



CS-2001 DATA STRUCTURE

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BINARY SEARCH TREE

Binary Search Trees (BSTs)

□ Binary Search Tree

Property:

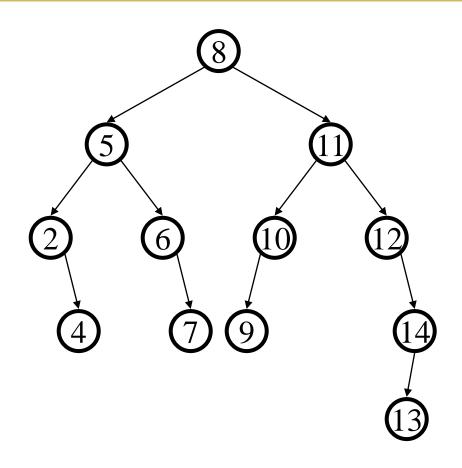
The value stored at a node is greater than

the value stored at its

left child and less than

the value stored at its

right child



Binary Search Trees (BSTs)

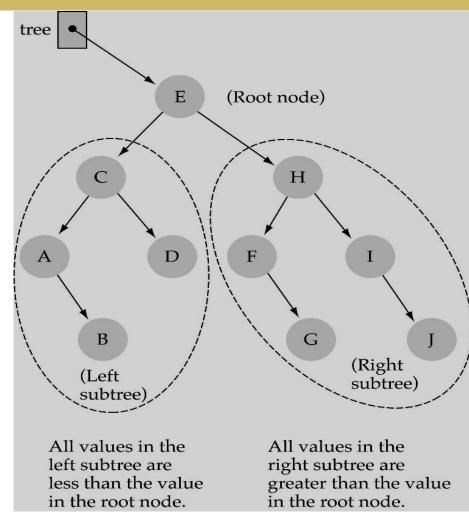
Binary Search TreeProperty:

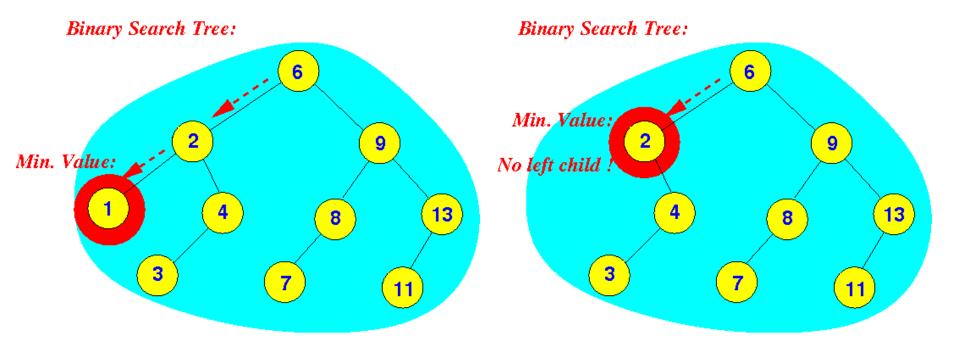
Where is the smallest element?

Ans: leftmost element

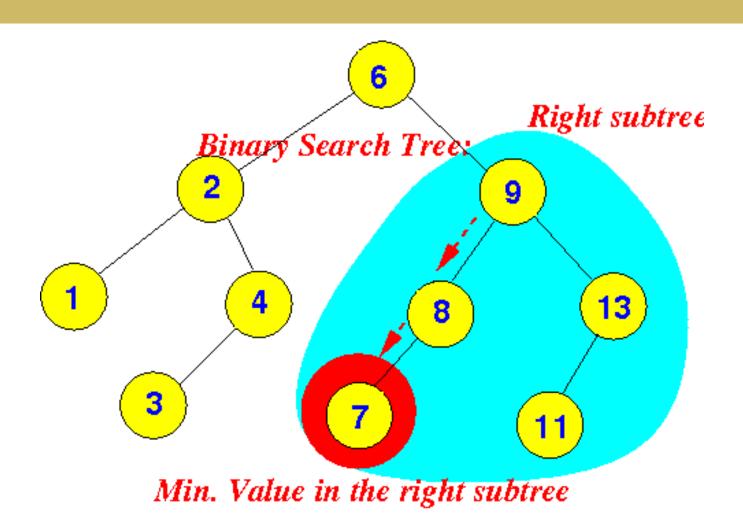
Where is the largest element?

