## 1 | THE EXTERNAL CORE MODEL IN-DUCTION

In this section we will prove the following unpublished theorem by Woodin.

**Theorem 1.0.1** (Woodin). Assume  $ZF + AD_{\mathbb{R}} + \Theta$  is regular. Then there is a generic extension of V satisfying  $DI^+$ .

Have a look at Trevor's thesis; he's doing something similar.

Assume thus that  $\mathsf{ZF} + \mathsf{AD}_{\mathbb{R}} + \Theta$  is regular.

Missing proof.