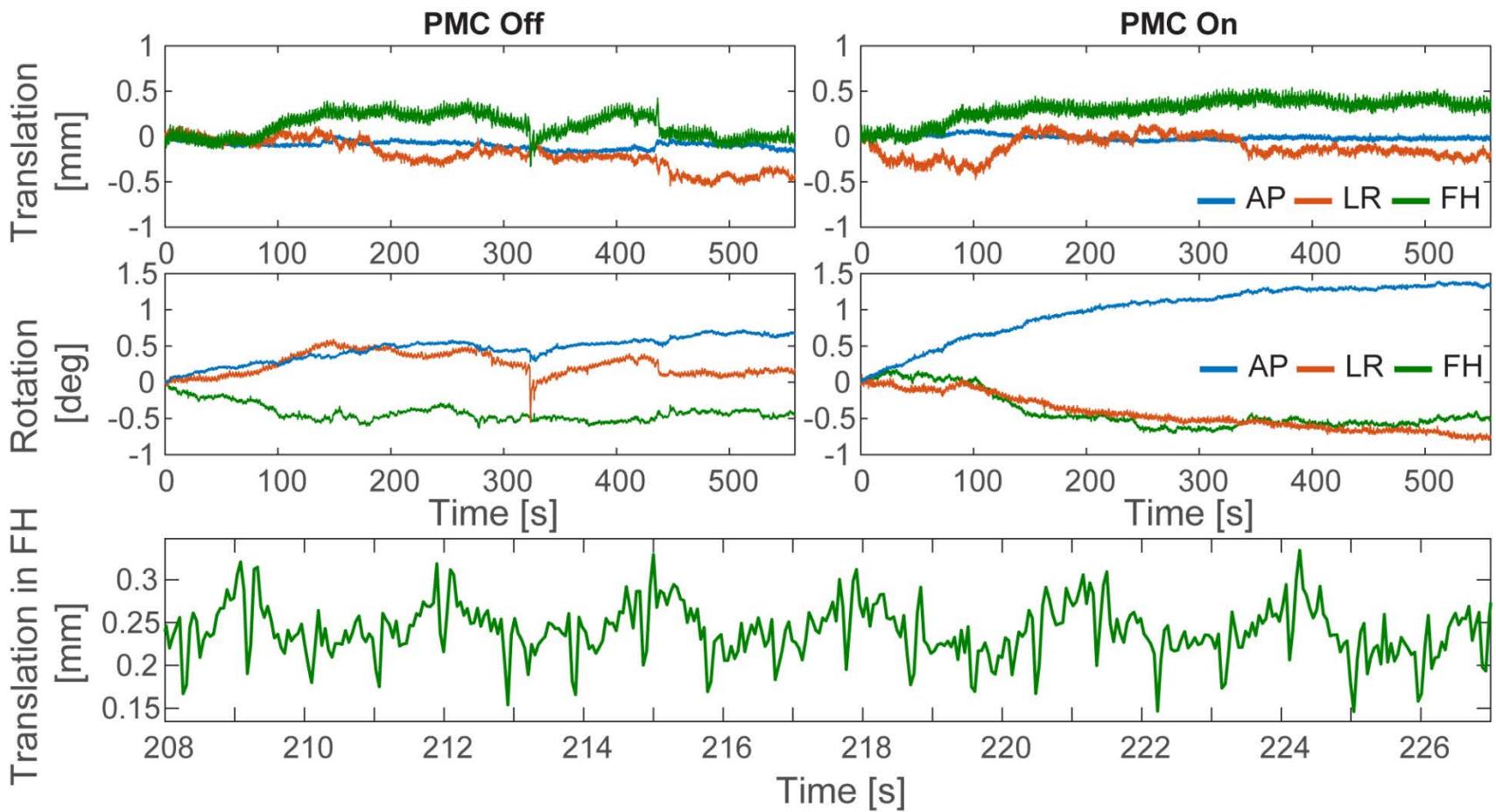


Measure field during imaging sequence



Motion Tracking and Correction

Precision: 5-20 μm , 0.01°