Ans: rightmost element





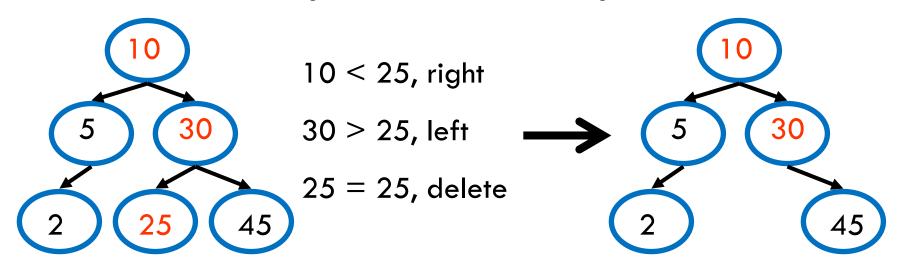
Min. Value in Right Subtree BST

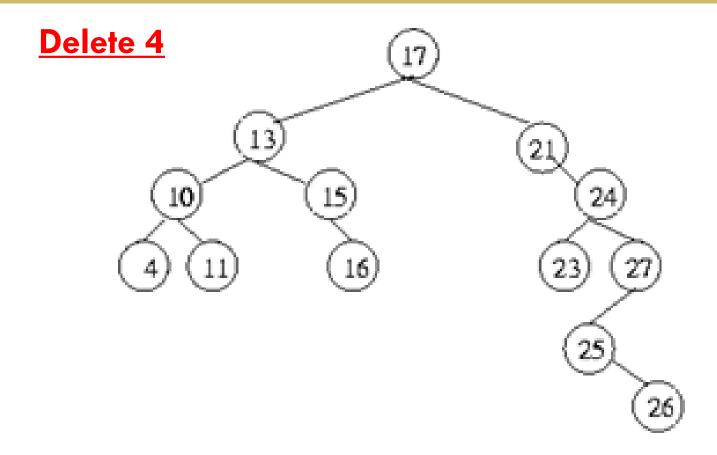


DELETION

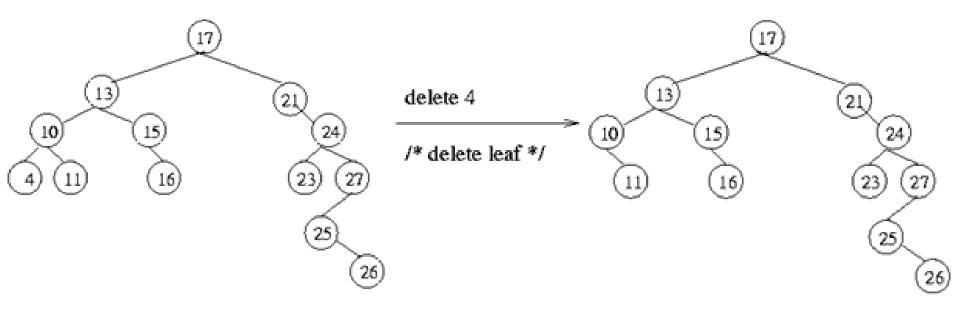
- A node being erased is not always going to be a leaf node
- There are three possible scenarios:
 - The node is a leaf node,
 - It has exactly one child, or
 - It has two children (it is a full node).

- □ Deleting a leaf node is quite easy
 - Find its parent
 - Set the child pointer that links it with the parent to NULL
 - Free the node's memory
- □ Consider deleting the node containing value 25





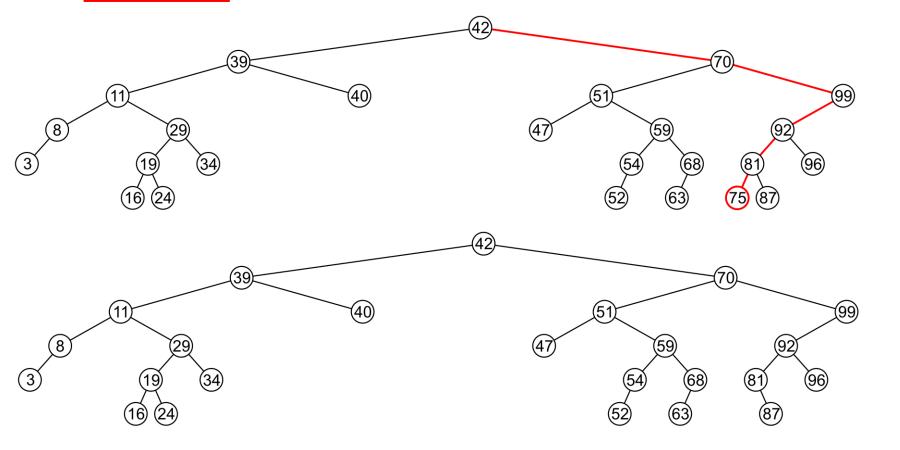
Delete 4 The node is deleted and left child of 10 is set to NULL



