GAME PLAYING

Снартев 6

Outline

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- ♦ Perfect play
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- Aesource limits and approximate evaluation
- Sames of chance
- oitsmoini toetrect information ♦

Games vs. search problems

"Unpredictable" opponent \Rightarrow solution is a strategy specifying a move for every possible opponent reply

Time limits \Rightarrow unlikely to find goal, must approximate

Plan of attack:

- Computer considers possible lines of play (Babbage, 1846)
- ◆ Algorithm for perfect play (Zermelo, 1912; Von Meumann, 1944)
- Finite horizon, approximate evaluation (Zuse, 1945; Wiener, 1948;
 Shannon, 1950)
- First chess program (Turing, 1951)
- Machine learning to improve evaluation accuracy (Samuel, 1952–57)
- Pruning to allow deeper search (McCarthy, 1956)

Types of games

deterministic

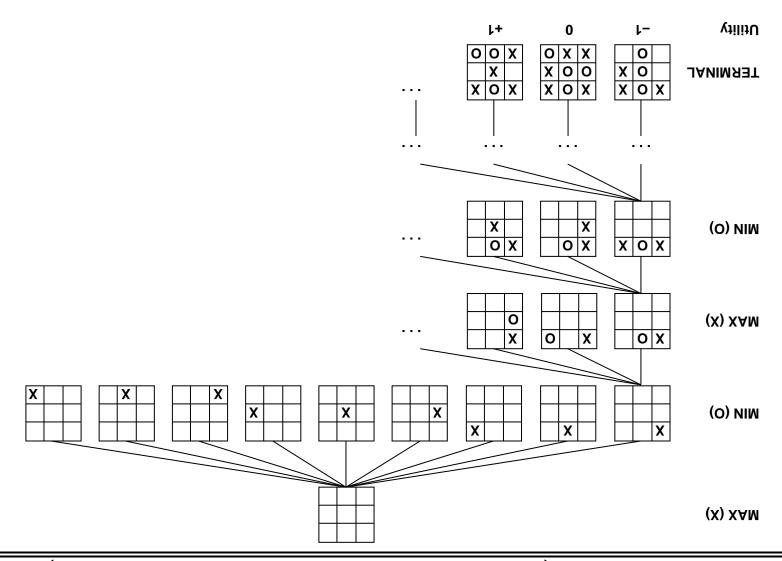
chess, checkers, backgammon battleships, bridge, poker, scrabble battleships, bridge, poker, scrabble nuclear war

chance

perfect information

imperfect information

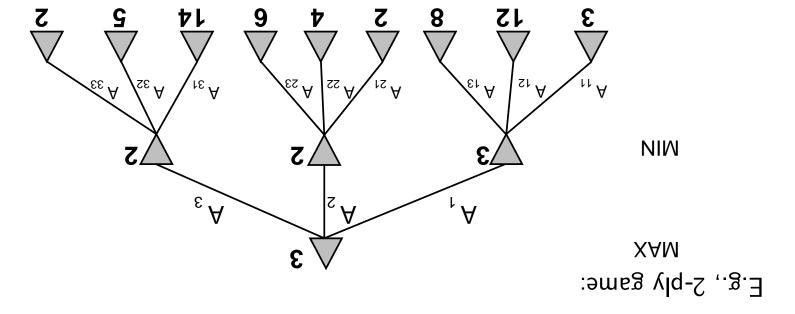
Game tree (2-player, deterministic, turns)



xsminilM

Perfect play for deterministic, perfect-information games

Idea: choose move to position with highest minimax value = best achievable payoff against best play



Minimax algorithm

```
ustania n
           for a, s in Successors(state) do v \leftarrow MIN(v, MAX-VALUE(s))
                                                                      \infty \rightarrow \Omega
                  if Terminal-Test(state) then return Utility(state)
                         function MIN-Value (state) returns a utility value
                                                                   ususta u
           for a, s in Successors(state) do v \leftarrow MAX(v, MIN-VALUE(s))
                                                                    \infty - \longrightarrow \Omega
                  if Terminal-Test(state) then return Utility(state)
                        function MAX-VALUE (state) returns a utility value
return the a in ACTIONS(state) maximizing MIN-VALUE(RESULT(a, state))
                                        eare state in game state in game
                    function Minimax-Decision (state) returns an action
```

Complete ??

Complete?? Only if tree is finite (chess has specific rules for this). MB a finite strategy can exist even in an infinite tree!