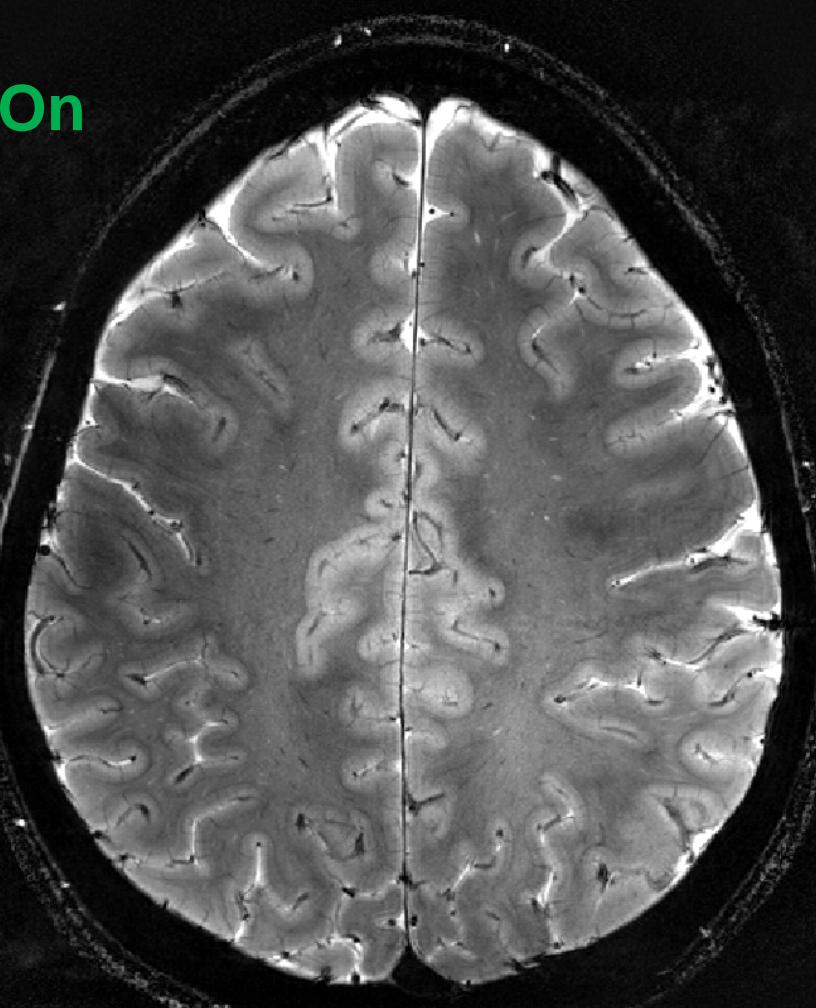
Motion Tracking and Correction

7T, T2*w, 300 μ m

Off

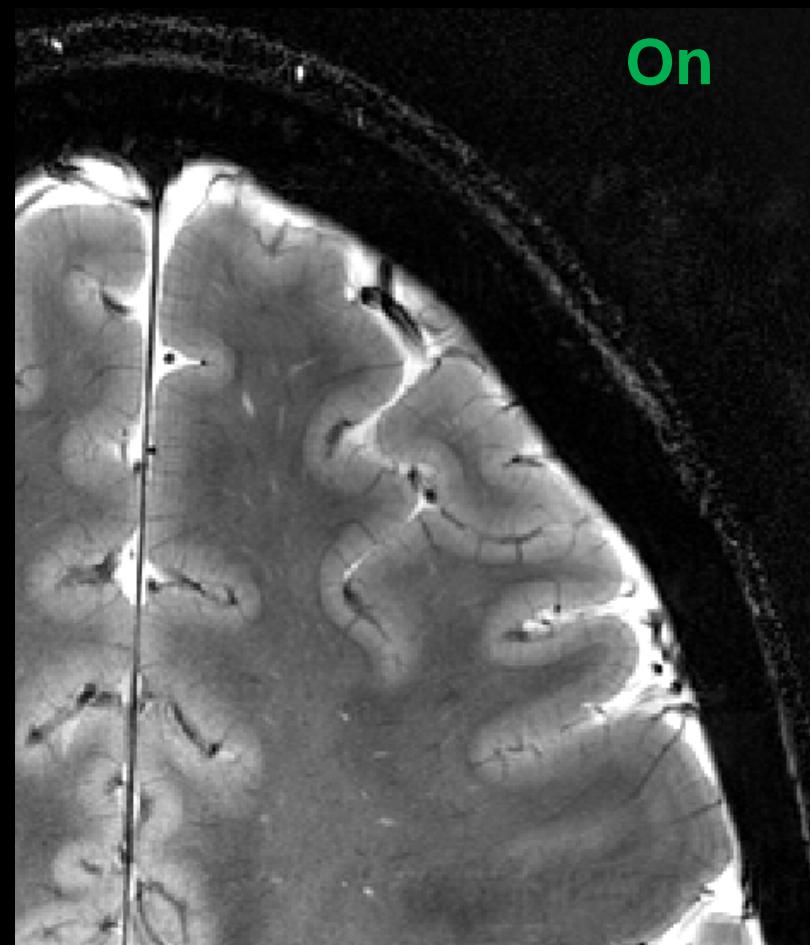
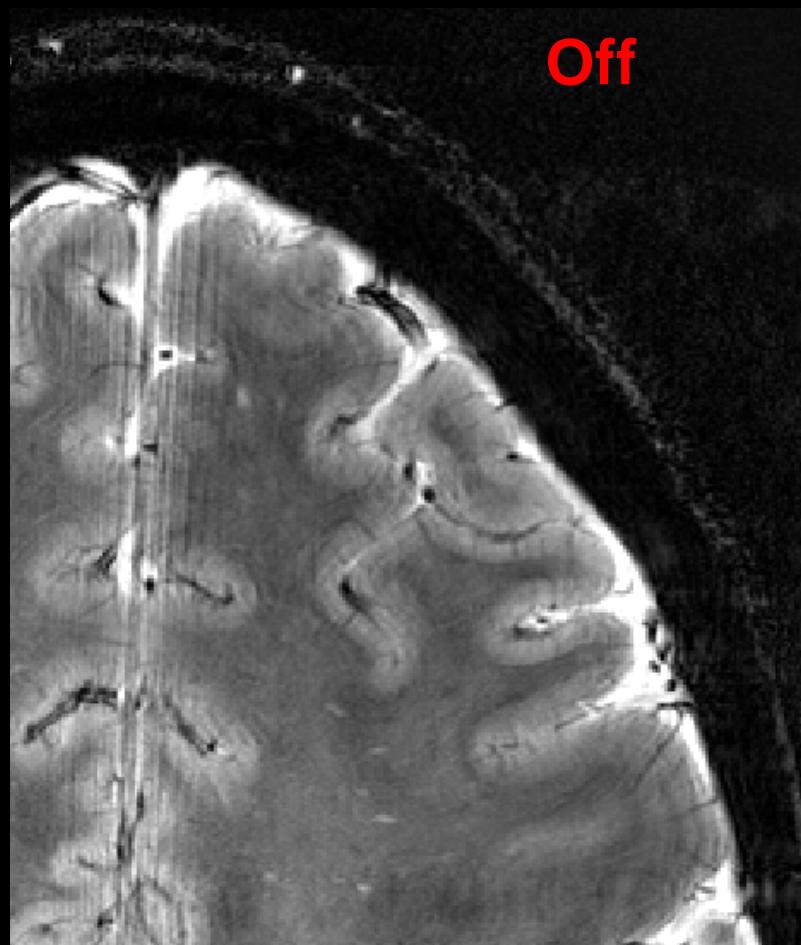


