

Python Basics with Numpy (optional assignment)

Welcome to your first assignment. This exercise gives you a brief introduction to Python. Even if you've used Python before, this will help familiarize you with functions we'll need.

Instructions:

- You will be using Python 3.
- Avoid using for-loops and while-loops, unless you are explicitly told to do so.
- Do not modify the (# GRADED FUNCTION [function name]) comment in some cells.
Your work would not be graded if you change this. Each cell containing that comment should only contain one function.
- After coding your function, run the cell right below it to check if your result is correct.

After this assignment you will:

- Be able to use iPython Notebooks
- Be able to use numpy functions and numpy matrix/vector operations
- Understand the concept of "broadcasting"
- Be able to vectorize code

Let's get started!

About iPython Notebooks

iPython Notebooks are interactive coding environments embedded in a webpage. You will be using iPython notebooks in this class. You only need to write code between the `### START CODE HERE ###` and `### END CODE HERE ###` comments. After writing your code, you can run the cell by either pressing "SHIFT"+"ENTER" or by clicking on "Run Cell" (denoted by a play symbol) in the upper bar of the notebook.

We will often specify "(≈ X lines of code)" in the comments to tell you about how much code you need to write. It is just a rough estimate, so don't feel bad if your code is longer or shorter.

Exercise: Set test to "Hello World" in the cell below to print "Hello World" and run the two cells below.

In []:

```
### START CODE HERE ### (≈ 1 line of code)  
test = None  
### END CODE HERE ###
```

In []:

```
print ("test: " + test)
```

Expected output: test: Hello World

What you need to remember:

- Run your cells using SHIFT+ENTER (or "Run cell")
- Write code in the designated areas using Python 3 only
- Do not modify the code outside of the designated areas

1 - Building basic functions with numpy

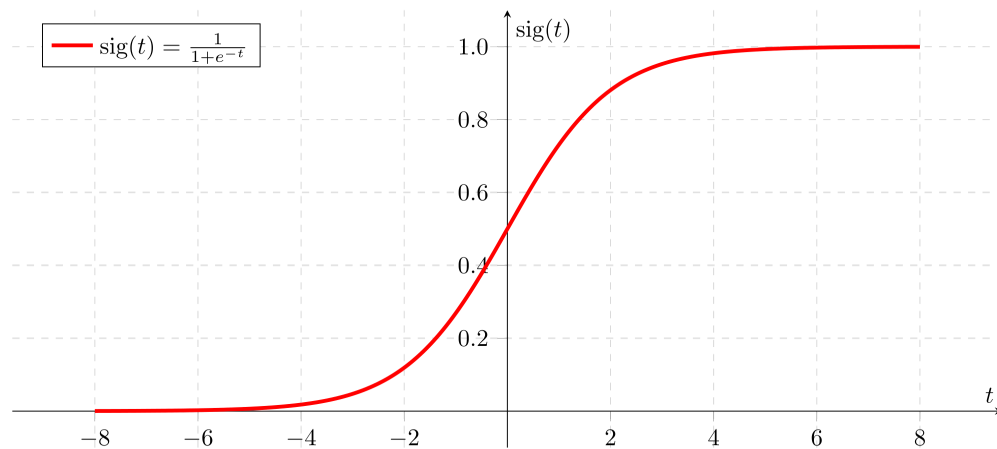
Numpy is the main package for scientific computing in Python. It is maintained by a large community (www.numpy.org). In this exercise you will learn several key numpy functions such as `np.exp`, `np.log`, and `np.reshape`. You will need to know how to use these functions for future assignments.

1.1 - sigmoid function, `np.exp()`

Before using `np.exp()`, you will use `math.exp()` to implement the sigmoid function. You will then see why `np.exp()` is preferable to `math.exp()`.

Exercise: Build a function that returns the sigmoid of a real number x . Use `math.exp(x)` for the exponential function.

