# A Novel Single-Switch Cascaded DC-DC Converter of Boost and Buck-Boost Converters

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# **Keywords**

«Single-switch», «Cascaded converter», «DC-DC converter», «Boost converter», «Buck-boost converter»

#### **Abstract**

This paper proposes a novel single-switch dc-dc converter with voltage gain D/(1-D)<sup>2</sup> by cascading a Boost converter and a Buck-boost converter. The proposed converter has the advantages of simple circuit structure and extended voltage conversion ratio. The operating principle and steady-state analysis of the proposed converter are discussed in detail. Finally, a prototype is implemented to verify theoretical analysis.

#### Introduction

In recent year, high voltage gain dc-dc converters play more and more important role in many industry applications such as uninterrupted power supplies, power factor correctors, distributed photovoltaic (PV) generation systems and fuel cell energy conversion systems [1-10]. In these applications, a classical boost converter is normally used, but the extremely high duty cycle will result in large conduction loss on the power devices and serious reverse recovery problems [11]. Thus, the conventional boost converter would not be acceptable for realizing high step-up voltage gain along with high efficiency.

To achieve a high conversion ratio without operating at extremely high duty ratio, some converters based on transformers or coupled inductors or tapped inductors have been provided [12-15]. However, the leakage inductance in the transformer, coupled inductor or tapped inductor will cause high voltage spikes in the switches and reduce system efficiency. In order to solve the voltage spike, snubber circuits, such as resistor–capacitor–diode snubber, nondissipative snubber and active clamp circuit, can be applied, but increase the complexity of converter structure.

Some nonisolated topologies have been proposed to achieve a high conversion ratio and avoid operating at extremely high-duty cycle. These converters include the switched-capacitor type [16], switched-inductor type [17], the voltage-doubler circuit [18], and the capacitor-diode voltage multiplier [19]. All of them can obtain higher voltage gain than the conventional boost converter. However, more switched capacitor or switched-inductor stages are needed for an extremely large conversion ratio, which result in higher cost and complex circuit.

The voltage gain can be extended to satisfy the high-step-up requirements by employing the cascade structure. A cascaded boost converter with two stages was proposed in [20]. However, the cascade converter requires two sets of power devices and control circuits, which is complex and expensive. The two switches in the cascade boost converter can be integrated into one switch to reduce circuit complexity [21]. Furthermore, [22] proposed three single-switch cascaded converters, including quadratic buck converter, quadratic buck-boost converter, and buck-buck-boost converter, whose voltage gain is  $D^2$ ,  $D^2/(1-D)^2$  and  $D^2/(1-D)$ , respectively.

A novel single-switch cascaded dc-dc converter of boost and buck-boost converts is proposed in this paper. The voltage conversion ratio is extended to D/(1-D)<sup>2</sup>. The proposed converter operates as basic boost and buck-boost converters in cascade. The features of the proposed converter are as follows: 1) the voltage gain is increased by operating as basic boost and buck-boost converters in cascade, compared with classical dc-dc converters; 2) only one switch is used to realize cascaded converter of basic boost and buck-boost converters, which efficiently simplify the circuit structure; 3) the number of magnetic components is small, where only two inductors are used just like Cuk and Sepic converter.

Operating principle of the proposed converter in steady-state is given firstly. Secondly, the circuit performance is analyzed, while the static voltage gain is derived. Next, the experimental results are provided to verify the analysis. A valuable summary is made in final.

## Operating principle of the proposed converter

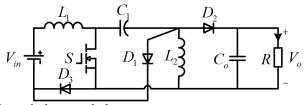


Fig. 1 The proposed single-switch cascaded converter

Fig. 1 shows the circuit structure of the proposed converter, which consists of an active switch S, diodes  $D_1$ ,  $D_2$  and  $D_3$ , an input inductor  $L_1$ , an output inductor  $L_2$ , a storage energy capacitor  $C_1$  and an output capacitor  $C_o$ .

The input inductance  $L_1$  is assumed to be large enough so that input current  $i_{L1}$  is continuous. Capacitors  $C_1$  and  $C_o$  are sufficiently large, and the voltages across them are considered constant during one switching period.

When the inductor current  $i_{L2}$  is in continuous conduction mode, L<sub>2</sub>-CCM is used to denote the operating mode; and L<sub>2</sub>-DCM stands for the mode in which  $i_{L2}$  is in discontinuous conduction mode.

#### A. L<sub>2</sub>-CCM

Based on the aforementioned assumption, Fig. 2(a) illustrates some key waveforms under  $L_2$ -CCM, and the corresponding equivalent circuits are shown in Fig. 3(a) and (b). The operating stages are described as follows.

