

Project 1

STAT 355

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1 Part 1

1000 random numbers were generated using a Bernoulli random variable with $n = 20$, $p = 0.4$

```
# initializing variables
x <- 20
N <- 1000
p <- 0.4
generatedData <- rbinom(N, x, p)
```

1.1 Distribution

Distribution of the data was plotted with a histogram using ggplot2 in Figure 1.

```
# plot a histogram
ggplot() + aes(generatedData) +
  geom_histogram(binwidth=1, color="black", fill="white") + labs(y="Count")
```

1.2 Mean, Variance, and Standard Deviation

The mean, variance and standard deviation of the data were computed with the following snippet to generate Table 1:

```
# print out the mean, variance and standard deviation
paste("Mean:", signif(mean(generatedData), digits=4),
      "| Variance:", signif(var(generatedData), digits=4),
      "| Standard Deviation:", signif(sqrt(var(generatedData)), digits=4))
```

Table 1: Statistics		
Mean	Variance	Standard Deviation
8.000	5.000	2.222

1.3 Summary

Summary statistics were generated with the following snippet to generate Table 2:

```
# print out the summary statistics
summary(generatedData)
```

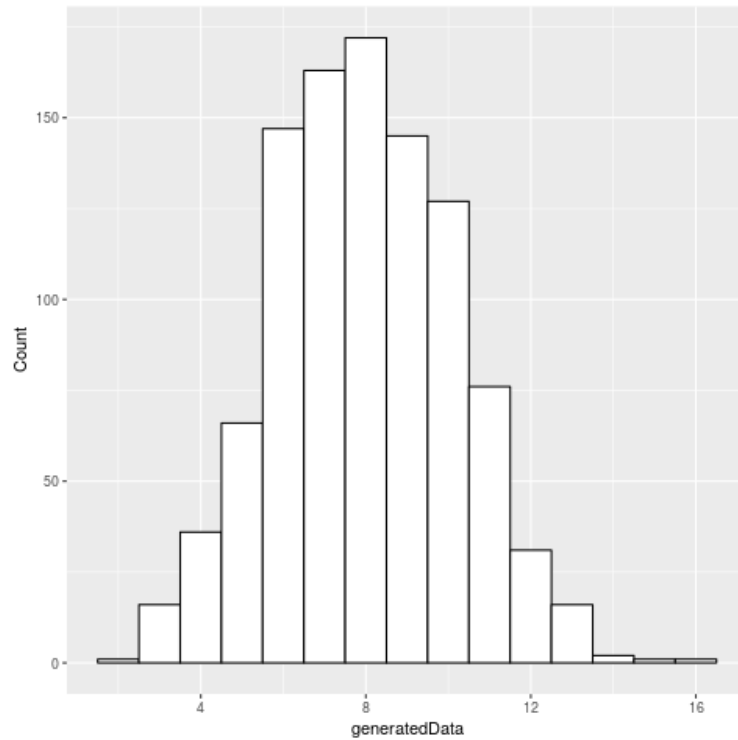


Figure 1: Histogram of the Generated Data

Table 2: Summary Statistics					
Minimum	1st Quar.	Median	Mean	3rd Quar.	Maximum
2.000	6.000	8.000	7.931	9.000	15.000

1.4 Relative Frequencies

The frequencies and relative frequencies of the generate data were computed with the following snippet:

```
# frequencies
fable(generatedData)

# relative frequencies
fable(generatedData)/N
```

The relative frequencies were then plotted in a barplot as in Figure 2:

```
# generate barplot of the relative frequencies
ggplot(data=relfreq, aes(x=generatedData, y=Freq)) +
  geom_bar(color="black", fill="white", stat="identity") +
  labs(y="Relative Frequency")
```

