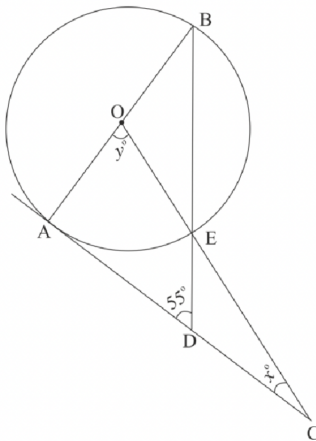


# AI1103 Assignment-1

AI21BTECH11026  
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## 1 QUESTION-7A

- 1.1. In the given figure  $AC$  is a tangent to the circle with centre  $O$ . If  $\angle ADB = 55^\circ$ , find  $x$  and  $y$ . Give reasons for your answers.



then,

$$OB = OE = r$$

Then the length of the chord BE becomes  $2r\cos 35^\circ$ .

Applying 'cosine' rule in  $\triangle BOE$ ,

$$\begin{aligned}(BE)^2 &= (OB)^2 + (OE)^2 - 2(OB)(OE)\cos(\angle BOE) \\ (2r\cos 35^\circ)^2 &= r^2 + r^2 - 2r^2\cos(180 - y) \\ 4r^2\cos^2 35^\circ &= 2r^2 - 2r^2\cos(180 - y) \\ 2\cos^2 35^\circ &= 1 - \cos(180 - y) \\ \cos(180 - y) &= -\cos 70^\circ \quad (\because 1 - \cos^2 \theta = \cos 2\theta) \\ \cos(180 - y) &= \cos(180 - 70) \\ \therefore y &= 70^\circ \\ \therefore x &= 20^\circ \quad (\because x = 90 - y)\end{aligned}$$

**Solution:**

Given,

$$\angle BDA = 55^\circ, \angle OCA = x^\circ, \angle AOC = y^\circ$$

As  $AC$  is a tangent to the given circle,

$$\angle OAC = \angle BAD = 90^\circ$$

Angle Sum Property for  $\triangle OAC$ ,

$$\angle OAC + \angle OCA + \angle AOC = 180^\circ$$

$$90^\circ + x^\circ + y^\circ = 180^\circ$$

$$x^\circ + y^\circ = 90^\circ$$

Angle Sum Property for  $\triangle ABD$ ,

$$\angle ABD + \angle BAD + \angle BDA = 180^\circ$$

$$\angle ABD + 90^\circ + 55^\circ = 180^\circ$$

$$\angle ABD = 35^\circ$$

$$\angle BOE + y^\circ = 180^\circ$$

$$\angle BOE = 180 - y$$

Let the radius of the circle be ' $r$ '.