?? <u>IsmitqO</u>

Complete?? Yes, if tree is finite (chess has specific rules for this)

Optimal?? Yes, against an optimal opponent. Otherwise??

Time complexity??

Complete?? Yes, if tree is finite (chess has specific rules for this)

Optimal?? Yes, against an optimal opponent. Otherwise??

Time complexity $O(b^m)$

Space complexity??

```
Complete?? Yes, if tree is finite (chess has specific rules for this) Optimal?? Yes, against an optimal opponent. Otherwise?? Time complexity?? O(b^m)
```

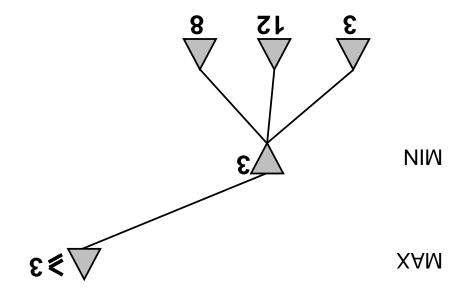
But do we need to explore every path?

⇒ exact solution completely infeasible

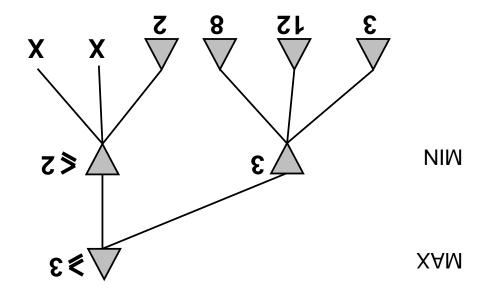
For chess, bpprox35, mpprox100 for "reasonable" games

Space complexity?? O(bm) (depth-first exploration)

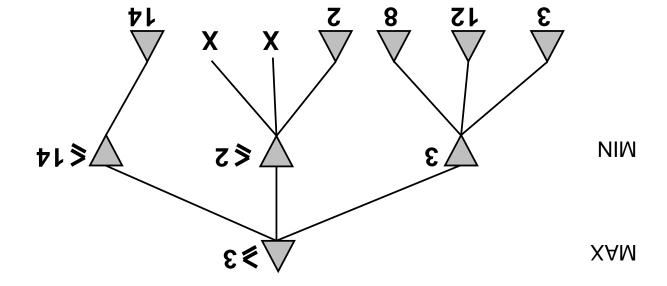
o-pruning example



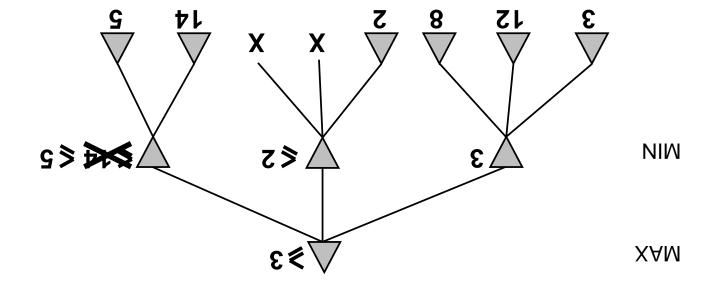
o-pruning example



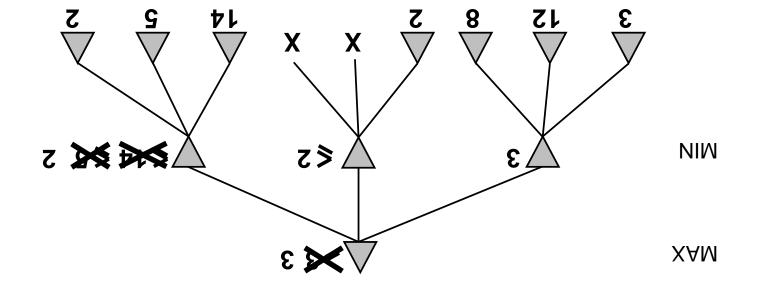
example β



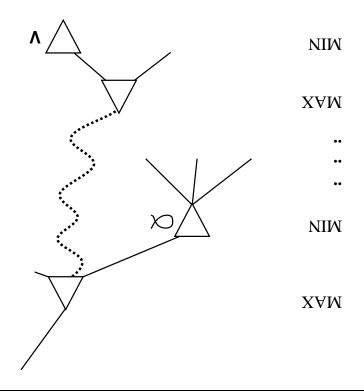
example β



example β



Why is it called $\alpha - \beta$?



