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**1 STL Useful Tips**

1.1 Common libraries

/\*\*\* Functions \*\*\*/

#include<algorithm>

#include<functional> // for hash

#include<climits> // all useful constants

#include<cmath>

#include<cstdio>

#include<cstdlib> // random

#include<ctime>

#include<iostream>

#include<sstream>

#include<iomanip> // right justifying std::right and std::setw(width)

/\*\*\* Data Structure \*\*\*/

#include<deque> // double ended queue

#include<list>

#include<queue> // including priority\_queue

#include<stack>

#include<string>

#include<vector>

**1.2 I/O**

// iostream and cstdio are both using I/O streams

// However, they have different behavior,

// pay attention on them if you’re using them together.

// cin does not concern with ’\n’ at end of each line

// however scanf or getline does concern with ’\n’ at end of each line

// ’\n’ will be ignored when you use cin to read char.

// when you use getline(cin, str) to read a whole line of input

// please add an extra getline before inputing if previous inputs are numbers

cin >> n;

getline(cin, str) // wasted getline

getline(cin, str) // real input string

1.3 Useful constant

INT\_MIN

INT\_MAX

LONG\_MIN

LONG\_MAX

LLONG\_MIN

LLONG\_MAX

(~0u) // infinity (for long and long long)

// use (~0u)>>2 for int.

**1.4 Space waster**

// consider to redefine data types to void data range problem

#define int long long // make everyone long long

#define double long double // make everyone long double

// function definitions

#undef int // main must return int

int main(void)

#define int long long // redefine int

// rest of program

1.5 Tricks in cmath

// when the number is too large. use powl instead of pow.

// will provide you more accuracy.

powl(a, b)

(int)round(p, (1.0/n)) // nth root of p

1.6 Initialize array with predefined value

// for 1d array, use STL fill\_n or fill to initialize array

fill(a, a+size\_of\_a, value)

fill\_n(a, size\_of\_a, value)

// for 2d array, if want to fill in 0 or -1

memset(a, 0, sizeof(a));

// otherwise, use a loop of fill or fill\_n through every a[i]

fill(a[i], a[i]+size\_of\_ai, value) // from 0 to number of row.

1.7 Modifying sequence operations

void copy(first, last, result);

void swap(a,b);

void swap(first1, last1, first2); // swap range

void replace(first, last, old\_value, new\_value); // replace in range

void replace\_if(first, last, pred, new\_value); // replace in conditions

// pred can be represented in function

// e.x. bool IsOdd (int i) { return ((i%2)==1); }

void reverse(first, last); // reverse a range of elements

void reverse\_copy(first, last, result); // copy a reverse of range of elements

void random\_shuffle(first, last); // using built-in random generator to shuffle array

1.8 Merge

// merge sorted ranges

void merge(first1, last1, first2, last2, result, comp);

// union of two sorted ranges

void set\_union(first1, last1, first2, last2, result, comp);

// intersection of two sorted ranges

void set\_interaction(first1, last1, first2, last2, result, comp);

// difference of two sorted ranges

void set\_difference((first1, last1, first2, last2, result, comp);

1.9 String

// Searching

unsigned int find(const string &s2, unsigned int pos1 = 0);

unsigned int rfind(const string &s2, unsigned int pos1 = end);

unsigned int find\_first\_of(const string &s2, unsigned int pos1 = 0);

unsigned int find\_last\_of(const string &s2, unsigned int pos1 = end);

unsigned int find\_first\_not\_of(const string &s2, unsigned int pos1 = 0);

unsigned int find\_last\_not\_of(const string &s2, unsigned int pos1 = end);

// Insert, Erase, Replace

string& insert(unsigned int pos1, const string &s2);

string& insert(unsigned int pos1, unsigned int repetitions, char c);

string& erase(unsigned int pos = 0, unsigned int len = npos);

string& replace(unsigned int pos1, unsigned int len1, const string &s2);

string& replace(unsigned int pos1, unsigned int len1, unsigned int repetitions, char c);

// String streams

stringstream s1;

int i = 22;

s1 << "Hello world! " << i;

cout << s1.str() << endl;

1.10 Heap

template <class RandomAccessIterator>

void push\_heap (RandomAccessIterator first, RandomAccessIterator last);

template <class RandomAccessIterator, class Compare>

void push\_heap (RandomAccessIterator first, RandomAccessIterator last,

                                    Compare comp);

                    template <class RandomAccessIterator>

                    void pop\_heap (RandomAccessIterator first, RandomAccessIterator last);

                    template <class RandomAccessIterator, class Compare>

                    void pop\_heap (RandomAccessIterator first, RandomAccessIterator last,

                                   Compare comp);

                    template <class RandomAccessIterator>

                    void make\_heap (RandomAccessIterator first, RandomAccessIterator last);

                    template <class RandomAccessIterator, class Compare>

                    void make\_heap (RandomAccessIterator first, RandomAccessIterator last,

                                    Compare comp );

                    template <class RandomAccessIterator>

                    void sort\_heap (RandomAccessIterator first, RandomAccessIterator last);

                    template <class RandomAccessIterator, class Compare>

                    void sort\_heap (RandomAccessIterator first, RandomAccessIterator last,

                                    Compare comp);

                    template <class RandomAccessIterator>

                    RandomAccessIterator is\_heap\_until (RandomAccessIterator first,

                            RandomAccessIterator last);

                    template <class RandomAccessIterator, class Compare>

                    RandomAccessIterator is\_heap\_until (RandomAccessIterator first,

                            RandomAccessIterator last

                            Compare comp);

                    1.11 Sort

                    void sort(iterator first, iterator last);

                    void sort(iterator first, iterator last, LessThanFunction comp);

                    void stable\_sort(iterator first, iterator last);

                    void stable\_sort(iterator first, iterator last, LessThanFunction comp);

                    void partial\_sort(iterator first, iterator middle, iterator last);

                    void partial\_sort(iterator first, iterator middle, iterator last, LessThanFunction comp);

                    bool is\_sorted(iterator first, iterator last);

                    bool is\_sorted(iterator first, iterator last, LessThanOrEqualFunction comp);

// example for sort, if have array x, start\_index, end\_index;

                    sort(x+start\_index, x+end\_index);

                    /\*\* sort a map \*\*/

// You cannot directly sort a map<key type, mapped data type>

// if you only want to sort in key type

// you can use insert method to copy map into another map

// b.insert(make\_pair(it->first, it->second) /\* it is a map iterator \*/

// this will result a map which sorts key type in increasing order

// if you want to sort key type in decreasing order, then declare your map as

// something like:

// map<char, int, greater<char> >

// if you want to sort based on key, you need to copy the data to a vector

// where elements of vector are pair.

// you can define a PAIR type by using:

                    typedef pair<char, int> PAIR;

// suppose this is the map

                    map<char, int> a;

// sort vector in decreasing order

                    bool cmp\_by\_value(const PAIR& lhs, const PAIR& rhs)

{

    return lhs.second > rhs.second;

}

// sort key in increasing order

bool cmp\_by\_char(const PAIR& lhs, const PAIR& rhs)

{

    return lhs.first < rhs.first;

}

// copy map data to vector

vector<PAIR> b(a.begin(), a.end());

// sort data

sort(b.begin(), b.end(), cmp\_by\_value);

// you can still call your data by b[i].first and b[i].second.

// THE ABOVE CODES ARE EXAMPLE FOR SORTING A MAP.

// PLEASE USE IT FOR YOUR OWN DEMANDS.

1.12 Permutations

bool next\_permutation(iterator first, iterator last);

bool next\_permutation(iterator first, iterator last, LessThanOrEqualFunction comp);

bool prev\_permutation(iterator first, iterator last);

bool prev\_permutation(iterator first, iterator last, LessThanOrEqualFunction comp);

1.13 Searching

// will return address of iterator, call result as \*iterator;

iterator find(iterator first, iterator last, const T &value);

iterator find\_if(iterator first, iterator last, const T &value, TestFunction test);

bool binary\_search(iterator first, iterator last, const T &value);

bool binary\_search(iterator first, iterator last, const T &value, LessThanOrEqualFunction comp);

1.14 Random algorithm

srand(time(NULL));

// generate random numbers between [a,b)

rand() % (b - a) + a;

// generate random numbers between [0,b)

rand() % b;

// generate random permutations

random\_permutation(anArray, anArray + 10);

random\_permutation(aVector, aVector + 10);

**2 Number Theory**

**2.1 Prime number under 100**

// there are 25 numbers

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37,

41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

**2.4 If prime number**

bool prime(int n)

{

    if (n<2) return false;

    if (n<=3) return true;

    if (!(n%2) || !(n%3)) return false;

    for (int i=5; i\*i<=n; i+=6)

        if (!(n%i) || !(n%(i+2))) return false;

    return true;

}

**2,5** **Narayana numbers**

N(n,k)=(nCk)\*(nC(k−1))/n

The number of expressions containing n pairs of parentheses, which are correctly matched and which contain k distinct nestings. For instance, N(4,2)=6 as with four pairs of parentheses six sequences can be created which each contain two times the sub-pattern ‘()’.