**Mode I** [ $t_0$ - $t_1$ ]: Switch S conducts at  $t=t_0$ . Diodes  $D_1$  and  $D_2$  are reverse-biased by  $V_{C1}$  and  $V_{C1}+V_o$ , respectively. Only diode  $D_3$  is ON. Fig. 3(a) shows the current-flow path. The energy of dc source  $V_{in}$  is transferred to the inductor  $L_1$  through S and  $D_3$ . Therefore, inductor current  $i_{L1}$  is increasing linearly. The voltage of the inductor  $L_2$  is  $V_{C1}$  and the capacitor  $C_1$  is discharging its energy to  $L_2$  though S. The inductor current  $i_{L2}$  is increasing. Meanwhile, the load R is supplied by the output capacitor  $C_o$ . This stage ends at  $t=t_1$ .

**Mode II**  $[t_1-t_2]$ : Fig. 3(b) depicts the current-flow path of this stage. Once S is turned OFF at  $t=t_1$ ,  $i_{L1}$  is forced to flow through  $D_1$ , inductor  $L_1$  and dc source  $V_{in}$  charge capacitor  $C_1$  instantaneously.

Therefore,  $i_{L1}$  declines linearly. At the same time,  $i_{L2}$  is forced to flow through  $D_2$  and the energy stored in inductor  $L_2$  is transferred to the output capacitor  $C_o$  and load R. Thus,  $i_{L2}$  declines linearly and  $D_3$  is reverse-biased by  $V_{in}$ . This stage end at  $t=t_2$ .

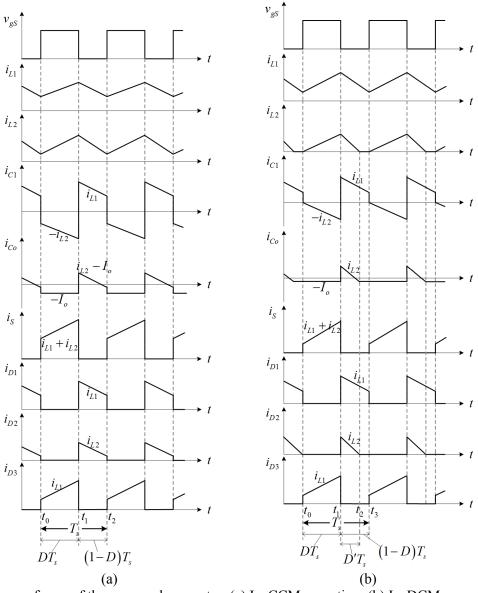
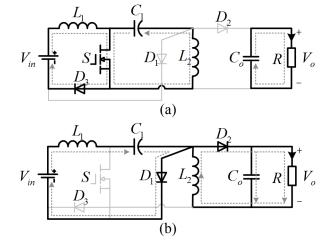


Fig. 2 Key waveforms of the proposed converter: (a) L<sub>2</sub>-CCM operation; (b) L<sub>2</sub>-DCM operation



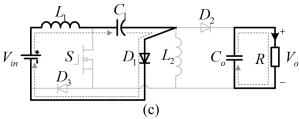


Fig. 3 Equivalent circuits of operating stages: (a) Mode I; (b) Mode II; (c) Mode III.

#### B. $L_2$ -DCM

The key waveforms of the proposed converter under  $L_2$ -DCM are shown in Fig. 2(b). There are three main stages during one switching cycle. The equivalent circuits for each subinterval are shown in Fig. 3(a), (b) and (c). Modes I and II are same with  $L_2$ -CCM, and only case III is presented.

**Mode III**  $[t_2-t_3]$ : Diode  $D_2$  is blocked when the current  $i_{L2}$  reaches zero at  $t=t_2$ . During this time interval, switch S and diodes  $D_2$ ,  $D_3$  are turned OFF, only diode  $D_1$  is turned ON. The current path is shown in Fig. 3(c). The dc source  $V_{in}$  is in series with inductor  $L_1$  and keeps transferring energy to the capacitor  $C_1$  through  $D_1$ . Since the energy stored in  $L_2$  is empty, the energy stored in  $C_0$  is discharged to load R. This stage ends when switch S is turned ON at  $t=t_3$ , the next switching period will begin again.

# Steady-state analysis of the proposed converter

To simplify the analysis, all components are considered to be ideal, and the losses of the power devices are not considered.