Deletion of a Leaf Node

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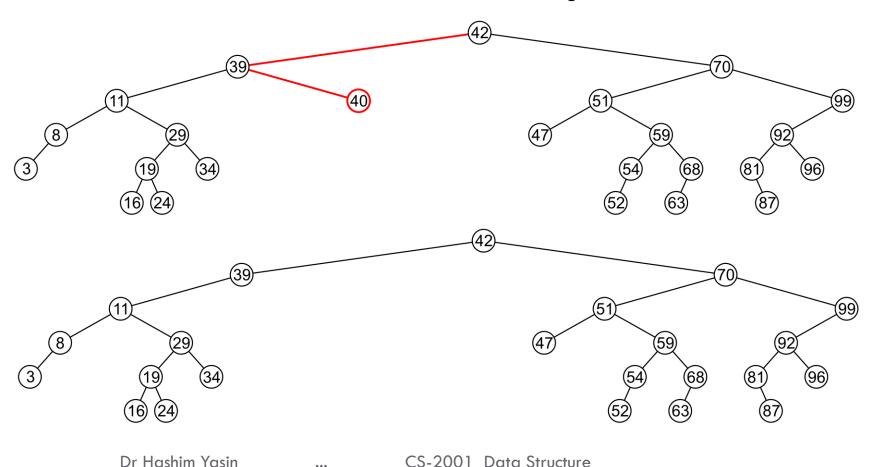
Delete 75 The node is deleted and left child of 81 is set to NULL



CS-2001 Data Structure

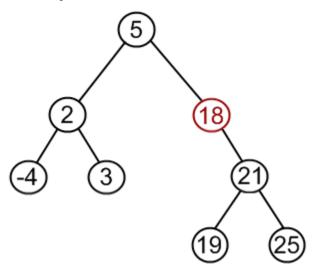
Deletion of a Leaf Node

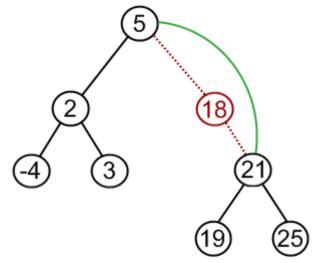
Delete 40 The node is deleted and right child of 39 is set to NULL



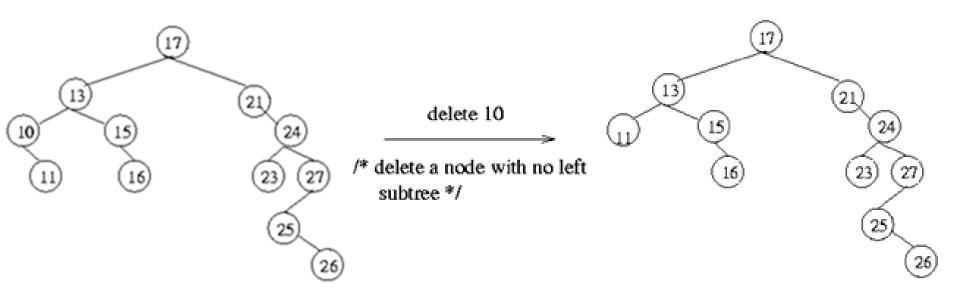
Deletion of a Node with Child

- □ If a node has only one child (left or right)
 - Simply promote the subtree associated with the child
- Consider deleting 18 which has one right child
 - Node 18 is deleted and the right tree of node 5 is updated to point to 21





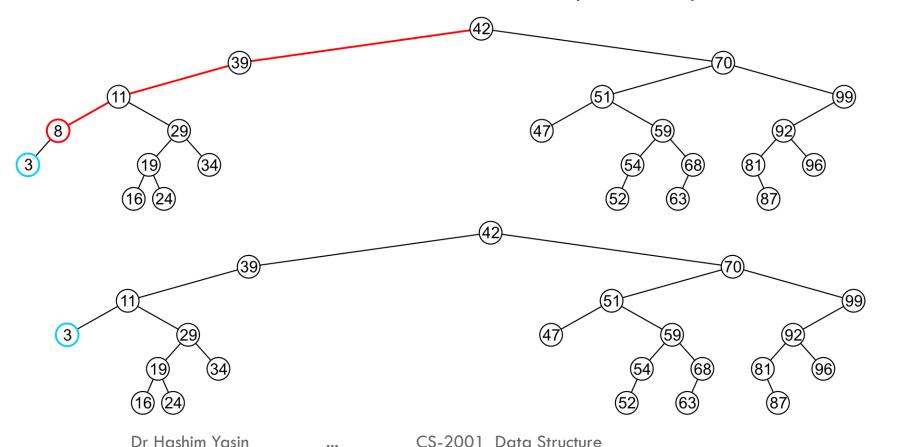
Delete 10 (left subtree)



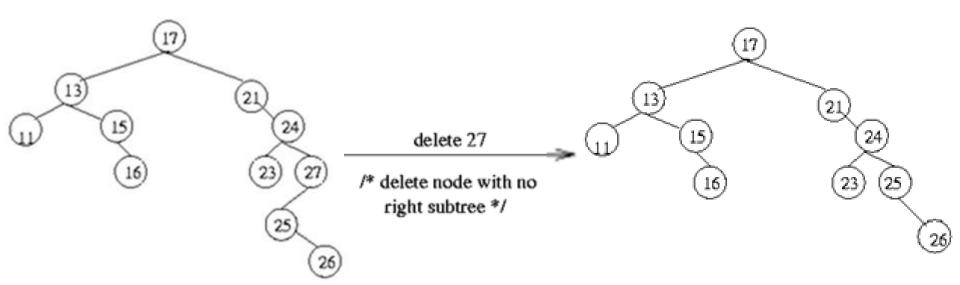
Deletion of a Node with Child

Delete 8 (left subtree)

Node 8 is deleted and the left tree of 11 is updated to point to 3.