Reminder: $\text{sigmoid}(x) = \frac{1}{1+e^{-x}}$ is sometimes also known as the logistic function. It is a non-linear function used not only in Machine Learning (Logistic Regression), but also in Deep Learning.



To refer to a function belonging to a specific package you could call it using `package_name.function()`. Run the code below to see an example with `math.exp()`.

In [1]:

```
# GRADED FUNCTION: basic_sigmoid

import math

def basic_sigmoid(x):
    """
    Compute sigmoid of x.

    Arguments:
    x -- A scalar

    Return:
    s -- sigmoid(x)
    """

    ### START CODE HERE ### (≈ 1 line of code)
    s = 1/(1+math.exp(-x))
    ### END CODE HERE ###

    return s
```

In [2]:

```
basic_sigmoid(3)
```

Out[2]:

```
0.9525741268224334
```

Expected Output:

<code>basic_sigmoid(3)</code>	0.9525741268224334
-------------------------------	--------------------

Actually, we rarely use the "math" library in deep learning because the inputs of the functions are real numbers. In deep learning we mostly use matrices and vectors. This is why numpy is more useful.

In [3]:

```
### One reason why we use "numpy" instead of "math" in Deep Learning ###
x = [1, 2, 3]
basic_sigmoid(x) # you will see this give an error when you run it, because x is a vector.
```

```
-----
-----
TypeError                                 Traceback (most recent
  call last)
<ipython-input-3-2e11097d6860> in <module>()
      1 ### One reason why we use "numpy" instead of "math" in D
deep Learning ###
      2 x = [1, 2, 3]
----> 3 basic_sigmoid(x) # you will see this give an error when
you run it, because x is a vector.

<ipython-input-1-951c5721dbfa> in basic_sigmoid(x)
     15
     16     ### START CODE HERE ### (= 1 line of code)
----> 17     s = 1/(1+math.exp(-x))
     18     ### END CODE HERE ###
     19
```

TypeError: bad operand type for unary -: 'list'

In fact, if $x = (x_1, x_2, \dots, x_n)$ is a row vector then $np.exp(x)$ will apply the exponential function to every element of x . The output will thus be: $np.exp(x) = (e^{x_1}, e^{x_2}, \dots, e^{x_n})$

In [4]:

```
import numpy as np

# example of np.exp
x = np.array([1, 2, 3])
print(np.exp(x)) # result is (exp(1), exp(2), exp(3))

[ 2.71828183  7.3890561  20.08553692]
```

Furthermore, if x is a vector, then a Python operation such as $s = x + 3$ or $s = \frac{1}{x}$ will output s

as a vector of the same size as x.

In [5]:

```
# example of vector operation
x = np.array([1, 2, 3])
print (x + 3)
```

[4 5 6]

Any time you need more info on a numpy function, we encourage you to look at [the official documentation \(https://docs.scipy.org/doc/numpy-1.10.1/reference/generated/numpy.exp.html\)](https://docs.scipy.org/doc/numpy-1.10.1/reference/generated/numpy.exp.html).

You can also create a new cell in the notebook and write `np.exp?` (for example) to get quick access to the documentation.

Exercise: Implement the sigmoid function using numpy.

Instructions: x could now be either a real number, a vector, or a matrix. The data structures we use in numpy to represent these shapes (vectors, matrices...) are called numpy arrays. You don't need to know more for now.

$$\text{For } x \in \mathbb{R}^n, \text{sigmoid}(x) = \text{sigmoid} \begin{pmatrix} x_1 \\ x_2 \\ \dots \\ x_n \end{pmatrix} = \begin{pmatrix} \frac{1}{1+e^{-x_1}} \\ \frac{1}{1+e^{-x_2}} \\ \dots \\ \frac{1}{1+e^{-x_n}} \end{pmatrix} \quad (1)$$

In [6]:

```
# GRADED FUNCTION: sigmoid

import numpy as np # this means you can access numpy functions by writing np.fu

def sigmoid(x):
    """
    Compute the sigmoid of x

    Arguments:
    x -- A scalar or numpy array of any size

    Return:
    s -- sigmoid(x)
    """

    ### START CODE HERE ### (= 1 line of code)
    s = 1/(1+np.exp(-x))
    ### END CODE HERE ###

    return s
```