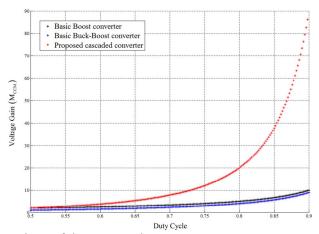


Fig. 4: Voltage gain comparison of the proposed converter, Boost converter and Buck-Boost converter

### A. L<sub>2</sub>-CCM

Using the inductor volt-second balance principle to the inductors  $L_1$  and  $L_2$ , the following equations can be established.

$$\int_{0}^{DT_{s}} V_{in} dt + \int_{DT_{s}}^{T_{s}} \left( V_{in} - V_{C1} \right) dt = 0$$
 (1)

$$\int_{0}^{DT_{s}} V_{C1} dt + \int_{DT_{s}}^{T_{s}} (-V_{o}) dt = 0$$
 (2)

Then, the dc voltage gain  $M_{CCM}$  is obtained as

$$M_{CCM} = \frac{V_o}{V_{in}} = \frac{D}{(1-D)^2}$$
 (3)

Fig. 4 demonstrates the relationships between the voltage gain and the duty cycle in the basic boost converter, buck-boost converter, and the proposed converter under  $L_2$ -CCM. It is found that the proposed converter can realize higher voltage gain with the same duty cycle.

#### B. $L_2$ -DCM

If D' is defined as the duty cycle of the inductor current  $i_{L2}$  from peak point down to zero. By applying the volt-second balance principle to the inductors  $L_1$  and  $L_2$ , the following equations are derived.

$$\int_{0}^{DT_{s}} V_{in} dt + \int_{DT_{s}}^{T_{s}} \left( V_{in} - V_{C1} \right) dt = 0$$
(4)

$$\int_{0}^{DT_{s}} V_{C1} dt + \int_{DT}^{(D+D')T_{s}} (-V_{o}) dt = 0$$
(5)

Then, the voltage gain are obtained

$$M_{DCM} = \frac{V_o}{V_{in}} = \frac{D}{(1-D)D'}$$
 (6)

The currents flow capacitor  $C_o$  at mode I, II, and III are  $-I_o$ ,  $i_{L2}$ - $I_o$  and  $-I_o$ , respectively. According to the current-balance principle on capacitor  $C_o$ , the following equation can be established.

$$\int_{0}^{DT_{s}} \left( -I_{o} \right) dt + \int_{DT_{s}}^{(D+D')T_{s}} \left( i_{L2} - I_{o} \right) dt + \int_{(D+D')T_{s}}^{T_{s}} \left( -I_{o} \right) dt = 0$$
 (7)

Since  $I_o = V_o/R_L$ , the following relationship can be obtained.

$$D'^2 + \frac{2L_2 f_s}{R} D' - \frac{2L_2 f_s}{R} = 0$$
 (8)

where  $f_s$  is the switching frequency.

### C. Boundary condition between L2-CCM and L2-DCM

If the proposed converter is operating in boundary condition mode (BCM) between L2-CCM and L2-DCM, the peak value of the inductor current  $i_{L2}$  is given as

$$I_{L2p} = \frac{V_{C1}}{L_2} DT_S \tag{9}$$

The currents flow capacitor  $C_o$  at mode I and II are  $I_o$  and  $I_{L2}$ , respectively. According to the current-balance principle on capacitor  $I_o$ , the following equation can be established.

$$\int_{0}^{DT_{s}} \left( -I_{o} \right) dt + \int_{DT_{s}}^{T_{s}} \left( i_{L2} - I_{o} \right) dt = 0$$
 (10)

Thus

$$\frac{1}{2}I_{L2p}(1-D) = I_o \tag{11}$$

The normalized inductor time constant  $\tau_{L2}$  is defined as

$$\tau_{L2} \equiv \frac{L_2 f_s}{R_I} \tag{12}$$

Since  $I_o = V_o/R_L$ , by substituting (4), (9) and (12) into (11), the boundary normalized inductor time constant  $\tau_{L2B}$  is obtained, which is

$$\tau_{L2B} = \frac{(1-D)^2}{2} \tag{13}$$

Based on (13), the relationship between  $\tau_{L2B}$  and duty cycle D is plotted in Fig. 5. Once the  $\tau_{L2}$  is higher than  $\tau_{L2B}$ , the proposed converter is operating in  $L_2$ -CCM, but in  $L_2$ -DCM when the  $\tau_{L2}$  is lower than  $\tau_{L2B}$ .

