Flight Delay

The data set provided contains flight details for 5,819,811 flights for the different months of 2014. The features include categorical variables such as Month, Carrier, Origin Airport Id and Destination Airport Id. Ther are ordinal variables such as Day of month, Day of week and cancelled. There also are numeric variables such as Departure delay, carrier delay, weather delay and distance.

```
require(dplyr)
require(gbm)
load(file="2014flights.Rdata")
```

Feature Engineering

We wish to build a model that would predict the delay time of a flight. Hence, we need remove all the cancelled flights as there cannot be any record of a delay linked to those flights. The carrier delay and weather delay have missing values for most of the observations so it s better to drop those features. Our response is the arrival delay as that would be the final delay for the flight. The arrival delay has a few missing values. There could be two possibilities for this. The first being that there was no delay and hence these were left blank, or the delay was not recored at all. The second case seems to be more likely as the flights that had no delay had a value of 0 and the flights that do not have the arrival delay recorded are also mssing the actual elapsed time and the air time. Hence I removed these observations as imputing zeroes here may have resulted in a weaker model.

```
df <- df %>% filter(CANCELLED==0)
#df<-df[,-c(4,6,8,11,12,13,20,24,25,26,27,28,29)]
df<-df[,-c(4,6,8,9,1,12,13,15,16,20,24,28,29)]
df<-na.omit(df)
format(object.size(df),units='MiB')
## [1] "477.5 MiB"

Y<- df$ARR_DELAY
X<- df[-13]</pre>
```

Training and Test set

I split the data into training and testing set for the purpose of getting the estimate of the risk. I split the data randomly in the ration of 70:30.

```
smp_size <- floor(0.7 * nrow(df))

set.seed(123)
train_ind <- sample(seq_len(nrow(df)), size = smp_size)

X_train <- X[train_ind, ]
X_test <- X[-train_ind, ]

Y_train <- Y[train_ind]
Y_test <- Y[-train_ind]</pre>
```

Modelling

I chose the boosting method to generate a predictive model for the follwing reasons. 1] The model can handle more categories than any other modelling technique. 2] I can control the number of iterations easily. 3] The learning rate can be changed to create a model that learns slowly 4] It is easier to utilize all 8 cores of the machine to process in parallel.

An ideal model would be one which would learn slowly over a long perod of time. In other words, a model which has a very low learning rate and a very high number of iterations. This is not possible as we are limited by the computing power available.

Model 1

I started of with a very basic model. This model performs only 10 iterations with a very high learning rate of 1. I used the gaussian distribution in order to get the mean squared error. The model performs a 3 fold cross validation and utilizes all 8 cores of the machine.

At the end of 10 iterations, the model has a training error of 152.023 which is very high but considering the small amount of iterations, is not very surprising. The model provides the departure delay as the most influential feature. It is highly correlated with the arrival delay, which makes sense as the late a flight leaves its place of origin, the more the chances are that it will arrive late at its destination. The other influential variables are the distance, actual time elapsed, carrier and the destination. These are the features that influence the delay time of a flight. The model performs only as well on the test set as it did on the training set with a risk estimate of 152.023

```
> out.boost<- gbm(Y_train~.,data=X_train,
                distribution="gaussian",
                n.trees=10.
                shrinkage=1,
                 interaction.depth=3,
                bag.fraction = 0.5,
                n.minobsinnode = 10.
                 cv.folds = 3,
                 keep.data=TRUE,
                verbose=TRUE,
                n.cores=8)
       TrainDeviance
                       ValidDeviance
                                        StepSize
                                                    Improve
Iter
     1
            380.2851
                                  nan
                                          1.0000 1162.2218
                                           1.0000
     2
            288.8450
                                  nan
                                                    91.2287
     3
            242.9612
                                          1.0000
                                                    44.9896
                                  nan
     4
            211.1285
                                  nan
                                           1.0000
                                                    31.9552
                                                    21.7915
     5
                                          1.0000
            189, 2688
                                  nan
     6
            180.7461
                                  nan
                                          1.0000
                                                     8.3922
     7
            175.1888
                                  nan
                                          1.0000
                                                     5.4617
     8
            170.3177
                                          1,0000
                                                     4.8614
                                  nan
     9
            159.2060
                                          1.0000
                                                    11.0357
                                  nan
   10
                                          1.0000
            152.2414
                                  nan
                                                     6.8032
> boost.sum<-summary(out.boost)
> boost.sum
                                     var
                                              rel.inf
                               DEP_DELAY 98.18396193
DEP_DELAY
DISTANCE
                                DISTANCE 0.97604584
ACTUAL_ELAPSED_TIME ACTUAL_ELAPSED_TIME
                                          0.61932380
CARRIER
                                 CARRIER
                                          0.15151396
                                          0.06915447
DEST
                                    DEST
                                          0.00000000
MONTH
                                   MONTH
DAY_OF_MONTH
                            DAY_OF_MONTH
                                          0.00000000
DAY_OF_WEEK
                             DAY_OF_WEEK
                                          0.00000000
ORIGIN_AIRPORT_ID
                      ORIGIN_AIRPORT_ID 0.00000000
ORIGIN
                                  ORIGIN
                                          0.00000000
DEST_AIRPORT_ID
                         DEST_AIRPORT_ID
                                          0.00000000
DEST_CITY_NAME
                          DEST_CITY_NAME
                                          0.00000000
                                          0.00000000
DEST_STATE_ABR
                          DEST_STATE_ABR
CRS_DEP_TIME
                            CRS_DEP_TIME
                                          0.00000000
AIR_TIME
                                AIR_TIME 0.00000000
> out.boost
gbm(formula = Y_train ~ ., distribution = "qaussian", data = X_train,
    n.trees = 10, interaction.depth = 3, n.minobsinnode = 10,
    shrinkage = 1, bag.fraction = 0.5, cv.folds = 3, keep.data = TRUE,
    verbose = TRUE, n.cores = 8)
A gradient boosted model with gaussian loss function.
10 iterations were performed.
The best cross-validation iteration was 10.
There were 15 predictors of which 5 had non-zero influence.
> best.iter<- gbm.perf(out.boost,method = "cv")</pre>
> f.predict<- predict(out.boost,X_test,best.iter)
> print(mean((Y_test-f.predict)**2))
[1] 152.023
> most.influential = which(names(X_train)%in%boost.sum[1:1,1])
> plot(out.boost,i.var=most.influential)
                1200
              ((DEP_DELAY)
                800
                900
                400
                200
```

