

N-Queens Problem

N=4

Q			
	Q		
		Q	
			Q

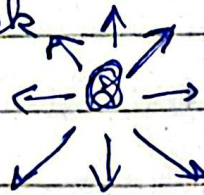
↓

By this arrangement
every row and column
have one
Queen

Rules

- Every row should have Q
- Every column should have one Queen
- None of Queen should attack each other.

A Queen can attack
in 8 direction



But in this case it can
attack so not good arrangement.
So a better arrangements are

①

	Q		
			Q
Q			
		Q	

②

		Q	
Q			
			Q
	Q		

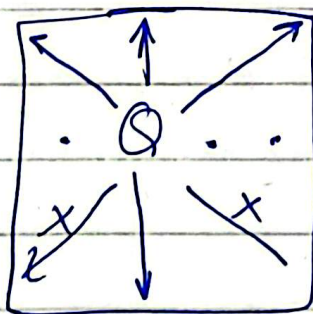
On every function call we
increase row

backtrack (board, row)

and

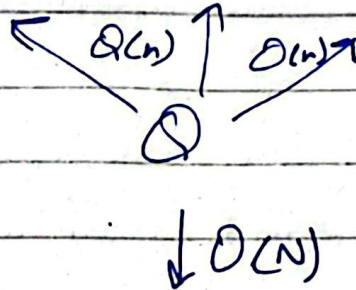
```
for col in range(n);  
    if is-safe (board, row, col):  
        then board = Q  
        backtrack (board, row+1)  
    then board = "."
```

and is-safe is checking
upper left diagonal .
upper right diagonal .
and column



these two not
 cuz we are not
 adding in them
 yet

But it is not efficient
 cuz on every adding of
 Queen



that's why $O(N) + O(N) + O(N)$
 $O(N) * O(N)$

OPTIMIZED SOLUTION:

We can reduce checking again and
 again by having hash sets of
 cols, diag neg, diag pos.

	0	1	2	3	4	5	6	7
0	0	1	2	3	4	5	6	7
1	1	2	3	4	5	6	7	8
2	2	3	4	5	6	7	8	9
3	3	4	5	6	7	8	9	10
4	4	5	6	7	8	9	10	11
5	5	6	7	8	9	10	11	12
6	6	7	8	9	10	11	12	13
7	7	8	9	10	11	12	13	14

as we can see the pattern.
 if

if I place a Queen at
lets say 5 and 7

So $5+7=12$ is added in set
this is for left row and
lower diagonal.
top right to bottom left

for upper diagonal

formula ~~$(r-1) + (c-row)$~~ $(row - col)$

	0	1	2	3	4	5	6	7
0	7	8	9	10	11	12	13	14
1	6	7	8	9	10	11	12	13
2	5	6	7	8	9	10	11	12
3	4	5	6	7	8	9	10	11
4	3	4	5	6	7	8	9	10
5	2	3	4	5	6	7	8	9
6	1	2	3	4	5	6	7	8
7	0	1	2	3	4	5	6	7

let say i fill $board[5][6] = Q$
then instead of checking
all i can just $5-6=1$
which is also $2-1=1$
in set then not safe
same $6-7=1$ is also so the
Queen is not safe if it
is in that block.

Same for row + col

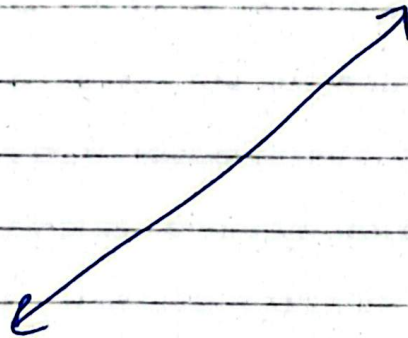
if we see ~~5+7+2~~ then

$$4+4=8$$

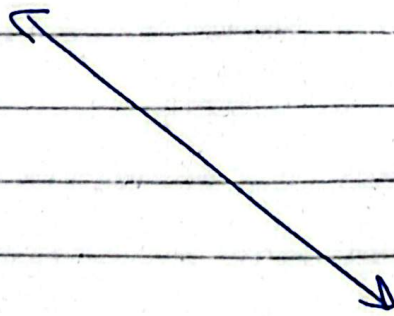
Same as $3+5=8$ same as

$$2+6=8$$

So row + col check



row - col check



and one sel for col