In [7]:

```
x = np.array([1, 2, 3])
sigmoid(x)
```

Out[7]:

```
array([ 0.73105858,  0.88079708,  0.95257413])
```

Expected Output:

<code>sigmoid([1,2,3])</code>	<code>array([0.73105858, 0.88079708, 0.95257413])</code>
-------------------------------	---

1.2 - Sigmoid gradient

As you've seen in lecture, you will need to compute gradients to optimize loss functions using backpropagation. Let's code your first gradient function.

Exercise: Implement the function `sigmoid_grad()` to compute the gradient of the sigmoid function with respect to its input x . The formula is:

$$\text{sigmoid_derivative}(x) = \sigma'(x) = \sigma(x)(1 - \sigma(x)) \quad (2)$$

You often code this function in two steps:

1. Set s to be the sigmoid of x . You might find your `sigmoid(x)` function useful.

2. Compute $\sigma'(x) = s(1 - s)$

In [14]:

```
# GRADED FUNCTION: sigmoid_derivative

def sigmoid_derivative(x):
    """
    Compute the gradient (also called the slope or derivative) of the sigmoid function.
    You can store the output of the sigmoid function into variables and then use them.

    Arguments:
    x -- A scalar or numpy array

    Return:
    ds -- Your computed gradient.
    """

    ### START CODE HERE ### (= 2 lines of code)
    s = 1/(1+np.exp(-x))
    ds = s*(1-s)
    ### END CODE HERE ###

    return ds
```

In [15]:

```
x = np.array([1, 2, 3])
print ("sigmoid_derivative(x) = " + str(sigmoid_derivative(x)))
```

```
sigmoid_derivative(x) = [ 0.19661193  0.10499359  0.04517666]
```

Expected Output:

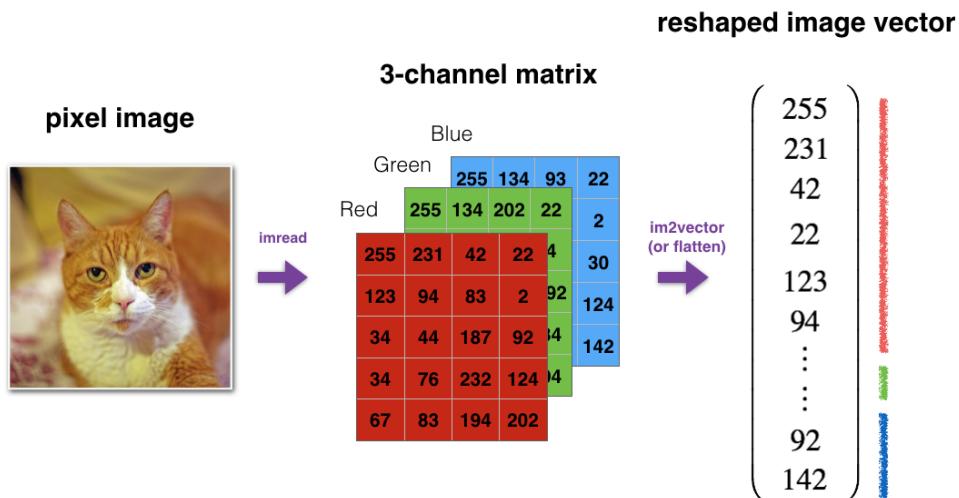
<code>sigmoid_derivative([1,2,3])</code>	<code>[0.19661193 0.10499359 0.04517666]</code>
--	--

1.3 - Reshaping arrays

Two common numpy functions used in deep learning are `np.shape` (<https://docs.scipy.org/doc/numpy/reference/generated/numpy.ndarray.shape.html>) and `np.reshape()` (<https://docs.scipy.org/doc/numpy/reference/generated/numpy.reshape.html>).

