

# ASSIGNMENT-2 : ICSE 12,2019

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## PROBLEM 8-A :

Evaluate :

$$\int \frac{x(1+x^2)}{1+x^4} dx$$

**Solution:**

Let

$$x^2 = t \quad (1)$$

$$\implies 2x dx = dt \quad (2)$$

$$\implies x dx = \frac{dt}{2} \quad (3)$$

From (1) and (3),

$$\int \frac{x(1+x^2)}{1+x^4} dx = \int \frac{(1+t)}{2(1+t^2)} dt \quad (4)$$

$$\int \frac{(1+t)}{2(1+t^2)} dt = \frac{1}{2} \int \frac{1}{1+t^2} dt + \frac{1}{2} \int \frac{t}{1+t^2} dt \quad (5)$$

$$= \frac{1}{2} \tan^{-1}(t) + \frac{1}{2} \int \frac{t}{1+t^2} dt + C_1 \quad (6)$$

$$\therefore \int \frac{1}{1+x^2} dx = \tan^{-1}(x) + C$$

Let

$$1+t^2 = z \quad (7)$$

$$\implies 2t dt = dz \quad (8)$$

$$\implies t dt = \frac{dz}{2} \quad (9)$$

From (7) and (9)

$$\int \frac{t}{1+t^2} dt = \frac{1}{2} \int \frac{dz}{z} \quad (10)$$

$$= \frac{1}{2} \ln z \quad (11)$$

$$\therefore \int \frac{dx}{x} = \ln x + C$$

From (1), (6), (7) and (11)

$$\int \frac{x(1+x^2)}{1+x^4} dx = \frac{1}{2} \tan^{-1}(x^2) + \frac{1}{4} \ln(1+x^4) \quad (12)$$