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## New Sub-classifications for Prime and Composite Numbers

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### Abstract

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A new evidence has emerged suggesting that prime and composite numbers should be sub-classified into additive (primes with prime digit sums or composites with composite digit sums) and non-additive (primes with non-prime digit sums or composites with non-composite digit sums) classes. The numbers 114 and 506 act as twin numbers to produce an unmistakable evidence for the new sub-classification.

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### Twin Numbers: 114 and 506

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$114 \div 2 = 57$   
 $\text{median}(1..57) = 29$   
 $57 \times 29 = 1653$   
where  
16th prime = 53

There are 16 prime numbers with prime digit sums up to 114:

2, 3, 5, 7, 11, 23, 29, 41, 43, 47, 61, 67, 83, 89, 101, 113.

There are 53 composite numbers with composite digit sums up to 114:

4, 6, 8, 9, 15, 18, 22, 24, 26, 27, 28, 33, 35, 36, 39, 40, 42, 44, 45, 46, 48, 51, 54, 55, 57, 60, 62, 63, 64, 66, 68, 69, 72, 75, 77, 78, 80, 81, 82, 84, 86, 87, 88, 90, 91, 93, 95, 96, 99, 105, 108, 112, 114.

Similarly,

$506 \div 2 = 253$   
 $\text{median}(1..253) = 127$   
 $253 \times 127 = 32131$   
where  
32nd prime = 131

There are 42<sup>+</sup> prime numbers with non-prime digit sums up to 506:

13, 17, 19, 31, 37, 53, 59, 71, 73, 79, 97, 103, 107, 109, 127, 149, 163, 167, 181, 211, 233, 239, 251, 257, 271, 277, 293, 307, 347, 349, 367, 383, 389, 419, 431, 433, 439, 457, 479, 491, 499, 503.

There are 131 composite numbers with non-composite digit sums up to 506:

10, 12, 14, 16, 20, 21, 25, 30, 32, 34, 38, 49, 50, 52, 56, 58, 65, 70, 74, 76, 85, 92, 94, 98, 100, 102, 104, 106, 110, 111, 115, 119, 120, 122, 124, 128, 133, 140, 142, 146, 148, 155, 160, 164, 166, 175, 182, 184, 188, 200, 201, 203, 205, 209, 210, 212, 214, 218, 221, 230, 232, 236, 238, 245, 247, 250, 254, 256, 265, 272, 274, 278, 287, 289, 290, 292, 296, 298, 300, 302, 304, 308, 319, 320, 322, 326, 328, 335, 340, 344, 346, 355, 362, 364, 368, 371, 377, 380, 382, 386, 388, 391, 395, 403, 407, 410, 412, 416, 418, 425, 427, 430, 434, 436, 445, 452, 454, 458, 469, 470, 472, 476, 478, 481, 485, 490, 494, 496, 500, 502, 506.



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### Further Work

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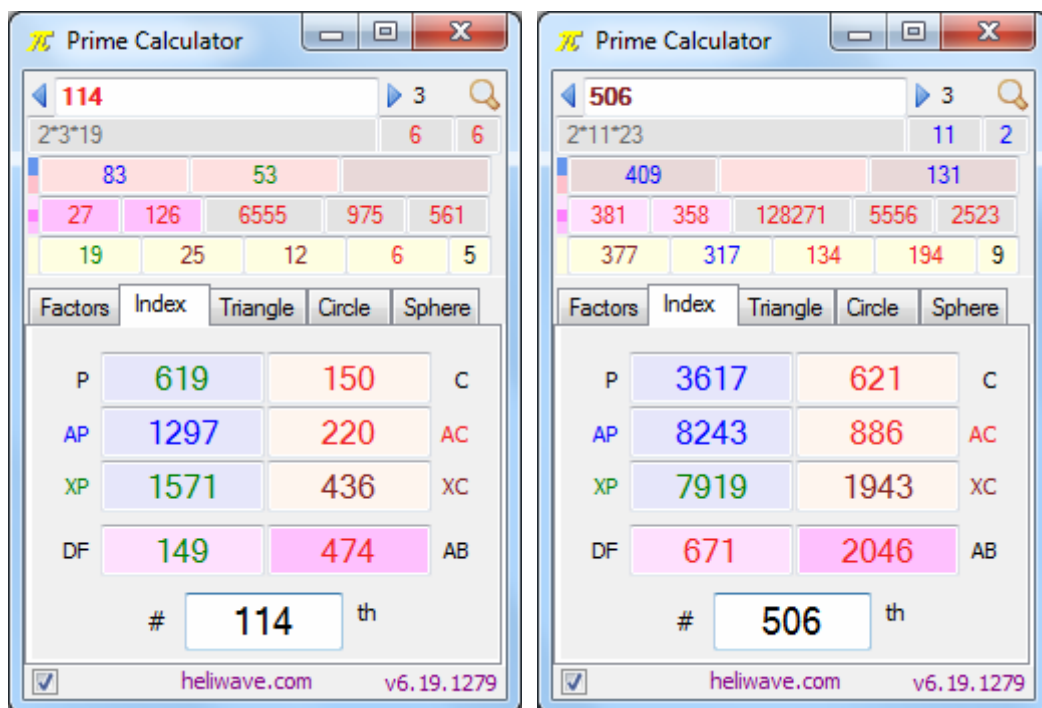
A computer program was written to search for natural numbers that exhibit the same pattern as number 114, namely taking half N multiply by median(1...half N) to produce a concatenated prime and its index, but no other number has been found except 506.

And only, the number 13444 was found to exhibit similar pattern (not the same pattern) as number 114 to produce a concatenated composite (not prime) and its index:

$13444 \div 2 = 6722$   
 $6722 \div 2 = 3361$   
 $6722 \times 3361 = 22592642$   
where  
2259th composite = 2642

Up to  $N = 7,000,000$  was tested before realizing that the search was diverging and would never find new such HalfN\_MedianHalfN\_IndexPrime numbers. Therefore, a mathematical proof is needed to show that only numbers 114 and 506 exhibit this phenomenon.

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PrimeCalculator is part of QuranCode software at <http://qurancode.com>

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†  $42 = 32 + 10$   
32 non-additive primes with a digit sum  $\neq 10$   
and  
10 non-additive primes with a digit sum  $= 10$ :  
19, 37, 73, 109, 127, 163, 181, 271, 307, 433.  
where  
Sum:  $19 + 37 + 73 + 109 + 127 + 163 + 181 + 271 + 307 + 433 = 1720$   
Sum of the first 31 prime numbers from 2 to 127 = 1720