

Today's content

1. Introduction
2. Rat in a maze
3. Generate all permutations.
(unique chars)
4. Generate all permutations.
(dupl chars)
5. Subset.

} will not be covered

Backtracking → subset of recursion + Generate all possibilities

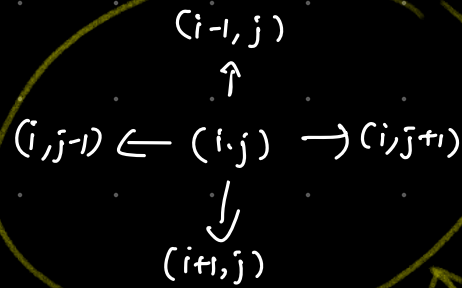
Recursion: Solving problems using subproblems.

Rat in a maze

source

	0	1	2	3	4	5	6
0	2	0	0	1	0	0	0
1	2	1	0	1	0	1	0
2	2	1	0	0	1	0	0
3	2	2	1	0	1	0	1
4	1	2	1	0	0	0	0
5	2	2	0	1	0	1	0

destination



possible movements

1. check if we can move from source to destination.

You should not visit the same box again.

→ keep track of visited cells.

→ $\text{boolean}[N][M]$

- true (cell is visited)
- false (cell is not visited)

→ $\text{arr}[N][M]$

- 0 (empty cell)
- 1 (blocked cell)
- 2 (visited)

$\text{boolean checkPath}(\text{arr}[N][M], i, j)$

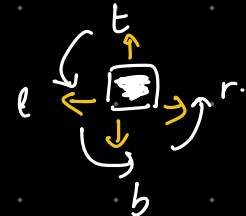
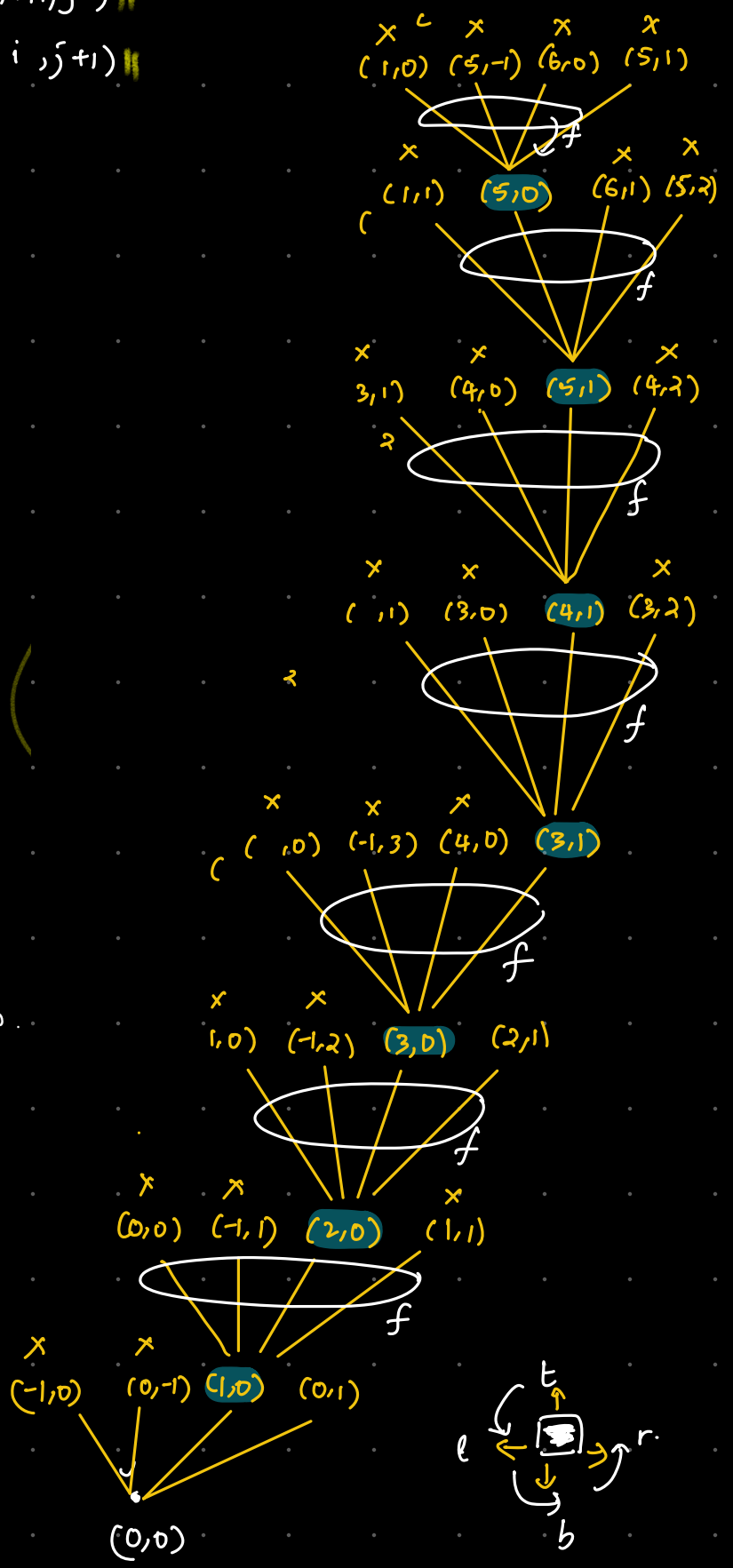
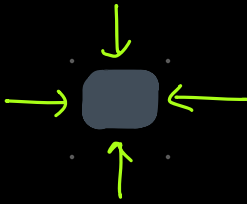
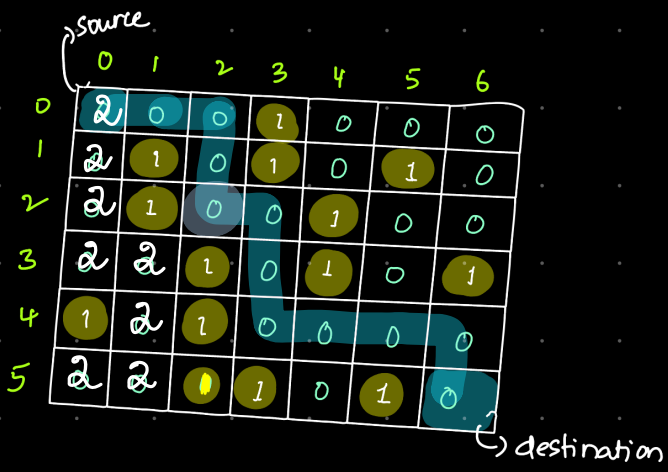
if ($i == N-1$ & $j == M-1$)
return true