- `X.shape` is used to get the shape (dimension) of a matrix/vector `X`.
- `X.reshape(...)` is used to reshape `X` into some other dimension.

For example, in computer science, an image is represented by a 3D array of shape $(length, height, depth = 3)$. However, when you read an image as the input of an algorithm you convert it to a vector of shape $(length * height * 3, 1)$. In other words, you "unroll", or reshape, the 3D array into a 1D vector.



Exercise: Implement `image2vector()` that takes an input of shape $(length, height, 3)$ and returns a vector of shape $(length * height * 3, 1)$. For example, if you would like to reshape an array `v` of shape (a, b, c) into a vector of shape $(a * b, c)$ you would do:

```
v = v.reshape((v.shape[0]*v.shape[1], v.shape[2])) # v.shape[0] = a ;
v.shape[1] = b ; v.shape[2] = c
```

- Please don't hardcode the dimensions of image as a constant. Instead look up the quantities you need with `image.shape[0]`, etc.

In [26]:

```
# GRADED FUNCTION: image2vector
def image2vector(v):
    """
    Argument:
    image -- a numpy array of shape (length, height, depth)

    Returns:
    v -- a vector of shape (length*height*depth, 1)
    """

    ### START CODE HERE ### (= 1 line of code)
    v = v.reshape((v.shape[0]* v.shape[1]* v.shape[2], 1))
    ### END CODE HERE ###

    return v
```

In [27]:

```
# This is a 3 by 3 by 2 array, typically images will be (num_px_x, num_px_y, 3)
image = np.array([[[ 0.67826139,  0.29380381],
                    [ 0.90714982,  0.52835647],
                    [ 0.4215251 ,  0.45017551]],

                  [[ 0.92814219,  0.96677647],
                    [ 0.85304703,  0.52351845],
                    [ 0.19981397,  0.27417313]],

                  [[ 0.60659855,  0.00533165],
                    [ 0.10820313,  0.49978937],
                    [ 0.34144279,  0.94630077]]])

print ("image2vector(image) = " + str(image2vector(image)))
```

```
image2vector(image) = [[ 0.67826139]
 [ 0.29380381]
 [ 0.90714982]
 [ 0.52835647]
 [ 0.4215251 ]
 [ 0.45017551]
 [ 0.92814219]
 [ 0.96677647]
 [ 0.85304703]
 [ 0.52351845]
 [ 0.19981397]
 [ 0.27417313]
 [ 0.60659855]
 [ 0.00533165]
 [ 0.10820313]
 [ 0.49978937]
 [ 0.34144279]
 [ 0.94630077]]
```

Expected Output:

image2vector(image)	[[0.67826139] [0.29380381] [0.90714982] [0.52835647] [0.4215251] [0.45017551] [0.92814219] [0.96677647] [0.85304703] [0.52351845] [0.19981397] [0.27417313] [0.60659855] [0.00533165] [0.10820313] [0.49978937] [0.34144279] [0.94630077]]
----------------------------	--

1.4 - Normalizing rows

Another common technique we use in Machine Learning and Deep Learning is to normalize our data. It often leads to a better performance because gradient descent converges faster after normalization. Here, by normalization we mean changing x to $\frac{x}{\|x\|}$ (dividing each row vector of x by its norm).

For example, if

$$x = \begin{bmatrix} 0 & 3 & 4 \\ 2 & 6 & 4 \end{bmatrix} \quad (3)$$

then

$$\|x\| = np.linalg.norm(x, axis = 1, keepdims = True) = \begin{bmatrix} 5 \\ \sqrt{56} \end{bmatrix} \quad (4)$$

and

$$x_{normalized} = \frac{x}{\|x\|} = \begin{bmatrix} 0 & \frac{3}{5} & \frac{4}{5} \\ \frac{2}{\sqrt{56}} & \frac{6}{\sqrt{56}} & \frac{4}{\sqrt{56}} \end{bmatrix} \quad (5)$$

Note that you can divide matrices of different sizes and it works fine: this is called broadcasting and you're going to learn about it in part 5.