**2.6 Prime factorization**

// smallest prime factor of a number.

function factor(int n)

{

    int a;

    if (n%2==0)

        return 2;

    for (a=3; a<=sqrt(n); a++++)

    {

        if (n%a==0)

            return a;

    }

    return n;

}

// complete factorization

int r;

while (n>1)

{

r = factor(n);

    printf("%d", r);

    n /= r;

}

**2.7 Leap year**

bool isLeap(int n)

{

    if (n%100==0)

        if (n%400==0) return true;

        else return false;

    if (n%4==0) return true;

    else return false;

}

**2.8 Binary exponiential**

int binpow (int a, int n)

{

    int res = 1;

    while (n)

        if (n & 1)

        {

            res \*= a;

            --n;

        }

        else

        {

            a \*= a;

            n >>= 1;

        }

    return res;

}

**2.9 a**

**b mod p**

long powmod(long base, long exp, long modulus)

{

    base %= modulus;

    long result = 1;

    while (exp > 0)

    {

        if (exp & 1) result = (result \* base) % modulus;

        base = (base \* base) % modulus;

        exp >>= 1;

    }

    return result;

}

**2.10 Factorial mod**

**//n! mod p**

int factmod (int n, int p)

{

    long long res = 1;

    while (n > 1)

    {

        res = (res \* powmod (p-1, n/p, p)) % p;

        for (int i=2; i<=n%p; ++i)

            res=(res\*i) %p;

        n /= p;

    }

    return int (res % p);

}

**2.11 Generate combinations**

// n>=m, choose M numbers from 1 to N.

void combination(int n, int m)

{

    if (n<m) return ;

    int a[50]= {0};

    int k=0;

    for (int i=1; i<=m; i++) a[i]=i;

    while (true)

    {

        for (int i=1; i<=m; i++)

            cout << a[i] << " ";

        cout << endl;

        k=m;

        while ((k>0) && (n-a[k]==m-k)) k--;

        if (k==0) break;

        a[k]++;

        for (int i=k+1; i<=m; i++)

            a[i]=a[i-1]+1;

    }

}

2.12 10-ary to m-ary

char a[16]= {’0’,’1’,’2’,’3’,’4’,’5’,’6’,’7’,’8’,’9’,

             ’A’,’B’,’C’,’D’,’E’,’F’

            };

            string tenToM(int n, int m)

{

    int temp=n;

    string result="";

    while (temp!=0)

    {

        result=a[temp%m]+result;

        temp/=m;

    }

    return result;

}

**2.13 m-ary to 10-ary**

string num="0123456789ABCDE";

           int mToTen(string n, int m)

{

    int multi=1;

    int result=0;

    for (int i=n.size()-1; i>=0; i--)

    {

        result+=num.find(n[i])\*multi;

        multi\*=m;

    }

    return result;

}

**2.14 Binomial coefficient**

#define MAXN 100 // largest n or m

long binomial\_coefficient(n,m) // compute n choose m

int n,m;

{

    int i,j;

    long bc[MAXN][MAXN];

    for (i=0; i<=n; i++) bc[i][0] = 1;

    for (j=0; j<=n; j++) bc[j][j] = 1;

    for (i=1; i<=n; i++)

        for (j=1; j<i; j++)

            bc[i][j] = bc[i-1][j-1] + bc[i-1][j];

    return bc[n][m];

}

**2.16 Eulerian numbers**

        N

        k

        = k

          n − 1

          k

          + (n − k + 1)

          n − 1

          k − 1

          (2)

// This is the number of permutations of length n with exactly k ascending sequences or runs.

// Basis: k=0 has value 1

#define MAXN 100 // largest n or k

          long eularian(n,k)

          int n,m;

{

    int i,j;

    long e[MAXN][MAXN];

    for (i=0; i<=n; i++) e[i][0] = 1;

    for (j=0; j<=n; j++) e[0][j] = 0;

    for (i=1; i<=n; i++)

        for (j=1; j<i; j++)

            e[i][j] = k\*e[i-1][j] + (i-j+1)\*e[i-1][j-1];

    return e[n][k];

}

**2.17 Karatsuba algorithm in Java**

// fast algorithm to find multiplication of two big numbers.

import java.math.BigInteger;

import java.util.Random;

class Karatsuba

{

    private final static BigInteger ZERO = new BigInteger("0");

    public static BigInteger karatsuba(BigInteger x, BigInteger y)

    {

        int N = Math.max(x.bitLength(), y.bitLength());

        if (N <= 2000) return x.multiply(y);

        N=(N/2)+(N %2);

        BigInteger b = x.shiftRight(N);

        BigInteger a = x.subtract(b.shiftLeft(N));

        BigInteger d = y.shiftRight(N);

        BigInteger c = y.subtract(d.shiftLeft(N));

        BigInteger ac = karatsuba(a, c);

        BigInteger bd = karatsuba(b, d);

        BigInteger abcd = karatsuba(a.add(b), c.add(d));

        return ac.add(abcd.subtract(ac).subtract(bd).shiftLeft(N)).add(bd.shiftLeft(2\*N));

    }

    public static void main(String[] args)

    {

        long start, stop, elapsed;

        Random random = new Random();

        int N = Integer.parseInt(args[0]);

        BigInteger a = new BigInteger(N, random);

        BigInteger b = new BigInteger(N, random);

        start = System.currentTimeMillis();

        BigInteger c = karatsuba(a, b);

        stop = System.currentTimeMillis();

        System.out.println(stop - start);

        start = System.currentTimeMillis();

        BigInteger d = a.multiply(b);

        stop = System.currentTimeMillis();

        System.out.println(stop - start);

        System.out.println((c.equals(d)));

    }

}

2.18 Euler’s totient function

// the positive integers less than or equal to n that are relatively prime to n.

int phi (int n)

{

    int result = n;

    for (int i=2; i\*i<=n; ++i)

        if(n %i==0)

        {

            while(n %i==0)

                n /= i;

            result -= result / i;

        }

    if (n > 1)

        result -= result / n;

    return result;

}

**2.19 Split plane**

n lines can split a plane in (n+1)n

2 + 1 sub-regions.

3 Searching Algorithms

**3.1 Find rank k in array**

int find(int l, int r, int k)

{

    int i=0,j=0,x=0,t=0;

    if (l==r) return a[l];

    x=a[(l+r)/2];

    t=a[x];

    a[x]=a[r];

    a[r]=t;

    i=l-1;

    for (int j=l; j<=r-1; j++)

        if (a[j]<=a[r])

        {

            i++;

            t=a[i];

            a[i]=a[j];

            a[j]=t;

        }

    i++;

    t=a[i];

    a[i]=a[r];

    a[r]=t;

    if (i==k) return a[i];

    if (i<k) return find(i+1, r,k);

    return find(l, i-1, k);

}

**3.2 KMP Algorithm**

#include <iostream>

#include <string>

#include <vector>

using namespace std;

typedef vector<int> VI;

void buildTable(string& w, VI& t)

{

    t = VI(w.length());

    int i = 2, j = 0;

    t[0] = -1;

    t[1] = 0;

    while(i < w.length())

    {

        if(w[i-1] == w[j])

        {

            t[i] = j+1;

            i++;

            j++;

        }

        else if(j > 0) j = t[j];

        else

        {

            t[i] = 0;

            i++;

        }

    }

}

int KMP(string& s, string& w)

{

    int m = 0, i = 0;

    VI t;

    buildTable(w, t);

    while(m+i < s.length())

    {

        if(w[i] == s[m+i])

        {

            i++;

            if(i == w.length()) return m;

        }

        else

        {

            m += i-t[i];

            if(i > 0) i = t[i];

        }

    }

    return s.length();

}

int main(void)

{

    string a = (string) "The example above illustrates the general technique for assembling "+

               "the table with a minimum of fuss. The principle is that of the overall search: "+

               "most of the work was already done in getting to the current position, so very "+

               "little needs to be done in leaving it. The only minor complication is that the "+

               "logic which is correct late in the string erroneously gives non-proper "+

               "substrings at the beginning. This necessitates some initialization code.";

    string b = "table";

    int p = KMP(a, b);

    cout << p << ": " << a.substr(p, b.length()) << " " << b << endl;

    return 0;

}

4 Dynamic Programming

4.1 0/1 Knapsack problems

#include<iostream>

using namespace std;

int f[1000]= {0};

             int n=0, m=0;

             int main(void)

{

    cin >> n >> m;

    for (int i=1; i<=n; i++)

    {

        int price=0, value=0;

        cin >> price >> value;

        for (int j=m; j>=price; j--)

            if (f[j-price]+value>f[j])

                f[j]=f[j-price]+value;

    }

    cout << f[m] << endl;

    return 0;

}

**4.2 Complete Knapsack problems**

#include<iostream>

using namespace std;

int f[1000]= {0};

             int n=0, m=0;

             int main(void)

{

    cin >> n >> m;

    for (int i=1; i<=n; i++)

    {

        int price=0, value=0;

        cin >> price >> value;

        for (int j=price; j<=m; j++)

            if (f[j-price]+value>f[j])

                f[j]=f[j-price]+value;

    }

    cout << f[m] << endl;

    return 0;

}

**4.3 Longest common subsequence (LCS)**

int dp[1001][1001];

int lcs(const string &s, const string &t)