On

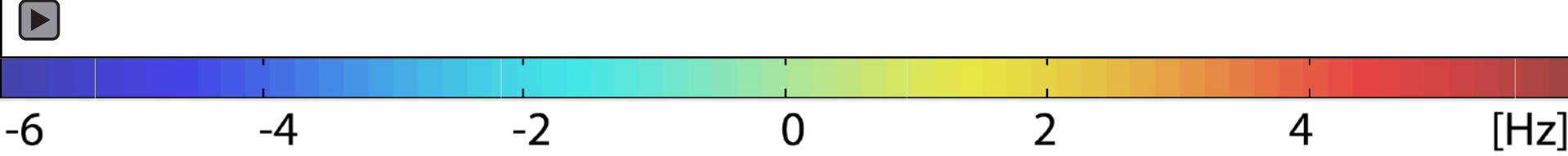


Motion Tracking and Correction

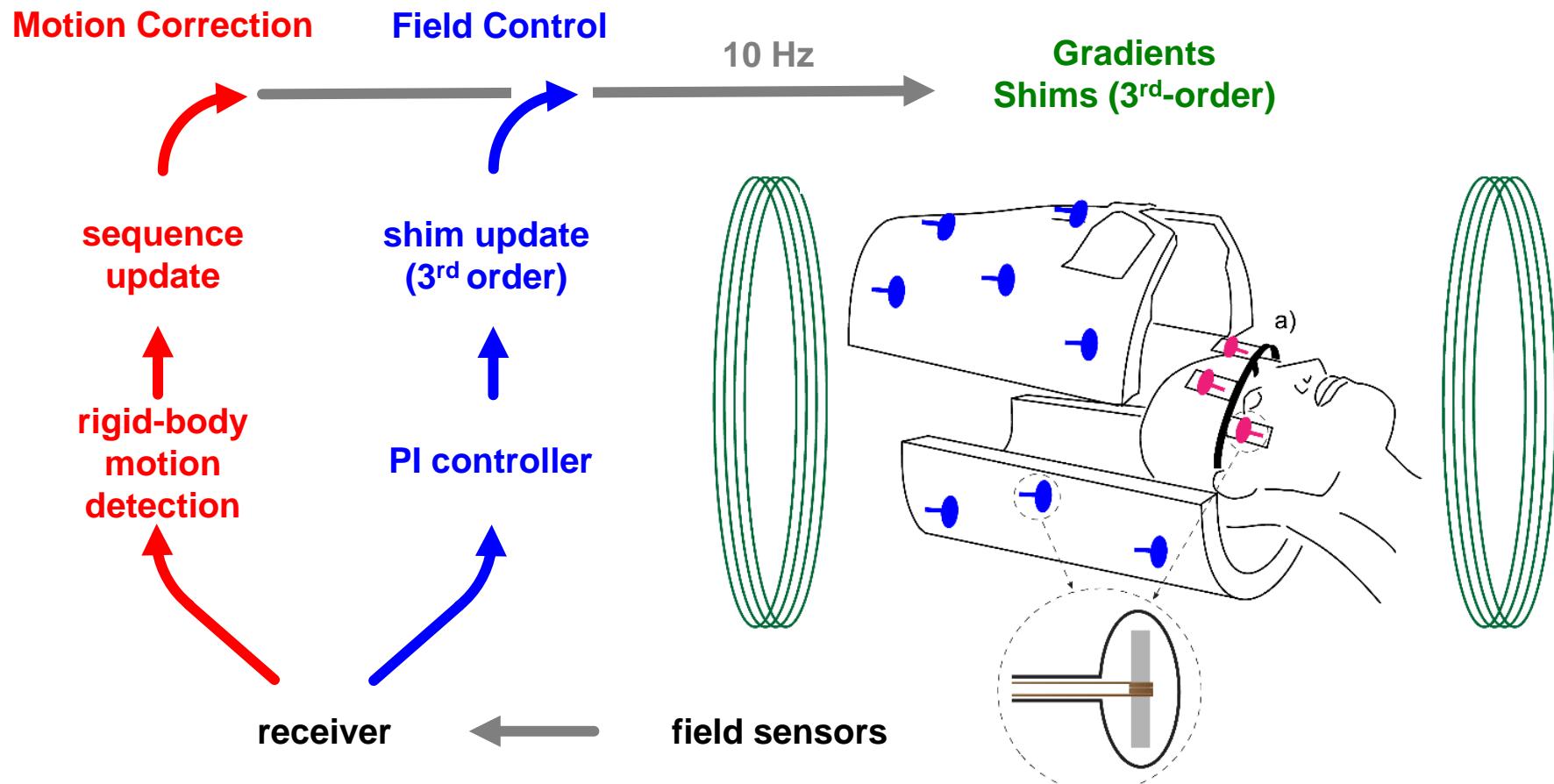
7T, T2*, high-resolution (300 μm)



