



CS-2001 DATA STRUCTURE

Dr. Hashim Yasin

National University of Computer and Emerging Sciences,

Faisalabad, Pakistan.

EXPRESSIONS

Expressions

An algebraic expression is a legal combination of operands and the operators.

Operand is the quantity on which a mathematical operation is performed.

Operator is a symbol which signifies a mathematical or logical operation.

Expressions

- INFIX: expressions in which operands surround the operator.
- POSTFIX: operator comes after the operands, also known as Reverse Polish Notation (RPN).
- PREFIX: operator comes before the operands, also Known as Polish notation.

Example

- □ Infix: A+B
- □ Postfix: AB+
- □ Prefix: +AB

Examples

<u>Infix</u>	PostFix	Prefix
A+B	AB+	+AB
(A+B) * (C + D)	AB+CD+*	*+AB+CD
A-B/(C*D^E)	ABCDE^*/-	-A/B*C^DE

INFIX TO POSTFIX CONVERSION

Infix to Postfix ... Algorithm

Algorithm: Q is the given infix expression & we want P.

- 1. Scan Q from left to right and repeat steps 2 to 6 for each element of Q until the STACK is empty.
- 2. If an operand is encountered, add it to P
- If a left parenthesis is encountered, push it onto STACK.
- 4. If an operator X is encountered, then:
 - a. Repeatedly pop from STACK and add to P each operator which has same or higher precedence than X
 - b. Push X on STACK

- 5. If a right parenthesis is encountered, then:
 - a. Repeatedly pop from STACK and add to P each operator until a left parenthesis is encountered
 - b. Remove the left parenthesis. [Do not add it to P]
- 6. Exit

Infix to Postfix ... Examples

```
(((A + B)*(C - E))/(F + G))
```

- □ stack: <empty>
- □ output: [A B + C E * F G + /]

stackVect

infixVect

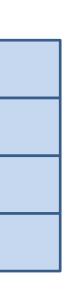
$$(a+b-c)*d-(e+f)$$

postfixVect

$$ab + c - d * ef + -$$

Infix to Postfix ... Examples

Transform Infix to Postfix



 Because the expression is ended, we pop all the operators in the stack

10 2 8 * + 3 -

EVALUATING A POSTFIX EXPRESSION

Evaluating a Postfix Expression

Algorithm: P is the given postfix expression.

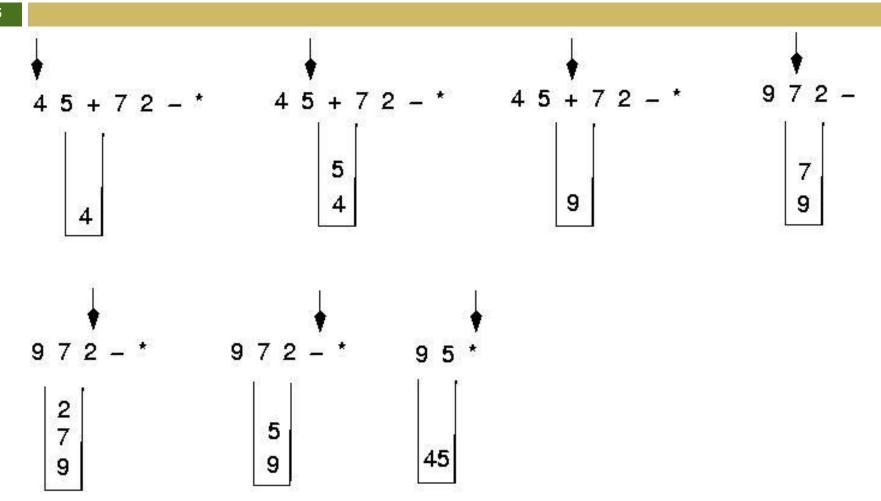
- 1. Scan P from left to right and repeat steps 3 & 4 for each element of P until the sentinel ")" is encountered.
- 2. If an operand is encountered, push it on STACK
- 3. If an operator is encountered, then:
 - a. Pop two operands from STACK: A & B
 - b. Evaluate: A operator B
 - c. Push result on STACK
- 4. Set value equal to the top element on STACK
- 5. Exit