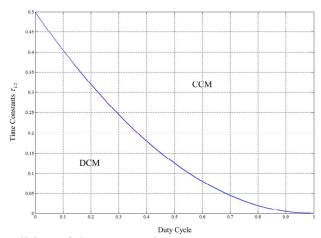


Fig. 5 The boundary condition of the proposed converter

## **Experimental Results**

To demonstrate the effectiveness of the theoretical analysis, a prototype of the proposed converter was built and tested. The test setup is shown in Fig. 6 and the components used in the prototype are listed in Table I. A PWM signal with fixed duty ratio is generated to control the switch on or off.

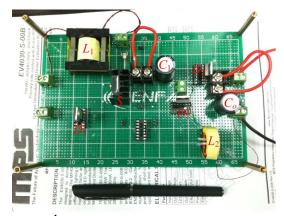


Fig. 6 The prototype of the proposed converter.

**Table I Utilized Components and Parameters of Prototype** 

Components	Parameters	Components	Parameters
Output power $P_o$	36W	Output Inductor $L_2$	150uH
Input voltage $V_{in}$	10V	Capacitor $C_1$	470uF
Output voltage $V_o$	60V	Output capacitor $C_o$	100uF
Switching frequency $f_s$	50kHz	Power MOSFET S	STW15NA50
Input inductor $L_1$	400uH	Diodes $D_1/D_2/D_3$	BYV34

Typical waveforms in L<sub>2</sub>-CCM are demonstrated in Fig. 7. Fig. 7(a) illustrates the gate signal of switch  $(v_{gS})$ , the voltage across  $C_1$ , and the output voltage  $V_o$ . Fig. 7(b) illustrates  $v_{gS}$  and the voltage of switch S, and the output voltage  $V_o$ . Fig. 7(c) shows  $v_{gS}$  and inductor currents  $i_{L1}$  and  $i_{L2}$ . Fig. 7(d) gives  $v_{gS}$  and capacitor currents  $i_{C1}$  and  $i_{Co}$ , which are agreed well with the theoretical analysis.

In order to verify the feasibility of  $L_2$ -DCM, the experimental waveforms under light-load are shown in Fig. 8. The inductor current  $i_{L2}$  declines to zero during the off state of switch S. The experimental results are consistent with the theoretical analysis as well.

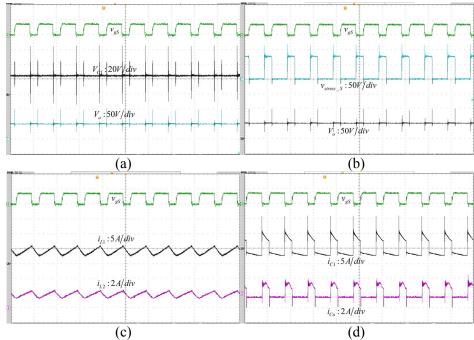
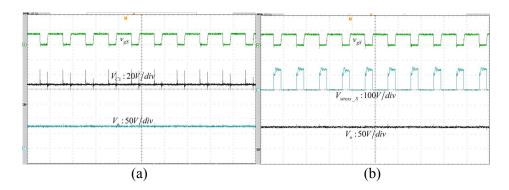


Fig. 7 Experimental waveforms under L<sub>2</sub>-CCM: (a)  $v_{gS}$ ,  $v_{C1}$ ,  $V_o$ . (b)  $v_{gS}$ ,  $v_{S}$ ,  $V_o$ ; (c)  $v_{gS}$ ,  $i_{L1}$ ,  $i_{L2}$ ; (d)  $v_{gS}$ ,  $i_{C1}$ ,  $i_{Co}$ .



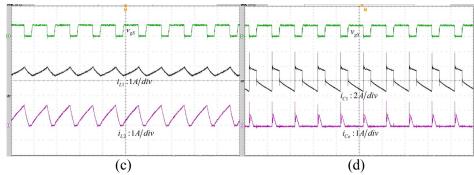


Fig. 8 Experimental waveforms under L<sub>2</sub>-DCM: (a)  $v_{gS}$ ,  $v_{C1}$ ,  $V_o$ ; (b)  $v_{gS}$ ,  $v_{S}$ ,  $V_o$ ; (c)  $v_{gS}$ ,  $i_{L1}$ ,  $i_{L2}$ ; (d)  $v_{gS}$ ,  $i_{C1}$ ,  $i_{Co}$ .

### **Conclusion**

A novel single-switch cascaded converter is proposed in this paper. Only single switch is used to realize the cascaded converter of basic boost and buck-boost converters. The voltage conversion ratio is extended to  $D/(1-D)^2$ . The proposed converter operates as basic boost and buck-boost converters in cascade, which has simple circuit structure with extended voltage conversion ratio compared with some other high step-up converters. The number of magnetic components is reduced, where only two inductors are used just like Cuk and Sepic converters, results in lower cost and simple circuit.

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