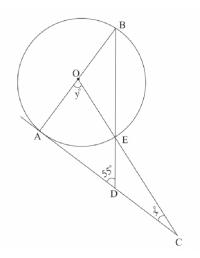
1

AI1103 Assignment-1 Class 10 ICSE-2019

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Question 7(a)

In the given figure AC is a tangent to the circle with centre O. If $\angle ADB = 55^{\circ}$, find x and y. Give reasons for your answers.



Solution:

Given,

$$\angle BDA = 55^{\circ}, \angle OCA = x^{\circ}, \angle AOC = y^{\circ}$$

As AC is a tangent to the given circle, $\angle OAC = \angle BAD = 90^{\circ}$

Angle Sum Property for $\triangle OAC$,

$$\angle OAC + \angle OCA + \angle AOC = 180^{\circ}$$
 (1)

$$90^{\circ} + x^{\circ} + y^{\circ} = 180^{\circ}$$
 (2)

$$x^{\circ} + y^{\circ} = 90^{\circ} \qquad (3)$$

Angle Sum Property for $\triangle ABD$,

$$\angle ABD + \angle BAD + \angle BDA = 180^{\circ}$$
 (4)

$$\angle ABD + 90^{\circ} + 55^{\circ} = 180^{\circ}$$
 (5)

$$\angle ABD = 35^{\circ}$$
 (6)

As AB is a straight line,

$$\angle BOE + y^{\circ} = 180^{\circ} \tag{7}$$

$$\angle BOE = 180 - y \tag{8}$$

Let the radius of the circle be r. then,

$$\implies OB = OE = r$$

Then the length of the chord BE becomes $2rcos35^{\circ}$.

Applying 'cosine' rule in $\triangle BOE$,

$$BE^{2} = OB^{2} + OE^{2} - 2(OB)(OE)cos(\angle BOE)$$
(9)

$$(2rcos35)^2 = r^2 + r^2 - 2r^2cos(180 - y)$$
(10)

$$4r^2cos^235 = 2r^2 - 2r^2cos(180 - y)$$
 (11)

$$2\cos^2 35 = 1 - \cos(180 - y) \tag{12}$$

$$\cos(180 - y) = -\cos 70\tag{13}$$

$$(: 1 - \cos^2\theta = \cos 2\theta) \tag{14}$$

$$cos(180 - y) = cos(180 - 70) \tag{15}$$

$$\implies y = 70^{\circ} \tag{16}$$

$$\implies x = 20^{\circ}$$
 (17)