

array : 0 2 5 1 8 14

$\overset{2}{\text{---}} \overset{3}{\text{---}} \overset{-4}{\text{---}} \overset{7}{\text{---}} \overset{6}{\text{---}}$

Difference

prefix : 2 $2+3=5$ $5-4=1$ $1+7=8$ $8+6=14$

আমরা difference জানা থাকায় Array restore
করতে পেরেছি।

Range update using naive approach

array : 2 5 1 8 14

queries :

| | | |
|---|---|---|
| 1 | 4 | 2 |
| 2 | 5 | 6 |
| 1 | 5 | 3 |

 } (from, to, value)
* 1-based index

array : 2 5 1 8 14

$+2$ $+2$ $+2$ $+2$

$+6$ $+6$ $+6$ $+6$

$+3$ $+3$ $+3$ $+3$ $+3$

* naive

updated array : 7 16 12 19 23

Complexity : $O(n \times q) \rightarrow O(n^2)$

Difference array for efficient range updates

Task₁: 1-4 Range এ 2 যোগ করা।

array :

| | | | | | |
|---|---|---|---|---|----|
| 0 | 2 | 5 | 1 | 8 | 14 |
|---|---|---|---|---|----|

 → একটি কোষে
বৈধি নব
(কঃ effect নাই)

difference :

| | | | | | | |
|---|----|---|---|---|----|---|
| 0 | +2 | 0 | 0 | 0 | -2 | 0 |
|---|----|---|---|---|----|---|

pref :

Task₂:

| | | |
|---|---|---|
| 1 | 4 | 2 |
| 2 | 5 | 6 |
| 2 | 4 | 3 |

 } → l, r, value

original array:

| | | | | | |
|---|---|---|---|---|----|
| 0 | 2 | 5 | 1 | 8 | 14 |
|---|---|---|---|---|----|

 → একটি কোষে
বৈধি নব

difference array :

| | | | | | | |
|---|----|--------|---|---|--------|----|
| 0 | +2 | +(6+3) | 0 | 0 | -(2-3) | -6 |
|---|----|--------|---|---|--------|----|

prefix :

| | | | | | | |
|---|---|----|---|---|----|----|
| 0 | 2 | 11 | 0 | 0 | -5 | -6 |
|---|---|----|---|---|----|----|

(arr + prefix) : 0 4 16 12 10 20 → কাজ নাই

Observation: $O(1)$ এ আমরা সবগুলো value কে
update করে দিচ্ছি। সবার ক্ষেত্রে $O(n)$ এ array
আপডেট করে দিবা।

$O(nr) \rightarrow O(n)$
// optimized

summary

- * স্ক্যান করে (1-based index)
- * difference array \rightarrow diff (n+2)
2টা index বেশি নিব।
- * prefix sum \rightarrow pref (n+2)

```
1  vector<int> v(n+1); // let, initialized with values
2      vector<int> diff(n+2), pref(n+2);
3
4      for (int i = 1; i <= q; i++)
5      {
6          int l, r, data; cin >> l >> r >> data;
7
8          diff[l] += data;
9          diff[r + 1] -= data;
10     }
11
12     for (int i = 1; i <= n; i++)
13     {
14         pref[i] = pref[i-1] + diff[i];
15     }
16
17     for (int i = 1; i <= n; i++)
18     {
19         cout << v[i] + pref[i] << ' ';
20     }
21     cout << nl;
```