Evaluating a Postfix Expression

```
WHILE more input items exist
  Get an item
  IF item is an operand
   stack.Push(item)
  ELSE
   stack.Pop(operand2)
   stack.Pop(operand1)
   Compute result
   stack.Push(result)
stack.Pop(result)
```

Evaluating a Postfix Expression

15



	3+-382/+*2\$3+				
S.N.	Symbol Scan	Operand 1	Operand 2	Value	STA
1	6				6

S.N.	Symbol Scan	Operand 1	Operand 2	Value	STACK
1.	6				6
2.	2				6,2
3.	3				6,2,3
4.	+	2	3	5	6,5
5.	-	6	5	1	1
		•		•	

P= 623+-382/+*2\$3+

S.N.	Symbol Scan	Operand 1	Operand 2	Value	STACK
1.	6				6
2.	2				6,2
3.	3				6,2,3
4.	+	2	3	5	6,5
5.	-	6	5	1	1

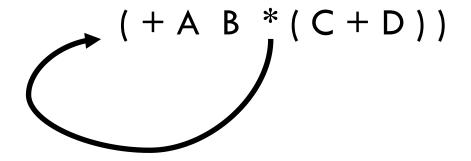


P= 623+-382/+*2\$3+ Operand 1 Operand 2 S.N. Symbol Scan Value STACK 1. 6 2. 6,2 6,2,3 3. 6,5 4. 5. 6 6. 1,3 7. 1,3,8 8. 1,3,8,2 9. 1,3,4 10. 1,7 11. 12. 7,2 49 13. 49 49,3 14. 52 15. 49 52

INFIX TO PREFIX CONVERSION

Move each operator to the left of its operands & remove the parentheses:

Move each operator to the left of its operands & remove the parentheses:



Move each operator to the left of its operands & remove the parentheses:

Move each operator to the left of its operands & remove the parentheses:

$$* + A B + C D$$

Order of operands does not change!

Example; (A-(B/C))*((D*E)-F)

S.N.	Scan symbol	Prefix stack	Opstack
1.))
2.	F	F)
3.	-	F)-
4.)	F)-)
5 .	E	FE)-)
6.	*	FE)-)*
7.	D	FED)-)*
8.	(FED*)-

Next?

Example; (A-(B/C))*((D*E)-F)

S.N.	Scan symbol	Prefix stack	Opstack
1.))
2.	F	F)
3.	-	F)-
4.)	F)-)
5.	E	FE)-)
6.	*	FE)-)*
7 .	D	FED)-)*
8.	(FED*)-
9.	(FED*-	
10.	*	FED*-	*
11.)	FED*-	*)
12.)	FED*-	*))
13.	C	FED*-C	*))
14.	/	FED*-C	*))/
15.	В	FED*-CB	*))/
16.	(FED*-CB/	*)
17.	-	FED*-CB/	*)-
18.	A	FED*-CB/A	*)-
19.	(FED*-CB/A-	*
		FED*-CB/A-*	

Hence, the required prefix expression is *-A/BC-*DEF

EVALUATING A PREFIX EXPRESSION

Evaluation of Prefix Expression

- 1) Read prefix string from right to left until there is a data.
- 2) Repeat;

If char is operand add to prestack

If char is operator

- operand 1= pop prestack.
- operand 2= pop prestack.
- result= value after applying operator between operand
 1 and operand
- push the result into prestack.
- 3) pop prestack get required value.

Tracing +-*+12/421\$42

S.N.	Scan Symbol	Operand 1	Operand 2	Value	Prestack
1. 2. 3. 4. 5.	2 4 \$ 1 2	4	2	16	2 2,4 16 16,1 16,1,2

Mext?