{

    int m = s.size(), n = t.size();

    if (m == 0 || n == 0) return 0;

    for (int i=0; i<=m; ++i)

        dp[i][0] = 0;

    for (int j=1; j<=n; ++j)

        dp[0][j] = 0;

    for (int i=0; i<m; ++i)

        for (int j=0; j<n; ++j)

            if (s[i] == t[j])

                dp[i+1][j+1] = dp[i][j]+1;

            else

                dp[i+1][j+1] = max(dp[i+1][j], dp[i][j+1]);

    return dp[m][n];

}

**4.4 Longest increasing common sequence (LICS)**

#include<iostream>

using namespace std;

int a[100]= {0};

            int b[100]= {0};

            int f[100]= {0};

            int n=0, m=0;

            int main(void)

{

    cin >> n;

    for (int i=1; i<=n; i++) cin >> a[i];

    cin >> m;

    for (int i=1; i<=m; i++) cin >> b[i];

    for (int i=1; i<=n; i++)

    {

        int k=0;

        for (int j=1; j<=m; j++)

        {

            if (a[i]>b[j] && f[j]>k) k=f[j];

            else if (a[i]==b[j] && k+1>f[j]) f[j]=k+1;

        }

    }

    int ans=0;

    for (int i=1; i<=m; i++)

        if (f[i]>ans) ans=f[i];

    cout << ans << endl;

    return 0;

}

**4.5 Longest Increasing Subsequence (LIS)**

#include<iostream>

using namespace std;

int n=0;

      int a[100]= {0}, f[100]= {0}, x[100]= {0};

      int main(void)

{

    cin >> n;

    for (int i=1; i<=n; i++)

    {

        cin >> a[i];

        x[i]=INT\_MAX;

    }

    f[0]=0;

    int ans=0;

    for(int i=1; i<=n; i++)

    {

        int l=0, r=i;

        while (l+1<r)

        {

            int m=(l+r)/2;

            if (x[m]<a[i]) l=m;

            else r=m;

// change to x[m]<=a[i] for non-decreasing case

        }

        f[i]=l+1;

        x[l+1]=a[i];

        if (f[i]>ans) ans=f[i];

    }

    cout << ans << endl;

    return 0;

}

**4.6 Maximum submatrix**

// URAL 1146 Maximum Sum

#include<iostream>

using namespace std;

int a[150][150]= {0};

                 int c[200]= {0};

                 int maxarray(int n)

{

    int b=0, sum=-100000000;

    for (int i=1; i<=n; i++)

    {

        if (b>0) b+=c[i];

        else b=c[i];

        if (b>sum) sum=b;

    }

    return sum;

}

int maxmatrix(int n)

{

    int sum=-100000000, max=0;

    for (int i=1; i<=n; i++)

    {

        for (int j=1; j<=n; j++)

            c[j]=0;

        for (int j=i; j<=n; j++)

        {

            for (int k=1; k<=n; k++)

                c[k]+=a[j][k];

            max=maxarray(n);

            if (max>sum) sum=max;

        }

    }

    return sum;

}

int main(void)

{

    int n=0;

    cin >> n;

    for (int i=1; i<=n; i++)

        for (int j=1; j<=n; j++)

            cin >> a[i][j];

    cout << maxmatrix(n);

    return 0;

}

**4.7 Partitions of integers**

#define MAXN 100 // largest n or m

long int\_coefficient(n,k) // compute f(n,k)

int n,m;

{

    int i,j;

    long f[[MAXN][MAXN];

                 f [1][1] = 1;

                 for (i=0; i<=n; i++) f[i][0] = 0;

                 for (i=1; i<=n; i++)

                 for (j=1; j<i; j++)

                 if (i-j <= 0)

                 f[i][j] = f[i][k-1];

                 else

                 f[i][j] = f[i-j][k]+f[i][k-1];

                 return f[n][k];

      }

      4.8 Partitions of sets

      Number of ways to partition n + 1 items into k sets.

      n

      k

          = k

            n − 1

            k

            +

            n − 1

            k − 1

            (3)

      where

      n

      1

      =

          n

          n

          = 1 (4)

            5 Trees

            5.1 Tree traversal

            int L[100]= {0};

int R[100]= {0};

            void DLR(int m)

{

    cout << m << " ";

    if (L[m]!=0) DLR(L[m]);

    if (R[m]!=0) DLR(R[m]);

}

void LDR(int m)

{

    if (L[m]!=0) LDR(L[m]);

    cout << m << " ";

    if (R[m]!=0) LDR(R[m]);

}

void LRD(int m)

{

    if (L[m]!=0) LRD(L[m]);

    if (R[m]!=0) LRD(R[m]);

    cout << m << " ";

}

int main(void)

{

    cin >> n;

    for (int i=1; i<=n; i++)

        cin >> L[i] >> R[i];

    DLR(1);

    cout << endl;

    LDR(1);

    cout << endl;

    LRD(1);

    cout << endl;

    return 0;

}

**5.2 Depth and width of tree**

#include <iostream>

#include <queue>

#include <stack>

using namespace std;

int l[100]= {0};

            int r[100]= {0};

            stack<int> mystack;

            int n=0;

            int w=0;

            int d=0;

            int depth(int n)

{

    if (l[n]==0 && r[n]==0)

        return 1;

    int depthl=depth(l[n]);

    int depthr=depth(r[n]);

    int dep=depthl>depthr ? depthl:depthr;

    return dep+1;

}

void width(int n)

{

    if (n<=d)

    {

        int t=0,x;

        stack<int> tmpstack;

        while (!mystack.empty())

        {

            x=mystack.top();

            mystack.pop();

            if (x!=0)

            {

                t++;

                tmpstack.push(l[x]);

                tmpstack.push(r[x]);

            }

        }

        w=w>t?w:t;

        mystack=tmpstack;

        width(n+1);

    }

}

int main(void)

{

    cin >> n;

    for (int i=1; i<=n; i++)

        cin >> l[i] >> r[i];

    d=depth(1);

    mystack.push(1);

    width(1);

    cout << w << " " << d << endl;

    return 0;

}

***6 Graph Theory***

**6.1 Graph representation**

// The most common way to define graph is to use adjacency matrix

// example:

// (1) (2) (3) (4) (5)

// (1) 2 0 5 0 0

// (2) 4 2 0 0 1

// (3) 3 0 0 1 4

// (4) 6 9 0 0 0

// (5) 1 1 1 1 5

// it’s always a square matrix.

// suppose a graph has n nodes, if given exactly adjacency matrix

for (int i=1; i<=n; i++)

for (int j=1; i<=n; j++)

{

    cin << a[i][j] << endl;

    }

// Usually will go like this representation in data

// start\_node end\_node weight

// suppose m lines

for (int i=1; i<=m; i++)

{

int x=0, y=0, t=0;

cin >> x >> y >> t;

a[x][y]=t;

// if undirected graph

    a[y][x]=t;

}

// another variant: on the ith line, has data as

// end\_node weight

// when you read data, you can assign matrix as

a[i][x]=t;

// if undirected graph

        a[x][i]=t;

// Initialization of graph !!!IMPORTANT

// Depends on usage, normally initialize as 0 for all elements in matrix.

// so that 0 means no connection, non-0 means connection

// (for problem without weight, use weight as 1)

// If weights are important in this context (especially searching for path)

// Initialize graph as infinity for all elements in matrix.

// Another way to store graph is Adjacency list

// No space advantage if using array (unknown maximum number for in-degree).

// Big space advantage if using dynamic data structure (like list, vector).

// each row represent a node and its connectivity.

// we don’t need it so much due to it’s search efficiency.

// let’s define a node as

        struct Node

{

    int id; // node id

    int w; // weight

};

// suppose n nodes and m lines of inputs as

// start\_node end\_node weight

// assume using <vector> in this example

// g is a vector, and each element of g is also a vector of Node

for (int i=1; i<=m; i++)

{

int x=0, y=0, t=0;

cin >> x >> y >> t;

Node temp;

temp.id=y;

temp.w=t;

g[x].push\_back(temp);

// if undirected

    temp.id=x;

    g[y].push\_back(temp);

}

// Note that you don’t need this node structure if graph has only connectivity information.

/\*\*\*\* Special Structure \*\*\*\*/

// Special structure here is usually not a typical graph, like city-blocks, triangles

// They are represented in 2-d array and shows weights on nodes instead of edges.

// Note that in this case travel through edge has no cost, but visit node has cost.

// Triangles: Read data like this

// 1

// 1 2

// 4 2 7

// 7 3 1 5

// 6 2 9 4 6

for (int i=1; i<=n; i++)

for (int j=i; j<=n; j++)

    cin >> a[i][j];

// Simple city-blocks: it’s just like first form of adjacency matrix, but this time

// represents weights on nodes, may not be square matrix.

// 1 2 4 5 6

// 2 4 5 1 3

// 4 5 2 3 6

        for (int i=1; i<=n; i++)

            for (int j=1; <=m; j++)

                cin >> a[i][j];

// More complex data structures: typical city-block structure may has some constraints on

// questions, but it has no boundaries. However, some questions requires to form a maze.

// In these cases, data structures can be very flexible, it totally depends on how the question

// presents the data. A usual way is to record it’s adjacent blocks information:

                struct Block

        {

            bool l[4]; // if has 8 neighbors then use bool l[8];

// label them as your favor, e.x.