Breathing Fluctuations at 7T



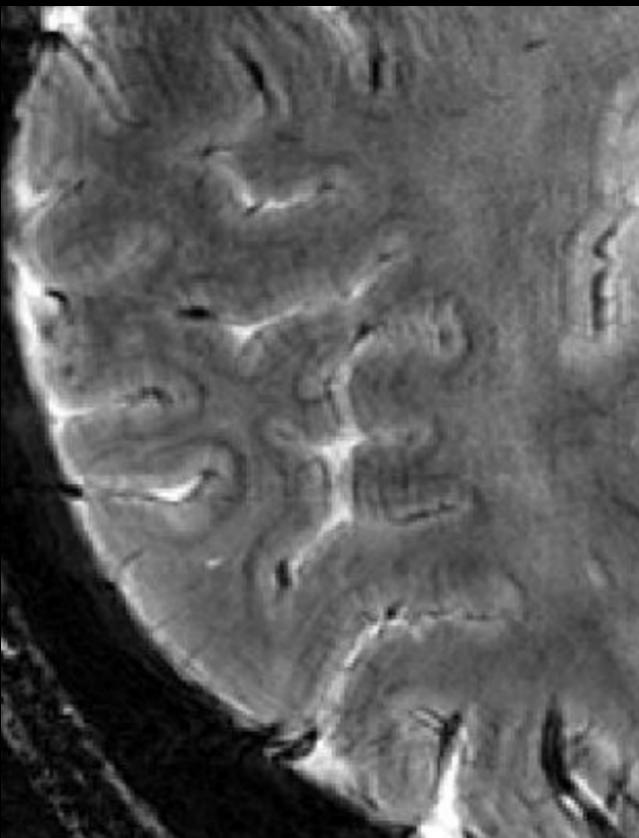
Real-Time Field and Motion Correction



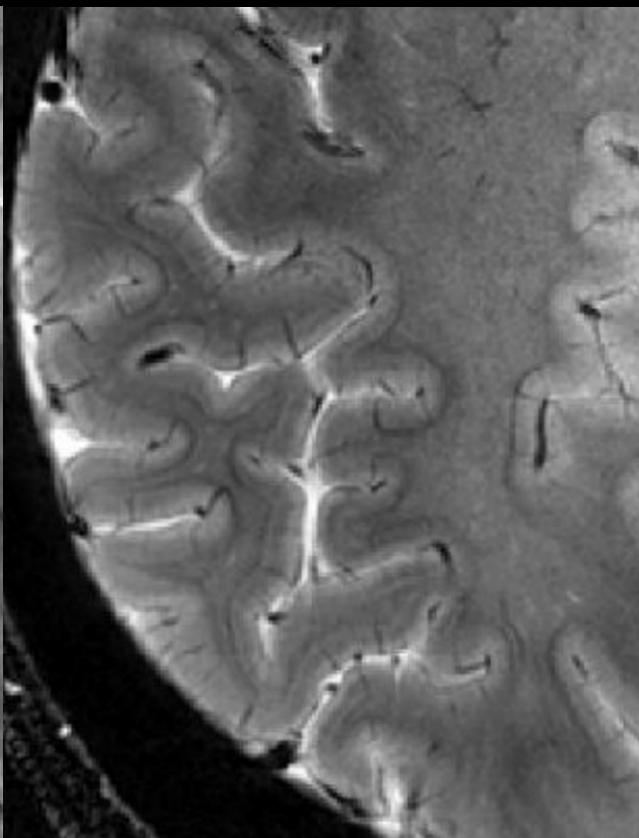
