

DYNAMIC PROGRAMMING.

Solution ways:

→ Tabulation → Bottom up

→ Memorization → Top - Down

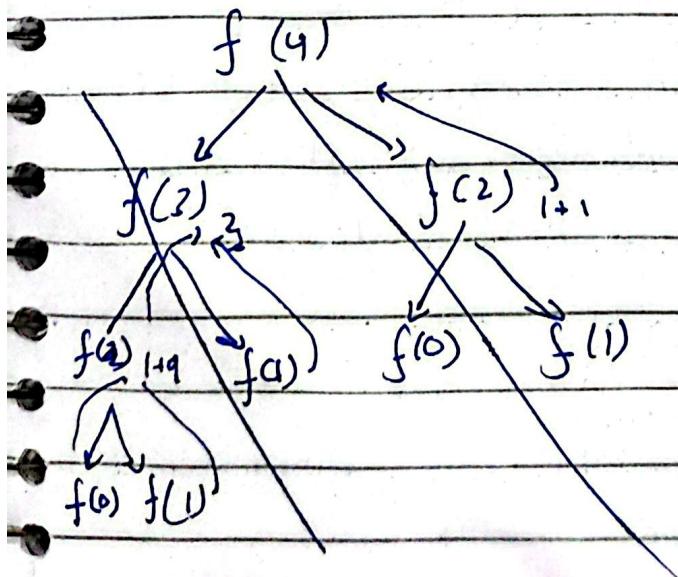
Fibonacci:

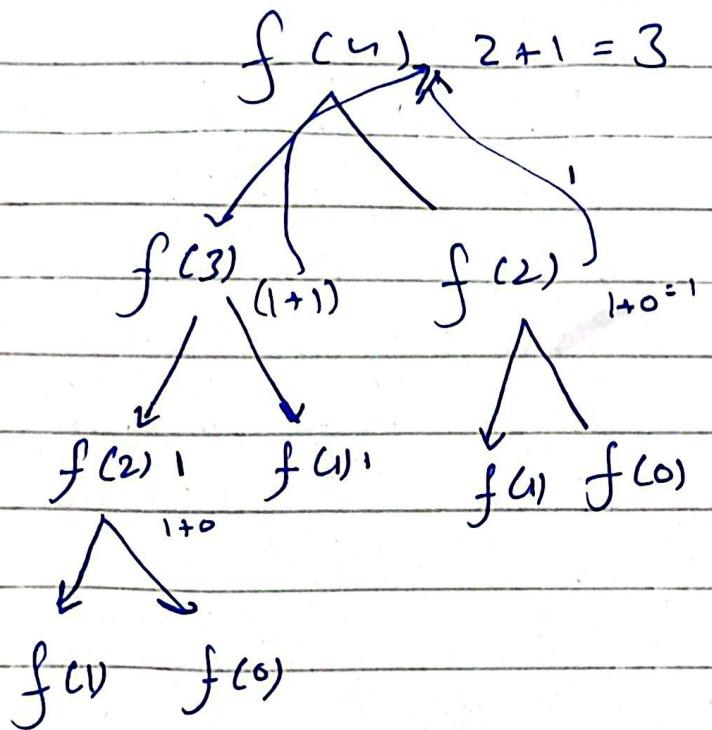
0 1 1 2 3 5 8 13

every number is sum of 2 numbers
before it.

for $f(4) = 3$

code in file to find any number in
fib sequence.





If it is a waste of time in
a. way cuz there is no
need of recomputing $f(2)$ cuz along
the way it is calculated in
the process in left side we should
not recompute it right side again.

So that's called an overlapping subproblem.
this is where memorization jumps in.

Memorization :

tend to store the value
of subproblem in some map/table.

if we create an array and.

$$dp = [\dots]$$

So when $f(2)$ is calculated
it will store

$$dp = [\dots | \dots]$$

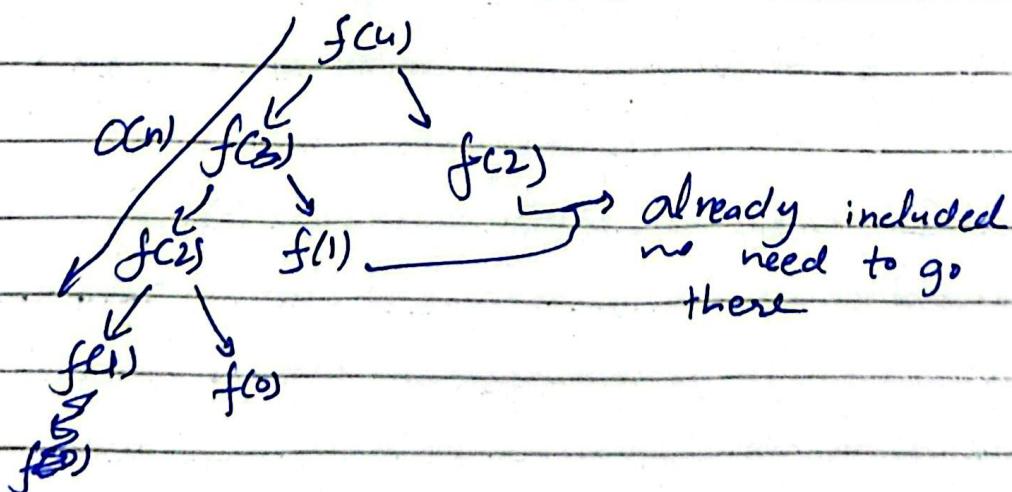
So when next time we are going on
 $f(2)$ it will see if it is already
in the storage.

code in file:

Also

TC is reduced to $O(n)$

as now tree is like



Also

$$SC = DC(n) + DC(n)$$

recursion array
stack.