// 1 1 2 3

// 4 x 2 8 x 4

// 3 7 6 5

// true if there is path, false if there is boundary

// other informations (optional)

                int weight;

                int component\_id;

// etc.

            };

// Note that usually we use array from index 1 instead of 0 because sometimes

// you need index 0 as your boundary, and start from index 1 will give you

// advantage on locating nodes or positions

**6.2 Flood fill algorithm**

//component(i) denotes the

//component that node i is in

void flood\_fill(new\_component)

do

    num\_visited = 0

                  for all nodes i

                  if component(i) = -2

                                        num\_visited = num\_visited + 1

                                                component(i) = new\_component

                                                        for all neighbors j of node i

                                                            if component(j) = nil

                                                                        component(j) = -2

                                                                                until num\_visited = 0

                                                                                        void find\_components()

                                                                                        num\_components = 0

                                                                                                for all nodes i

                                                                                                    component(node i) = nil

                                                                                                            for all nodes i

                                                                                                                if component(node i) is nil

                                                                                                                    num\_components = num\_components + 1

                                                                                                                            component(i) = -2

                                                                                                                                    flood\_fill(component num\_components)

**6.3 SPFA — shortest path**

                                                                                                                                    int q[3001]= {0}; // queue for node

                                          int d[1001]= {0}; // record shortest path from start to ith node

                                          bool f[1001]= {0};

                                          int a[1001][1001]= {0}; // adjacency list

                                          int w[1001][1001]= {0}; // adjacency matrix

                                          int main(void)

                        {

                            int n=0, m=0;

                            cin >> n >> m;

                            for (int i=1; i<=m; i++)

                                {

                                    int x=0, y=0, z=0;

                                    cin >> x >> y >> z; // node x to node y has weight z

                                    a[x][0]++;

                                    a[x][a[x][0]]=y;

                                    w[x][y]=z;

                                    /\*

                                    // for undirected graph

                                    a[x][0]++;

                                    a[y][a[y][0]]=x;

                                    w[y][x]=z;

                                    \*/

                                }

                                int s=0, e=0;

                                cin >> s >> e; // s: start, e: end

                                SPFA(s);

                                cout << d[e] << endl;

                                return 0;

                            }

void SPFA(int v0)

{

    int t,h,u,v;

    for (int i=0; i<1001; i++) d[i]=INT\_MAX;

    for (int i=0; i<1001; i++) f[i]=false;

    d[v0]=0;

    h=0;

    t=1;

    q[1]=v0;

    f[v0]=true;

    while (h!=t)

    {

        h++;

        if (h>3000) h=1;

        u=q[h];

        for (int j=1; j<=a[u][0]; j++)

        {

            v=a[u][j];

            if (d[u]+w[u][v]<d[v]) // change to > if calculating longest path

            {

                d[v]=d[u]+w[u][v];

                if (!f[v])

                {

                    t++;

                    if (t>3000) t=1;

                    q[t]=v;

                    f[v]=true;

                }

            }

        }

        f[u]=false;

    }

}

**6.4 Floyd-Warshall algorithm – shortest path of all pairs**

// map[i][j]=infinity at start

void floyd()

{

    for (int k=1; k<=n; k++)

        for (int i=1; i<=n; i++)

            for (int j=1; j<=n; j++)

                if (i!=j && j!=k && i!=k)

                    if (map[i][k]+map[k][j]<map[i][j])

                        map[i][j]=map[i][k]+map[k][j];

}

6.5 Prim — minimum spanning tree

int d[1001]= {0};

             bool v[1001]= {0};

             int a[1001][1001]= {0};

             int main(void)

{

    int n=0;

    cin >> n;

    for (int i=1; i<=n; i++)

    {

        int x=0, y=0, z=0;

        cin >> x >> y >> z;

        a[x][y]=z;

    }

    for (int i=1; i<=n; i++)

        for (int j=1; j<=n; j++)

            if (a[i][j]==0) a[i][j]=INT\_MAX;

    cout << prim(1,n) << endl;

}

int prim(int u, int n)

{

    int mst=0,k;

    for (int i=0; i<d.length; i++) d[i]=INT\_MAX;

    for (int i=0; i<v.length; i++) v[i]=false;

    d[u]=0;

    int i=u;

    while (i!=0)

    {

        v[i]=true;

        k=0;

        mst+=d[i];

        for (int j=1; j<=n; j++)

            if (!v[j])

            {

                if (a[i][j]<d[j]) d[j]=a[i][j];

                if (d[j]<d[k]) k=j;

            }

        i=k;

    }

    return mst;

}

**6.6 Eulerian circuit**

// USACO Fence

#include<iostream>

using namespace std;

int f[100]= {0}, ans[100]= {0};

            bool g[100][100]= {0}, v[100]= {0};

            int n=0, m=0, c=0;

            void dfs(int k)

{

    for (int i=1; i<=n; i++)

        if (g[k][i])

        {

            g[k][i]=false;

            g[i][k]=false;

            dfs(i);

        }

    m++;

    ans[m]=k;

}

int main(void)

{

    cin >> n >> m;

    for (int i=1; i<=m; i++)

    {

        int x=0, y=0;

        g[x][y]=true;

        g[y][x]=true;

        f[x]++;

        f[y]++;

    }

    m=0;

    int k1=0;

    for (int i=1; i<=n; i++)

    {

        if (f[i]%2==1) k1++;

        if (k1>2)

        {

            cout << "error" << endl;

            return 0;

        }

        if (f[i]%2 && c==0) c=i;

    }

    if (c==0) c=1;

    dfs(x);

    for (int i=m; i>=1; i--) cout << ans[i] << endl;

    return 0;

}

**6.7 Topological sort**

// Find any solution of topological sort.

#include<iostream>

using namespace std;

int f[100]= {0}, ans[100]= {0};

            bool g[100][100]= {0}, v[100]= {0};

            int n=0, m=0;

            void dfs(int k)

{

    int i=0;

    v[k]=true;

    for (int i=1; i<=n; i++)

        if (g[k][i] && !v[i]) dfs(i);

    m++;

    ans[m]=k;

}

int main(void)

{

    cin >> n >> m;

    for (int i=1; i<=m; i++)

    {

        int x=0, y=0;

        cin >> x >> y;

        g[y][x]=true;

    }

    m=0;

    for (int i=1; i<=n; i++)

        if (!v[i]) dfs(i);

    for (int i=1; i<=n; i++) cout << ans[i] << endl;

    return 0;

}

**// Find the order of topological sort is dictionary minimum**

#include<iostream>

using namespace std;

int f[100]= {0}, ans[100]= {0};

            bool g[100][100]= {0}, v[100]= {0};

            int n=0, m=0;

            int main(void)

{

    cin >> n >> m;

    for (int i=1; i<=m; i++)

    {

        int x=0, y=0;

        cin >> x >> y;

        g[x][y]=true;

        f[y]++;

    }

    for (int i=1; i<=n; i++)

    {

        for (int j=1; j<=n; j++)

        {

            if (f[j]==0 && !v[j]) break;

            if (f[j]!=0)

            {

                cout << "error" << endl;

                return 0;

            }

            ans[i]=j;

            v[j]=true;

            for (int k=1; k<=n; k++)

                if (g[j][k]) f[k]--;

        }

    }

    for (int i=1; i<=n; i++) cout << ans[i] << endl;

    return 0;

}

**7 Individual Templates**

***7.1 Template by sadiq***

#include <bits/stdc++.h>

using namespace std;

#define int long long

#define db long double

#define vci vector<int>

#define vcb vector<bool>

#define sti set<int>

#define stc set<char>

#define mpi map<int, int>

#define mpib map<int, bool>

#define pri pair<int, int>

#define str string

#define pb push\_back

#define pop pop\_back

#define fr(i, a, n, b) for (int i = a; i < n; i += b)

#define frr(i, a, n, b) for (int i = a; i >= n; i -= b)

#define ato(it, a) for (auto it : a)

#define all(a) a.begin(), a.end()

#define allr(a) a.rbegin(), a.rend()

#define srt(a) sort(all(a))

#define rvrs(a) reverse(all(a))

#define upb(a, x) (upper\_bound(all(a), x) - a.begin())

#define lwb(a, x) (lower\_bound(all(a), x) - a.begin())

#define mxel(a) (max\_element(all(a)) - a.begin())

#define miel(a) (min\_element(all(a)) - a.begin())

#define FAST ios\_base::sync\_with\_stdio(false), cin.tie(NULL), cout.tie(NULL)

#define TC int T;cin >> T;cin.ignore();fr(I, 1, T + 1, 1)

#define endl "\n"

#define yes cout << "YES\n"

#define no cout << "NO\n"

#define p(x) cout << x

#define ps(x) cout << x << " "

#define pl(x) cout << x << "\n"

#define nl cout << "\n"

#define akkas p("Case " << I << ": ");

int32\_t main()

{

    FAST;

    TC

    solve();

    return 0;

}

**//PRIME FACTORIZATION**

vector <int> prime; // Stores generated primes

char sieve[SIZE]; // 0 means prime

void primeSieve ( int n ) {

    sieve[0] = sieve[1] = 1; // 0 and 1 are not prime

    prime.push\_back(2); // Only Even Prime

    for ( int i = 4; i <= n; i += 2 ) sieve[i] = 1; // Remove multiples of 2

    int sqrtn = sqrt ( n );

    for ( int i = 3; i <= sqrtn; i += 2 ) {

        if ( sieve[i] == 0 ) {

            for ( int j = i \* i; j <= n; j += 2 \* i ) sieve[j] = 1;

        }

    }

    for ( int i = 3; i <= n; i += 2 ) if ( sieve[i] == 0 ) prime.push\_back(i);

}

/\*

prime divisor -> p1,p2,p3

p1^a\*p2^b\*p3^c

NOD : (a+1)(b+1)(c+1)

SOD 1: (p1^0+P1^1+..+p1^a)(p2^0+P2^1+..+p2^b)(p3^0+P3^1+..+p3^c)

SOD 2: ((p1^(a+1)-1)/(a-1)) ((p2^(b+1)-1)/(b-1)) ((p3^(c+1)-1)/(c-1))

\*/

int Set(int N, int pos) { return N = N | (1 << pos); }

int reset(int N, int pos){ return N = N & ~ (1 << pos); }

bool check(int N, int pos){ return (bool) (N & (1 << pos)); }

\*/

**//DSU**

#include<bits/stdc++.h>

using namespace std;

int par[100];

//eta parent find korar jonno

int find(int u){

    if(u==par[u]) return u;

    else{

        return par[u]=find(par[u]);

    }

}

//eta duitar parent chack kore join kore

void join(int u,int v){

    int pu=find(u);

    int pv=find(v);

    if(pu!=pv){

        par[pu]=par[pv];//v er parent er parent value update korsi ekhane

    }

}

int main()

{

    int n;

    cin>>n;

    for(int i=1;i<=n;i++) par[i]=i;

    int m;

    cin>>m;

    for(int i=0;i<m;i++){

        int u,v;

        cin>>u>>v;

        join(u,v);

    }

    //shobar parent check korlam

    for(int i=1;i<=n;i++){

        cout<<find(i)<<endl;

    }

}

**///SEGMENT TREE**

/// first u have to build

const int N = 3e5 + 10;

int tree[N << 2];

int arr[N];

void build(int u, int i, int j)

{

if (i == j) /// leap node

{

tree[u] = arr[i];

return;

}

int mid = (i + j) >> 1;

build(2 \* u, i, mid); /// left child

build(2 \* u + 1, mid + 1, j); /// right child

tree[u] = tree[2 \* u] ^ tree[2 \* u + 1]; /// build as per required

}

void update(int u, int i, int j, int idx, int x)

{

if (i == j)

{

tree[u] ^= x; /// here is update as per required

return;

}

int mid = (i + j) >> 1;

if (idx <= mid) update(2 \* u, i, mid, idx, x);

else update(2 \* u + 1, mid + 1, j, idx, x);

tree[u] = tree[2 \* u] ^ tree[2 \* u + 1]; /// ja change hoise , se jonno range gulao update korte hocche

}

int query(int u, int i, int j, int b, int e)

{

if (e < i or j < b) return 0; /// out of required range

if (i >= b and j <= e) return tree[u]; /// range is full inside in required range

int mid = (i + j) >> 1;

int left = query(2 \* u, i, mid, b, e);

int right = query(2 \* u + 1, mid + 1, j, b, e);

return  left ^ right; /// here is operation as per require

}

**Catalan num:**

Cn = C0Cn-1 + C1Cn-2 + C2Cn-3 + … + Cn-1C0

Cn = (2n, n)/(n+1) = (2n)!/((n+1)!n!)

12+22+32+…+n2 = n(n+1)(2n+1)/6

Sum of arith srs Sn = n/2[2a + (n-1)d]

a/sinA = b/sinB = c/sinC = 2R

Circum rad R=(abc)/√((a+b+c)(b+c−a)(c+a−b)(a+b−c))

cosA = (b2+c2-a2)/2bc

///BINARY STRING TO LONG LONG INT

string s = "1001";

long long int xx = stoll(s,0,2)

////

/// PRIME DIVISOR/FACTOR FACTORIZATION

int prime\_divisor\_factorization(int n)

{

    /// 12 = (2^2)\*(3^1) ,so 12's divisor is = (2+1)\*(1+1) = 6;

    vector<int>dd(n + 50, 0);

    dd[1] = 1;

    for (int i = 2; i \* i <= n + 5; i++)

    {

        if (dd[i]) continue;

        for (int j = i + i; j <= n + 5; j += i)

        {

            if (!dd[j]) dd[j] = i; /// inserting into dd[j] j's very first prime divisor;

        }

    }

    rep(i, n + 5) if (!dd[i]) dd[i] = i;///those are not yet fill is prime and prime's first prime divisor is itself;

    int sum = 0;

    for (int i = 1; i <= n; i++)

    {

        int xx = i;

        int d = 1;

        while (xx > 1)

        {

            int yy = dd[xx];///yy is very first prime divisor of xx;

            int ff = 0;

            while (xx % yy == 0) xx /= yy, ff++;

            d \*= (ff + 1);

        }

        sum += i \* d;

    }

    return sum;

}

/// NLOGN DIVISOR COUNT

vector<int>arr(10000005)

for (int i = 1; i < n + 2; i++)

        for (int j = i; j < n + 2; j += i)

            arr[j]++;

///

///DIF 1D

#include <bits/stdc++.h>

using namespace std;

const int N = 1e6 + 100;

int D[N], a[N];

int main() {

    // freopen("in.txt", "r", stdin);

    ios::sync\_with\_stdio(0);

    cin.tie(0);

    int n, q;

    cin >> n >> q;

    while(q--) {

        int l, r;

        cin >> l >> r;

        D[l]++, D[r+1]--;

    }

    for(int i = 1; i <= n; i++) {

        a[i] = a[i-1] + D[i];

    }

    return 0;

}

**/// DIF 2D**

#include <bits/stdc++.h>

using namespace std;

const int N = 2005;

int D[N][N], a[N][N];

int main() {

    int n, m, q;

    cin >> n >> m >> q;

    while(q--) {

        int x1, y1, x2, y2;

        cin >> x1 >> y1 >> x2 >> y2;

        D[x1][y1]++;

        D[x2+1][y2+1]++;

        D[x1][y2+1]--;

        D[x2+1][y1]--;

    }

    for(int x = 1; x <= n; x++) {

        for(int y = 1; y <= m; y++) {

            a[x][y] = a[x][y-1] + a[x-1][y] - a[x-1][y-1] + D[x][y];

        }

    }

    return 0;

}

**/// PREFIX SUM 1D**

#include <bits/stdc++.h>

using namespace std;

const int N = 1e6+100;

int a[N], pref[N];

int main() {

    int n;

    cin >> n;

    for(int i = 1; i <= n; i++) cin >> a[i];

    for(int i = 1; i <= n; i++) {

        pref[i] = pref[i-1] + a[i];

    }

    int q;

    cin >> q;

    while(q--) {

        int l, r;

        cin >> l >> r; // a[l]+a[l+1]+...+a[r]

        cout << pref[r] - pref[l-1] << "\n";

    }

    return 0;

}

**/// PREFIX SUM 2D**

#include <bits/stdc++.h>

using namespace std;

const int N = 2005;

int a[N][N], pref[N][N];

int main() {

    int n, m;

    cin >> n >> m;

    for(int i = 1; i <= n; i++) {

        for(int j = 1; j <= m; j++) {

            cin >> a[i][j];

        }

    }

    // precal

    for(int x = 1; x <= n; x++) {

        for(int y = 1; y <= m; y++) {

            pref[x][y] = a[x][y] + pref[x][y-1] + pref[x-1][y] - pref[x-1][y-1];

        }

    }

    int q;

    cin >> q;

    while(q--) {

        int x1, y1, x2, y2;

        cin >> x1 >> y1 >> x2 >> y2;

        int sum = pref[x2][y2] - pref[x1-1][y2] - pref[x2][y1-1] + pref[x1-1][y1-1];

        cout << sum << "\n";

    }

    return 0;

}

**///HASHING**

#include <bits/stdc++.h>

#define ff first

#define ss second

#define mp make\_pair

using namespace std;

typedef long long LL;

typedef pair<LL, LL> PLL;

const PLL M=mp(1e9+7, 1e9+9);   ///Should be large primes

const LL base=347;              ///Should be a prime larger than highest value

const int N = 1e6+7;            ///Highest length of string

ostream& operator<<(ostream& os, PLL hash) {

    return os<<"("<<hash.ff<<", "<<hash.ss<<")";

}

PLL operator+ (PLL a, LL x)     {return mp(a.ff + x, a.ss + x);}

PLL operator- (PLL a, LL x)     {return mp(a.ff - x, a.ss - x);}

PLL operator\* (PLL a, LL x)     {return mp(a.ff \* x, a.ss \* x);}

PLL operator+ (PLL a, PLL x)    {return mp(a.ff + x.ff, a.ss + x.ss);}

PLL operator- (PLL a, PLL x)    {return mp(a.ff - x.ff, a.ss - x.ss);}

PLL operator\* (PLL a, PLL x)    {return mp(a.ff \* x.ff, a.ss \* x.ss);}

PLL operator% (PLL a, PLL m)    {return mp(a.ff % m.ff, a.ss % m.ss);}

PLL power (PLL a, LL p) {

    if (p==0)   return mp(1,1);

    PLL ans = power(a, p/2);

    ans = (ans \* ans)%M;

    if (p%2)    ans = (ans\*a)%M;

    return ans;

}

///Magic!!!!!!!