 α is the best value (to MAX) found so far off the current path If V is worse than α , MAX will avoid it \Rightarrow prune that branch Define β similarly for MIN

The &-s algorithm

```
same as MAX-VALUE but with roles of lpha, eta reversed
                     function MIN-Value (state, a, b) returns a utility value
                                                                      a uinjai
                                                            (v, \Omega)XAIM \to \Omega
                                                 u muter mean b
                                        v \leftarrow MAX(v, MIN-VALUE(s, \alpha, \beta))
                                           for a, s in Successors(state) do
                                                                      \infty - \longrightarrow \Omega
                   if Terminal-Test(state) then return Utility(state)
  \beta, the value of the best alternative for MIN along the path to state
 \circ t, the value of the best alternative for MAX along the path to state
                                          inputs: state, current state in game
                    function MAX-VALUE (state, \alpha, \beta) returns a utility value
return the a in ACTIONS(state) maximizing MIN-VALUE(RESULT(a, state)
                  function ALPHA-BETA-DECISION (state) returns an action
```

Repetition Residual Properties

Pruning does not affect final result

Good move ordering improves effectiveness of pruning

With "perfect ordering," time complexity = $O(b^{m/2})$ \Rightarrow doubles solvable depth

A simple example of the value of reasoning about which computations are relevant (a form of metareasoning)

Unfortunately, 35^{50} is still impossible!

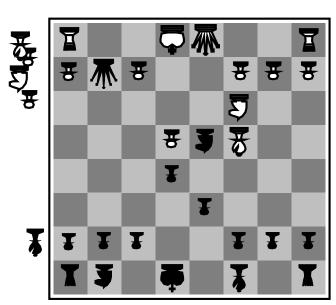
Resource limits

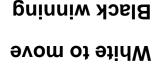
Standard approach:

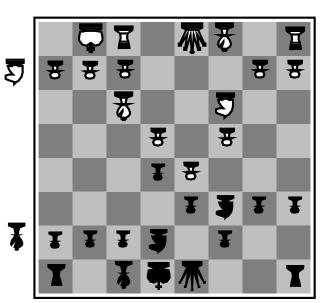
- Use Cutoff-Test instead of Terminal-Test
 e.g., depth limit (perhaps add quiescence search)
- Use EVAL instead of UTILITY
 i.e., evaluation function that estimates desirability of position

Suppose we have 100 seconds, explore 10^4 nodes/second $\Rightarrow 10^6$ nodes per move $\approx 35^{8/2}$ modes program $\Rightarrow \alpha - \beta$ reaches depth $8 \Rightarrow$ pretty good chess program

Evaluation functions







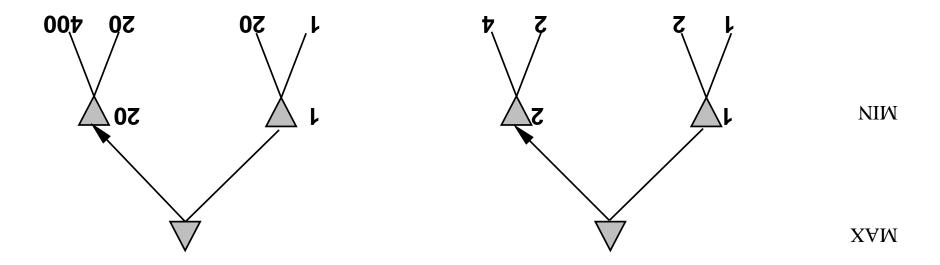
Black to move White slightly better

For chess, typically linear weighted sum of features

$$Eval(s) = u_1 f_1(s) + \dots + (s)_2 f_2(s) + \dots + (s)_n f_n(s)$$

e.g., $w_1=9$ with $f_1(s)=0$ mumber of black queens), etc.

Digression: Exact values don't matter



Behaviour is preserved under any monotonic transformation of EVAL

Only the order matters: payoff in deterministic games acts as an ordinal utility function

Deterministic games in practice

Checkers: Chinook ended 40-year-reign of human world champion Marion Tinsley in 1994. Used an endgame database defining perfect play for all positions involving 8 or fewer pieces on the board, a total of 443,748,401,247 positions.