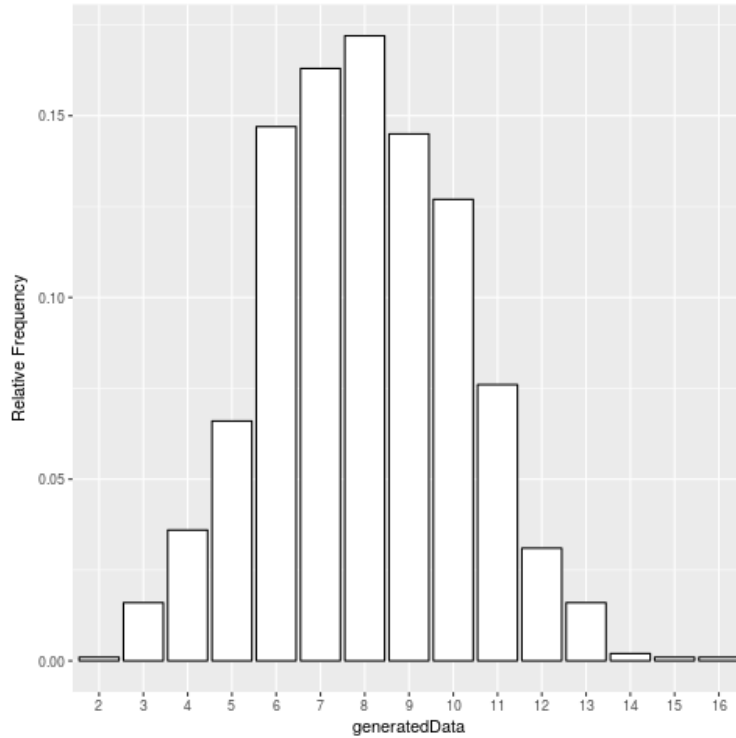


Figure 2: Relative Frequencies of the Generated Data

1.5 Binomial Table

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2 Part 2

A very large batch of components has arrived at a distributor. The batch can be characterized as acceptable only if the proportion of defective components is at most 0.10. The distributor decides to randomly select 10 components and to accept the batch only if the number of defective components in the sample is at most 2.

2.1 Probability

The probabilities of accepting the lot were computed with the proportion of defective components as $p = 0.01, 0.05, 0.10, 0.20, 0.25$.

```
# generate binomial probabilities
signif(pbinom(2, size=10, prob=0.01), digits=4)
signif(pbinom(2, size=10, prob=0.05), digits=4)
signif(pbinom(2, size=10, prob=0.10), digits=4)
signif(pbinom(2, size=10, prob=0.20), digits=4)
signif(pbinom(2, size=10, prob=0.25), digits=4)
```

2.2 Characteristic Curve

The characteristic curve for the acceptance sampling plan was generated as Figure 3 with the following snippet:

```
# plot the charactersitic curve
ggplot(bnomDF, aes(x=p, y=px)) + geom_line() + geom_point(color="red") +
  labs(x="p", y="P(Acceptance)")
```

