

K-th Permutation.

Brute force $O(n! \times n)$

We can generate all the permutations then can store them in an array and at $[k-1]$ index we will have answer.

Optimal Solution:

$$n=4 \quad K=17$$

$$\text{if } n=4 \quad n! = 24$$

So there will be 24 sequences.

if we start permutation from

$$\begin{aligned} & \begin{array}{l} \rightarrow 1 + (2, \overset{3!}{3}, 4) \\ \rightarrow 2 + (1, \overset{3!}{3}, 4) \\ \rightarrow 3 + (1, \overset{3!}{2}, 4) \\ \rightarrow 4 + (1, \overset{3!}{2}, 3) \end{array} \left. \vphantom{\begin{array}{l} \rightarrow 1 + (2, \overset{3!}{3}, 4) \\ \rightarrow 2 + (1, \overset{3!}{3}, 4) \\ \rightarrow 3 + (1, \overset{3!}{2}, 4) \\ \rightarrow 4 + (1, \overset{3!}{2}, 3) \end{array}} \right\} 6 \text{ total} \\ & \hspace{15em} = 24 \end{aligned}$$

As

$$n=4, K=17$$

make
an
array

$$(1, 2, 3, 4)$$

0 1 2 3

$$1 + (2, 3, 4) \} 6 \text{ (0-5)}$$

$$2 + (1, 3, 4) \} 6 \text{ (6-11)}$$

$$3 + (1, 2, 4) \} 6 \text{ (12-17)}$$

$$4 + (1, 2, 3) \} 6 \text{ (18-23)}$$

24

first
1, 2, 3, 4 \rightarrow 0

⋮

4, 3, 2, 1 \rightarrow 23th
last

If the question is saying we have to find 17 permutation (16) if 0 based indexing. So we are looking that pair

as we can see first number in 16th permutation is 3 which is $\frac{16}{6} \text{ wants} = 2^{\text{th}}$ total no in a pair

index which is 3

So our sequence is lying in range 12-17 and $\frac{16}{6} = 4^{\text{th}}$ sequence it is

So we select 3
 then find the 4 permutations
 - in (1, 2, 4)
 again

$$\begin{aligned} 1 + [2, 4] &\} 2 \text{ (0-1)} \\ 2 + [1, 4] &\} 2 \text{ (2-3)} \\ \rightarrow 4 + [1, 2] &\} 2 \text{ (4-5)} \end{aligned}$$

Now 6 are total

So

3 4 _ _

Now again

$$K=4$$

$$\frac{4}{2} = 2 \text{ and } 4 \div 2$$

last is selected then

\rightarrow Now 0th permutation as $4 \div 2 = 0$

the 0th
 permutation
 among all
 of these.

$$\begin{aligned} 1 + [2] &\} 1 \text{ (0+0)} \\ 2 + [1] &\} \frac{1}{2} \text{ (1+1)} \end{aligned}$$

$$\text{So } K = \frac{0}{1} = 0$$

$$K \div 1 = 0$$

3 4 1 2 \rightarrow 0th.

cur after select

2 []
nothing left

So the whole algorithm is.

initially we are at 4

~~16 / 4 = 4~~

$24 / 4 = 6 \rightarrow$ a block of 6

$(4-1)! = 3! = 6$

at each point
total = $(n-1)!$
perm

} 6
} 6
} 6 $\leftarrow 16 / 6 = 4$
} 6

and $idx = K // \text{total perm.}$

$= 16 / 6 = 2$

so `num.pop(2)`

and `res.append(nums[idx])`

} 2 $(3-1)!$
} 2 $(0-1)$
} 2 $(2-3)$
} 2 $(4-5)$

} 1
} 1

$$n=4 \quad K=13$$

$$nums = [1, 2, 3, 4]$$

~~fact~~

$$fact = (n-1)!$$

$$idx = K // fact$$

$$res.append(nums[idx])$$

$$nums.pop(idx)$$

$$K \% = fact$$

loop from back

$$i=4$$

$$fact = 3! = 6$$

$$idx = 13 / 6 = 2 \quad K // fact$$

$$res = [3]$$

$$nums = [1, 2, 4]$$

$$K = 1$$

$$i=3$$

$$f = 2$$

$$idx = 1 / 2 = 0$$

$$res = [3, 1]$$

$$nums = [2, 4]$$

$$K = 1 \% 2 = 1$$

$l = 2$

$f = 1$

$idx = 1 // 1 = 1$

$res = [3, 1, 4]$

$num = [2]$

$k = 0$

$i = 1$

$f = 1$

$idx = 0$

$res = [3, 1, 4, 2]$

$num = []$

$k = 0$

What we are doing it
making chunks

then idx to see in which chunks
it falls.

and grab that number first
element then moves on.