Tracing +-*+12/421\$42 Operand 2 Operand 1 S.N. Scan Symbol Value Prestack 1. 2,4 3. 16 16 4. 5. 6. 16,1 16,1,2 16,1,2,4 7. 8. 16,1,2 16,1,2,2 9. 16,1,2,2,1 10. 16,1,2,3 11. 16,1,6 16,5 12. 6 13. 5 21 16 21

Infix Expression	: A+B*(C^D-E)
------------------	---------------

Reverse Infix expression:)E-D^C(*B+A

Reverse brackets: (E-D^C)*B+A

Token	Action	Result	Stack	Notes		
(Push (to stack		(
E	Add E to the result	E	(
-	Push - to stack	E	(-			
D	Add D to the result	ED	(-			
۸	Push ^ to stack	ED	(- ^			
С	Add C to the result	EDC	(- ^			
	Pop ^ from stack and add to result	EDC^	(-	Do process until (is popped		
)	Pop - from stack and add to result	EDC^-	(from stack		
	Pop (from stack	EDC^-				
*	Push * to stack	EDC^-	*			
В	Add B to the result	EDC^-B	*			
	Pop * from stack and add to result	EDC^-B		has lawer arreadence than A		
+	Push + to stack	EDC^-B*	+	- has lower precedence than ^		
Α	Add A to the result	EDC^-B*A	+			
				Given expression is iterated, do		
	Pop + from stack and add to result	EDC^-B*A+		Process till stack is not Empty, I		
	will give the final result					
	Prefix Expressio	n (Reverse Result): +A*B-^CDE			

POSTFIX TO INFIX CONVERSION

Postfix to Infix ... Algorithm

Iterate the given expression from left to right, one character at a time

- 1. If a character is operand, push it to stack.
- 2. If a character is an operator,
 - 1. pop operand from the stack, say it's s1.
 - 2. pop operand from the stack, say it's s2.
 - 3. perform (s2 operator s1) and push it to stack.
- 3. Once the expression iteration is completed, initialize the result string and pop out from the stack and add it to the result.
- 4. Return the result.

Postfix to Infix ... Examples

Input: Postfix expression: **AB+**

Output: Infix expression- (A + B)

Input: Postfix expression: ABC/-AK/L-*

Output: Infix expression: ((A-(B/C))*((A/K)-L))

Postfix Expression : ABC/-AK/L-* Token Stack Action Notes

Α	Push A to stack	[A]	
В	Push B to stack	[A, B]	
С	Push C to stack	[A, B, C]	
	Pop C from stack	[A, B]	Pop two operands from stack, C
/	Pop B from stack	[A]	and B. Perform B/C and push (B/C)
	Push (B/C) to stack	[A, (B/C)]	to stack

Postfix Expression : ABC/-AK/L-*				
Token	Action	Stack	Notes	
Α	Push A to stack	[A]		
В	Push B to stack	[A, B]		
С	Push C to stack	[A, B, C]		
	Pop C from stack	[A, B]	Pop two operands from stack, C	
/	Pop B from stack	[A]	and B. Perform B/C and push (B/C)	
	Push (B/C) to stack	[A, (B/C)]	to stack	
	Pop (B/C) from stack	[A]	Pop two operands from stack, (B/C)	
-	Pop A from stack	[]	and A. Perform A-(B/C) and push	
	Push (A-(B/C)) to stack	[((A-(B/C))]	(A-(B/C)) to stack	
Α	Push A to stack	[(A-(B/C)), A]		
К	Push K to stack	[(A-(B/C)), A, K]		
	Pop K from stack	[(A-(B/C)), A]	Pop two operands from stack, K	
/	Pop A from stack	[((A-(B/C))]	and A. Perform A/K and push (A/K)	
	Push (A/K) to stack	[(A-(B/C)), (A/K)]	to stack	