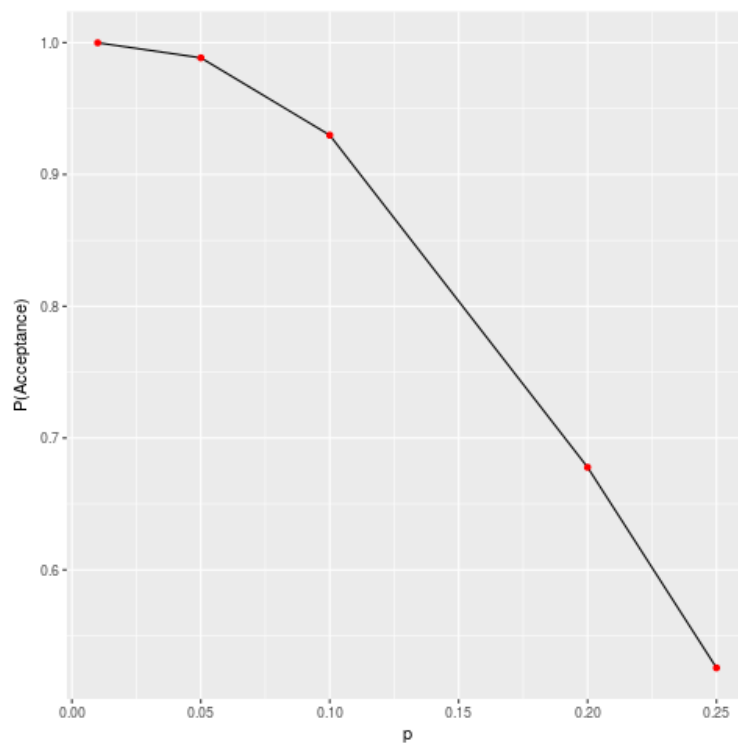


Figure 3: Relative Frequencies of the Generated Data

2.3 Probability with Different Maximum Acceptable Sample

The probabilities of accepting the lot were computed with the same proportions of defective components with the maximum sample changed to 1 and its characteristic curve was plotted as Figure 4

```
# generate binomial probabilities
signif(pbinom(1, size=10, prob=0.01), digits=4)
signif(pbinom(1, size=10, prob=0.05), digits=4)
signif(pbinom(1, size=10, prob=0.10), digits=4)
signif(pbinom(1, size=10, prob=0.20), digits=4)
signif(pbinom(1, size=10, prob=0.25), digits=4)
```

2.4 Probability with Different Sample Size

The probabilities of accepting the lot were computed with the same proportions of defective components with the sample size changed to 15 and its characteristic curve was plotted as Figure 5

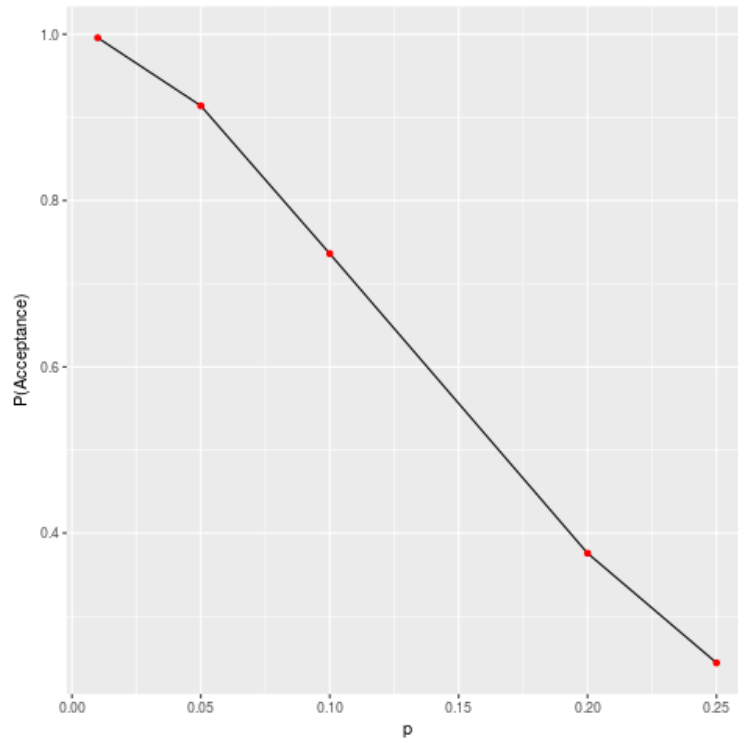


Figure 4: Relative Frequencies of the Generated Data

```
# generate binomial probabilities
signif(pbinom(1, size=15, prob=0.01), digits=4)
signif(pbinom(1, size=15, prob=0.05), digits=4)
signif(pbinom(1, size=15, prob=0.10), digits=4)
signif(pbinom(1, size=15, prob=0.20), digits=4)
signif(pbinom(1, size=15, prob=0.25), digits=4)
```

2.5 Outcomes

The second characteristic curve (part (C), Figure 4) seems to be the most satisfactory because of its near linear relationship between the proportion and their probability.

