

BITWISE OPERATORS:

- AND

a	b	$a \& b$
0	0	0
0	1	0
1	0	0
1	1	1

- OR

a	b	$a b$
0	0	0
0	1	1
1	0	1
1	1	1

NOT:

a	b
0	1
1	0

* Where ever you and 1 by any number it gives that number

1010

1111

1010

② XOR ^

a	b	$a \wedge b$
0	0	0
0	1	0
1	0	0
1	1	1

* only 1 should be true.

* Whenever we XOR any number with 1 we get opposite (NOT) of that number

$$\begin{array}{r} a = 10101 \\ \underline{11111} \\ 01010 \end{array}$$

NOT

$$a \wedge 0 = a$$

$$a \wedge a = 0$$

SHIFT OPERATORS

$$a = 10_{10} = 1010_2 = 10$$

$$a \ll 1 = 0100_2 = 4$$

In formula terms:

if i left shift a $\ll b$ times

the ans = $a * 2^b$

Right SHIFT

$$a = 10_{10} = 1010_{10} \Rightarrow 0101 = 5$$

This is always ignored
in every
number system

$$\text{formula} = a \gg b = \frac{a}{2^b}$$

Problem for finding i th bit:

$n \Rightarrow$ mask with $n-1$ zeros

if $n=4$

the $1 \ll 3$

and

Solution is $n \& (1 \ll (n-1))$.

OR Set the i th bit

Position of right most set bit

Ans = $N \& (-N)$

Negative Numbers in binary

$n = -10$ in binary

suppose = 10 in in one byte

0000 1010
MSB tells us value of number. LSB tells if the number is even or odd.
if number is positive
or negative
1 = negative
0 = positive

To convert a number to negative.

Step 1 : take compliment

Step 2 : add 1 to it

∴ 10 in binary

$$\begin{array}{r} 0000 \cdot 1010 \\ \text{Not 10} = 1111 \cdot 0101 \\ + 1 = \quad \quad \quad 1 \\ \hline (1111 \cdot 0110) \text{ in negative.} \end{array}$$

So

in programming $((\sim \text{number}) + 1)$

Also in 1 byte it can store as high as 128

from -128 to 128

Cuz MSB gives the sign of number.

till 127 Cuz 0. Also - of 0 is also 0 so -128 to 127.

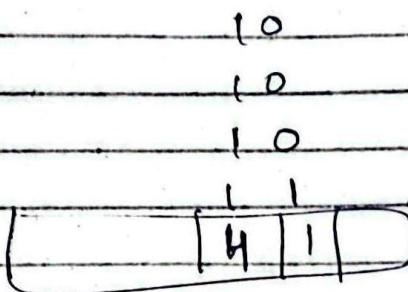
for n bits

$$-2^{n-1} \text{ to } 2^{n-1} - 1 \quad n = \text{no of bits}$$

range of number.

Q: find the no that appeared once
all other are appeared 3 times.

$$arr = [2, 2, 2, 3]$$



if there was no 3 then

$$\begin{array}{|c|c|} \hline 1 & 0 \\ \hline \end{array} \quad \% 3 = 0$$

but in cool of 3

$$\begin{array}{|c|c|} \hline 1 & 0 \\ \hline 1 & 0 \\ \hline 1 & 0 \\ \hline 1 & 1 \\ \hline \end{array} \quad \% 3 = 1$$

\hookrightarrow result = 00000001

we can also use this approach
for K like if K times
appeared.

Pascal triangle Problem:

```
1  
1 1  
1 2 1  
1 3 3 1  
1 4 6 4 1  
1 5 10 10 5 1
```

find the sum of n^{th} row:

Solution ($1 \ll \text{row}$)

Q:

range xor for $(a, b) = \text{xor}(b) \wedge \text{xor}(a-1)$

Q: Prime numbers

2, 3, 5, 7, 13

a number which
is divisible by itself
and only

if 13

only divisible

$\boxed{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13}$

not divisible by them
so if any of them
divide it then not
prime.

we can also move till \sqrt{n}
cuz

if 36 is to check

1	*	36
2	*	18
3	*	12
4	*	9
6	*	6
9	*	4
12	*	3
18	*	2
36	*	1

it is same
so we don't need to

but till $\sqrt{36} + 1$

cuz in range
function last one
is excluded.