if ($i < 0$ || $j < 0$ || $i > N$ || $j > M$ || $\text{arr}[i][j] == 1$ || $\text{arr}[i][j] == 2$)
return false

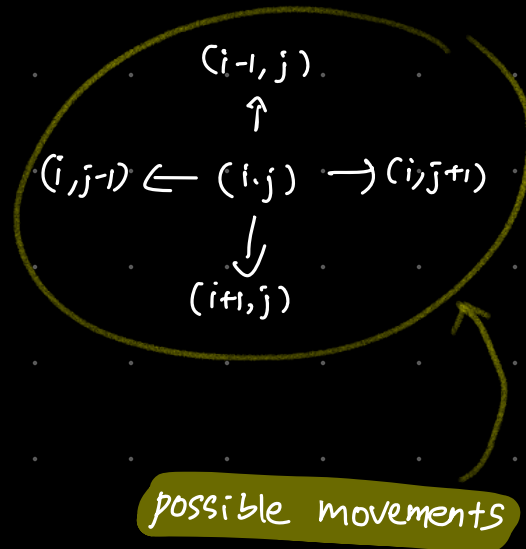
$\text{arr}[i][j] = 2$

return {
 $\text{checkPath}(\text{arr}, i-1, j)$ ||
 $\text{checkPath}(\text{arr}, i, j-1)$ ||
 $\text{checkPath}(\text{arr}, i+1, j)$ ||
 }

checkPath (arr, i, j+1)



$dx = [-1, 0, 1, 0]$
 $dy = [0, -1, 0, 1]$



boolean checkPath (arr[N][M], i, j)

if ($i == N-1$ & $j == M-1$)
 return true

arr[i][j] = 2.

$dx = [-1, 0, 1, 0]$
 $dy = [0, -1, 0, 1]$

for ($k=0; k<4; k++$)

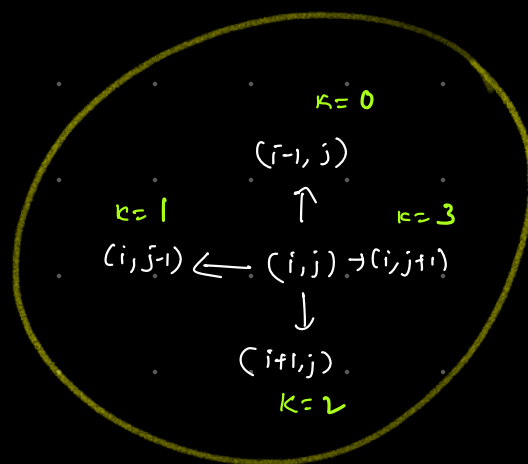
$nI = i + dx[k]$

$nJ = j + dy[k]$

if ($nI \geq 0$ & $nJ \geq 0$ & $nI < N$ & $nJ < M$ & $arr[nI][nJ] == 0$)

return checkPath(arr, nI, nJ)

return false



TC: $O(4 * N * M) = O(N * M)$

SC: $O(N * M)$ (∵ In worst case, every fn call will be stored)

- ① Generate all permutations of a string, without modifying the string.
 char[] arr → contains unique characters.

A: [a b c]

o/p: $\begin{bmatrix} abc & acb & bac \\ bca & cab & cba \end{bmatrix}$

$$\underline{3} * \underline{2} * \underline{1} = 6 \Rightarrow 3!$$

$$\underline{N} * \underline{N-1} * \underline{N-2} * \dots * 1 = N!$$



void printPermutations(char[] arr, int idx, char[] ans, bool[] vis)

if (idx == n) print(ans), return

for (i = 0; i < n; i++)

if (visited[i] == false)

visited[i] = true

ans[idx] = arr[i]

printPermutations(arr, idx + 1, ans, vis)

visited[i] = false

T.C: $O(n!)$

S.C: $O(n)$

```
if (idx == n) print(ans), return
```

```
for (i = 0; i < n; i++)
```

```
if (visited[i] == false)
```

```
visited[i] = true
```

```
ans[idx] = arr[i]
```

```
printPermutations(arr, idx+1, ans, vis)
```

```
visited[i] = false
```

i = 1

idx = 2

ans →

a	c	b
---	---	---

vis →

t	t	t
---	---	---

arr
i/p →

a	b	c
---	---	---

pp(arr, 0, ans, vis)

i = 0

i = 1

i = 2

pp(arr, 1, ans, vis)

i = 0

i = 1

i = 2

nothing

pp(arr, 2, ans, vis)

pp(arr, 2, ans, vis)

nothing

nothing

pp(arr, 3, ans, vis)

↓
print(abc)

nothing

pp(arr, 3, ans, vis)

↓
print(acb)