

## EE 343 Problem Set 6

1. **9.4-1** Two independent random voltage processes  $x_1(t)$  and  $x_2(t)$  are applied to an RC network, as shown in figure 9.14. The two random noise processes have the following PSD:

$$S_{x_1} = \frac{2\alpha}{\alpha^2 + (j2\pi f)^2} \quad S_{x_2} = K$$

Find the PSD and the power  $P_y$  of the output random process  $y(t)$ .



- **11.1-4** An alternative to the optimum filter is a suboptimum filter, where we assume a particular filter form and adjust its parameters to maximize  $\rho$ . Such filters are inferior to the optimum filter but may be simpler to design.

For a rectangular pulse  $p(t)$  of height  $A$  and width  $T_b$  at the input, determine  $\rho_{max}$  if, instead of the matched filter, a one-stage RC filter with  $H(\omega) = 1/(1 + j\omega RC)$  is used. Assume a white Gaussian noise of PSD  $N/2$ . Show that the optimum performance is achieved when  $1/RC = 1.26/T_b$ .

*Hint:* Set  $d\rho^2/dx = 0(x = T_b/RC)$ .

2. Let  $X_1$  and  $X_2$  be iid Gaussian random variables with mean 0 and variance 1.
- (a) Let  $Y_1 = X_1 - 2X_2 + 1$  and  $Y_2 = 2X_1 + X_2 - 1$ . Find the  $E(Y_1)$ ,  $E(Y_2)$ ,  $VAR(Y_1)$ ,  $VAR(Y_2)$ , and the  $COV(Y_1, Y_2)$ .
  - (b) Find the joint pdf of  $Y_1$  and  $Y_2$ . What type of random vector is this?
  - (c) Find a linear transformation of  $Y_1$  and  $Y_2$  to produce  $Z_1$  and  $Z_2$  that are iid

Gaussian random variables with mean 0 and variance 1.

(d) Implement the random variables in a) -c) on MATLAB. Find the sample means, variances, and covariances. Is the transformation unique?

3.