**CMPE 323: Signals and Systems**

**Dr. LaBerge**

**Lab 06 Report**

**Fourier Series and the Gibbs Phenomenon**

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6. **Introduction**

This lab explores the computation of the complex coefficients of a Fourier Series by direction computation and by evaluation of the analytical answer obtained in class.

1. **Equipment**

A computer with MATLAB installed.

1. **Procedure**
   1. **Computing the Coefficients**

Create an “infinite” square wave with the following functions:

where and is the duration of the pulse. Plot at least 7 periods of the periodic waveform using a sample rate of 10,000 sps. Is this waveform even or odd? Plot the waveform using professional practices.

Analytically compute the Fourier coefficients given by the analysis equation:

Write the closed form, simplified expression for the coefficients as a function of and .

Using the simulated x(t) developed above, numerically compute the coefficients for x(t) implementing 3. Compute the range and hold onto it for future use. Your answer will be complex. Examine the imaginary part and determine if it contributes to the answer. Based on your conclusion, plot the computed values and the theoretical values and compare them.

* 1. **Synthesizing the Waveform**

Using the computed in 3.1, synthesize an estimate of your periodic waveform over the full interval. The synthesis equation is:

where controls the number of terms in the estimate.

Compute estimates for *.* For each estimate, plot the real part of the estimate and the original waveform, . Comment on any differences.

For each estimate, compute the mean squared error (MSE) defined by

Plot the estimates as a function of .

* 1. **The Gibbs Phenomenon**

The finite sum estimate, , of the square wave exhibits a characteristic shape known as the Gibbs Phenomenon. This characteristic occurs whenever a limited number of Fourier coefficients (or a bandlimited Fourier Transform) is used to estimate a piecewise continuous time waveform. On a single plot, show the Gibbs Phenomenon for all of your *K*-limited estimates of the square wave by plotting only the region . Comment on the shape and extent of the Gibbs phenomenon as the number of terms in the sum increases.

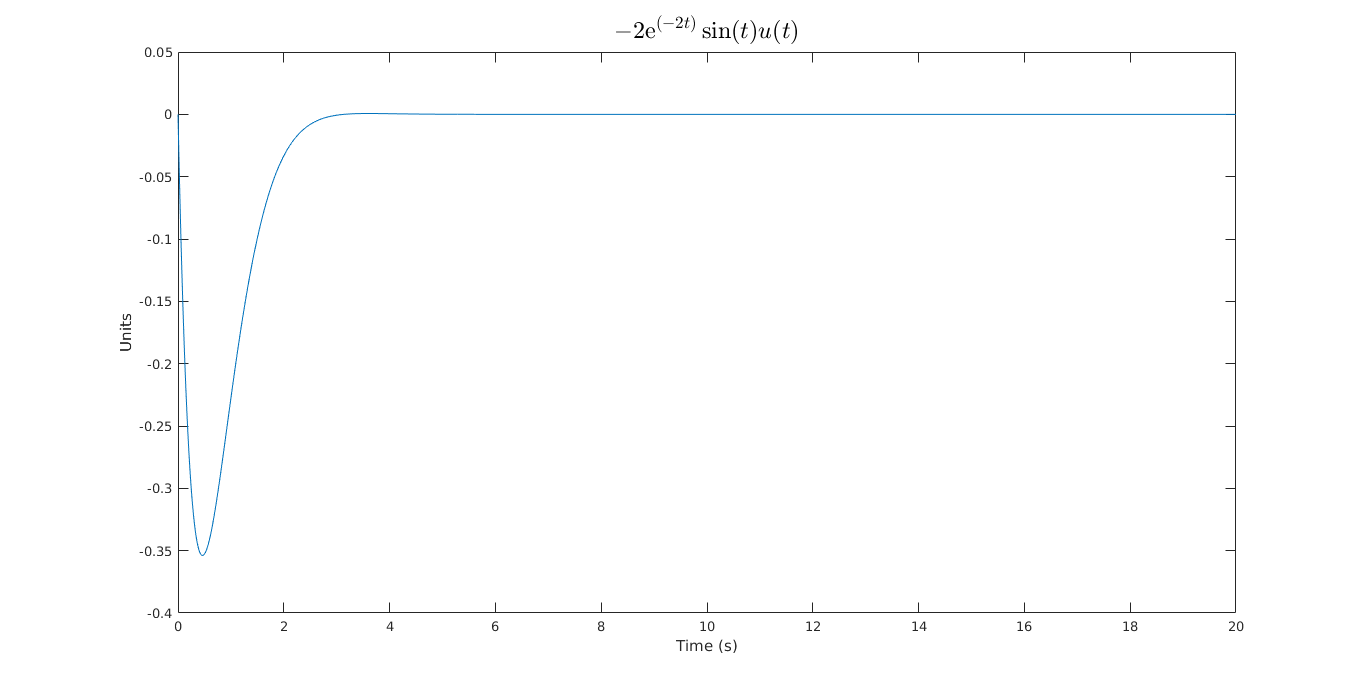
* 1. **A Different Waveform**

Create a new waveform,

where . This produces a periodic saw-tooth wave. Repeat the process used in 3.1 and 3.2 to synthesize from K-sums of the Fourier coefficients. Comment on any Gibbs phenomenon effects on your estimates.

1. **Results**

The output suggests only one pair of complex conjugate pair as the partial fraction expansion. Therefore, there was only one component of the impulse response, plotted below:



**Figure 5: The Impulse Response of the Second Transfer Function**

1. **Appendices**
   1. **Appendix A**

Please refer to the attached script as Appendix A. The definition and documentation of the function polezero\_plot() that was used for the entire lab is located there.