Real-Time Field and Motion Correction

T2*w at 7T

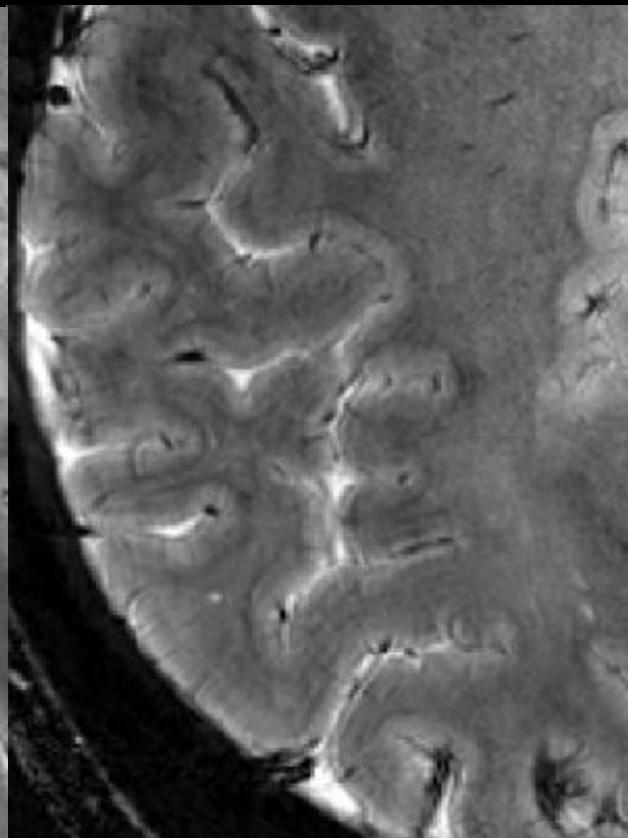
field control only

