

# IOITC 2019

## Team Selection Test 1

### Figure 8

A *Figure – 8* consists of 2 convex polygons which share a single common edge. Apart from this shared edge (and the 2 common vertices), they do not share anything else, and they do not intersect or touch with each other anywhere else. The areas that they enclose should also be disjoint. The 2 convex polygons which constitute the Figure-8 should both have at least 3 vertices each, of which 2 are common.

You are given  $N$  distinct points in the 2d plane such that no three points are collinear. You need to construct a Figure-8 which has each of its vertices as one of the  $N$  given points, and which encloses all the  $N$  points. That is, each of the  $N$  points, should either be a vertex of the Figure-8, or should be inside it. And you want to construct this in such a way, that the number of points from among the  $N$  points, which are on the boundary of the Figure-8 is maximized. Output this maximum number possible.

### Input

- The first line contains a single integer,  $T$ , which denotes the number of testcases. The description of each testcase follows.
- The first line of each testcase contains a single integer,  $N$ , which denotes the number of points.
- The  $i^{th}$  of the next  $N$  lines contains two space-separated integers,  $x_i$  and  $y_i$ . This denotes the coordinates of the  $i^{th}$  point.

### Output

For each testcase, output a single integer in a new line, which should denote the maximum number of points on the boundary of a valid Figure-8.

### Constraints

- $-10^5 \leq x_i, y_i \leq 10^5$
- No two points in a single testcase will be the same.
- No three points in a single testcase will be collinear.

### Subtasks

- Subtask 1: 32%:  $1 \leq T \leq 10$  and  $4 \leq N \leq 50$
- Subtask 2: 68%:  $T = 1$  and  $4 \leq N \leq 400$

### Sample Input 1

```
1
4
3 4
6 7
4 1
9 5
```

### Sample Output 1

4

### Explanation 1

There are 2 valid Figure-8s possible in this case. One possibility, which is shown in the image below, is to have the convex polygons  $P_1P_2P_3$  and  $P_2P_4P_3$ , which have the edge  $P_2P_3$  in common. Or you could also have the Figure-8 which consists of the two polygons  $P_1P_2P_4$  and  $P_1P_3P_4$ . In both the cases, all the 4 points are on the boundary of the Figure-8, and hence the maximum is 4, which is the answer.

