IOITC 2019 Team Selection Test 2

Check SCC v2.0

The jury has a hidden directed graph G. It has N nodes which are numbered from 1 to N. Your job is to figure out whether it is strongly connected ¹. You can ask queries of the following type:

• Give two disjoint subsets A and B of the vertex set. The jury will tell you whether there is at least one edge going from a vertex of A to a vertex of B in G.

Interaction Protocol

You can ask at most Q queries of the kind described above (see subtasks section for value of Q). To interact with the jury, you have two options:

Use the supplied contestant.cpp file

You have to implement the function solve. To ask questions, call the function query with two std::vector arguments -A and B respectively. The call will return True if there is an edge from A to B, and False otherwise. If you exceed the query limit, the call will terminate your program gracefully.

When you think you have the answer, return from solve with True if you believe G is strongly connected, and False otherwise.

Directly interact with stdin/stdout

You should read N, the number of vertices in G.

To ask a query, print the alphabet Q. Then in the next line print the size of A, followed by the elements of A in another line. Then do the same for B. After printing your query please flush the output with either std::cout << std::flush;, std::cout << std::endl, or fflush(stdout);

The jury will respond with 1 if there is an edge from A to B, 0 if there isn't, or -1 if something is wrong ie.

- You asked too many queries.
- Your query doesn't follow the format described above.

In either case, your program should terminate gracefully to receive a useful WA verdict.

This response of the jury should be inputted from stdin (eg. using cin).

To print the final answer, print the letter A followed by a space, and then YES if you believe G is strongly connected, and NO otherwise. This does not count towards the query limit. After you print this, please terminate gracefully.

Constraints

- $2 \le N \le 128$
- G does not have self-loops, but it may have anti-parallel edges (ie. (u, v) and (v, u) might both be edges of G).

¹A directed graph G is strongly connected if for every pair of vertices u and v there exists a path from u to v and there exists a path from v to u

Subtasks

(Q denotes the query-limit)

• Subtask 1: 6%: $N \le 64$ and Q = 4200.

• Subtask 2: 43%: Q = 3600.

• Subtask 3: 22%: Q = 2019.

• Subtask 4: 29%: Q = 1800.

Sample

(Note that the dotted lines are for clarity, and will not exist in actual interaction)

| 6 | | | | |
|---|---|---|---|---|
| | Q | | | |
| | 3 | | | |
| | 1 | 2 | 3 | |
| | 3 | | | |
| | 4 | 5 | 6 | |
| 1 | | | | |
| | Q | | | |
| | 4 | | | |
| | | | 2 | 6 |
| | 1 | 2 | 3 | |
| | 2 | | 3 | |
| | | | 3 | |
| 0 | 2 | | 3 | |

Explanation

The digraph corresponding to the interaction above:

