



CSE260: Digital Logic Design
Summer 2025
Quiz - 01
Duration: 20 minutes

A

Name: <u>Solution</u>	ID:	Section:
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1.CO1	Multiply $(1BE)_{16}$ by $(13)_8$. Must show your workings and answer in base-8.	5
2.CO1	Add $(42)_{10}$ and $-(85)_{10}$ in 10 bits using 1's complement number system. Justify whether there is an overflow or not.	5
3.CO1	Suppose you are organizing a charity event with $(1D5)_{16}$ other students. Each person, including yourself, donates $(13)_8$ taka. Then you used the money to spend $(42143)_5$ on food. How much money was left after paying all the expenses? Show your answer in decimal.	5

$$1) (1BE)_{16} = 000110111110 \\ = (0676)_8$$

$$\begin{array}{r} 2^2 \quad 2^2 \\ 2 \quad 6 \quad 7 \quad 6 \\ \times \quad 13 \\ \hline 1 \quad 1 \quad 2 \quad 4 \quad 7 \quad 2 \\ 6 \quad 7 \quad 6 \quad \times \\ \hline 1 \quad 1 \quad 4 \quad 5 \quad 2 \end{array}$$

Ans: $(11452)_8$

$$\begin{array}{r} 2 \\ 8 \overline{) 16} \\ \underline{-16} \\ 2 \end{array} \quad \begin{array}{r} 2 \\ 8 \overline{) 23} \\ \underline{-16} \\ 7 \end{array}$$

$$\begin{array}{r} 2 \\ 8 \overline{) 20} \\ \underline{-16} \\ 4 \end{array} \quad \begin{array}{r} 1 \\ 8 \overline{) 13} \\ \underline{-8} \\ 5 \end{array}$$

$$\begin{array}{r} 1 \\ 8 \overline{) 12} \\ \underline{-8} \\ 4 \end{array} \quad \begin{array}{r} 1 \\ 8 \overline{) 9} \\ \underline{-8} \\ 1 \end{array}$$

$$2) \begin{array}{r} 2 \overline{) 42} \\ 2 \overline{) 21} \quad 0 \\ 2 \overline{) 10} \quad 1 \\ 2 \overline{) 5} \quad 0 \\ 2 \overline{) 2} \quad 1 \\ 2 \overline{) 1} \quad 0 \\ 0 \quad 1 \end{array}$$

$$(42)_{10} = (101010)_2$$

$$+42 \\ \text{in 10-bits} = (0000101010)_{10}$$

$$\begin{array}{r} 2 \overline{) 85} \\ 2 \overline{) 42} \quad 1 \\ 2 \overline{) 21} \quad 0 \\ 2 \overline{) 10} \quad 1 \\ 2 \overline{) 5} \quad 0 \\ 2 \overline{) 2} \quad 1 \\ 2 \overline{) 1} \quad 0 \\ 0 \quad 1 \end{array}$$

$$(85)_{10} = (1010101)_2$$

$$+85 \\ \text{in 10-bits} = (0001010101)_{10} \\ -85 = (1110101010)_{10}$$

$$\begin{array}{r}
 0000^1 1010^1 10 \\
 + 11101010^1 10 \\
 \hline
 (1111010100)_{15}
 \end{array}$$

Result $\rightarrow (1111010100)_{15}$

No overflow, since we are adding two different signed numbers.

$$3) (1DS)_{16} = 1 \times 16^2 + 13 \times 16^1 + 5 \times 16^0 = (469)_{10}$$

$$\text{Total students} = 469 + 1 = 470$$

$$\text{Each person} = (13)_6 = 1 \times 6^1 + 3 \times 6^0 = (9)_{10}$$

contributes

$$\text{Total money} = 470 \times 9 = (4230)_{10}$$

$$\begin{aligned}
 \text{food} &= (42143)_5 = 4 \times 5^4 + 2 \times 5^3 + 1 \times 5^2 + 4 \times 5^1 + 3 \times 5^0 \\
 &= (2798)_{10}
 \end{aligned}$$

$$\begin{aligned}
 \text{Total } \del{money} &= 4230 - 2798 \\
 \text{money left} &= (1432)_{10} \text{ taka}
 \end{aligned}$$