

DYNAMIC PROGRAMMING

Solution ways:

- Tabulation → Bottom up
- Memorization → Top-Down

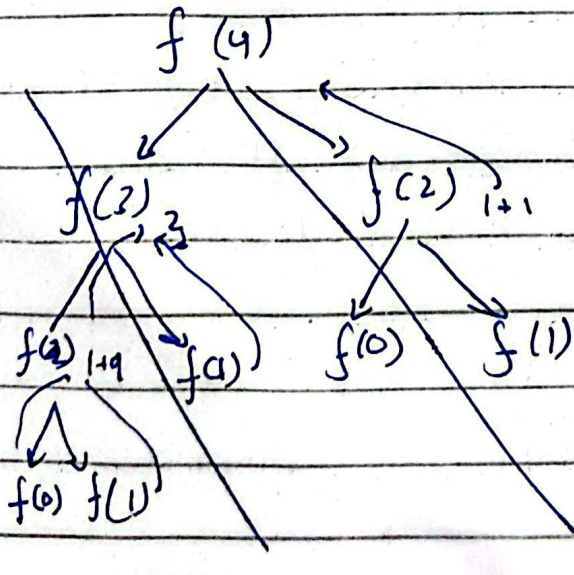
Fibonacci:

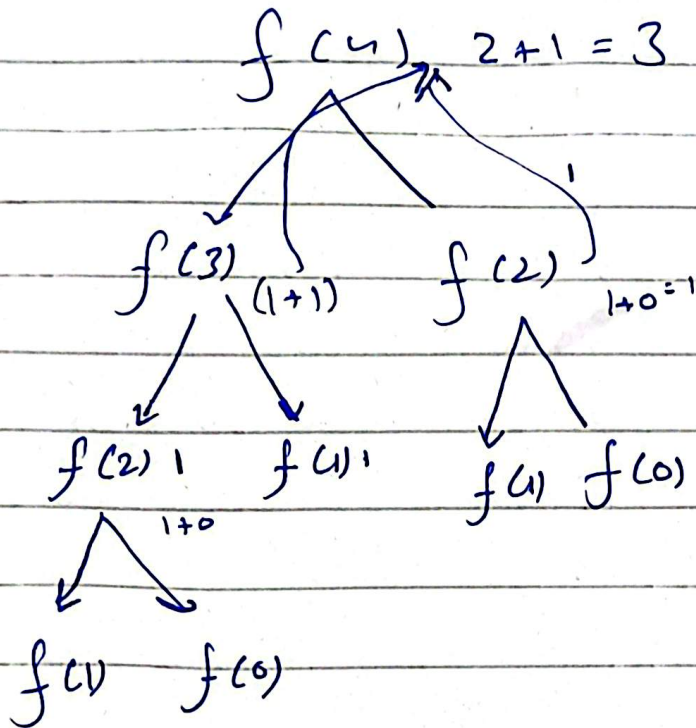
0 1 1 2 3 5 8 13

every number is sum of 2 numbers before it.

for $f(4) = 3$

code in file to find any number in fib sequence.





If is a waste of time in a way cuz there is no need of recompute $f(2)$ cuz along the way it is calculated in the process in left side we should not re compute it right side again.

So that's called an overlapping subproblem. this is where memorization jumps in.

Memorization :

tend to store the value of subproblem in some map/table.

if we create an array and.