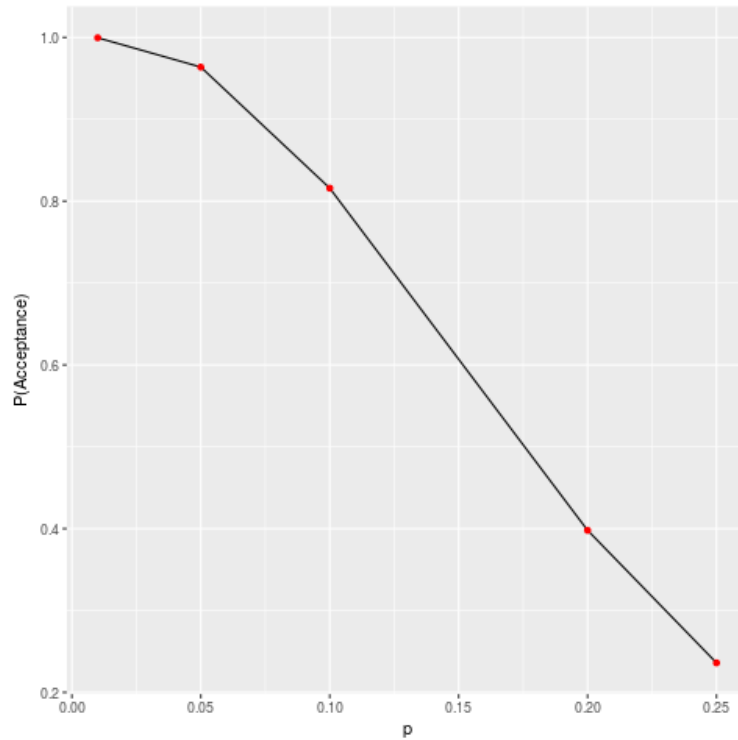


Figure 5: Relative Frequencies of the Generated Data

main.R

```
library(ggplot2)

x <- 20
N <- 1000
p <- 0.4
generatedData <- rbinom(N, x, p)

# a
png(filename="hist.png")
ggplot() + aes(generatedData) +
  geom_histogram(binwidth=1, color="black", fill="white") +
  labs(y="Count")
dev.off()

# b
# print out the mean, variance and standard deviation
paste("Mean:", signif(mean(generatedData), digits=4),
      "| Variance:", signif(var(generatedData), digits=4),
      "| Standard Deviation:", signif(sqrt(var(generatedData)), digits=4)
)

# c
# print out the summary statistics
summary(generatedData)

# d
relfreq <- ftable(generatedData)/N
relfreq <- as.data.frame(relfreq)
png(filename="relfreq.png")
ggplot(data=relfreq, aes(x=generatedData, y=Freq)) +
```

```

    geom_bar(color="black", fill="white", stat="identity") +
    labs(y="Relative Frequency")
dev.off()

# e

# 3.58
# a

# generate binomial probabilities
bnomDF <- data.frame(
  p=c(0.01, 0.05, 0.10, 0.20, 0.25),
  px=c(
    signif(pbinom(2, size=10, prob=0.01), digits=4),
    signif(pbinom(2, size=10, prob=0.05), digits=4),
    signif(pbinom(2, size=10, prob=0.10), digits=4),
    signif(pbinom(2, size=10, prob=0.20), digits=4),
    signif(pbinom(2, size=10, prob=0.25), digits=4)
  )
)
print(bnomDF)

# b

png(filename="charcurve1.png")
ggplot(bnomDF, aes(x=p, y=px)) + geom_line() + geom_point(color="red") +
  labs(x="p", y="P(Acceptance)")
dev.off()

# c

bnomDF <- data.frame(
  p=c(0.01, 0.05, 0.10, 0.20, 0.25),
  px=c(
    signif(pbinom(1, size=10, prob=0.01), digits=4),
    signif(pbinom(1, size=10, prob=0.05), digits=4),
    signif(pbinom(1, size=10, prob=0.10), digits=4),
    signif(pbinom(1, size=10, prob=0.20), digits=4),
    signif(pbinom(1, size=10, prob=0.25), digits=4)
  )
)
print(bnomDF)

png(filename="charcurve2.png")
ggplot(bnomDF, aes(x=p, y=px)) + geom_line() + geom_point(color="red") +
  labs(x="p", y="P(Acceptance)")
dev.off()

# d

bnomDF <- data.frame(
  p=c(0.01, 0.05, 0.10, 0.20, 0.25),
  px=c(
    signif(pbinom(2, size=15, prob=0.01), digits=4),
    signif(pbinom(2, size=15, prob=0.05), digits=4),
    signif(pbinom(2, size=15, prob=0.10), digits=4),
    signif(pbinom(2, size=15, prob=0.20), digits=4),
    signif(pbinom(2, size=15, prob=0.25), digits=4)
  )
)
print(bnomDF)

png(filename="charcurve3.png")
ggplot(bnomDF, aes(x=p, y=px)) + geom_line() + geom_point(color="red") +
  labs(x="p", y="P(Acceptance)")
dev.off()

```
