

1. With 3  $n$ -sided rolls, there are  $n^3$  possibilities.

The probability that either of the pair of persons roll the same face of the die is therefore  $n/n^3 = 1/n^2$ .

Therefore

$$\begin{aligned} P(A_{12}) = P(A_{13}) = P(A_{23}) &= \frac{n}{n^3} \\ &= \frac{1}{n^2} \end{aligned}$$

But if both the events  $A_{12}$  and  $A_{13}$  takes place, that is both persons 1 and 2 and persons 1 and 3 roll the same face, then that yields  $A_{23}$ .

That is, if both persons 1 and 2 and persons 1 and 3 roll the same face, then that implies persons 1 and 3 rolled the same face.

But the outcome of person 3's roll is not dependent on the other persons.

That is, pairwise  $A_{12}$  and  $A_{13}$ ,  $A_{12}$  and  $A_{23}$ , and  $A_{13}$  and  $A_{23}$  are independent.

But if considered individually, they are dependent.

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10. The permutations of a word is given by:

$$\frac{(\text{length of word})!}{(\text{repetitions of A})!(\text{repetitions of B})! \dots (\text{repetitions of Z})!}$$

(a) Since there are no repeating characters, the permutation is simply:

$$\begin{aligned}\text{permutations} &= \text{length}(\text{children})! \\ &= 8! \\ &= 40320\end{aligned}$$

□

(b) Since the characters *o* repeats 2 times, *k* repeats 2 times, and *e* repeats 3 times:

$$\begin{aligned}\text{permutations} &= \frac{\text{length}(\text{bookkeeper})!}{(\text{repetitions of o})!(\text{repetitions of k})!(\text{repetitions of e})!} \\ &= \frac{10!}{2!2!3!} \\ &= 151200\end{aligned}$$

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