

Assignment 2 :

2Q : Maximum likelihood Estimation (MLE) for θ .

we are given a normal distribution

$$f(x) = \frac{1}{\sqrt{8\pi}} e^{-\frac{(x-\theta)^2}{8}}$$

The given Expression values :

$$x_1 = 10, x_2 = 13, x_3 = 15, x_4 = 20.$$

MLE formula

MLE for θ in normal distribution when variance (σ^2) is

$$\hat{\theta} = \frac{\sum x_i}{N}$$

where

x_i = given values

N = number of observations.

Computing θ manually :

substituting the given values :

$$\hat{\theta} = \frac{10 + 13 + 15 + 20}{4}$$

$$\hat{\theta} = \frac{58}{4}$$

$$\hat{\theta} = 14.5$$

MLE estimate of $\theta = 14.5$