

## N-Queens Problem

$N=4$

Q			
	Q		
		Q	
			Q



By this arrangement  
every row and column  
have one  
Queen

### Rules

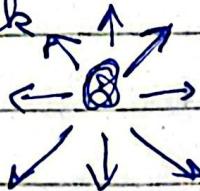
→ Every row should  
have Q

→ Every column  
should have

one Queen

→ None of  
Queens should  
attack each  
other.

A Queen can attack  
in 8 direction



But in this case it can  
attack so not good arrangement.  
So better arrangements are

①

		Q		
			Q	
				Q
	Q			

②

			Q
		Q	
			Q

On every function call we increase row

backtrack (board, row)

and

for col in range(n),

if is-safe (board, row, col),

then board = Q

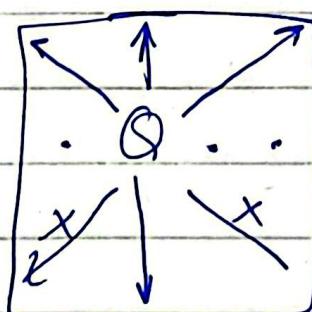
backtrack (board, row+1)

then board = ". "

and is-safe is checking  
upper left diagonal.

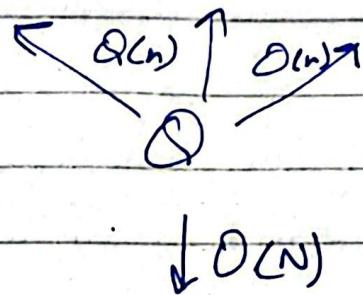
upper right diagonal.

and column



These two not  
cuz we are not  
adding in them  
yet

But it is not efficient  
cuz on every adding of  
Queen



that's why

$$O(N) + O(N) + O(N) \\ O(N) * O(N)$$

## OPTIMIZED SOLUTION:

we can reduce checking again and again by having hash sets of cols, diag neg, diag pos.

	0	1	2	3	4	5	6	7
0	0	1	2	3	4	5	6	7
1	1	2	3	4	5	6	7	8
2	2	1	3	4	5	6	7	9
3	3	4	5	6	7	8	9	10
4	4	5	6	7	8	9	10	11
5	5	6	7	8	9	10	11	12
6	6	7	8	9	10	11	12	13
7	7	8	9	10	11	12	13	14

as we can see the pattern.

if .

if I place a Queen at  
lets say S and T

So  $s_1=12$  is added in set

this is for left row and

# lower diagonal.

top right to bottom left

for upper diagonal

formula ~~(n-1) + (col-row)~~ (row - col)

0	1	2	3	4	5	6	7
1	6	7	8	9	10	11	12
2	5	6	7	8	9	10	11
3	4	5	6	7	8	9	10
4	3	4	5	6	7	8	9
5	2	3	4	5	6	7	8
6	1	2	3	4	5	6	7
7	0	1	2	3	4	5	6

let say I fill board  $[s][s] = Q$

then instead of checking

all I can just  $s-6=1$

which is also  $2-1=1$

in set then not safe

Same  $6-7=1$  is also so the

Queen is not safe if it

is in that block.

Same for row + col

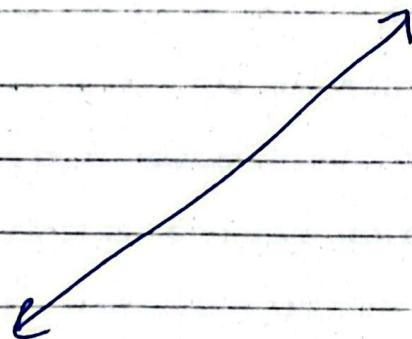
if we see ~~5+7=12~~ then

$$4+4=8$$

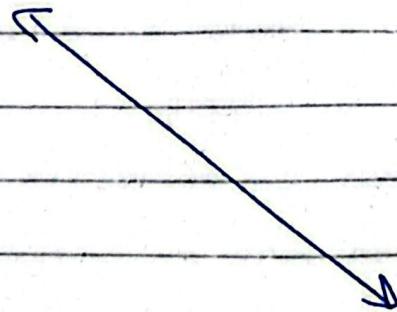
Same as  $3+5=8$  same as

$$2+6=8$$

So row + col check



row - col check



and one sel for col