PLL inverse(PLL a)  {

    return power(a, (M.ff-1)\*(M.ss-1)-1);

}

PLL pb[N];      ///powers of base mod M

PLL invb;

///Call pre before everything

void hashPre() {

    pb[0] = mp(1,1);

    for (int i=1; i<N; i++)

        pb[i] = (pb[i-1] \* base)%M;

    invb = inverse(pb[1]);

}

///Calculates Hash of a string

PLL Hash (string s) {

    PLL ans = mp(0,0);

    for (int i=0; i<s.size(); i++)

        ans=(ans\*base + s[i])%M;

    return ans;

}

///appends c to string

PLL append(PLL cur, char c) {

    return (cur\*base + c)%M;

}

///prepends c to string with size k

PLL prepend(PLL cur, int k, char c) {

    return (pb[k]\*c + cur)%M;

}

///replaces the i-th (0-indexed) character from right from a to b;

PLL replace(PLL cur, int i, char a, char b) {

    cur = (cur + pb[i] \* (b-a))%M;

    return (cur + M)%M;

}

///Erases c from the back of the string

PLL pop\_back(PLL hash, char c) {

    return (((hash-c)\*invb)%M+M)%M;

}

///Erases c from front of the string with size len

PLL pop\_front(PLL hash, int len, char c) {

    return ((hash - pb[len-1]\*c)%M+M)%M;

}

///concatenates two strings where length of the right is k

PLL concat(PLL left, PLL right, int k) {

    return (left\*pb[k] + right)%M;

}

///Calculates hash of string with size len repeated cnt times

///This is O(log n). For O(1), pre-calculate inverses

PLL repeat(PLL hash, int len, LL cnt) {

    PLL mul = (pb[len\*cnt] - 1) \* inverse(pb[len]-1);

    mul = (mul%M+M)%M;

    PLL ans = (hash\*mul)%M;

    if (pb[len].ff == 1)    ans.ff = hash.ff\*cnt;

    if (pb[len].ss == 1)    ans.ss = hash.ss\*cnt;

    return ans;

}

///Calculates hashes of all prefixes of s including empty prefix

vector<PLL> hashList(string s) {

    int n = s.size();

    vector<PLL> ans(n+1);

    ans[0] = mp(0,0);

    for (int i=1; i<=n; i++)

        ans[i] = (ans[i-1] \* base + s[i-1])%M;

    return ans;

}

///Calculates hash of substring s[l..r] (1 indexed)

PLL substringHash(const vector<PLL> &hashlist, int l, int r) {

    int len = (r-l+1);

    return ((hashlist[r] - hashlist[l-1]\*pb[len])%M+M)%M;

}

///Solves LightOJ 1255-Substring Frequency

///You are given two strings A and B. You have to find

///the number of times B occurs as a substring of A.

char buffer[N];

int main()

{

    hashPre();

    int t;

    scanf("%d", &t);

    for (int cs=1; cs<=t; ++cs)

    {

        string a, b;

        scanf("%s", buffer); a = buffer;

        scanf("%s", buffer); b = buffer;

        int na = a.size(), nb = b.size();

        PLL hb = Hash(b);

        vector<PLL> ha = hashList(a);

        int ans = 0;

        for (int i=1; i+nb-1<=na; i++)

            if (substringHash(ha, i, i+nb-1) == hb)  ans++;

        printf("Case %d: %d\n", cs, ans);

    }

}

**/// TRIE**

const int N = 1e6 + 100;

int tot\_node = 1;

int to[N][26];

int add(string &s) {

    int cur = 1; // root node

    for(int i = 0; i < s.size(); i++) {

        int c = s[i]-'a';

        if(!to[cur][c]) to[cur][c] = ++tot\_node;

        cur = to[cur][c];

    }

    return cur; // leaf node where this string ends

}

///

/// KMP PI TABLE (FUCKING MATERIALS)

vector<int> prefix\_function(string s) /// this will  return kmp pi table

{

    int n = s.size();

    vector<int> pi(n);/// pi[0] = 0, as per kmp condition

    for (int i = 1; i < n; i++)

    {   /// j = prefix length and end at j-1

        int j = pi[i - 1]; /// max prefix matched at i-1

        while (j > 0 and s[i] != s[j]) j = pi[j - 1];

        if (s[i] == s[j]) ++j;

        pi[i] = j;

    }

    return pi;

}

**/// DIGIT DP**

//  How many numbers x are there in the range a to b, where the digit d occurs exactly k times in x?

int a, b, d, k;

vii digit;

int n;

int dp[30][30][3];

/// DP[p][c][f] = Number of valid numbers <= b from this state

/// p = current position from left side (zero based)

/// c = number of times we have placed the digit d so far

/// f = the number we are building has already become smaller than b? [0 = no, 1 = yes]

int call(int idx, int cnt, int f)

{

    if (cnt > k) return 0;

    if (idx >= n) return cnt == k;

    if (dp[idx][cnt][f] != -1) return dp[idx][cnt][f];

    int limit;

    if (!f) limit = digit[idx];

    /// Digits we placed so far matches with the prefix of b

    /// So if we place any digit > num[pos] in the current position, then the number will become greater than b

    else limit = 9;

    /// The number has already become smaller than b. We can place any digit now.

    int xx = 0;

    /// Try to place all the valid digits such that the number doesn't exceed b

    for (int i = 0; i <= limit; i++)

    {

        int cnt1 = 0;

        int ff = f;

        if (!f and i < limit) ff = 1;/// The number is getting smaller at this position

        if (i == d) cnt1 = 1;

        xx += call(idx + 1, cnt + cnt1, ff);

    }

    return dp[idx][cnt][f] = xx;

}

int solve(int x)

{

    mem(dp, -1);

    digit.clear();

    while (x)

    {

        digit.em(x % 10);

        x /= 10;

    }

    reverse(all(digit));

    /// Stored all the digits of x in num for simplicity

    n = digit.size();

    return call(0, 0, 0);

}

signed main()

{

#ifndef ONLINE\_JUDGE

    freopen("input.txt", "r", stdin);

    freopen("output.txt", "w", stdout);

#endif

    cin >> a >> b >> d >> k;

    cout << solve(b) - solve(a - 1) << endll;

}

/////

/// SEGMENT TREE LAZY

const int N = 1e5 + 100;

int tree[N << 2], lz[N << 2];

void propagate(int u, int st, int en)

{

if (!lz[u]) return;

tree[u] += lz[u] \* (en - st + 1);

if (st != en)

{

lz[2 \* u] += lz[u];

lz[2 \* u + 1] += lz[u];

}

lz[u] = 0;

}

void update(int u, int st, int en, int l, int r, int x)

{

propagate(u, st, en);

if (r < st or en < l) return;

else if (st >= l and en <= r)

{

lz[u] += x;

propagate(u, st, en);

}

else

{

int mid = (st + en) >> 1;

update(2 \* u, st, mid, l, r, x);

update(2 \* u + 1, mid + 1, en, l, r, x);

tree[u] = tree[2 \* u] + tree[2 \* u + 1];

}

}

int query(int u, int st, int en, int l, int r)

{

propagate(u, st, en);

if (r < st or en < l) return 0;

else if (st >= l and en <= r) return tree[u];

else

{

int mid = (st + en) >> 1;

int left = query(2 \* u, st, mid, l, r);

int right = query(2 \* u + 1, mid + 1, en, l, r);

return left + right;

}

}

**/// Dijkstra**

const int N = 1e5 + 100;

vector<pii> gra[N];

ll dis[N];

int par[N];

int main()

{

    int node, edge; cin >> node >> edge;

    rep(i, edge)

    {

        int a, b, w; cin >> a >> b >> w;

        gra[a].emplace\_back(b, w);

        gra[b].emplace\_back(a, w);

    }

    priority\_queue<pii> pq;

    rep(i, node) dis[i] = 1e18 + 100;

    int src = 1;

    dis[src] = 0;

    par[1] = -1;

    pq.push ({ -dis[src], src});

    while (pq.size() > 0)

    {

        auto t = pq.top();

        pq.pop();

        int u = t.ss, d = -t.ff;

        if (dis[u] < d) continue;

        for (auto it : gra[u])

        {

            int v = it.ff, w = it.ss;

            if (dis[v] > dis[u] + w)

            {

                dis[v] = dis[u] + w;

                pq.push({ -dis[v], v});

                par[v] = u;

            }

        }

    }

    vector<int>path;

    int xx = node;

    while (xx != -1)

    {

        path.em(xx);

        xx = par[xx];

        if (xx == 0)

        {

            cout << -1;

            return 0;

        }

    }

    reverse(all(path));

    for (int it : path) cout << it << ' ';

}

// dp print

int dp[60][1500];

int dir[60][1500];

int knap(int i,int now)