Postfix Expression : ABC/-AK/L-*					
Token	Action	Stack	Notes		
Α	Push A to stack	[A]			
В	Push B to stack	[A, B]			
С	Push C to stack	[A, B, C]			
	Pop C from stack	[A, B]	Pop two operands from stack, C		
/	Pop B from stack	[A]	and B. Perform B/C and push (B/C)		
	Push (B/C) to stack	[A, (B/C)]	to stack		
	Pop (B/C) from stack	[A]	Pop two operands from stack, (B/C)		
-	Pop A from stack	[]	and A. Perform A-(B/C) and push		
	Push (A-(B/C)) to stack	[((A-(B/C))]	(A-(B/C)) to stack		
Α	Push A to stack	[(A-(B/C)), A]			
K	Push K to stack	[(A-(B/C)), A, K]			
	Pop K from stack	[(A-(B/C)), A]	Pop two operands from stack, K		
/	Pop A from stack	[((A-(B/C))]	and A. Perform A/K and push (A/K)		
	Push (A/K) to stack	[(A-(B/C)), (A/K)]	to stack		
L	Push L to stack	[(A-(B/C)), (A/K), L]			
	Pop L from stack	[(A-(B/C)), (A/K)]	Pop two operands from stack, L and		
-	Pop (A/K) from stack	[((A-(B/C))]	(A/K). Perform (A/K)-L and push		
	Push ((A/K)-L) to stack	[(A-(B/C)), ((A/K)-L)]	((A/K)-L) to stack		
*	Pop ((A/K)-L) from stack	[((A-(B/C))]	Pop two operands from stack,		
	Pop ((A-(B/C)) from stack	[]	(A/K)-L) and A-(B/C). Perform (A-(B/C))*((A/K)-L) and push		
	Push ((A-(B/C))*((A/K)-L)) to stack	[((A-(B/C))*((A/K)-L))]	((A-(B/C))*((A/K)-L)) to stack		
	Infix Expression: ((A-(B/C))*((A/K)-L))				

POSTFIX TO PREFIX CONVERSION

Postfix to Prefix ... Algorithm

Iterate the given expression from left to right, one character at a time

- 1. If the character is operand, push it to stack.
- 2. If the character is operator,
 - 1. Pop operand from the stack, say it's s1.
 - 2. Pop operand from the stack, say it's s2.
 - 3. perform (operator s2 s1) and push it to stack.
- 3. Once the expression iteration is completed, initialize the result string and pop out from the stack and add it to the result.
- 4. Return the result.

Postfix Expression : ABC/-AK/L-*				
Token	Action	Stack	Notes	
Α	Push A to stack	[A]		
В	Push B to stack	[A, B]		
С	Push C to stack	[A, B, C]		
	Pop C from stack	[A, B]	Pop two operands from	
/	Pop B from stack	[A]	stack, C and B. Perform /BC	
	Push /BC to stack	[A, /BC]	and push /BC to stack	