Chess: Deep Blue defeated human world champion Gary Kasparov in a six-game match in 1997. Deep Blue searches 200 million positions per second, uses very sophisticated evaluation, and undisclosed methods for extending some lines of search up to 40 ply.

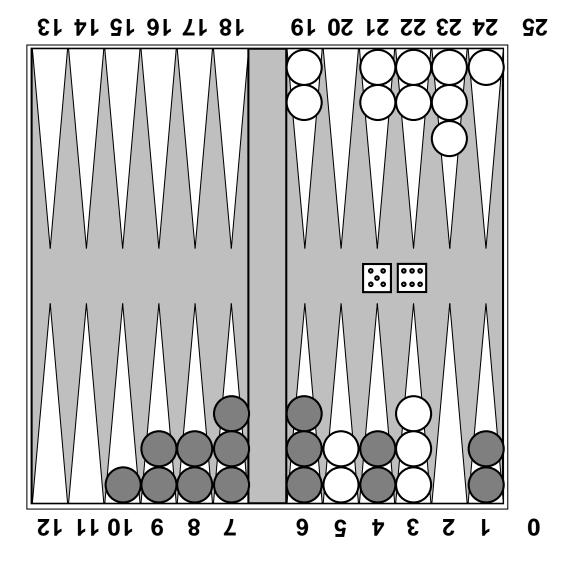
Othello: human champions refuse to compete against computers, who are

Go: human champions refuse to compete against computers, who are too bad. In go, b>300, so most programs use pattern knowledge bases to

suggest plausible moves.

too good.

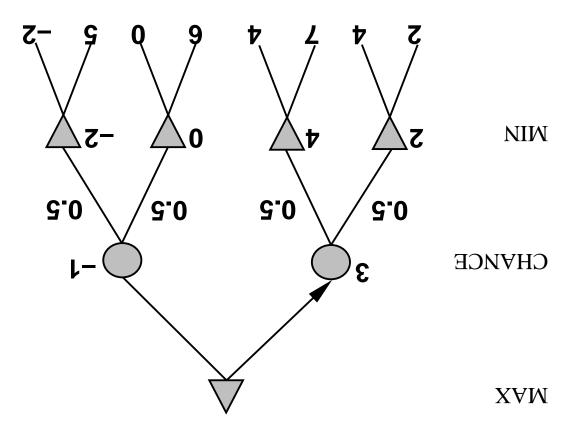
Nondeterministic games: backgammon



Nondeterministic games in general

In nondeterministic games, chance introduced by dice, card-shuffling

Simplified example with coin-flipping:



Algorithm for nondeterministic games

EXPECTIMINIMAX gives perfect play

Just like MINIMAX, except we must also handle chance nodes:

• •

if state is a MAX node then

return the highest Expectiminimax-Value of Successors(state)

if state is a Min node then

return the lowest Expectiminimax-Value of Successors(state)

if state is a chance node then

return average of Expectiminimax-Value of Successors(state)

. .

Nondeterministic games in practice

Dice rolls increase b: 21 possible rolls with 2 dice c discontinuon \approx 20 legal moves (can be 6,000 with 1-1 roll)

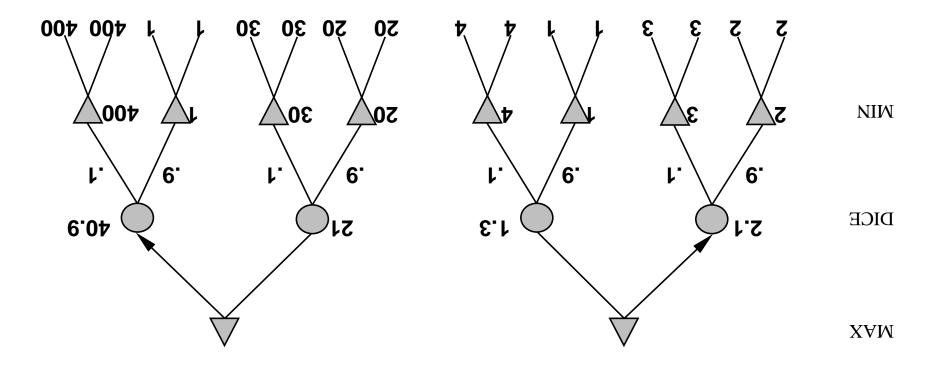
depth
$$4 = 20 \times (21 \times 20)^3 \approx 1.2 \times 10^9$$