Exercise: Implement `normalizeRows()` to normalize the rows of a matrix. After applying this function to an input matrix x , each row of x should be a vector of unit length (meaning length 1).

In [36]:

```
# GRADED FUNCTION: normalizeRows

def normalizeRows(x):
    """
    Implement a function that normalizes each row of the matrix x (to have unit
    length).

    Argument:
    x -- A numpy matrix of shape (n, m)

    Returns:
    x -- The normalized (by row) numpy matrix. You are allowed to modify x.
    """

    ### START CODE HERE ### (~ 2 lines of code)
    # Compute x_norm as the norm 2 of x. Use np.linalg.norm(..., ord = 2, axis
    x_norm = np.linalg.norm(x, ord=2, axis=1, keepdims=True)

    # Divide x by its norm.
    x = x/x_norm
    ### END CODE HERE ###

    return x
```

In [37]:

```
x = np.array([
    [0, 3, 4],
    [1, 6, 4]])
print("normalizeRows(x) = " + str(normalizeRows(x)))

normalizeRows(x) = [[ 0.          0.6          0.8          ]
 [ 0.13736056  0.82416338  0.54944226]]
```

Expected Output:

normalizeRows(x)	[[0. 0.6 0.8] [0.13736056 0.82416338 0.54944226]]
-------------------------	---

Note: In `normalizeRows()`, you can try to print the shapes of `x_norm` and `x`, and then rerun the assessment. You'll find out that they have different shapes. This is normal given that `x_norm` takes the norm of each row of `x`. So `x_norm` has the same number of rows but only 1 column. So how did it work when you divided `x` by `x_norm`? This is called broadcasting and we'll talk about it now!

1.5 - Broadcasting and the softmax function

A very important concept to understand in numpy is "broadcasting". It is very useful for performing mathematical operations between arrays of different shapes. For the full details on broadcasting, you can read the official [broadcasting documentation](http://docs.scipy.org/doc/numpy/user/basics.broadcasting.html) (<http://docs.scipy.org/doc/numpy/user/basics.broadcasting.html>).

Exercise: Implement a softmax function using numpy. You can think of softmax as a normalizing function used when your algorithm needs to classify two or more classes. You will learn more about softmax in the second course of this specialization.

Instructions:

- for $x \in \mathbb{R}^{1 \times n}$, $\text{softmax}(x) = \text{softmax}([x_1 \quad x_2 \quad \dots \quad x_n]) = \left[\frac{e^{x_1}}{\sum_j e^{x_j}} \quad \frac{e^{x_2}}{\sum_j e^{x_j}} \right]$
- for a matrix $x \in \mathbb{R}^{m \times n}$, x_{ij} maps to the element in the i^{th} row and j^{th} column of x , thus ,

$$\text{softmax}(x) = \text{softmax} \begin{bmatrix} x_{11} & x_{12} & x_{13} & \dots & x_{1n} \\ x_{21} & x_{22} & x_{23} & \dots & x_{2n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_{m1} & x_{m2} & x_{m3} & \dots & x_{mn} \end{bmatrix} = \begin{bmatrix} \frac{e^{x_{11}}}{\sum_j e^{x_{1j}}} & \frac{e^{x_{12}}}{\sum_j e^{x_{1j}}} & \frac{e^{x_{13}}}{\sum_j e^{x_{1j}}} & \dots & \frac{e^{x_{1n}}}{\sum_j e^{x_{1j}}} \\ \frac{e^{x_{21}}}{\sum_j e^{x_{2j}}} & \frac{e^{x_{22}}}{\sum_j e^{x_{2j}}} & \frac{e^{x_{23}}}{\sum_j e^{x_{2j}}} & \dots & \frac{e^{x_{2n}}}{\sum_j e^{x_{2j}}} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \frac{e^{x_{m1}}}{\sum_j e^{x_{mj}}} & \frac{e^{x_{m2}}}{\sum_j e^{x_{mj}}} & \frac{e^{x_{m3}}}{\sum_j e^{x_{mj}}} & \dots & \frac{e^{x_{mn}}}{\sum_j e^{x_{mj}}} \end{bmatrix}$$