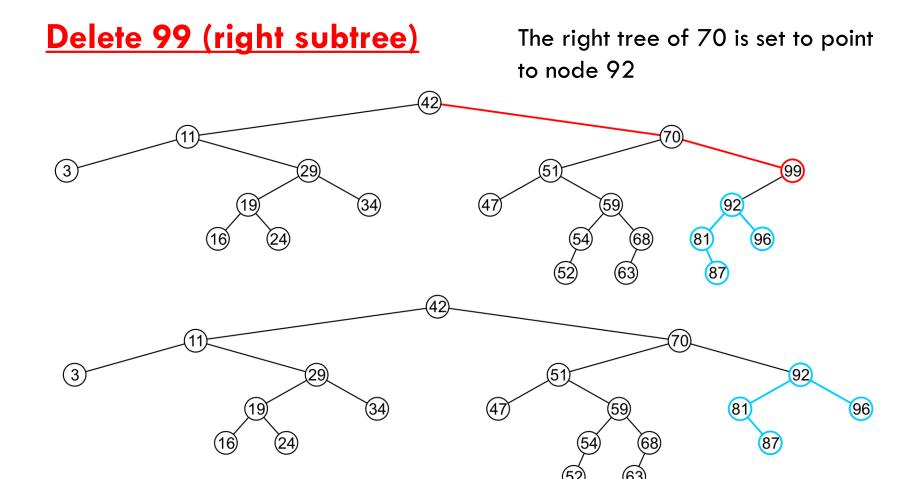


Delete 27 (right subtree)



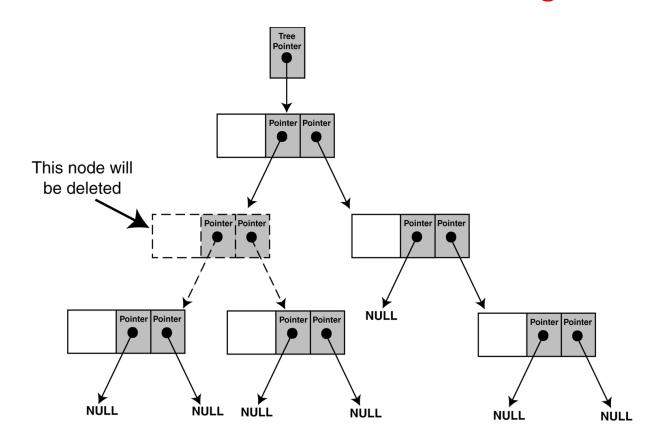
Deletion ... Node with

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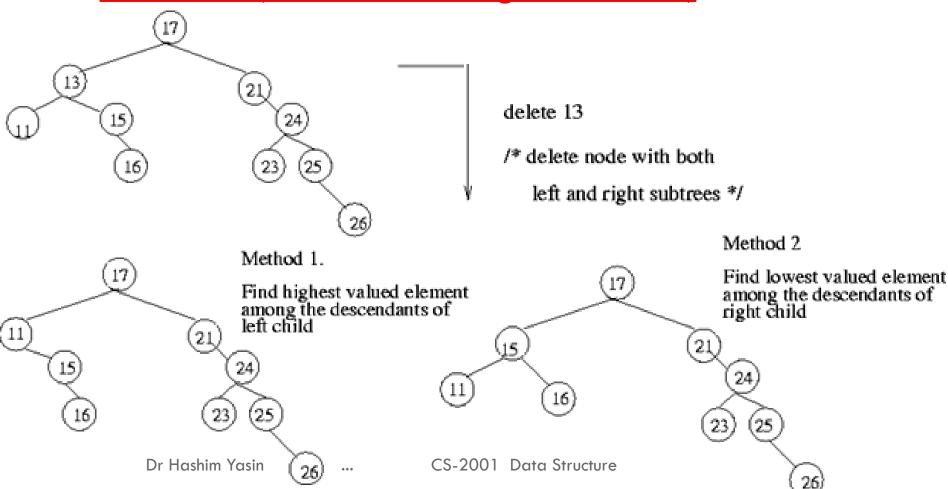


