

# 1 PYTHAGOREAN FORMULA

## 1.1 WHEN DO WE SWITCH TO PREFERRING ACTUAL WINNING PERCENTAGE?

$n_i$  is the number of games played by team  $i$

$X_i$  is the Pythag W% of team  $i$

$Y_i$  is the actual W% of team  $i$

$Z_i$  is the residual W% of team  $i$  ( $Y_i = X_i + Z_i$ )

INTUITION

Actual W% = Pythag W% + Residual

Outcome = Skill + Luck

$$Y_i = X_i + Z_i$$

MODEL

$$X_i \sim \text{ind. Normal}(\mu_i, \sigma_X^2/n_i)$$

$$\mu_i \sim \text{i.i.d. Normal}(0, \sigma_\mu^2)$$

Option #1 ( $Z_i$  is all luck):

$$Z_i \sim \text{i.i.d. Normal}(0, \sigma_Z^2/n_i)$$

Option #2 ( $Z_i$  is not purely luck):

$$Z_i \sim \text{ind. Normal}(\eta_i, \sigma_Z^2/n_i)$$

$$\mu_i \sim \text{i.i.d. Normal}(0, \sigma_\eta^2)$$

One can show that  $X_i$  does better than  $Y_i$  at estimating  $E[Y_i]$  if  $\sigma_\eta^2 < \sigma_Z^2/n$ , i.e.  $n < \sigma_Z^2/\sigma_\eta^2$ .

## 1.2 Exercises

1. Show that  $X_i$  does better than  $Y_i$  at estimating  $E[Y_i]$  if  $n < \sigma_Z^2/\sigma_\eta^2$ .