$dp = [_ _ _]$

So when $fib(2)$ is calculated
it will store

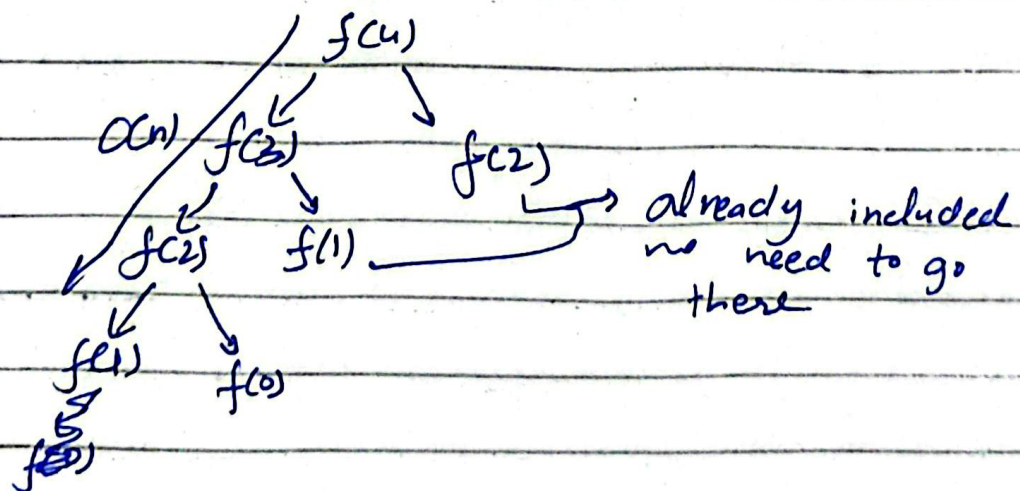
$dp = [_ _ 1 _]$

So when next time we are going on
 $fib(2)$ it will see if it is already
in the storage.

code in file.

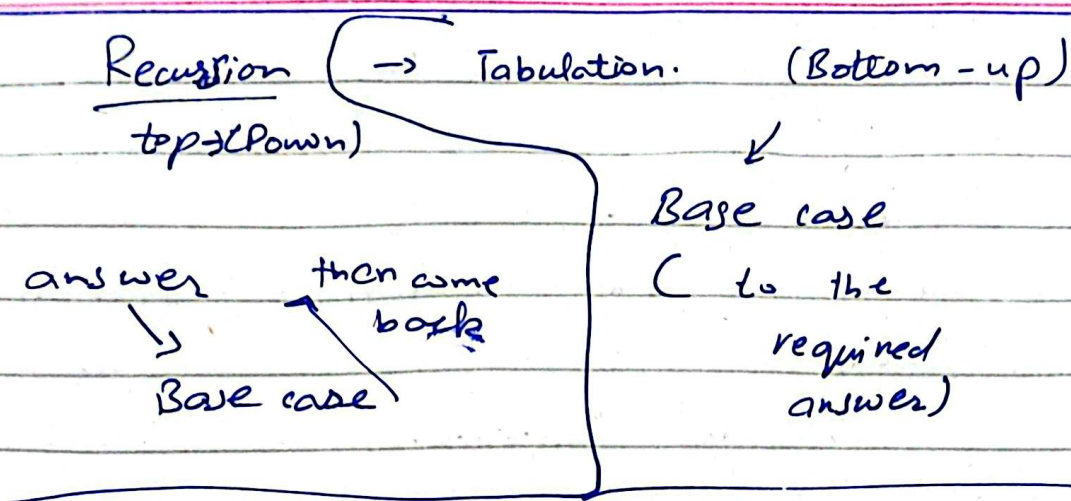
Also

TC is reduced to $O(n)$
cu2 now tree is like



Also

$$SC = \underbrace{O(n)}_{\text{recursion stack}} + \underbrace{O(n)}_{\text{array}}$$



in order to convert to tabulation we do this.

$dp[0] = 0$
 $dp[1] = 1$ } → base case.

Now from 2 and onward.

```
for (i = 2 → n) {  
     $dp[i] = dp[i-1] + dp[i-2]$   
}
```

TC → $O(N)$

SC → $O(N)$ → we want to minimize this as well.

}

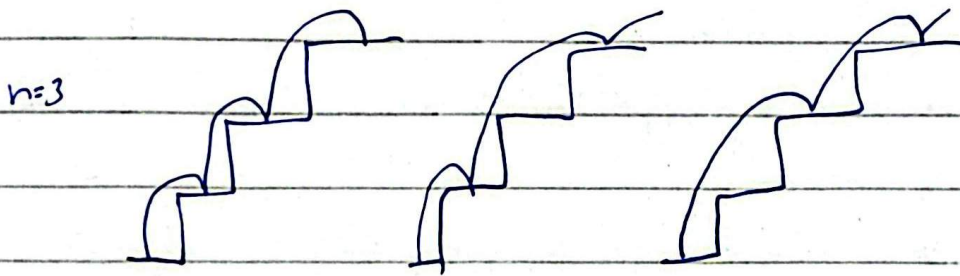
for that for any i

	$(i-2)$	$(i-1)$	i				
	o	o	o	!	!	o	o
$i=2$	prev2	prev					
$i=3$		prev2	prev				
			prev2	prev			

So we don't need an array as well we just need two variables to store prev and prev2.