CS-2001 Data Structure

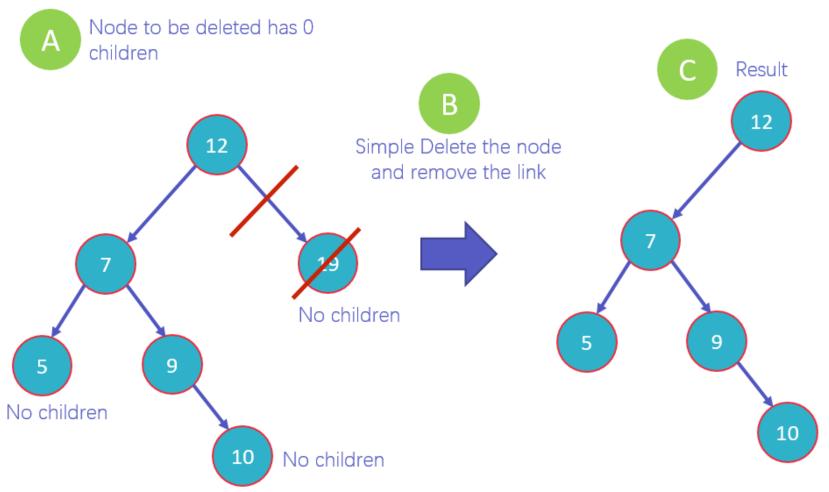
Delete a node that has both left and right subtrees:



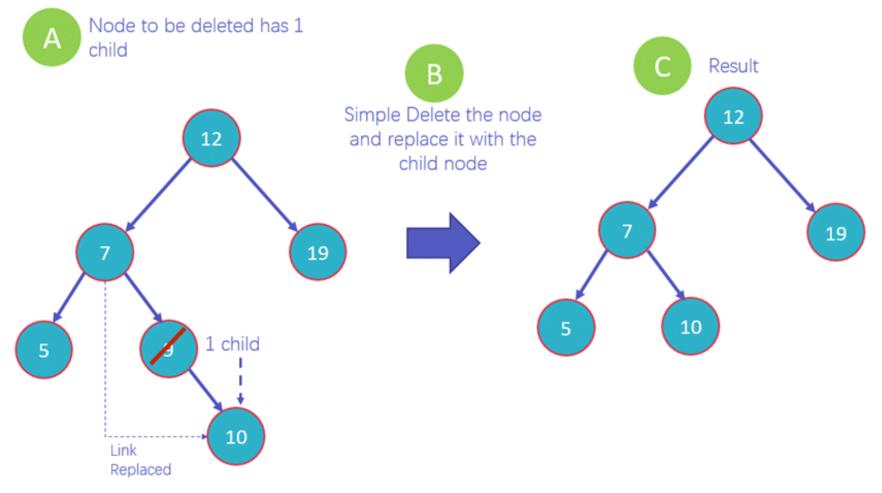
Delete 13 (both left and right subtrees)



