

به نام خدا



تمرین 5 طراحی زبان

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$$(\text{value-of } \text{exp1 } e \text{ s0}) = (l, s1)$$

$$(\text{value-of } \text{exp2 } e \text{ s1}) = (\text{val}, s2)$$

$$(\text{value-of } (\text{setref-exp } \text{exp1 } \text{exp2}) e \text{ s0}) = (\text{val}, [l=\text{val}]s2)$$

$$(\text{value-of } \text{exp1 } e \text{ s0}) = (l, s1)$$

$$(\text{value-of } (\text{deref-exp } \text{exp1}) e \text{ s0}) = (l, s1)$$

$$(\text{value-of } \text{exp1 } e \text{ s0}) = (\text{val}, s1)$$

$$(\text{value-of } (\text{newref-exp } \text{exp1}) e \text{ s0}) = (\text{ref-val}, [l=\text{val}]s1)$$

```
#lang racket
```

```
(define value-of
```

```
  (lambda (exp env)
```

```
    (cases expression exp
```

```
      (newref-exp (exp1)
```

```
        (let ((v1 (value-of exp1 env)))
```

```
          (ref-val (newref v1))))
```

```
      (deref-exp (exp1)
```

```
        (let ((v1 (value-of exp1 env)))
```

```
          (let ((ref1 (expval->ref v1)))
```

```
            (deref ref1))))
```

```
      (setref-exp (exp1 exp2)
```

```
        (let ((ref (expval->ref (value-of exp1 env))))
```

```
      (let ((val2 (value-of exp2 env)))
        (begin
          (setref! ref val2)
          val2))))
  )))
```

```
(define the-grammar
  '((program (expression) a-program)
    (expression("newref" "(" expression ")")newref-exp)
    (expression ("deref" "(" expression ")")deref-exp)
    (expression("setref" "(" expression "," expression ")")setref-exp)
  ))
```

```
(define-datatype expval expval?
  (ref-val
    (ref reference?))
```

```
(define-datatype expression expression?
  (newref-exp(exp1 expression?))
  (deref-exp(exp1 expression?))
  (setref-exp
    (exp1 expression?)
    (exp2 expression?)))
```

```
(define expval->ref
  (lambda (val)
```

```

(cases expval val
  (ref-val (ref) ref)
  (else (report-expval-extractor-error 'reference val))))

```

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Begin-end

```

(value-of exp0 e s0) = (val0, s1)
(value-of exp1 e s1) = (val1, s2)
...
(value-of expn e sn) = (valn, sn+1)

```

$(\text{value-of } (\text{begin-exp } (\text{exp0}, \text{exp1}, \dots, \text{expn})), e, s0) = (\text{valn}, \text{sn}+1)$

list

```

(value-of exp0 e s0) = (val0, s1)
(value-of exp1 e s1) = (val1, s2)
...
(value-of expn e sn) = (valn, sn+1)

```

$(\text{value-of } (\text{list-exp } (\text{exp0}, \text{exp1}, \dots, \text{expn})), e, s0)$
 $= ((\text{val0}, \text{val1}, \dots, \text{valn}), \text{sn}+1)$

New-list

$(\text{value-of } \text{exp1 } e \text{ } s0) = (\text{val}, s1)$

$(\text{value-of } (\text{newlist-exp } \text{exp1}) e \text{ } s0) = (\text{num-val}, s1)$

Get-list

```

(value-of exp1 e s0) = (val0, s1)
(value-of exp2 e s1) = (val1, s2)

```

$(\text{value-of } (\text{getlist-exp } \text{exp1 } \text{exp2}) e \text{ } s0) = ((\text{val0}, \text{val1}), s2)$

Set-list

(value-of exp1 e s0) = (val0, s1)

(value-of exp2 e s1) = (val1, s2)

(value-of exp3 e s2) = (val2, s3)

(value-of (setlist-exp exp1 exp2 exp3) e s0) = ((val0, val1, val2), s2)

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#lang racket

(define value-of

 (lambda (exp env)

 (cases expression exp

 (begin-exp (exp1 exps)

 (letrec

 ((value-of-begins

 (lambda (e1 es)

 (let ((v1 (value-of e1 env)))

 (if (null? es)

 v1

 (value-of-begins (car es) (cdr es))))))

 (value-of-begins exp1 exps)))

(setlist-exp (exps1 exps2 exps3)//list index value

 (if (null? exps)

 (list-val '())

 (list-val

 (append (exp3 (list (value-of (car exps1) env))

```

        (list (value-of (list-exp (cdr exps1))env))))))
(newlist-exp (exp1)
  (let ((val1 (value-of exp1 env)))
    (let ((num1 (expval->num val1))))))
(get-list-exp (exp exp2)
  (let ([l (value-of exp env store)])
    (let ([i (value-of exp2 env (car l))])
      (list-ref (expval->exp (cadr l))(expval->int (cadr i))))))
)))

```

(define the-grammar

```

'((program (expression) a-program)
  (expression ("begin" expression (arbno ";" expression) "end")begin-exp)
  [expression ("newlist" "(" expression ")") newlist-exp]
  (expression ("getlist" "(" expression "," expression ")") getlist-exp)
  (expression ("setlist" "(" expression "," expression "," expression ")") setlist-exp)
))

```

(define-datatype expression expression?

```

(begin-exp(exp1 expression?)(exps (list-of expression?)))
(newlist-exp(size number?))
(getlist-exp(exp1 expression?)(exp2 expression?))
(setlist-exp(exp1 expression?)(exp2 expression?) (exp3 expression?))
)