DP 2 Climbing Problems

Distinct ways to reach n^{th} stair
like



output = 3

initially we are at zero we have to
reach n^{th} stair

1D dp problems:

How do we understand How is this dp
problem?

Problem statements will be like :-

- Count the total no of ways.
- Minimum output.
- Max output.
- try all possible way comes in
- count, best way

That's when we apply recursions.

Short cut tricks:

- 1) try to represent problem in terms of index
- 2) do all possible stuff on that index according to problem statement
- 3) Sum of all stuffs \rightarrow count all ways.
min (of all stuffs) \rightarrow find min

$f(n) \rightarrow$ no of ways ($0 \rightarrow n$)

```
f(idx) {  
    if (idx == 0) return 1;  
    if (idx == 1) return 0;
```

either jump 1 or jump 2

```
    l = f(idx-1)
```

```
    r = f(idx-2)
```

```
    return l+r;
```

```
}
```


Frog jump

10	20	30	10	0-3
0	1	2	3	index

frog wants to go from 0-3

$i+2$ or $i+1$

if $\xrightarrow{10} \xrightarrow{10} \xrightarrow{20} = 40$
10 20 30 10

if $\xrightarrow{10} \xrightarrow{10} = 20 \rightarrow$ this is min.
10 20 30 10

if $\xrightarrow{20} \xrightarrow{20} = 40$
10 20 30 10

if

10 20 30 10

As we know if we are trying all ways then its a recursion problem.

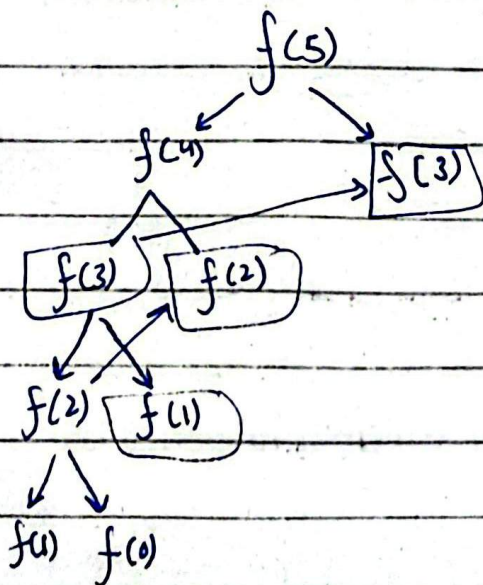
So in recursion steps are

- ① express the problem in terms of index
- ② do all possible stuffs on that index
- ③ take minimal of all stuffs.

$f(idx)$
if $(idx == 0)$ return 0;

$l = f(idx-1) + \text{abs}[arr[i] - arr[i-1]]$
if $(r = f(idx-2) + \text{abs}[arr[i] - arr[i-2]])$
($idx > 1$)
return $\min(l, r)$

Now for Memorization just include
the min for that index
like



if for idx 3 or 2 or 1
we have already
stored min then no
need to go there.

Recursions to DP steps

Memorization

- ① look at what parameter is changing.
like idx in this problem.
- ② Before returning add it up
- ③ whenever call a recursion first check if it is already computed.

As in recursion we were going
top to down.



But in tabulation we do Bottom up

first $dp = [] * n + 1$

Base case $idx == 0$

for

$dp[0] = 0$

then

for $(i = 1 \rightarrow n)$

{ first step = $dp[i-1] + \text{abs}(\text{arr}[i-1] - \text{arr}[i])$

if $i > 1$:

$ss = dp[i-2] + \text{abs}(\text{arr}[i-2] - \text{arr}[i-1])$

$dp[i] = \min(\text{first}, \text{second})$ }

More optimization

$dp1 = 0$

$dp2 = 0$

$i = 1$

10 20 30 10

$curr = 10$ $dp1 = 10$
 $dp2 = 0$

10 20 30 10

$dp1 = 10$

$dp2 = 10$

$curr = 10$

10 20 30 10

$dp2 = 10$

$dp1 = 20$

$curr = 20$