500

1000

DEP_DELAY

1500

2000

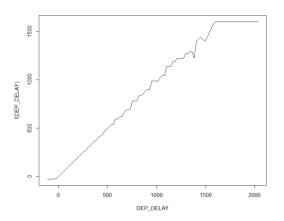
Model 2

The second model I generated performed 300 iterations with a learning rate of 0.5. As expected, the model learns slower than the previous one but the higher number of iterations successfully form a better model than before.

The training error for this model is 144.9521. The most influential feature is the departure delay once again. The other influencial feature include origin, destination, carrier and month. This model performs better on the test set as well with a estimated risk of 145.8233

```
> out.boost<- gbm(Y_train~.,data=X_train,
                distribution="gaussian",
                 n.trees=300,
                shrinkage=0.5,
                 interaction.depth=3,
                bag.fraction = 0.5,
                n.minobsinnode = 10,
                 cv.folds = 3,
                keep.data=TRUE,
                verbose=TRUE,
                n. cores=6)
       TrainDeviance
                       ValidDeviance
                                        StepSize
                                                    Improve
Iter
     1
            670.9827
                                  nan
                                           0.5000 871.7971
     2
            366.3748
                                  nan
                                           0.5000
                                                   301.8876
     3
            253.5090
                                  nan
                                           0.5000
                                                   111.5636
            208.8926
                                           0.5000
                                  nan
                                                    44.6594
                                           0.5000
     5
            191.7110
                                  nan
                                                    16.9631
     6
            184.3492
                                           0.5000
                                                     7.1307
                                  nan
                                           0.5000
                                                     3.8736
     7
            180,4218
                                  nan
     8
            177.3906
                                  nan
                                           0.5000
                                                     2.9145
     9
                                           0.5000
            175.6283
                                  nan
                                                     1.7213
    10
            174.3547
                                           0.5000
                                                     1.2512
                                  nan
    20
            162.1208
                                           0.5000
                                                     0.5619
                                  nan
    40
                                           0.5000
            153.5854
                                                     0.2276
                                  nan
    60
            151.0596
                                  nan
                                           0.5000
                                                     0.1291
    80
            149.2930
                                           0.5000
                                                     0.0655
                                  nan
   100
                                           0.5000
            148,4071
                                  nan
                                                     0.0156
   120
            147.9339
                                           0.5000
                                                     0.0024
                                  nan
   140
            147.3724
                                           0.5000
                                                     0.0113
                                  nan
   160
            146.9384
                                  nan
                                           0.5000
                                                     0.0124
   180
            146.6292
                                           0.5000
                                                    -0.0008
                                  nan
   200
            146.3979
                                  nan
                                           0.5000
                                                    -0.0034
   220
            145.8849
                                  nan
                                           0.5000
                                                     0.0225
                                           0.5000
   240
            145.6933
                                                     0.0034
                                  nan
   260
            145.3223
                                  nan
                                           0.5000
                                                    -0.0018
            145.0609
                                           0.5000
                                                     0.0170
   280
                                  nan
   300
            144.9521
                                  nan
                                           0.5000
                                                    -0.0054
```

```
> summary(out.boost)
                                                   rel.inf
                                          var
                                    DEP_DELAY 98.92904409
DEP_DELAY
ORIGIN
                                       ORIGIN 0.36930104
                                               0.29825246
DEST
                                         DEST
CARRIER
                                               0.26139367
                                      CARRIER
MONTH
                                        MONTH 0.06525464
CRS_DEP_TIME
                                 CRS_DEP_TIME
                                               0.02358437
DAY_OF_WEEK
                                  DAY_OF_WEEK
                                               0.01897030
DAY_OF_MONTH
                                 DAY_OF_MONTH
                                               0.01718767
                                               0.01701176
DEST_CITY_NAME
                              DEST_CITY_NAME
ORIGIN_AIRPORT_ID
                           ORIGIN_AIRPORT_ID
                                               0.00000000
ORIGIN_CITY_MARKET_ID ORIGIN_CITY_MARKET_ID
                                               0.00000000
                             DEST_AIRPORT_ID 0.00000000
DEST_AIRPORT_ID
DEST_AIRPORT_SEQ_ID
                         DEST_AIRPORT_SEQ_ID 0.00000000
DEST_CITY_MARKET_ID
                         DEST_CITY_MARKET_ID
                                               0.00000000
                                               0.00000000
DEST_STATE_ABR
                              DEST_STATE_ABR
> out.boost
gbm(formula = Y_train \sim ., distribution = "gaussian", data = X_train, n.trees = 300, interaction.depth = 3, n.minobsinnode = 10,
    shrinkage = 0.5, bag.fraction = 0.5, cv.folds = 3, keep.data = TRUE,
    verbose = TRUE, n.cores = 6)
A gradient boosted model with gaussian loss function.
300 iterations were performed.
The best cross-validation iteration was 300.
There were 15 predictors of which 9 had non-zero influence.
> best.iter<- gbm.perf(out.boost,method = "cv")
> f.predict<- predict(out.boost,X_test,best.iter)
> print(mean((Y_test-f.predict)**2))
[1] 145.8233
```



