

# Pitch trajectory density estimation for predicting future outcomes

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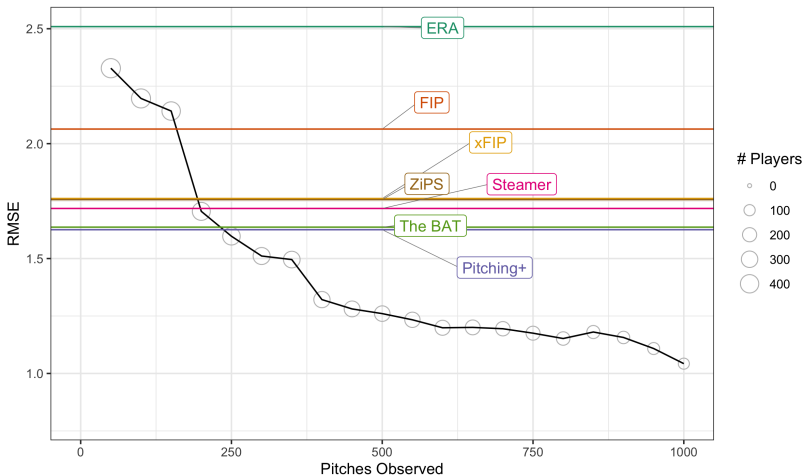
Saberseminar 2023



RICE SOCIAL SCIENCES  
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# Pitch Modeling

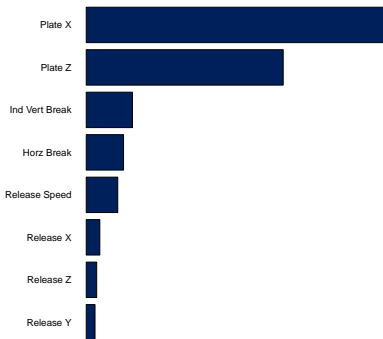
RELIEVERS | Pitching+ Within Season Relative to Prior Season ERA Estimators



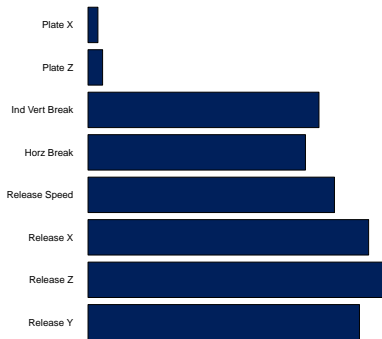
<https://library.fangraphs.com/pitching/stuff-location-and-pitching-primer/>

# The Conundrum

Variable Importance<sup>1</sup>



Variable Reliability<sup>2</sup>

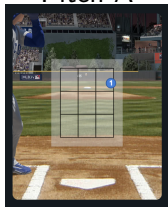


<sup>1</sup> fractional contribution of each feature's splits to gradient boosting pitch model

<sup>2</sup> (between-pitcher variance) / (total variance); varies by pitch type (here: RHB FB)

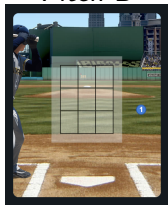
## An Example

Pitch A



- Fastball on 0-0 count
- 91 mph w/ 15 inches rise
- located on the edge of the zone
- 68% called strike, 11% foul, 8% ball in play, 8% called ball, 5% swinging strike ( $-0.04$  runs)

Pitch B



- Fastball on 0-0 count
- 98 mph w/ 20 inches rise
- located a foot off of the plate
- 99.6% called ball ( $+0.04$  runs)

## Two Sources of Noise

1. Random variation in the outcome given the pitch trajectory
  - This is addressed by Pitching+, PitchingBot, etc.
2. Random variation in the pitch trajectory itself
  - This is NOT addressed by Pitching+, PitchingBot, etc.

# The Approach

1. Fit a model to predict pitch outcome given its trajectory
  - We use gradient boosting, not the focus today
2. Estimate the probability distribution over pitch trajectories
  - Depends on pitcher, batter side, count, etc.
3. Apply the model 1. to the distribution 2.
  - As opposed to applying the model to the observed pitches

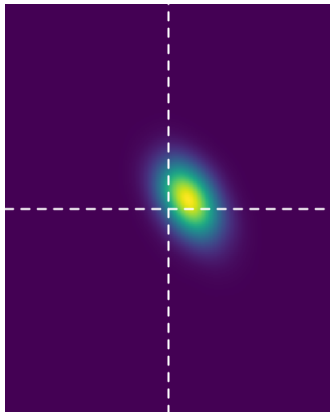
# Bayesian Hierarchical Model

Within each pitch type:

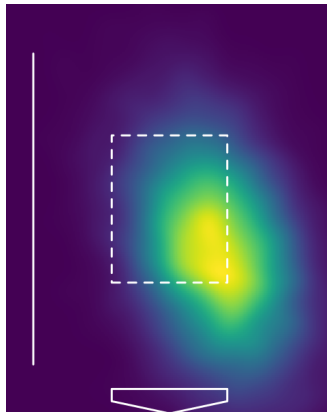
- We model each pitch as multivariate normal in 9 dimensions
  - $x/y/z$  release point,  $x/y/z$  release velocity,  $x/y/z$  acceleration
- Each pitcher has 81 parameters:
  - $9 \times 4 = 36$  parameters for **mean**
    - Main effect plus interactions w/ balls, strikes, batter side
  - $9 \times 1 = 9$  parameters for **variance**
  - $\binom{9}{2} = 36$  parameters for **correlation** between dimensions
- Each (ball, strike, batter side) combo has 18 parameters:
  - 9 parameters for mean, 9 parameters for variance
- We find the maximum *a posteriori* (MAP) model fit using the optimize function (automatic differentiation) from cmdstanr