```

```

(define expval->list
  (lambda (val)
    (cases expval val
      (bool-val (lst) lst)
      (else (report-expval-extractor-error 'list val))))))

```

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```

#lang racket

(define the-grammar
  '((program (expression) a-program)
    (expression("(" expression expression ")")call-exp)
    (expression("letrec"(arbno identifier "(" identifier ")" "=" expression)"in" expression)letrec-
exp)
  ))

```

```

(define value-of
  (lambda (exp env)
    (cases expression exp
      (call-exp (rator rand)
        (let ((proc (expval->proc (value-of rator env)))
              (arg (value-of rand env)))
          (apply-procedure proc arg)))
      (letrec-exp (proc-names bound-vars proc-bodies letrec-body)
        (value-of letrec-body
          (extend-env-rec*
            proc-names bound-vars proc-bodies env))))))

```

)))

(define-datatype environment environment?

(empty-env)

(extend-env(saved-var symbol?) (saved-ref reference?) (saved-env environment?))

(extend-env-rec*

(p-names (list-of identifier?))(b-vars (list-of identifier?))(bodies (list-of expression?))(saved-env environment?)))

(define-datatype expression expression?

(call-exp

(rator expression?)(rand expression?))

(letrec-exp

(proc-names (list-of identifier?))(bound-vars (list-of identifier?))(proc-bodies (list-of expression?))(letrec-body expression?))

)

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(6

توابع bool و Zero برای بول استفاده میشوند.

#lang racket

(define type-of

(lambda (exp tenv)

(cases expression exp


```

[zero?-exp (exp1) (let ([ty1 (type-of exp1 tenv)])
  (check-equal-type! ty1 (int-type) exp1)
  (bool-type)))]
[if-exp (exp1 exp2 exp3) (let ([ty1 (type-of exp1 tenv)]
  [ty2 (type-of exp2 tenv)]
  [ty3 (type-of exp3 tenv)])
  (check-equal-type! ty1 (bool-type) exp1)
  (check-equal-type! ty2 ty3 exp)
  ty2)]
)))

```

(define the-grammar

```

'([program (expression) a-program]
  [expression ("zero?" "(" expression ")") zero?-exp]
  [expression ("if" expression "then" expression "else" expression) if-exp]
  ))

```

(define check-equal-type!

```

(lambda (ty1 ty2 exp)
  (when (not (equal? ty1 ty2))
    (report-unequal-types ty1 ty2 exp))))

```

(define expval->bool

```

(lambda (v)
  (cases expval v
    [bool-val (bool) bool]
    [num-val (num) (if (equal? num 0) #f #t)]
  ))

```

```
[else (expval-extractor-error 'bool v)))]))
```

```
(define value-of  
  (lambda (exp env)  
    (cases expression exp  
      [zero?-exp (exp1) (let ([val1 (expval->num (value-of exp1 env))])  
        (if (zero? val1)  
            (bool-val #f)  
            (bool-val #t)))]  
      [if-exp (exp0 exp1 exp2) (if (expval->bool (value-of exp0 env))  
        (value-of exp1 env)  
        (value-of exp2 env)))]))
```

(7

1.

```
letrec ? even (x : ?) 2 = if zero?(x) then 1 else (odd -(x, 1)) 3
```

```
? odd (x : ?) 4 = if zero?(x) then 0 else (even -(x, 1)) 5 in (odd 13)
```

با توجه به گفته کلاس کل آن int است و هر کدام int -> Int است.

2.

```
let p = zero?(1) in if p then 88 else 99
```

```
bool -> int
```

3.

```
let f = proc (z) z in proc (x) -(f x), 1
```

```
((t -> int) -> (t -> int))
```

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توابع bool و Zero برای بول استفاده میشوند.

```
#lang racket
```

```
(define type-of
```

```
  (lambda (exp tenv subst)
```

```
    (cases expression exp
```

```
      [zero?-exp (exp1) (cases answer (type-of exp1 tenv subst)
```

```
        [an-answer (type1 subst1) (let ([subst2 (unifier type1 (int-type) subst1 exp)])
```

```
          (an-answer (bool-type) subst2))]))]
```

```
    [if-exp (exp1 exp2 exp3)
```

```
      (cases answer (type-of exp1 tenv subst)
```

```
        [an-answer (ty1 subst) (let ([subst (unifier ty1 (bool-type) subst exp1)])
```

```
          (cases answer (type-of exp2 tenv subst)
```

```
            [an-answer (ty2 subst) (cases answer (type-of exp3 tenv subst)
```

```
              [an-answer (ty3 subst) (let ([subst (unifier ty2
```

```
                ty3
```

```
                subst
```

```
                exp)])
```

```
              (an-answer ty2
```

```
                subst)))])))])))]
```

```
    )))
```

```
(define value-of
```

```
  (lambda (exp env)
```

```
    (cases expression exp
```

```
      [zero?-exp (exp1) (let ([val1 (expval->num (value-of exp1 env))])
```

```
        (if (zero? val1)
```

```
          (bool-val #f)
```

```
          (bool-val #t)))]
```

```
      [if-exp (exp0 exp1 exp2) (if (expval->bool (value-of exp0 env))
```

```
        (value-of exp1 env)
        (value-of exp2 env))])
    )))
```

```
(define expval->bool
  (lambda (v)
    (cases expval v
      [bool-val (bool) bool]
      [num-val (num) (if (equal? num 0) #f #t)]
      [else (expval-extractor-error 'bool v)])))
```

```
(define the-grammar
  '([program (expression) a-program]
    [expression ("zero?" "(" expression ")") zero?-exp]
    [expression ("if" expression "then" expression "else" expression) if-exp]))
```