In [52]:

```
# GRADED FUNCTION: softmax

def softmax(x):
    """Calculates the softmax for each row of the input x.

    Your code should work for a row vector and also for matrices of shape (n, m)

    Argument:
    x -- A numpy matrix of shape (n,m)

    Returns:
    s -- A numpy matrix equal to the softmax of x, of shape (n,m)
    """

    ### START CODE HERE ### (= 3 lines of code)
    # Apply exp() element-wise to x. Use np.exp(...).
    x_exp = np.exp(x)

    # Create a vector x_sum that sums each row of x_exp. Use np.sum(..., axis =
    x_sum = np.sum(x_exp, axis=1, keepdims=True)
    print(x_sum.shape)

    # Compute softmax(x) by dividing x_exp by x_sum. It should automatically us
    s = x_exp / x_sum

    ### END CODE HERE ###

    return s
```

In [53]:

```
x = np.array([
    [9, 2, 5, 0, 0],
    [7, 5, 0, 0, 0]])
print("softmax(x) = " + str(softmax(x)))

(2, 1)
softmax(x) = [[ 9.80897665e-01  8.94462891e-04  1.79657674e-0
2  1.21052389e-04
1.21052389e-04]
 [ 8.78679856e-01  1.18916387e-01  8.01252314e-04  8.0125231
4e-04
8.01252314e-04]]
```

Expected Output:

softmax(x)	[[9.80897665e-01 8.94462891e-04
	1.79657674e-02 1.21052389e-04
	1.21052389e-04] [8.78679856e-01
	1.18916387e-01 8.01252314e-04
	8.01252314e-04 8.01252314e-04]]

Note:

- If you print the shapes of `x_exp`, `x_sum` and `s` above and rerun the assessment cell, you will see that `x_sum` is of shape (2,1) while `x_exp` and `s` are of shape (2,5). `x_exp/x_sum` works due to python broadcasting.

Congratulations! You now have a pretty good understanding of python numpy and have implemented a few useful functions that you will be using in deep learning.

What you need to remember:

- `np.exp(x)` works for any `np.array x` and applies the exponential function to every coordinate
- the sigmoid function and its gradient
- `image2vector` is commonly used in deep learning
- `np.reshape` is widely used. In the future, you'll see that keeping your matrix/vector dimensions straight will go toward eliminating a lot of bugs.
- numpy has efficient built-in functions
- broadcasting is extremely useful

2) Vectorization

In deep learning, you deal with very large datasets. Hence, a non-computationally-optimal function can become a huge bottleneck in your algorithm and can result in a model that takes ages to run. To make sure that your code is computationally efficient, you will use vectorization. For example, try to tell the difference between the following implementations of the dot/outer/elementwise product.