Recursion → Tabulation. (Bottom-up)
top→(down)

answer
↓
Base case

then come
back

Base case

(to the
required
answer)

in order to convert to tabulation
we do this.

$$\begin{aligned} dp[0] &= 0 \\ dp[1] &= 1 \end{aligned} \quad \left. \right\} \rightarrow \text{base case.}$$

Now from 2nd onward.

for ($i=2 \rightarrow n$) {

$$dp[i] = dp[i-1] + dp[i-2]$$

}

TC $\rightarrow O(N)$

SC $\rightarrow O(N) \rightarrow$ we want to minimize
this as well.

{

for that for any i

$(i-2) \quad (i-1) \quad i$

.. ! ! ..

$i=2 \quad \text{prev2} \quad \text{prev}$

$i=3 \quad \text{prev2} \quad \text{prev}$

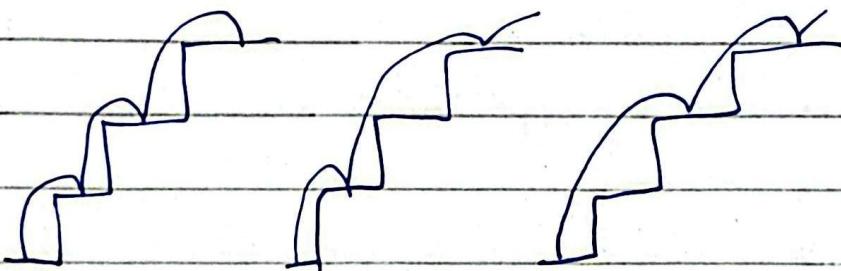
$\text{prev2} \quad \text{prev}$

So we don't need an array as
well we just need two variables
to store prev and prev2.

DP 2 Climbing Problems

Distinct ways to reach n^{th} stair
like

$n=3$



output = 3

initially we are at zero we have to
reach n^{th} stair

1D dp problems:

How do we understand How is this dp
problem?

Problem statements will be like :-

- Count the total no of ways.
- Minimum output.
- Max output.
- try all possible way comes in
- count, best way

That's when we apply recursions.

Short cut trick:

1) try to represent problem in terms of index

2) do all possible stuff on that index according to problem statement

3) Sum of all stuffs \rightarrow count all ways.
 \min (of all stuffs) \rightarrow find min

$f(n) \rightarrow$ no of ways ($0 \rightarrow n$)

$f(\text{idx}) \{$
if ($\text{idx} == 0$) return 1;
if ($\text{idx} == 1$) return 0;

either jump 1 or jump 2

$l = f(\text{idx}-1)$

$r = f(\text{idx}-2)$

return $l+r$;

}

Frog jump

10 20 30 10 $0 \rightarrow 3$
0 1 2 3 index

frog wants to go from 0-3

i+2 or i+1

if $\xrightarrow{10} \xrightarrow{10} \xrightarrow{20} = 40$
10 20 30 10

if $\xrightarrow{10} \xrightarrow{10} = 20 \Rightarrow$ this is min.
10 20 30 10

if $\xrightarrow{20} \xrightarrow{20} = 40$
10 20 30 10

∴

10 20 30 10

As we know if we are trying all ways then its a recursion problem.

So in recursion steps are

- ① express the problem in terms of index
- ② do all possible stuffs on that index
- ③ take minimal of all stuffs.

$f(idx)$

if ($idx == 0$) return 0;

$$l = f(idx-1) + \text{abs}[\text{arr}[i] - \text{arr}[i-1]]$$

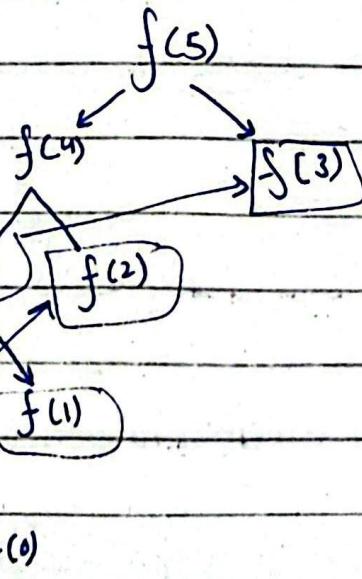
$$\text{if } r = f(idx-2) + \text{abs}[\text{arr}[i] - \text{arr}[i-2]] \\ (\ idx > 1)$$

$$\text{return min}(l, r)$$

Now for Memorization just include

the min for that index

like



if for idx 3 or 2 or 1
we have already
stored min then no
need to go there.

Recurssions to DP steps

Memorization

- ① Look at what parameter is changing.
like idx in the problem.
- ② Before returning add it up
- ③ whenever call a recursion first check
if it is already computed.

As in recursion we were going
top to down.



But in tabulation we do Bottom up

first $dp = [] * n + 1$

Base case $idx = 0$

so

$$dp[0] = 0$$

then

for ($i = 1 \rightarrow n$)

{ first step = $dp[i-1] + \text{abs}(\text{arr}[i-1] - \text{arr}[i])$

if $i > 1$:

$ss = dp[i-2] + \text{abs}(\text{arr}[i-2] - \text{arr}[i-1])$

$dp[i] = \min \{ \text{first}, \text{second} \}$ }

More optimization

$dp1 = 0$

$dp2 = 0$

$i = 1$

10 20 30 10

$curr = 10$ $dp1 = 10$

$dp2 = 0$

10 20 30 10

$dp1 = 10$

$dp2 = 10$

$curr = 10$

10 20 30 10

$dp2 = 10$

$dp1 = 20$

$curr = 20$