Token Action Stack Notes A Push A to stack [A] B Push B to stack [A, B] C Push C to stack [A, B, C] Pop C from stack [A, B] Pop two operands from stack, C and B. Perform /BC and push /BC to stack Push /BC to stack [A, BC] Pop two operands from stack, C and push /BC to stack Pop /BC from stack [A] Pop two operands from stack, /BC and A. Perform -A/BC and push -A/BC to stack Push -A/BC to stack [-A/BC, A] Fop two operands from stack K Push K to stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack, K and A. Perform /AI and push /AK to stack	Postfix Expression : ABC/-AK/L-*				
B Push B to stack [A, B] C Push C to stack [A, B, C] Pop C from stack [A, B] Pop two operands from stack, C and B. Perform /BC Push /BC to stack [A, BC] Pop /BC from stack [A, BC] Pop /BC from stack [A] Pop A from stack [A] Pop Two operands from stack, /BC and A. Perform -A/BC and push -A/BC to stack Push A to stack [-A/BC, A] K Push K to stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop K from stack [-A/BC, A] Pop two operands from stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack, K and A. Perform /Al	Token	Action	Stack	Notes	
C Push C to stack [A, B, C] Pop C from stack [A, B] Pop two operands from stack, C and B. Perform /BC and push /BC to stack Push /BC to stack [A, BC] Pop /BC from stack [A, BC] Pop A from stack [A] Pop C from stack [A] Pop two operands from stack, /BC and A. Perform -A/BC and push -A/BC to stack Push A to stack [-A/BC, A] Pop K from stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack, K and A. Perform /AI Stack, K and A. Perform /AI	А	Push A to stack	[A]		
Pop C from stack Pop B from stack Pop B from stack Push /BC to stack Pop /BC from stack Pop A from stack Pop A from stack Push -A/BC to stack Push A to stack Push K to stack Pop K from stack Pop K from stack Pop two operands from stack, /BC and push /BC to stack Pop two operands from stack, /BC and A. Perform -A/BC and push -A/BC to stack [-A/BC] Pop two operands from stack, /BC and push -A/BC to stack [-A/BC, A] Pop K from stack [-A/BC, A, K] Pop K from stack Pop two operands from stack [-A/BC, A, K] Pop two operands from stack [-A/BC, A, K]	В	Push B to stack	[A, B]		
/ Pop B from stack [A] stack, C and B. Perform /BC and push /BC to stack Pop /BC from stack [A] Pop two operands from stack, /BC and A. Perform -A/BC and push -A/BC to stack Push -A/BC to stack [-A/BC] Stack Push A to stack [-A/BC, A] K Push K to stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop K from stack [-A/BC, A] Pop two operands from stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack [-A/BC, A] Pop two operands from stack, K and A. Perform /A/BC to stack, K and A. Perform /A/BC to stack [-A/BC]	С	Push C to stack	[A, B, C]		
/ Pop B from stack [A] stack, C and B. Perform /BC and push /BC to stack Pop /BC from stack [A] Pop two operands from stack, /BC and A. Perform -A/BC and push -A/BC to stack Push -A/BC to stack [-A/BC] A Push A to stack [-A/BC, A] K Push K to stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack, K and A. Perform /A/BC and A. P		Pop C from stack	[A, B]	Pop two operands from	
Pop /BC from stack Pop A from stack Push -A/BC to stack Push A to stack Push K to stack Pop K from stack Pop K from stack Pop A from stack Pop K from stack Pop A from stack Pop K from stack Pop A from stack Pop A from stack Pop K from stack Pop A from stack Pop C from stack Pop two operands from stack, K and A. Perform /Al	/	Pop B from stack	[A]	stack, C and B. Perform /BC	
Pop A from stack Push -A/BC to stack Push A to stack Fush K to stack Pop K from stack Pop A from stack Pop A from stack Pop A from stack Pop B from stack Pop A from stack		Push /BC to stack	[A, /BC]	and push /BC to stack	
Pop A from stack Push -A/BC to stack Push A to stack Fush K to stack Push K to stack Pop K from stack Pop A from stack		Pop /BC from stack	[A]	stack, /BC and A. Perform	
Push -A/BC to stack [-A/BC] stack A Push A to stack [-A/BC, A] K Push K to stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack, K and A. Perform /All stacks.	-	Pop A from stack	[]		
K Push K to stack [-A/BC, A, K] Pop K from stack [-A/BC, A] Pop two operands from stack, K and A. Perform /All stack, K a		Push -A/BC to stack	[-A/BC]		
Pop K from stack [-A/BC, A] Pop two operands from stack [-A/BC] stack, K and A. Perform /Al	Α	Push A to stack	[-A/BC, A]		
/ Pop A from stack [-A/BC] stack, K and A. Perform /Al	К	Push K to stack	[-A/BC, A, K]		
/ Pop A from stack [-A/BC] stack, K and A. Perform /Al		Pop K from stack	[-A/BC, A]	1 op two operands nom	
Push /AK to stack [-A/BC, /AK] and push /AK to stack	/	Pop A from stack	[-A/BC]		
	Γ	Push /AK to stack	[-A/BC, /AK]	and push /AK to stack	

Postfix Expression : ABC/-AK/L-*				
Token	Action	Stack	Notes	
Α	Push A to stack	[A]		
В	Push B to stack	[A, B]		
С	Push C to stack	[A, B, C]		
	Pop C from stack	[A, B]	Pop two operands from	
/	Pop B from stack	[A]	stack, C and B. Perform /BC	
	Push /BC to stack	[A, /BC]	and push /BC to stack	
	Pop /BC from stack	[A]	Pop two operands from	
-	Pop A from stack	[]	stack, /BC and A. Perform -A/BC and push -A/BC to	
	Push -A/BC to stack	[-A/BC]	stack	
Α	Push A to stack	[-A/BC, A]		
K	Push K to stack	[-A/BC, A, K]		
	Pop K from stack	[-A/BC, A]	Pop two operands from	
/	Pop A from stack	[-A/BC]	stack, K and A. Perform /AK	
	Push /AK to stack	[-A/BC, /AK]	and push /AK to stack	
L	Push L to stack	[-A/BC, /AK, L]		
	Pop L from stack	[-A/BC, /AK]	Pop two operands from	
-	Pop /AK from stack	[-A/BC]	stack, L and /AK. Perform /AKL and push -/AKL to stack	
	Push -/AKL to stack	[-A/BC, -/AKL]		
	Pop -/AKL from stack	[-A/BC]	Pop two operands from	
*	Pop -A/BC from stack	[]	stack, -/AKL and -A/BC. Perform *-A/BC-/AKL and	
	Push *-A/BC-/AKL to stack	[*-A/BC-/AKL]	push *-A/BC-/AKL to stack	
	Prefix Expression: *-A/BC-/AKL			