In [54]:

```
import time

x1 = [9, 2, 5, 0, 0, 7, 5, 0, 0, 0, 9, 2, 5, 0, 0]
x2 = [9, 2, 2, 9, 0, 9, 2, 5, 0, 0, 9, 2, 5, 0, 0]

### CLASSIC DOT PRODUCT OF VECTORS IMPLEMENTATION ###
tic = time.process_time()
dot = 0
for i in range(len(x1)):
    dot += x1[i]*x2[i]
toc = time.process_time()
print ("dot = " + str(dot) + "\n ----- Computation time = " + str(1000*(toc - t
```



```
### CLASSIC OUTER PRODUCT IMPLEMENTATION ###
tic = time.process_time()
outer = np.zeros((len(x1),len(x2))) # we create a Len(x1)*Len(x2) matrix with c
for i in range(len(x1)):
    for j in range(len(x2)):
        outer[i,j] = x1[i]*x2[j]
toc = time.process_time()
print ("outer = " + str(outer) + "\n ----- Computation time = " + str(1000*(toc
```



```
### CLASSIC ELEMENTWISE IMPLEMENTATION ###
tic = time.process_time()
mul = np.zeros(len(x1))
for i in range(len(x1)):
    mul[i] = x1[i]*x2[i]
toc = time.process_time()
print ("elementwise multiplication = " + str(mul) + "\n ----- Computation time
```



```
### CLASSIC GENERAL DOT PRODUCT IMPLEMENTATION ###
W = np.random.rand(3,len(x1)) # Random 3*Len(x1) numpy array
tic = time.process_time()
gdot = np.zeros(W.shape[0])
for i in range(W.shape[0]):
    for j in range(len(x1)):
        gdot[i] += W[i,j]*x1[j]
toc = time.process_time()
print ("gdot = " + str(gdot) + "\n ----- Computation time = " + str(1000*(toc -
```

```
dot = 278
----- Computation time = 0.17135700000014964ms
outer = [[ 81.  18.  18.  81.   0.  81.  18.  45.   0.   0.   8
1.  18.  45.   0.
0.]
[ 18.   4.   4.  18.   0.  18.   4.  10.   0.   0.  18.   4.
10.   0.
0.]
[ 45.  10.  10.  45.   0.  45.  10.  25.   0.   0.  45.  10
```



```

[ 45.  10.  10.  45.   0.  45.  10.  25.   0.   0.  45.  10.
25.   0.
  0.]
[  0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.
  0.   0.
  0.]
[  0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.
  0.   0.
  0.]
[ 63.  14.  14.  63.   0.  63.  14.  35.   0.   0.  63.  14.
35.   0.
  0.]
[ 45.  10.  10.  45.   0.  45.  10.  25.   0.   0.  45.  10.
25.   0.
  0.]
[  0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.
  0.   0.
  0.]
[  0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.
  0.   0.
  0.]
[  0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.
  0.   0.
  0.]
[ 81.  18.  18.  81.   0.  81.  18.  45.   0.   0.  81.  18.
45.   0.
  0.]
[ 18.   4.   4.  18.   0.  18.   4.  10.   0.   0.  18.   4.
10.   0.
  0.]
[ 45.  10.  10.  45.   0.  45.  10.  25.   0.   0.  45.  10.
25.   0.
  0.]
[  0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.
  0.   0.
  0.]
[  0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.   0.
  0.   0.
  0.]]
----- Computation time = 0.34173600000020343ms
elementwise multiplication = [ 81.   4.  10.   0.   0.  63.  1
0.   0.   0.   0.  81.   4.  25.   0.   0.]
----- Computation time = 0.2041510000001523ms
gdot = [ 21.31416152  24.71141355  25.97502631]
----- Computation time = 0.24965099999985085ms