# Dylan Cease's Slider vs RHB in 0-0 Counts

Predicted Break Chart



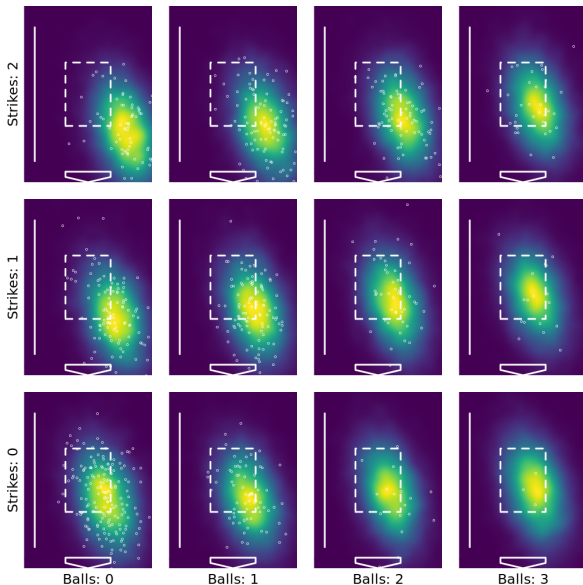
Predicted Plate Location



[saberpowers.shinyapps.io/predictive-pitch-score](https://saberpowers.shinyapps.io/predictive-pitch-score)

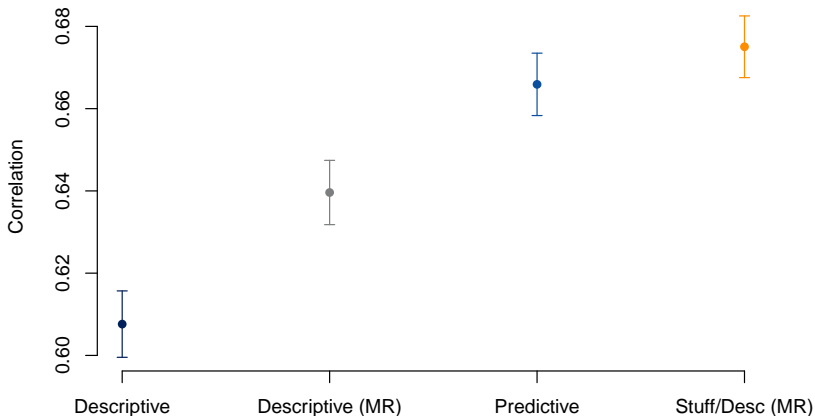


# Dylan Cease's Slider vs RHB in All Counts



# Does It Work?

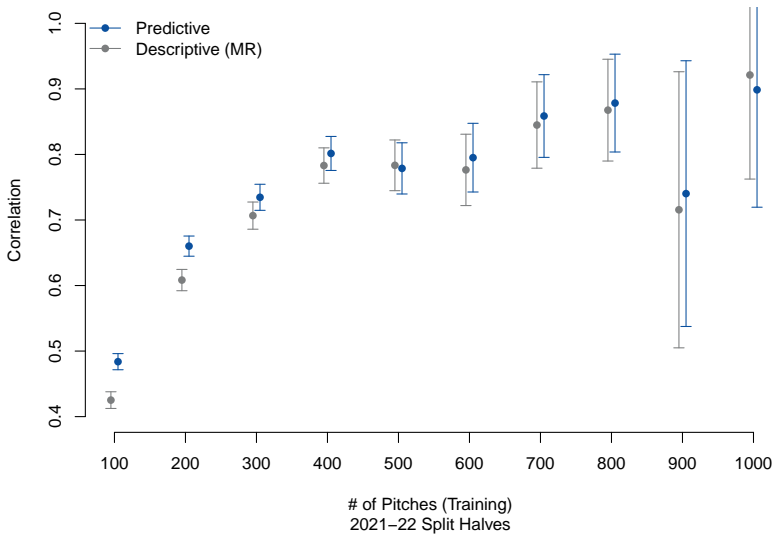
## Out-of-Sample Correlation with Descriptive Model



2021-22 Split Halves

# Does It Work?

## Out-of-Sample Correlation with Descriptive Model



# Leaderboard

Pitcher	PT	#	Stuff	Desc Score	Pred Score
Tyler Glasnow	all	1087	-8	-15	-18
Zack Wheeler	all	1912	-5	-17	-16
Spencer Strider	all	2164	-11	-14	-16
Sandy Alcantara	all	2094	-7	-12	-14
Pablo López	all	1662	1	-10	-13
Logan Webb	all	2183	-8	-12	-13
Shane Bieber	all	1820	-2	-11	-13
Bobby Miller	all	1067	-3	-10	-13
Hunter Greene	all	1322	-8	-10	-12
Bryce Miller	all	1179	-3	-12	-11

Showing 1 to 10 of 140 entries

Previous

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3

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...

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Next

[saberpowers.shinyapps.io/predictive-pitch-score](https://saberpowers.shinyapps.io/predictive-pitch-score)

# Conclusions

Takeaways:

1. Think more about the second source of noise  
(random variation in the pitch trajectory itself)
2. Pitch modeling predictions don't capture  
*all* of the predictive information in a pitch

What's coming up next:

- Better (simpler?) parameterization for distribution model
- Relax Gaussian assumption (unimodal with specific tails)

# Where to Find Us

[saberpowers.shinyapps.io/predictive-pitch-score](https://saberpowers.shinyapps.io/predictive-pitch-score)  
[github.com/saberpowers/predictive-pitch-score](https://github.com/saberpowers/predictive-pitch-score)

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