PREFIX TO INFIX CONVERSION

Prefix to Infix ... Algorithm

Iterate the given expression from <u>right to left</u> (in reverse order), one character at a time

- 1. If character is operand, push it to stack.
- 2. If character is operator,
 - pop operand from stack, say it's s1.
 - 2. pop operand from stack, say it's s2.
 - 3. perform (s1 operator s2) and push it to stack.
- 3. Once the expression iteration is completed, initialize result string and pop out from stack and add it to result.
- 4. Return the result.

Prefix Expression: *-A/BC-/AKL

Iterate right to left

Token	Action	Stack	Notes
L	Push L to stack	[L]	
К	Push K to stack	[L, K]	
A	Push A to stack	[L, K, A]	
	Pop A from stack	[L, K]	Pop two operands from stack, A
/	Pop K from stack	[L]	and K. Perform A/K and push (A/K)
	Push (A/K) to stack	[L, (A/K)]	to stack

Prefix Expression: *-A/BC-/AKL

Iterate right to left

Token	Action	Stack	Notes	
L	Push L to stack	[L]		
К	Push K to stack	[L, K]		
Α	Push A to stack	[L, K, A]		
	Pop A from stack	[L, K]	Pop two operands from stack, A	
/	Pop K from stack	[L]	and K. Perform A/K and push (A/I	
	Push (A/K) to stack	[L, (A/K)]	to stack	
	Pop (A/K) from stack	[L]	Pop two operands from stack,	
-	Pop L from stack	0	(A/K) and L. Perform (A/K)-L and	
	Push ((A/K)-L) to stack	[((A/K)-L)]	push ((A/K)-L) to stack	
С	Push C to stack	[((A/K)-L), C]		
В	Push B to stack	[((A/K)-L), C, B]		
	Pop B from stack	[((A/K)-L), C]	Pop two operands from stack, B	
/	Pop C from stack	[((A/K)-L)]	and C. Perform B/C and push (B/C)	
	Push (B/C) to stack	[((A/K)-L), (B/C)]	to stack	

Prefix Expression : *-A/BC-/AKL				
Iterate right to left				
Token	Action	Stack	Notes	
L	Push L to stack	[L]		
K	Push K to stack	[L, K]		
Α	Push A to stack	[L, K, A]		
	Pop A from stack	[L, K]	Pop two operands from stack, A	
/	Pop K from stack	[L]	and K. Perform A/K and push (A/K)	
	Push (A/K) to stack	[L, (A/K)]	to stack	
	Pop (A/K) from stack	[L]	Pop two operands from stack,	
-	Pop L from stack	[]	(A/K) and L. Perform (A/K)-L and	
	Push ((A/K)-L) to stack	[((A/K)-L)]	push ((A/K)-L) to stack	
С	Push C to stack	[((A/K)-L), C]		
В	Push B to stack	[((A/K)-L), C, B]		
	Pop B from stack	[((A/K)-L), C]	Pop two operands from stack, B	
/	Pop C from stack	[((A/K)-L)]	and C. Perform B/C and push (B/C)	
	Push (B/C) to stack	[((A/K)-L), (B/C)]	to stack	
Α	Push A to stack	[((A/K)-L), (B/C), A]		
-	Pop A from stack	[((A/K)-L), (B/C)]	Pop two operands from stack, A	
	Pop (B/C) from stack	[((A/K)-L)]		
	Push (A-(B/C)) to stack	[((A/K)-L), (A-(B/C))]	push (A-(B/C))to stack	
*	Pop (A-(B/C) from stack	[((A/K)-L)]	Pop two operands from stack,	
	Pop ((A/K)-L) from stack	[]	(A-(B/C) and ((A/K)-L). Perform (A-(B/C))*((A/K)-L) and push	
	Push ((A-(B/C))*((A/K)-L)) to stack	[((A-(B/C))*((A/K)-L))]	((A-(B/C))*((A/K)-L)) to stack	
	Infix Expression: ((A-(B/C))*((A/K)-L))			