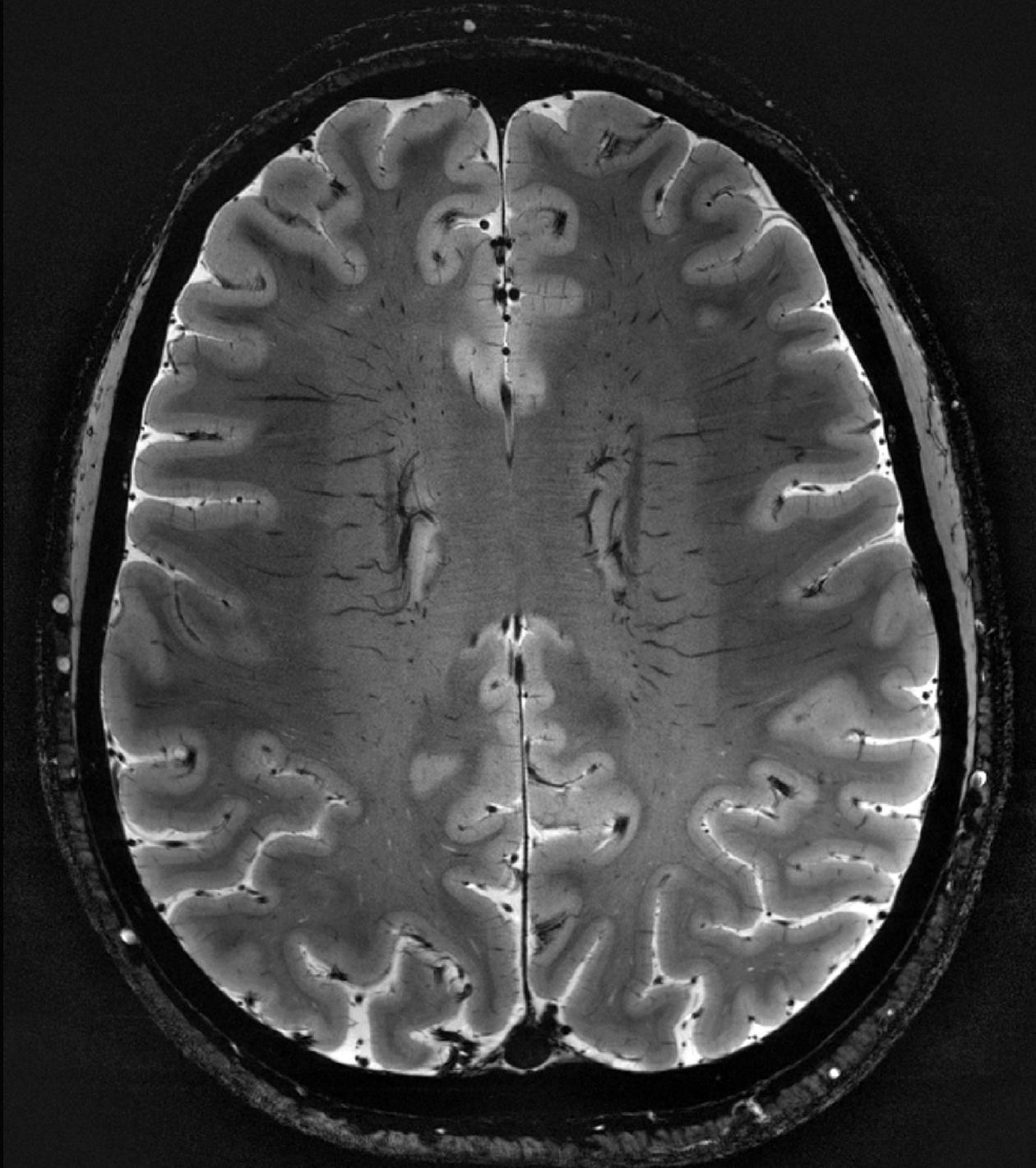


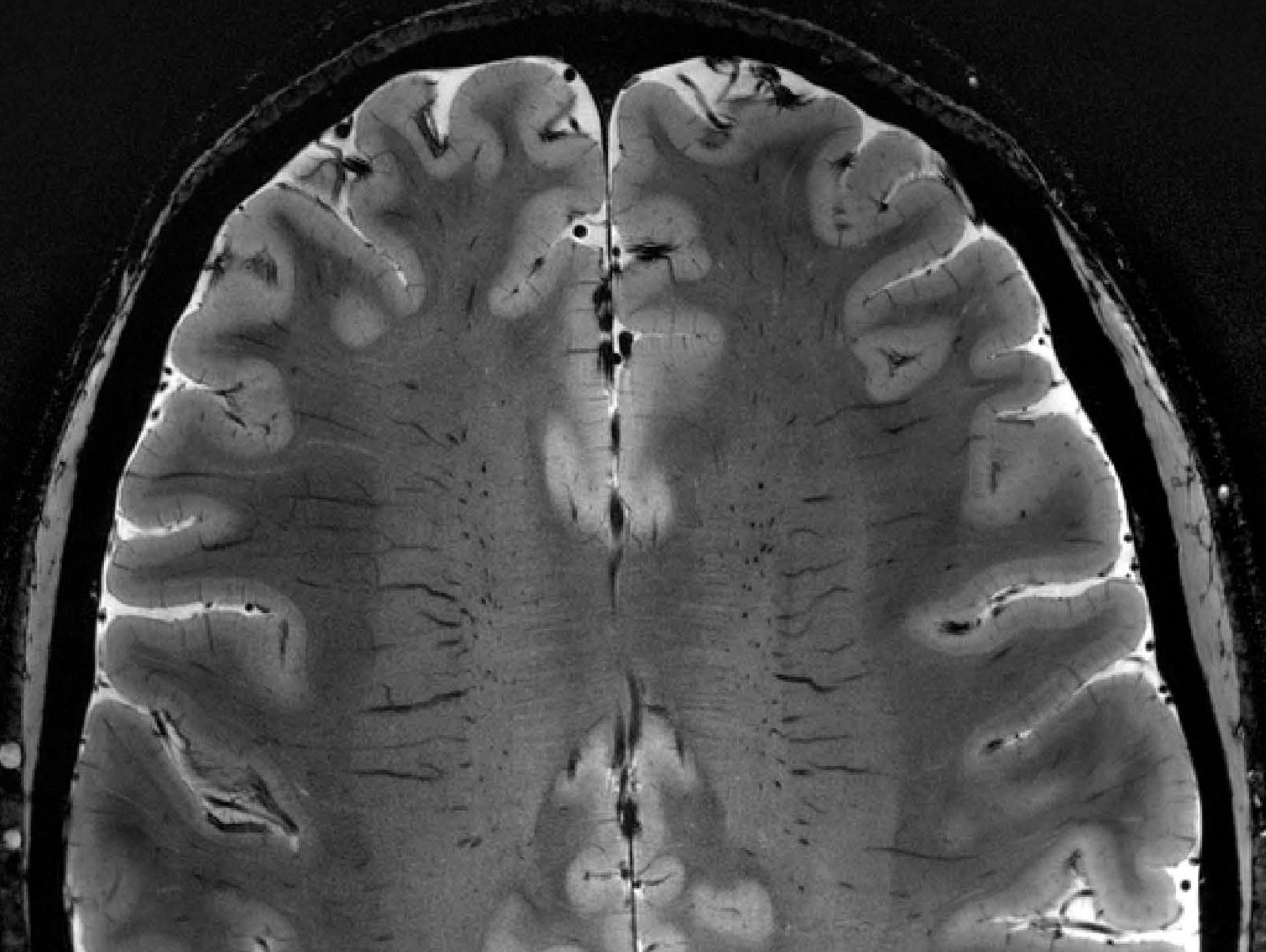
combined

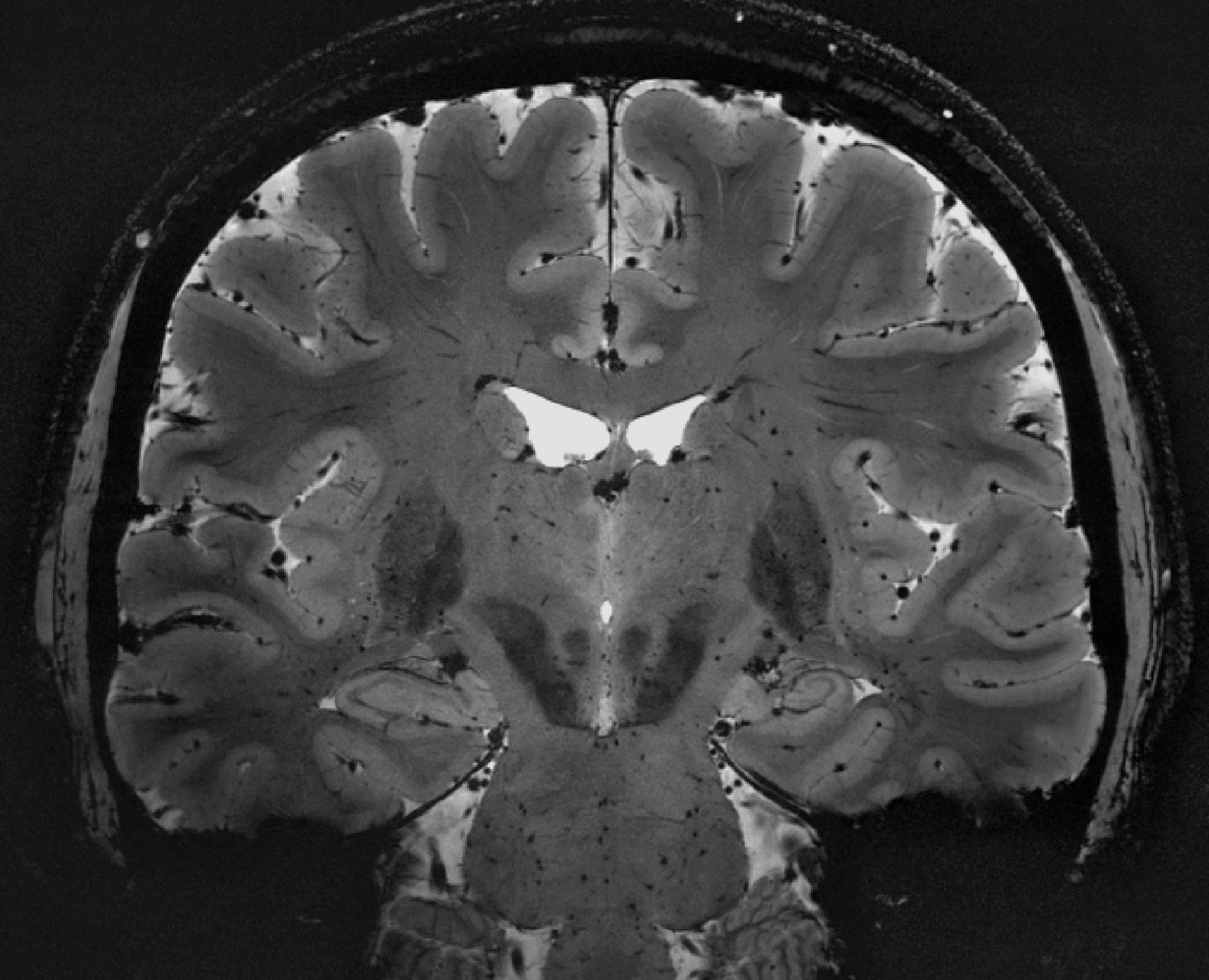