As depth increases, probability of reaching a given node shrinks ⇒ value of lookahead is diminished

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 $\mathrm{TDGAMMON}$ uses depth-2 search + very good EVAL \approx world-champion level

Digression: Exact values DO matter



Behaviour is preserved only by positive linear transformation of EVAL Hence EVAL should be proportional to the expected payoff

Games of imperfect information

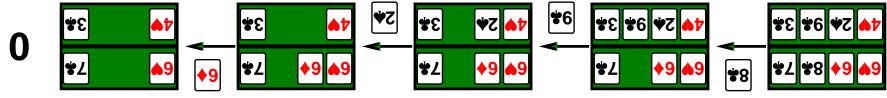
E.g., card games, where opponent's initial cards are unknown Typically we can calculate a probability for each possible deal Seems just like having one big dice roll at the beginning of the game* ldea: compute the minimax value of each action in each deal, then choose the action with highest expected value over all deals*

Special case: if an action is optimal for all deals, it's optimal.*

- GIB, current best bridge program, approximates this idea by 1) generating 100 deals consistent with bidding information
- 2) picking the action that wins most tricks on average

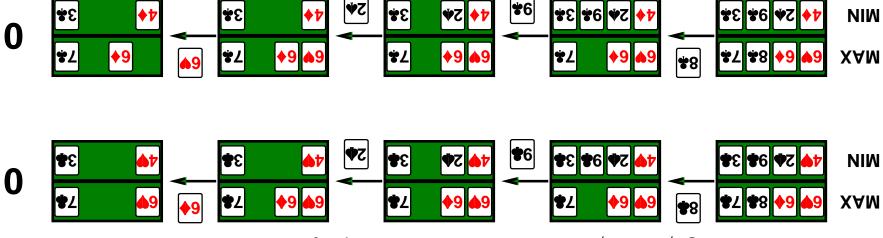
Exsmple

Four-card bridge/whist/hearts hand, MAX to play first



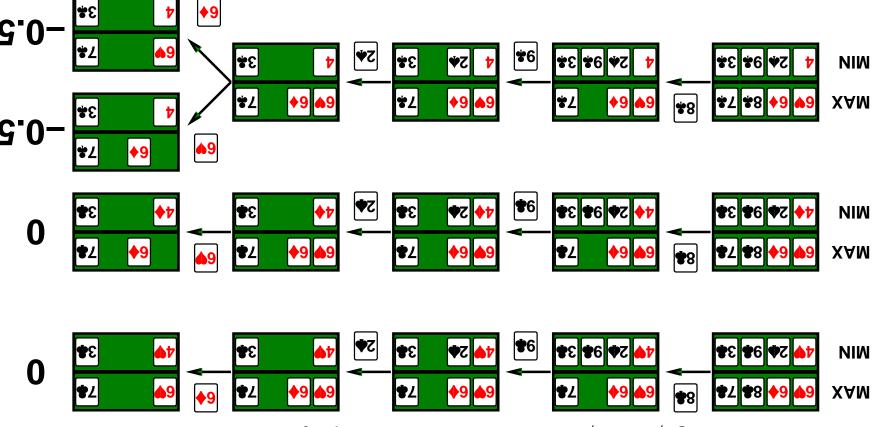
Exsmble

Four-card bridge/whist/hearts hand, $M\mathrm{AX}$ to play first



Exsmple

Four-card bridge/whist/hearts hand, M A X to play first



Commonsense example

Road A leads to a small heap of gold pieces Road B leads to a fork: take the left fork and you'll find a mound of jewels; take the right fork and you'll be run over by a bus.

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guess correctly and you'll find a mound of jewels; guess incorrectly and you'll be run over by a bus.

Proper analysis

 * Intuition that the value of an action is the average of its values in all actual states is \overline{WRONG}

With partial observability, value of an action depends on the information state or belief state the agent is in

Can generate and search a tree of information states

Leads to rational behaviors such as

- Acting to obtain information
- Signalling to one's partner
- Acting randomly to minimize information disclosure

Summary

Games are fun to work on! (and dangerous)

They illustrate several important points about AI

perfection is unattainable \Rightarrow must approximate

spection is unattainable \Rightarrow must approximate

ψ ancertainty constrains the assignment of values to states

 \diamondsuit optimal decisions depend on information state, not real state \diamondsuit

Games are to Al as grand prix racing is to automobile design