{

if(i>=cap)

return 0;

if(dp[i][now] != -1)

return dp[i][now];

int t1=0,t2=0;

if(now + arrw[i] <= n)

t1 = arrc[i] + knap(i+1,now+arrw[i]);

t2 = knap(i+1,now);

if(t1>t2)

dir[i][now] = 1;

else

dir[i][now] = 2;

return dp[i][now] = max(t1,t2);

}

vector <int> pri;

void print(int i,int now)

{

if(dir[i][now] == -1)

return;

if(dir[i][now] == 1)

{

pri.push\_back(i);

print(i+1,now+arrw[i]);

}

else

print(i+1,now);

}

***7.2 Template by Faisal***

// typedef long long int;

const int MX = 1e6+5;

#define pii pair<int, int>

template<typename T>

bool comp(T a, T b){//sort by descending

    return a > b;

}

**optimized Sieve(finds (n+1)th prime)**

vector<int> nth\_prime;

bitset<MX> visited;

void optimized\_prime(){

    nth\_prime.push\_back(2);

    for(int i=3; i<MX; i+=2){

            if(visited[i])

                continue;

            nth\_prime.push\_back(i);

            if(1ll\*i\*i > MX)

                continue;

            for(int j = i\*i; j< MX; j+= i+i)

                visited[j] = true;

    }

}

**stores smallest prime divisor of every num from 1 to x**

int spf[MX];

void sieve(){

    for(int i=1; i<MX; ++i)

        spf[i] = i;

    for(int i=2; i\*i<MX; ++i){

        if(spf[i] != i) continue;

        for(int j=i\*i; j<MX; j += i){

            if(spf[j]==j)

                spf[j] = i;

        }

    }

}

map<int, int> mp; **//prime factorization**

void factorize(int n)

{

    while(n != 1){

        mp[spf[n]]++;

        n /= spf[n];

    }

}

**when phi(1) to phi(n) is neeeded**

int phi[MX];

//bitset<MX> visited;// declared before in optimized SIEVE

void sieve\_phi(){

    for(int i=1; i<MX; ++i) phi[i] = i;

    visited[1] = 1;

    for(int i=2; i<MX; ++i){

        if(!visited[i]){

            for(int j = i; j<MX; j+=i){

                visited[j] = 1;

                phi[j] = phi[j]/i\*(i-1);

            }

        }

    }

}

**when only phi(n) is needed**

int phi(int n){ //O(sqrt(n))

    int res = n;

    for(int p=2; p\*p<=n; ++p){

        if(n%p== 0){

            while(n%p == 0)

                n /= p;

            res -= res/p;

        }

    }

    if(n>1) res -= res/n;

    return res;

}

**claculate nCR start**

typedef long long ll;

const int N = 4e5 + 5;

const int MOD = 1e9 + 7;

int fact[N], inv[N], ifact[N];

void init(){

inv[1] = fact[0] = ifact[0] = 1;

for (int i = 2; i < N; i++)

inv[i] = (ll)inv[MOD % i] \*

(MOD - MOD / i) % MOD;

for (int i = 1; i < N; i++)

fact[i] = (ll)fact[i - 1] \* i % MOD;

for (int i = 1; i < N; i++)

ifact[i] = (ll)ifact[i-1] \* inv[i]% MOD;

}

int nCr(int n, int r) {

if (r < 0 or r > n) return 0;

return (ll)fact[n] \* ifact[r] % MOD \* ifact[n - r] % MOD;

}

**// end nCR**

LL ModInv(int a, int M){    //M is prime

    return bigmod(a, M-2, M);

}

***7.3 Template by Rizu***

**Knight Moves**

int X[8]={2,1,-1,-2,-2,-1,1,2};

int Y[8]={1,2,2,1,-1,-2,-2,-1};

**//bit count in O(1)**

int BitCount(unsigned int u){

unsigned int uCount;

uCount = u - ((u >> 1) & 033333333333) - ((u >> 2) & 011111111111);

return ((uCount + (uCount >> 3)) & 030707070707) % 63;

}

**Matrix Exponentiation**

// A technique of computing a number raised to a square matrix in a fast and efficient manner.

// Uses properties of exponentiation and binary numbers for fast computation.

//

// Running time:

// O(m^3\*log(n)) where m is the size of the matrix and n is the power the matrix is being raised to.

//

// INPUT:

// - size of matrix m

// - the matrix A

// - the power n

// - modulo value mod

//

// OUTPUT:

// - the matrix A^n (all values mod m)

//

#include<bits/stdc++.h>

using namespace std;

typedef long long LL;

LL arr[60][60],res[60][60],tmp[60][60],m;

void matMul (LL a[][60], LL b[][60], LL mod)

{

for(int i=0; i<m; i++)

for(int j=0; j<m; j++)

{

tmp[i][j] = 0;

for(int k=0; k<m; k++)

{

tmp[i][j] += (a[i][k]\*b[k][j])%mod;

tmp[i][j] %= mod;

}

}

}

void power(LL n, LL mod)

{

for(int i=0; i<m; i++)

for(int j=0; j<m; j++)

if(i==j) res[i][j] = 1;

else res[i][j] = 0;

while(n)

{

if(n&1)

{

matMul(res,arr,mod);

for(int i=0; i<m; i++)

for(int j=0; j<m; j++) res[i][j] = tmp[i][j];

n--;

}

else

{

matMul(arr,arr,mod);

for(int i=0; i<m; i++)

for(int j=0; j<m; j++) arr[i][j] = tmp[i][j];

n/=2;

}

}

}

// BEGIN CUT

// The following code solves SPOJ problem #MPOW: Power of Matrix

int main()

{

ios\_base::sync\_with\_stdio(false); cin.tie(NULL); cout.tie(NULL);

//freopen("input.txt","r",stdin);freopen("output.txt","w",stdout);

LL t=1, n, mod=1e9+7; cin>>t;

while(t--)

{

cin>>m>>n;

for(int i=0; i<m; i++)

for(int j=0; j<m; j++) cin>>arr[i][j];

power(n,mod);

for(int i=0; i<m; i++)

{

for(int j=0; j<m; j++) cout<<res[i][j]<<" ";

cout<<"\n";

}

}

return 0;

}

// END CUT

**7.4** Given an undirected graph G with n nodes and m edges.We are required to find in it all the connected components,

i.e, several groups of vertices such that within a group each vertex can be reached from another and no path exists between different groups.

// O(n+m)

int n;

vector<int> g[MAXN];

bool used[MAXN];

vector<int> comp;

void dfs(int v)

{

used[v] = true;

comp.push\_back(v);

for (size\_t i = 0; i < (int)g[v].size(); ++i)

{

int to = g[v][i];

if (!used[to])

dfs(to);

}

}

void find\_comps(){

for (int i = 0; i < n; ++i)

used[i] = false;

for (int i = 0; i < n; ++i){

if (!used[i]){

comp.clear();

dfs(i);

cout << "Component:";

for (size\_t j = 0; j < comp.size(); ++j)

cout << ' ' << comp[j];

cout << endl;

}

}

}

**7.5 SCC**

const int N = 1002;

vector<int> adj[N], rev[N];

bitset<N> vis;

int n, m;

int comp[N]; // stores nth node is includedto which scc\_no

void DFS1(int node, stack<int> &TS){

vis[node] = true;

for (int child : adj[node])

if (!vis[child])

DFS1(child, TS);

TS.push(node);

}

void DFS2(int node, const int cc\_no, vector<int> &vec){

vis[node] = true;

comp[node] = cc\_no;

vec.push\_back(node);

for (int child : rev[node])

if (!vis[child])

DFS2(child, cc\_no,

vec);

}

auto SCC(){

vis.reset();

stack<int> TS;

for (int i = 1; i <= n; ++i)

if (!vis[i])

DFS1(i, TS);

// finding the SCCs using TopSort

vis.reset();

int cc\_no = 1;

vector<vector<int>> components;

while (!TS.empty())

{

int idx = TS.top();

TS.pop();

if (!vis[idx])

{

vector<int> vec;

DFS2(idx, cc\_no++, vec);

components.push\_back(vec);

}

}

return components;

}

signed main(){

cin >> n >> m;

for (int i = 0; i < m; ++i){

int u, v;

cin >> u >> v;

// --u, --v;

adj[u].push\_back(v);

rev[v].push\_back(u);

}

auto res = SCC();

int sz = res.size(), scc\_no = 1;

cout << "No. of SCC: " << sz << '\n';

for (auto x : res)

{

cout << "SCC no." << scc\_no++ << " includes nodes : ";

for (auto y : x) cout<<y<<' ';

cout << '\n';

}

}

**no. of ways and min cost of connecting the sccs**

const int MOD = 1e9 + 7, N = 1e5 + 2, INF = 1e18 + 2;

int n, m, comp[N];

vector<int> adj[N], rev[N];

bitset<N> vis;

void DFS1(int u, stack<int> &TS){

vis[u] = true;

for (int v : adj[u])

if (!vis[v])

DFS1(v, TS);

TS.push(u);

}

void DFS2(int u, const int scc\_no, int &min\_cost, int &ways, vector<int> &cost){

vis[u] = true;

comp[u] = scc\_no;

for (int v : rev[u])

if (!vis[v])

{

if (min\_cost == cost[v])

++ways;

else if (min\_cost > cost[v])

{

ways = 1;

min\_cost = cost[v];

}

DFS2(v, scc\_no, min\_cost, ways,

cost);