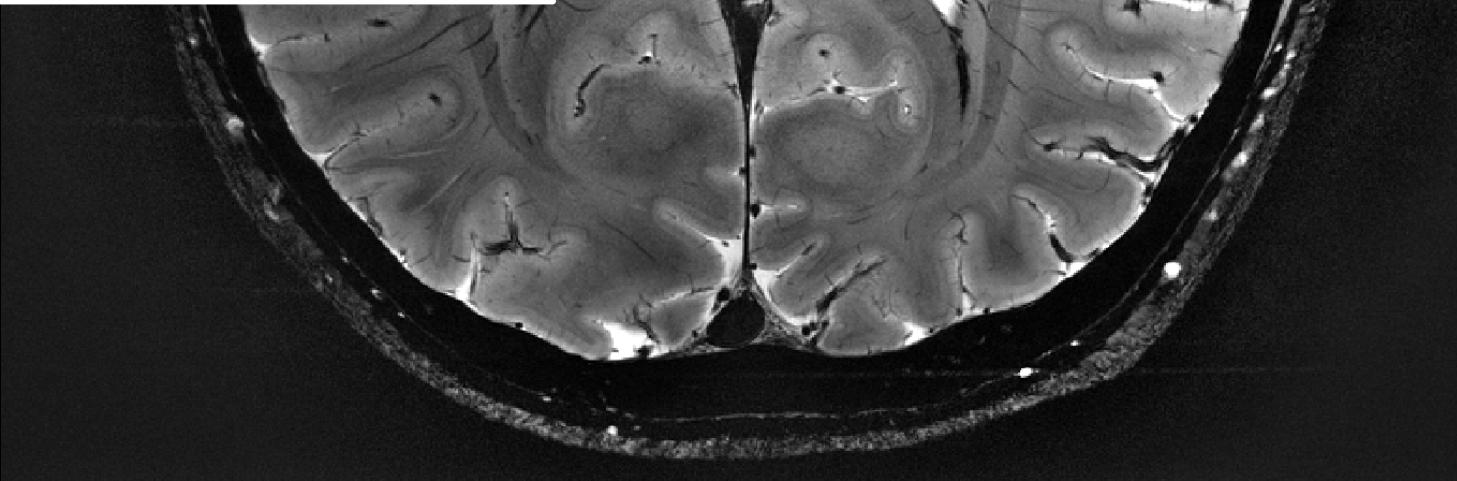
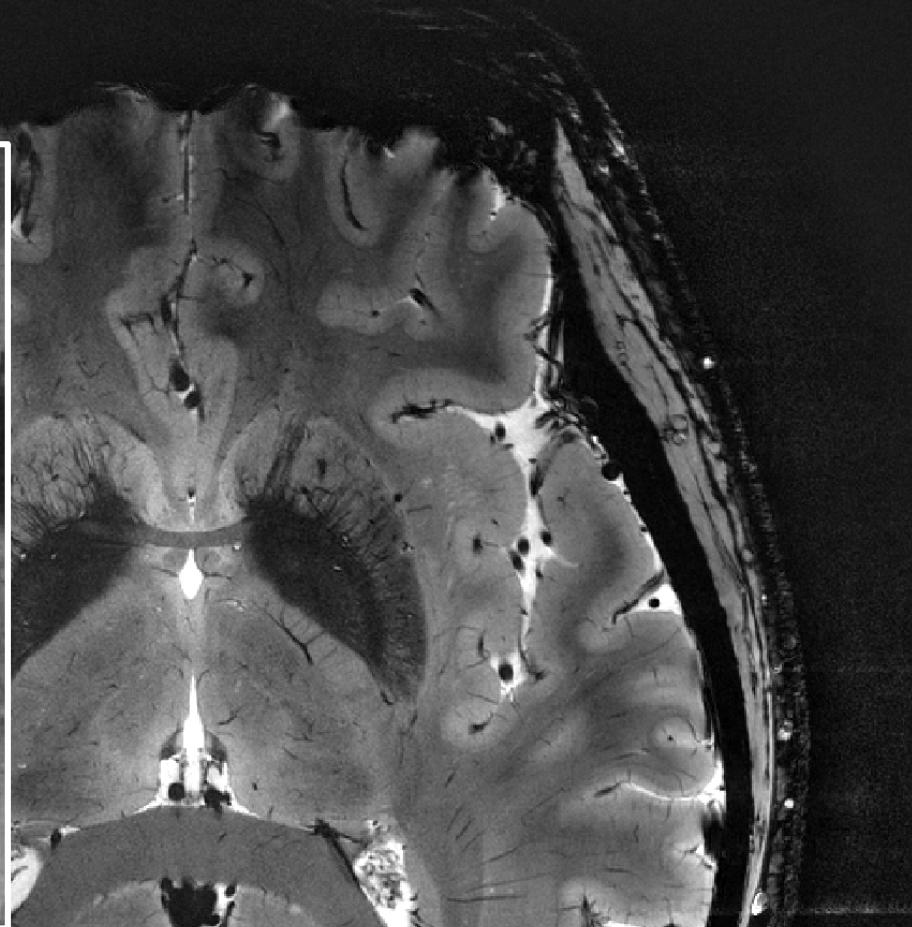
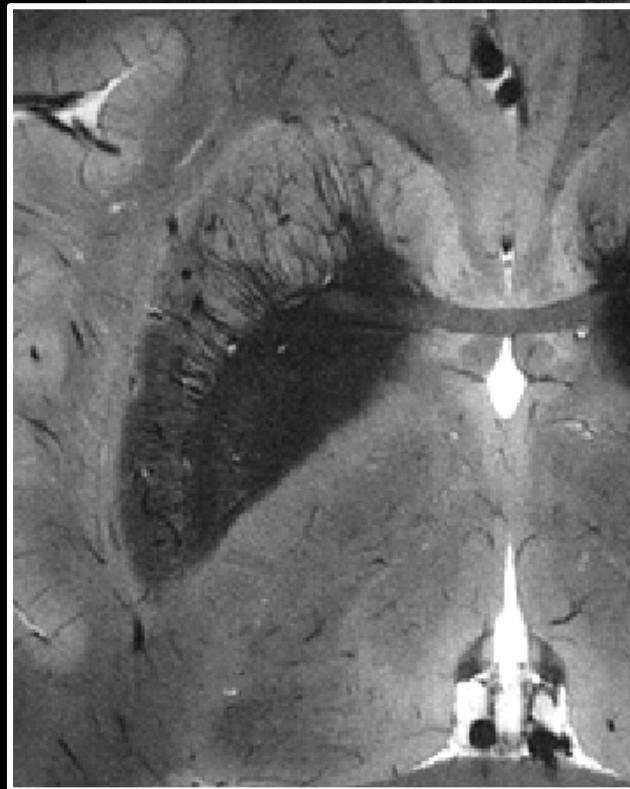
motion correction only

