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convert following formula to CNF

$$\forall x [\neg \exists z \text{Animal}(z) \wedge \text{kills}(x, z)] \Rightarrow [\forall y \neg \text{loves}(y, x)]$$

i) Eliminate Implication

$$\forall x [\neg \exists z \text{Animal}(z) \wedge \text{kills}(x, z)] \vee \forall y \neg \text{loves}(y, x)$$

ii) move \neg inwards

$$\neg \exists x p \equiv \forall x \neg p$$

$$\forall x [\forall z \neg (\text{Animal}(z) \wedge \text{kills}(x, z))] \vee \forall y \neg \text{loves}(y, x)$$

$$\forall x [\forall z \neg (\text{Animal}(z) \wedge \text{kills}(x, z))] \vee \forall y \neg \text{loves}(y, x)$$

$$\forall y \neg \text{loves}(y, x)$$

iii) Drop universal quantifiers

$$[\neg \text{Animal}(z) \vee \neg \text{kills}(x, z)] \vee \neg \text{loves}(y, x)$$

iv) CNF:-

$$\neg \text{Animal}(z) \vee \neg \text{kills}(x, z) \vee \neg \text{loves}(y, x)$$

Convert the sentences into FOA and prove using resolution.

(i) Cold and precipitation \Rightarrow Snow.

$\text{Cold}(x) \wedge \text{precipitation}(x) \Rightarrow \text{Snow}(x)$

$\neg (\text{Cold}(x) \wedge \text{precipitation}(x)) \vee \text{Snow}(x)$

$\neg \text{Cold}(x) \vee \neg \text{precipitation}(x) \vee \text{Snow}(x)$

(ii) January \rightarrow Cold

$\text{January}(x) \Rightarrow \text{Cold}(x)$

$\neg \text{January}(x) \vee \text{Cold}(x)$

(iii) ~~For~~ Clouds \rightarrow Precipitation.

$\text{clouds}(x) \Rightarrow \text{precipitation}(x)$

$\neg \text{clouds}(x) \vee \text{precipitation}(x)$

(iv) January(x)

(v) Clouds(x)

To prove :- $\text{Snow}(x)$

\rightarrow Resolution of (i) & (ii) (vi) $\neg \text{precipitation}(x) \vee \text{Snow}(x)$

\rightarrow Resolution of vi & iv $\vee \neg \text{Jan}(x)$

(vii) $\neg \text{precipitation}(x) \vee \text{Snow}(x)$

\rightarrow Resolution of (vii) and (iii)

(viii) $\text{Snow}(x) \vee \neg \text{Clouds}$

\rightarrow Resolution of viii and v

$\text{Snow}(x)$

hence proved