}

}

signed main(){

FIO cin >> n;

vector<int> cost(n + 1);

for (int i = 1; i <= n; ++i)

cin >> cost[i];

cin >> m;

while (m--){

int u, v;

cin >> u >> v;

adj[u].push\_back(v);

rev[v].push\_back(u);

}

int tot = 0, ways = 1;

stack<int> TS;

for (int i = 1; i <= n; ++i)

if (!vis[i])

DFS1(i, TS);

vis.reset();

int scc\_no = 0;

while (!TS.empty()){

int u = TS.top();

TS.pop();

if (!vis[u]){

int tmp\_cst = cost[u], tmp\_ways = 1;

DFS2(u, ++scc\_no, tmp\_cst,

tmp\_ways, cost);

tot += tmp\_cst;

ways = (ways \* tmp\_ways) % MOD;

}

}

cout << tot << ' ' << ways;

}

**7.6 sqrt decomposition(MO’s Algo)**

// https://www.spoj.com/problems/DQUERY/

#include <bits/stdc++.h>

using namespace std;

const int SIZE\_1 = 1e6 + 10, SIZE\_2 = 3e4 + 10;

class query{

public:

int l, r, indx;

};

int block\_size, cnt = 0;

int frequency[SIZE\_1], a[SIZE\_2];

void add(int indx){

++frequency[a[indx]];

if (frequency[a[indx]] == 1)

++cnt;

}

void sub(int indx){

--frequency[a[indx]];

if (frequency[a[indx]] == 0)

--cnt;

}

bool comp(query a, query b){

if (a.l / block\_size == b.l / block\_size)

return a.r < b.r;

return a.l / block\_size < b.l / block\_size;

}

signed main(){

int n; cin >> n;

for(int i = 0; i < n; ++i) cin>>a[i];

int q; cin >> q;

int ans[q] = {};

query Qur[q];

for (int i = 0; i < q; ++i){

int l, r; cin>>l>>r;

Qur[i].l = l - 1;

Qur[i].r = r - 1;

Qur[i].indx = i;

}

block\_size = sqrt(n); // sqrt(q) dileo hobe, but n is more accurate

sort(Qur, Qur + q, comp);

int ML = 0, MR = -1;

for(int i = 0; i < q; ++i) {

int L = Qur[i].l;

int R = Qur[i].r;

// fixing right pointer

while (MR < R) add(++MR);

while (MR > R) sub(MR--);

// fixiing left pointer

while (ML < L) sub(ML++);

while (ML > L) add(--ML);

ans[Qur[i].indx] = cnt;

}

for (int i = 0; i < q; ++i)

cout << ans[i] << '\n';

}

**7.7 Meet in the middle**

#include <bits/stdc++.h>

using namespace std;

int les\_equal(vector<int> &s, int key){

int siz = s.size();

int lo = 0, hi = siz - 1, ans = 0;

while (hi >= lo){

int mid = lo + (hi - lo) / 2;

if (s[mid] <= key){

ans = max(ans, mid);

lo = mid + 1;

}

else hi = mid - 1;

}

return ans;

}

signed main(){

FIO int n, n1, n2, t;

cin >> n >> t;

n1 = (n + 1) / 2;

n2 = n / 2;

int a1[n1]; for(int &i: a1) cin>>i;

int a2[n2]; for(int &i: a2) cin>>i;

vector<int> set1, set2;

for(int mask=0; mask < (1<<n1); ++mask){

int temp\_sum = 0;

for (int i = 0; i < n1; ++i){

int f = 1 << i;

if (f & mask)

temp\_sum += a1[i];

}

set1.push\_back(temp\_sum);

}

for(int mask=0; mask < (1<<n2); ++mask){

int temp\_sum = 0;

for (int i = 0; i < n2; ++i){

int f = 1 << i;

if (f & mask)

temp\_sum += a2[i];

}

set2.push\_back(temp\_sum);

}

sort(set2.begin(), set2.end());

// for(auto itr: set2) cout<<itr<<' ';

// cout<<'\n';

// for(auto itr: set1) cout<<itr<<' ';

// cout<<'\n';

int ans = 0;

for (auto it : set1){

int left = t - it;

if (left < 0) continue;

int indx = les\_equal(set2, left);

int temp\_sum\_set2 = (indx != -1 ? (it + set2[indx]) : 0);

if (temp\_sum\_set2 <= t)

ans = max(ans, temp\_sum\_set2);

}

cout<<ans;

}

**7.8 PIE(inclusion - exclusion)**

#include <bits/stdc++.h>

using namespace std;

inline int LCM(int a, int b){

return a \* b / \_\_gcd(a, b);

}

int PIE(int div[], int n, int num){

int sum = 0;

for(int msk=1; msk < (1<<n); ++msk){

int bit\_cnt = 0;

int cur\_lcm = 1;

for (int i = 0; i < n; ++i){

if (msk & (1 << i)){

++bit\_cnt;

cur\_lcm = LCM(cur\_lcm, div[i]);

}

}

int cur = num / cur\_lcm;

if (bit\_cnt & 1) sum += cur;

else sum -= cur;

}

return num - sum;

}

signed main(){

int n, m;

while (cin >> n >> m){

int a[m];

for(int &i : a)cin >> i;

cout << PIE(a, m, n) << '\n';

}

}

***Sublime\_ubuntu\_build***

"cmd" : ["g++ -std=c++17 $file\_name -o $file\_base\_name && timeout 4s ./$file\_base\_name<input.txt>output.txt"],

"selector" : "source.cpp",

"shell":true,

"working\_dir" : "$file\_path"

**topic : Expected Value**

If the probability that your candidate will win is strictly greater than W%, print

GET A CRATE OF CHAMPAGNE FROM THE BASEMENT!

If your candidate has no chance of winning,

Print RECOUNT!

Otherwise, print PATIENCE, EVERYONE!

#include <bits/stdc++.h>

using namespace std;

#define err 1e-15

double dp[103][103]; // dp[confirmed votes][unknown votes]

signed main(){

dp[0][0] = 1.0;

for(int i = 1; i < 101; ++i){

for(int j=0; j <= i; ++j){

dp[i][j] += 0.5 \* dp[i - 1][j];

// confirmed vote increased but the vote didn't go to my favour

dp[i][j + 1] += 0.5 \* dp[i - 1][j];

// confirmed vote increased and went to my favour

}

}

TC{

int n, a, b, w;

cin >> n >> a >> b >> w;

int un\_c = n - (a + b);

int flag = 101;

for(int i=0; i <= un\_c; ++i){

if(2\*a + 2\*i > n){

flag = i;

break;

}

}

double sum = 0;

for (int i = flag; i <= un\_c; ++i)

sum += dp[un\_c][i];

sum \*= 100;

sum -= err;

if (sum > w)

cout<<"GET A CRATE OF CHAMPAGNE FROM THE BASEMENT !\n";

else if(flag==101) cout<<"RECOUNT!\n";

else cout<<"PATIENCE,EVERYONE!\n";

}

}

**Chinese Remainder Theorem(Rizu)**

*// CRT Implementation for k Congrunces*

*// Given*

*//      x=a1(mod n1)*

*//      x=a2(mod n2)*

*//      .*

*//      x=at(mod nk)*

*// Find*

*//      x=x0+(u\*LCM(n1,n2,..,nk)) where u= ..,-2,-1,0,1,2,..*

*// Has Solution iff GCD(n1,n2) divides (a2-a1) at each step*

*//*

*// Running time: O(t\*log(LCM(n1,n2,n3,...,nk)))*

*//*

*// INPUT*

*// - a1,a2,a3,...,ak*

*// - n1,n2,n3,...,nk*

*//*

*// OUTPUT*

*// - x0*

*// - LCM(n1,n2,n3,...,nk)*

#include<bits/stdc++.h>

using namespace std;

#define LL long long

LL k;

const LL MAX=1e3+3;

LL arr[MAX],nrr[MAX];

LL normal(LL num, LL mod)

{

    num%=mod;

    if(num<0) num+=mod;

    return num;

}

struct gcdType{LL x,y,d;};

gcdType extGCD(LL a, LL b)

{

    if(b==0) return {1,0,a};

    gcdType puran=extGCD(b,a%b);

    gcdType notun={puran.y,puran.x-a/b\*puran.y,puran.d};

    return notun;

}

*// Kattis #generalchineseremainder: Chinese Remainder Theorem*

int main(){

    cin>>k;

    for(LL i=1; i<=k; i++)

    {

        cin>>arr[i]>>nrr[i];

        arr[i]=normal(arr[i],nrr[i]);

    }

    LL ans=arr[1];

    LL LCM=nrr[1];

    bool flag=true;

    for(LL i=2; i<=k; i++)

    {

        gcdType notun=extGCD(LCM,nrr[i]);

        LL x1=notun.x;

        LL gcd=notun.d;

        if((arr[i]-ans)%gcd) flag=false;

        LL notunLCM=LCM\*nrr[i]/gcd;

        ans=normal(ans+x1\*(arr[i]-ans)/gcd%(nrr[i]/gcd)\*LCM,notunLCM);

        LCM=notunLCM;

    }

    if(flag) cout<<ans<<" "<<LCM<<"\n";

    else cout<<"no solution\n";

    return 0;

}

*// End*