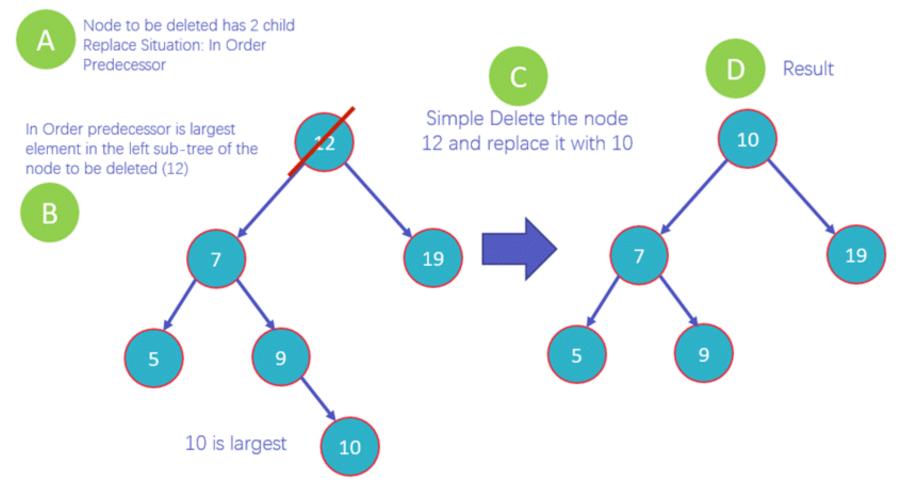
Delete Operation – Case 1



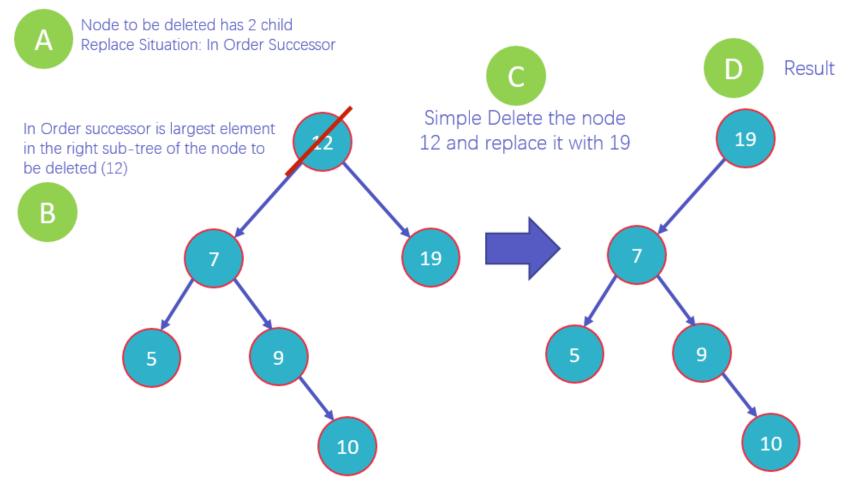
Delete Operation – Case 2

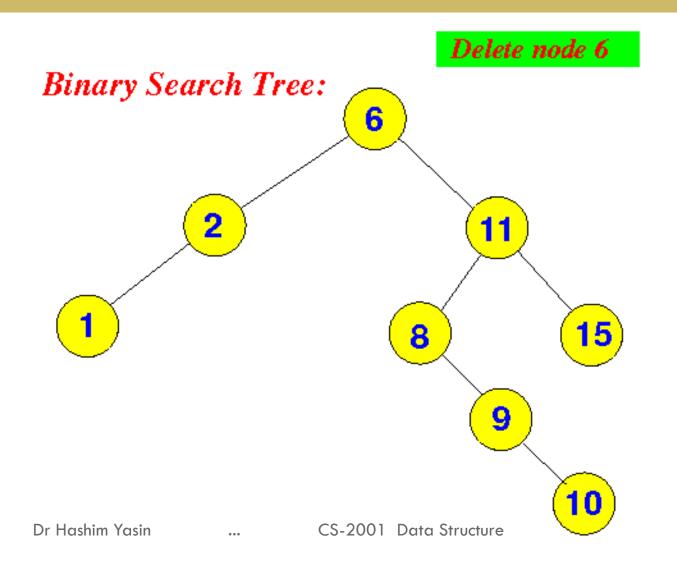


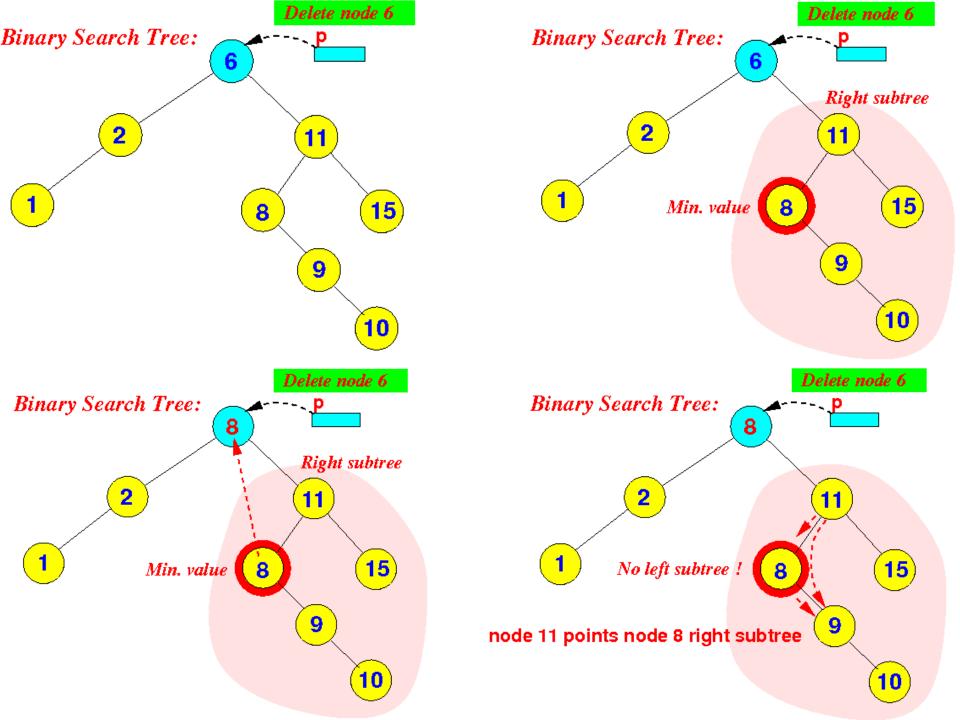
Delete Operation – Case 3 (a)



Delete Operation – Case 3 (b)