PREFIX TO POSTFIX CONVERSION

Prefix to Postfix ... Algorithm

Iterate the given expression from right to left, one character at a time

- 1. If the character is operand, push it to the stack.
- 2. If the character is operator,
 - 1. Pop an operand from the stack, say it's s1.
 - 2. Pop an operand from the stack, say it's s2.
 - 3. perform (s1 s2 operator) and push it to stack.
- 3. Once the expression iteration is completed, initialize the result string and pop out from the stack and add it to the result.
- 4. Return the result.

Prefix Expression : *-A/BC-/AKL				
Token	Action	e right to left Stack	Notes	
L	Push L to stack	[L]	Notes	
K	Push K to stack	[L, K]		
A	Push A to stack	[L, K, A]		
	Pop A from stack	[L, K]	Pop two operands from	
/	Pop K from stack	[L]	stack, A and K. Perform Al	
	Push AK/ to stack	[L, AK/]	and push AK/ to stack	

Prefix Expression : *-A/BC-/AKL				
Iterate right to left				
Token	Action	Stack	Notes	
L	Push L to stack	[L]		
K	Push K to stack	[L, K]		
Α	Push A to stack	[L, K, A]		
	Pop A from stack	[L, K]	Pop two operands from	
/	Pop K from stack	[L]	stack, A and K. Perform AK/	
	Push AK/ to stack	[L, AK/]	and push AK/ to stack	
	Pop AK/ from stack	[L]	Pop two operands from	
-	Pop L from stack	[]	stack, AK/ and L. Perform AK/L- and push AK/L- to	
	Push AK/L - to stack	[AK/L-]	stack	
С	Push C to stack	[AK/L-, C]		
В	Push B to stack	[AK/L-, C, B]		
	Pop B from stack	[AK/L-, C]	Pop two operands from	
/	Pop C from stack	[AK/L-]	stack, B and C. Perform BC/	
	Push BC/ to stack	[AK/L-, BC/]	and push BC/ to stack	

Prefix Expression : *-A/BC-/AKL						
	Iterate right to left					
Token	Action	Stack	Notes			
L	Push L to stack	[L]				
K	Push K to stack	[L, K]				
Α	Push A to stack	[L, K, A]				
	Pop A from stack	[L, K]	Pop two operands from			
/	Pop K from stack	[L]	stack, A and K. Perform AK/			
	Push AK/ to stack	[L, AK/]	and push AK/ to stack			
	Pop AK/ from stack	[L]	Pop two operands from			
-	Pop L from stack	[]	stack, AK/ and L. Perform AK/L- and push AK/L- to			
	Push AK/L- to stack	[AK/L-]	stack			
С	Push C to stack	[AK/L-, C]				
В	Push B to stack	[AK/L-, C, B]				
	Pop B from stack	[AK/L-, C]	Pop two operands from			
/	Pop C from stack	[AK/L-]	stack, B and C. Perform BC/			
	Push BC/ to stack	[AK/L-, BC/]	and push BC/ to stack			
Α	Push A to stack	[AK/L-, BC/, A]				
	Pop A from stack	[AK/L-, BC/]	Pop two operands from stack, A and BC/. Perform ABC/- and push ABC/-to stack			
-	Pop BC/ from stack	[AK/L-]				
	Push ABC/- to stack	[AK/L-, ABC/-]				
	Pop ABC/- from stack	[AK/L-]	Pop two operands from			
*	Pop AK/L- from stack	[]	stack, ABC/- and AK/L Perform ABC/-AK/L-* and			
	Push ABC/-AK/L-* to stack	[ABC/-AK/L-*]	push ABC/-AK/L-* to stack			

Postfix Expression: ABC/-AK/L-*

Reading Materials

- □ Nell Dale Chapter#4
- □ Schaum's Outlines Chapter#6
- □ D. S. Malik Chapter#7
- http://www.cs.man.ac.uk/~pjj/cs2121/fix.html
- https://algorithms.tutorialhorizon.com