Name:

1. (10 points) The algorithm P-Sum computes the sum of the elements of an array L of length n. Draw the DAG for P-Sum when L is an array of length 8. Determine the work, span, and parallelism from the DAG. Show all work.

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\begin{array}{ll} \operatorname{P-Sum}(L) \\ 1 & n = L.\operatorname{length} \\ 2 & \text{if } n == 1 \\ 3 & \text{return } L[1] \\ 4 & c = \lfloor n/2 \rfloor \\ 5 & x = \operatorname{spawn} \operatorname{P-Sum}(L[1 \ldots c]) \\ 6 & y = \operatorname{P-Sum}(L[c+1 \ldots n]) \\ 7 & \text{sync} \\ 8 & \operatorname{return } x + y \end{array}
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2. (10 points) The algorithm MAT-VEC computes the product of an n-by-n matrix A and an n-long vector x:

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\begin{array}{lll} \operatorname{Mat-Vec}(A) \\ 1 & n = A. \, rows \\ 2 & \operatorname{let} \, y \, \operatorname{be} \, \operatorname{a} \, \operatorname{new} \, \operatorname{vector} \, \operatorname{of} \, \operatorname{length} \, n \\ 3 & \operatorname{\mathbf{parallel}} \, \operatorname{\mathbf{for}} \, i = 1 \, \operatorname{\mathbf{to}} \, n \\ 4 & y_i = 0 \\ 5 & \operatorname{\mathbf{parallel}} \, \operatorname{\mathbf{for}} \, i = 1 \, \operatorname{\mathbf{to}} \, n \\ 6 & \operatorname{\mathbf{for}} \, \operatorname{\mathbf{new}} \, j = 1 \, \operatorname{\mathbf{to}} \, n \\ 7 & y_i = y_i + a_{ij} \cdot x_j \\ 8 & \operatorname{\mathbf{return}} \, y \end{array}
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Determine the work, span, and parallelism of MAT-VEC. What is the parallel slackness when n=256 and P=16? Show all work and any formulas used.