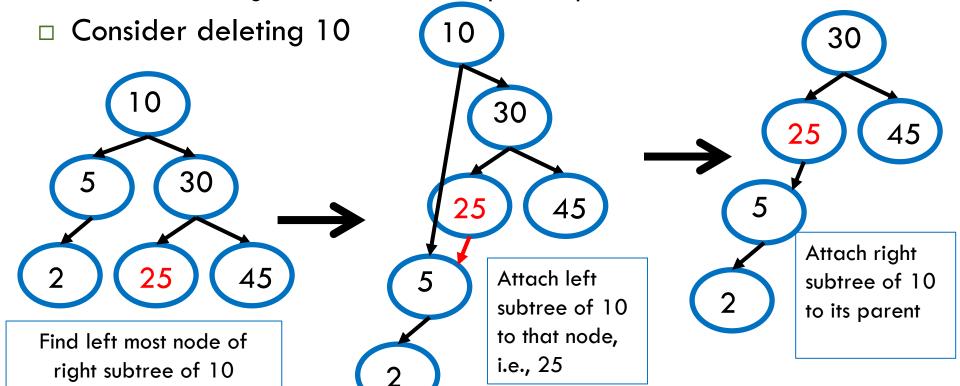






27

- Suppose node p with two children has to be deleted
 - Find a position in the right subtree of p to attach its left subtree
 - Left most node in the right subtree of node p (successor of p)
 - Attach the right subtree of node p to its parent



Implementation

The basis of our binary tree node is the following struct declaration:

```
struct TreeNode
{
    int value;
    TreeNode *left;
    TreeNode *right;
};
```

```
class IntBinaryTree{
private:
       struct TreeNode{
              int value;
              TreeNode *left;
              TreeNode *right;
       };
       TreeNode *root;
       void destroySubTree(TreeNode *);
       void deleteNode(int, TreeNode *&);
       void makeDeletion(TreeNode *&);
       void displayInOrder(TreeNode *);
       void displayPreOrder(TreeNode *);
       void displayPostOrder(TreeNode *);
 public:
       IntBinaryTree() { root = NULL; }
                                                    // Constructor
       ~IntBinaryTree() { destroySubTree(root); }// Destructor
       void insertNode(int);
       bool searchNode(int);
       void remove(int);
       void showNodesInOrder(){
                                   displayInOrder(root); }
       void showNodesPreOrder(){
                                   displayPreOrder(root); }
       void showNodesPostOrder(){
                                   displayPostOrder(root); }
};
```

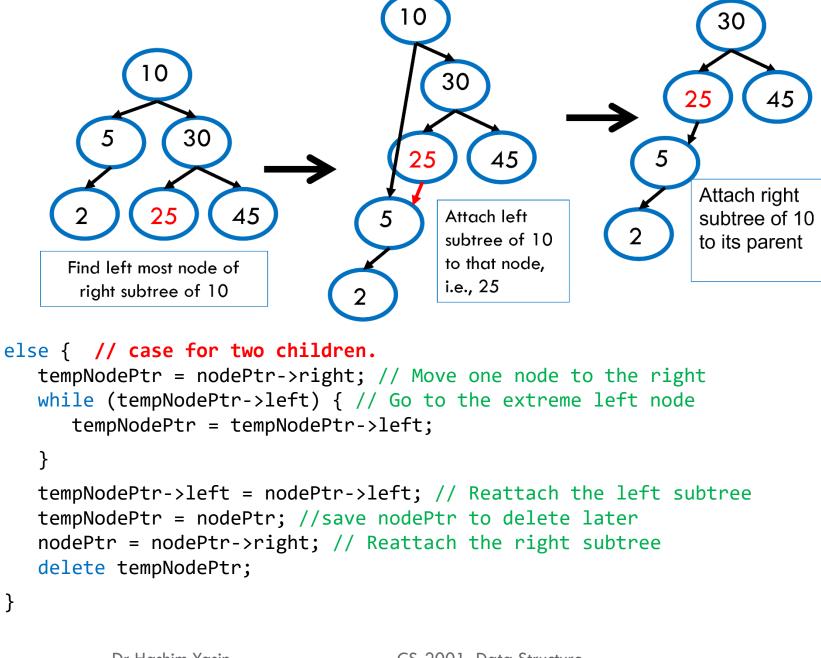
Implementation

```
void IntBinaryTree::deleteNode(int num, TreeNode *&nodePtr) {
   if (nodePtr == NULL) // node does not exist in the tree
        cout << num <<" not found.\n";
   else if (num < nodePtr->value)
        deleteNode(num, nodePtr->left); // find in left subtree
   else if (num > nodePtr->value)
        deleteNode(num, nodePtr->right); // find in right subtree
   else // num == nodePtr->value i.e., node is found
        makeDeletion(nodePtr); // actually deletes node from BST
}
```

Note:

- □ The declaration of the nodePtr parameter: TreeNode *&nodePtr;
- nodePtr is a reference to a pointer to a TreeNode structure
 - Any action performed on nodePtr is actually performed on the argument passed into nodePtr.

```
void IntBinaryTree::makeDeletion(TreeNode *&nodePtr) {
   TreeNode *tempNodePtr; // Temperary pointer
   if (nodePtr->right == NULL) { // case for one (left) child
      tempNodePtr = nodePtr;
      nodePtr = nodePtr->left; // Reattach the left child
      delete tempNodePtr;
   else if (nodePtr->left == NULL) { // case for one (right) child
      tempNodePtr = nodePtr;
      nodePtr = nodePtr->right; // Reattach the right child
      delete tempNodePtr;
   }
   else { // case for two children.
      tempNodePtr = nodePtr->right; // Move one node to the right
      while (tempNodePtr->left) { // Go to the extreme left node
         tempNodePtr = tempNodePtr->left;
      }
      tempNodePtr->left = nodePtr->left; // Reattach the left subtree
      tempNodePtr = nodePtr; //save nodePtr to delete later
      nodePtr = nodePtr->right; // Reattach the right subtree
      delete tempNodePtr;
```

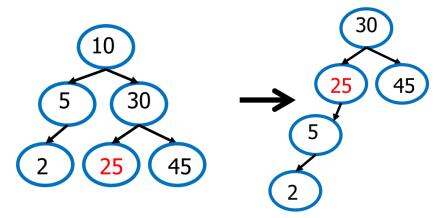


```
// This program builds a binary tree with 5 nodes.
// The DeleteNode function is used to remove two of them.
#include <iostream.h>
#include "IntBinaryTree.h"
void main(void) {
   IntBinaryTree tree;
   cout << "Inserting nodes.\n";</pre>
   tree.insertNode(5);
   tree.insertNode(8);
   tree.insertNode(3);
   tree.insertNode(12);
   tree.insertNode(9);
   cout << "Here are the values in the tree:\n";
   tree.showNodesInOrder();
   cout << "Deleting 8...\n";</pre>
   tree.remove(8);
   cout << "Deleting 12...\n";</pre>
   tree.remove(12);
   cout << "Now, here are the nodes:\n";</pre>
   tree.showNodesInOrder();
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```

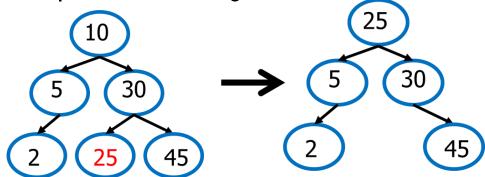
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   tree.remove(12);
   cout << "Now, here are the nodes:\n";</pre>
   tree.showNodesInOrder();
```

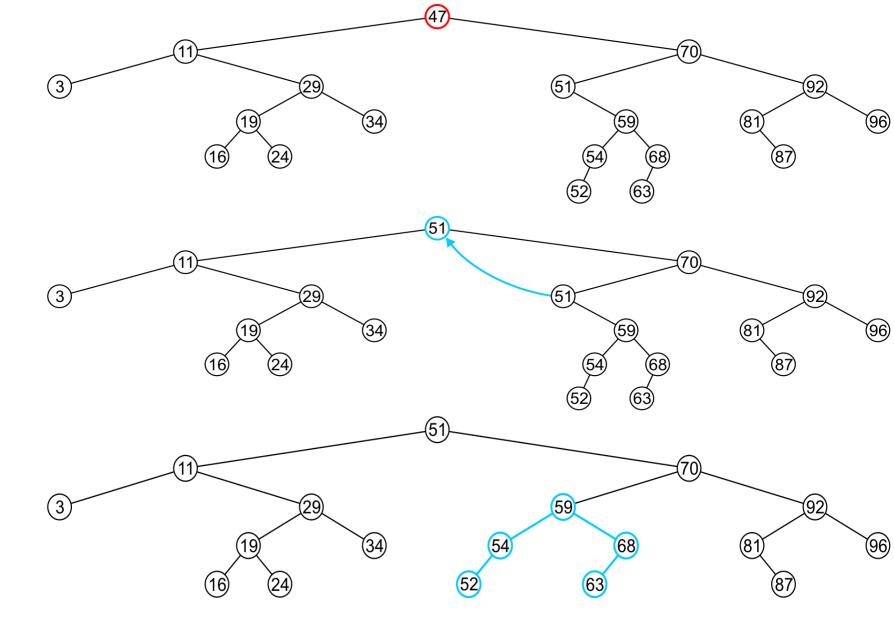
Program Output: Inserting nodes. Here are the values in the tree: 3 8 9 12 Deleting 8... Deleting 12... Now, here are the nodes: 3 5 9

Problem: Height of the BST increases



- □ A better Solution to delete node p with two children
 - Replace node p with the minimum object in the right subtree
 - Delete that object from the right subtree





Reading Materials

- □ Schaum's Outlines: Chapter # 7
- □ D. S. Malik: Chapter # 11
- □ Nell Dale: Chapter # 8
- □ Allen Weiss: Chapter # 4
- □ Tenebaum: Chapter # 5