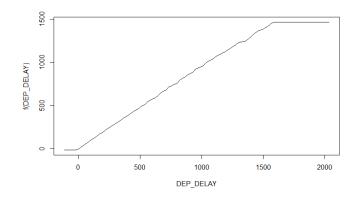
Model 3

This model is close to the kind of model we would look for through the boosting process. It performs 1000 iterations and learns extremely slow with a learning rate of only 0.01

The training error for this model is 108.2119. The most influential feature is the departure delay. Other important features include actual time elapsed, distance, carrier, origin and destination. The estimated risk via this model is 108.4275.

```
> out.boost<- gbm(Y_train~.,data=X_train,
+ distribution="gaussian",
+ n.trees=1000,
+ shrinkage=0.01,
+ interaction.depth=3,</pre>
```

```
bag.fraction = 0.5,
                n.minobsinnode = 10,
                 cv.folds = 3,
                 keep.data=TRUE,
                verbose=TRUE,
                n.cores=8)
                        ValidDeviance
Iter
       TrainDeviance
                                         StepSize
                                                     Improve
   900
            113.8680
                                           0.0100
                                                     0.0519
                                  nan
   920
            112.5226
                                           0.0100
                                                     0.0921
                                  nan
   940
            111.4374
                                  nan
                                           0.0100
                                                     0.0756
            110.4612
   960
                                  nan
                                           0.0100
                                                     0.0558
   980
            109.3279
                                                     0.0505
                                  nan
                                           0.0100
            108.2119
                                                     0.0838
  1000
                                  nan
                                           0.0100
> boost.sum<-summary(out.boost)</pre>
> boost.sum
                                              rel.inf
                                      var
                               DEP_DELAY 96.45393413
DEP_DELAY
ACTUAL_ELAPSED_TIME ACTUAL_ELAPSED_TIME
                                           1.94958108
                                DISTANCE
                                           1.29600429
DISTANCE
                                          0.17870909
CARRIER
                                 CARRIER
ORIGIN
                                  ORIGIN
                                           0.08555602
                                           0.03621540
DEST
                                     DEST
                                    MONTH
                                          0.00000000
MONTH
                            DAY_OF_MONTH
DAY_OF_MONTH
                                           0.00000000
DAY_OF_WEEK
                             DAY_OF_WEEK
                                           0.00000000
                                           0.00000000
ORIGIN_AIRPORT_ID
                       ORIGIN_AIRPORT_ID
                                           0.00000000
                         DEST_AIRPORT_ID
DEST_AIRPORT_ID
                                           0.00000000
DEST_CITY_NAME
                          DEST_CITY_NAME
DEST STATE ABR
                          DEST STATE ABR
                                           0.00000000
                                           0.00000000
CRS_DEP_TIME
                            CRS_DEP_TIME
AIR_TIME
                                AIR_TIME
                                           0.00000000
> best.iter<- gbm.perf(out.boost,method = "cv")</pre>
> f.predict<- predict(out.boost,X_test,best.iter)</pre>
> print(mean((Y_test-f.predict)**2))
[1] 108.4275
> most.influential = which(names(X_train)%in%boost.sum[1:1,1])
> plot(out.boost,i.var=most.influential)
```



So from the three models, we can say that departure delay, actual time elapsed and distance are the three most significant features in predicting the delay time of the flight.