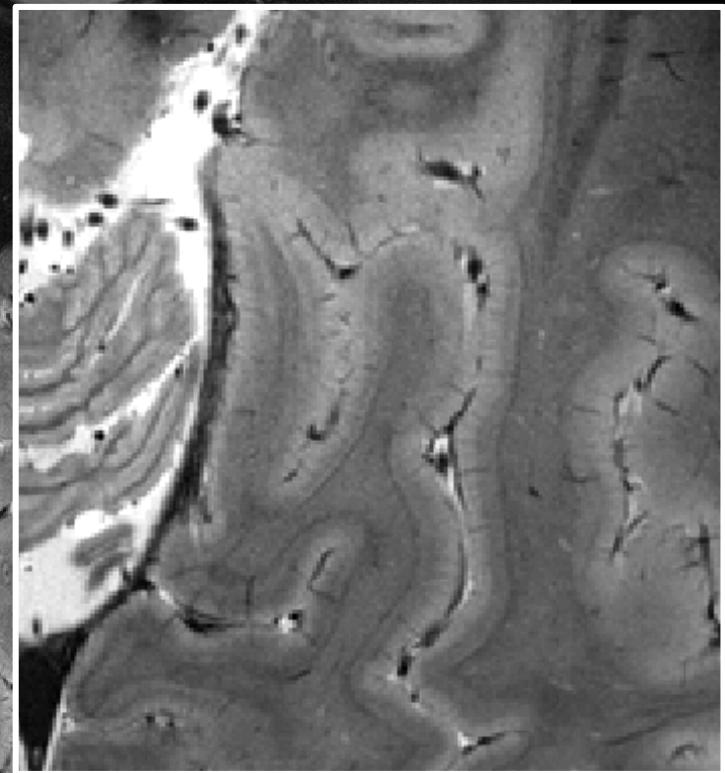
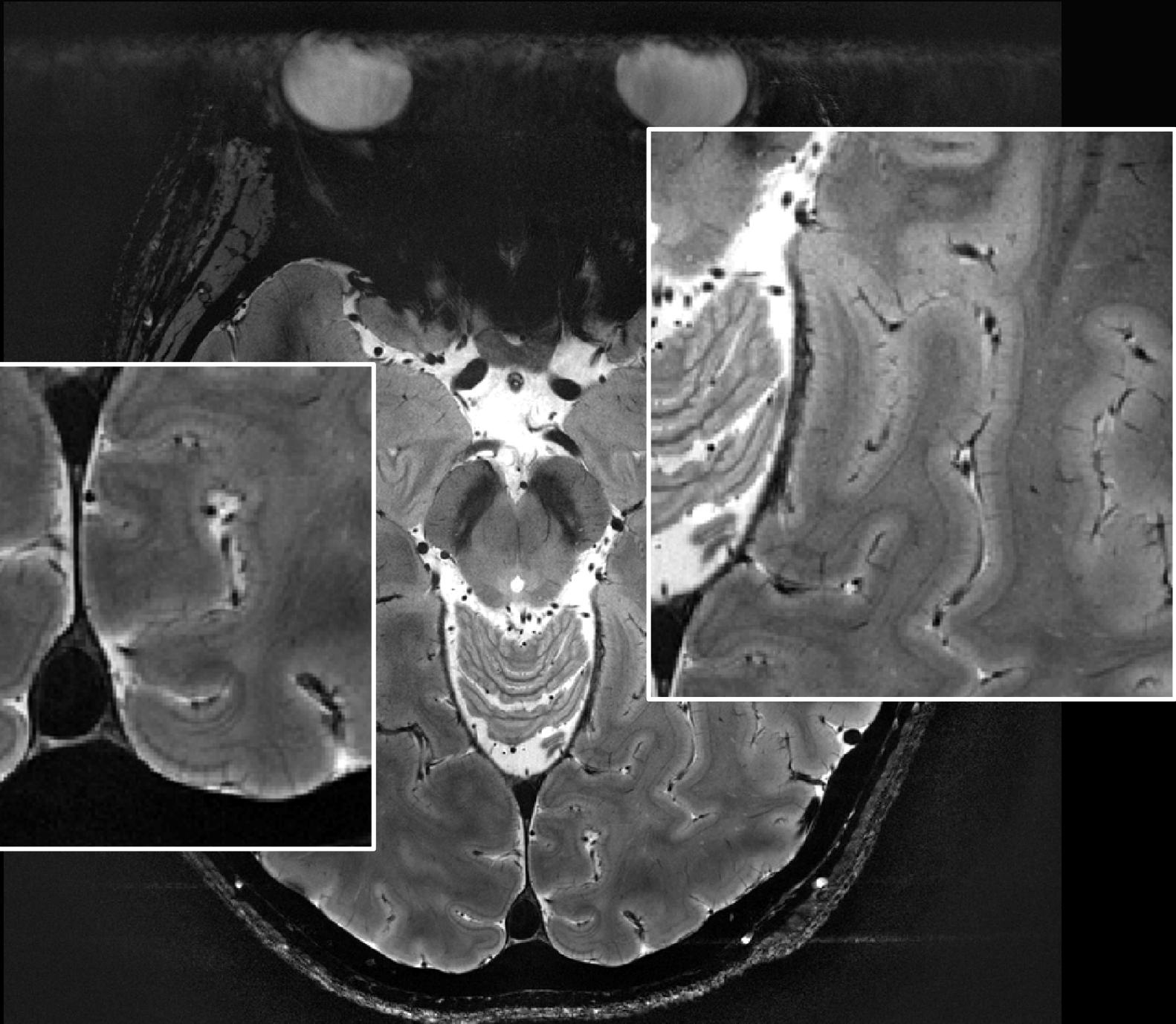
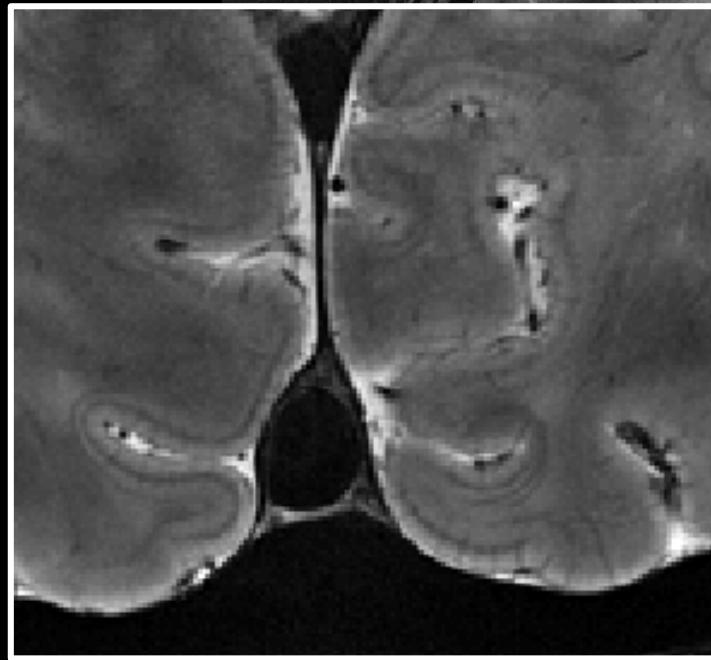












Imaging Mode:

Magnetic Resonance

- Probe: **radiofrequency waves**
- Wavelength: **5 – 150 cm**
- Matter interaction: **nuclear spin transitions**
- Modalities:
 - Magnetic Resonance Imaging (MRI)**
 - Magnetic Resonance Spectroscopy (MRS)**
 - Functional MRI (fMRI)**
- Resolution: **µm – mm**
- Applications: **body, neuro, cardiovascular, animal, economics, ...**
- Advantages: **non-ionizing, versatile contrast, function, metabolism**
- Limitations: **sensitivity, imaging speed, cost**