```

In [55]:

```
x1 = [9, 2, 5, 0, 0, 7, 5, 0, 0, 0, 9, 2, 5, 0, 0]
x2 = [9, 2, 2, 9, 0, 9, 2, 5, 0, 0, 9, 2, 5, 0, 0]

### VECTORIZED DOT PRODUCT OF VECTORS ###
tic = time.process_time()
dot = np.dot(x1,x2)
toc = time.process_time()
print ("dot = " + str(dot) + "\n ----- Computation time = " + str(1000*(toc - t

### VECTORIZED OUTER PRODUCT ###
tic = time.process_time()
outer = np.outer(x1,x2)
toc = time.process_time()
print ("outer = " + str(outer) + "\n ----- Computation time = " + str(1000*(toc

### VECTORIZED ELEMENTWISE MULTIPLICATION ###
tic = time.process_time()
mul = np.multiply(x1,x2)
toc = time.process_time()
print ("elementwise multiplication = " + str(mul) + "\n ----- Computation time

### VECTORIZED GENERAL DOT PRODUCT ###
tic = time.process_time()
dot = np.dot(W,x1)
toc = time.process_time()
print ("gdot = " + str(dot) + "\n ----- Computation time = " + str(1000*(toc -

dot = 278
----- Computation time = 0.16608599999967666ms
outer = [[81 18 18 81  0 81 18 45  0  0 81 18 45  0  0]
 [18  4  4 18  0 18  4 10  0  0 18  4 10  0  0]
 [45 10 10 45  0 45 10 25  0  0 45 10 25  0  0]
 [ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0]
 [ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0]
 [63 14 14 63  0 63 14 35  0  0 63 14 35  0  0]
 [45 10 10 45  0 45 10 25  0  0 45 10 25  0  0]
 [ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0]
 [ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0]
 [ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0]
 [81 18 18 81  0 81 18 45  0  0 81 18 45  0  0]
 [18  4  4 18  0 18  4 10  0  0 18  4 10  0  0]
 [45 10 10 45  0 45 10 25  0  0 45 10 25  0  0]
 [ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0]
 [ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0]]
----- Computation time = 0.14913199999977422ms
elementwise multiplication = [81  4 10  0  0 63 10  0  0  0 81
 4 25  0  0]
----- Computation time = 0.11678100000001024ms
gdot = [ 21  21 11 15  24  24  21 11 13 25  25  27 23 23 17
```

```
gout = [ 21.51416152  24.71141555  25.97502651]
----- Computation time = 0.1621109999998538ms
```

As you may have noticed, the vectorized implementation is much cleaner and more efficient. For bigger vectors/matrices, the differences in running time become even bigger.

Note that `np.dot()` performs a matrix-matrix or matrix-vector multiplication. This is different from `np.multiply()` and the `*` operator (which is equivalent to `.*` in Matlab/Octave), which performs an element-wise multiplication.

2.1 Implement the L1 and L2 loss functions

Exercise: Implement the numpy vectorized version of the L1 loss. You may find the function `abs(x)` (absolute value of `x`) useful.

Reminder:

- The loss is used to evaluate the performance of your model. The bigger your loss is, the more different your predictions (\hat{y}) are from the true values (y). In deep learning, you use optimization algorithms like Gradient Descent to train your model and to minimize the cost.
- L1 loss is defined as:

$$L_1(\hat{y}, y) = \sum_{i=0}^m |y^{(i)} - \hat{y}^{(i)}| \quad (6)$$

In [60]:

```
# GRADED FUNCTION: L1

def L1(yhat, y):
    """
    Arguments:
    yhat -- vector of size m (predicted labels)
    y -- vector of size m (true labels)

    Returns:
    loss -- the value of the L1 loss function defined above
    """

    ### START CODE HERE ### (≈ 1 line of code)
    loss = np.sum(np.abs(y-yhat))
    ### END CODE HERE ###

    return loss
```

In [61]:

```
yhat = np.array([.9, 0.2, 0.1, .4, .9])
y = np.array([1, 0, 0, 1, 1])
print("L1 = " + str(L1(yhat,y)))
```

L1 = 1.1

Expected Output:

L1	1.1
-----------	-----

Exercise: Implement the numpy vectorized version of the L2 loss. There are several way of implementing the L2 loss but you may find the function `np.dot()` useful. As a reminder, if $x = [x_1, x_2, \dots, x_n]$ then $\text{np.dot}(x, x) = \sum_{j=0}^n x_j^2$.

- L2 loss is defined as

$$L_2(\hat{y}, y) = \sum_{i=0}^m (y^{(i)} - \hat{y}^{(i)})^2 \quad (7)$$

In [74]:

```
# GRADED FUNCTION: L2

def L2(yhat, y):
    """
    Arguments:
    yhat -- vector of size m (predicted labels)
    y -- vector of size m (true labels)

    Returns:
    loss -- the value of the L2 loss function defined above
    """

    ### START CODE HERE ### (= 1 line of code)
    loss = np.sum(np.power(y-yhat,2))
    ### END CODE HERE ###

    return loss
```