

Instances for Optimality Tests

Sabino Roselli

January 26, 2022

In order to make the notation more compact, the time windows lower and upper bounds, $l_i, u_i \forall i \in \mathcal{K}$ respectively, are reported together using the format $\tau_i = [l_i, u_i] \forall i \in \mathcal{K}$.

Instance 1

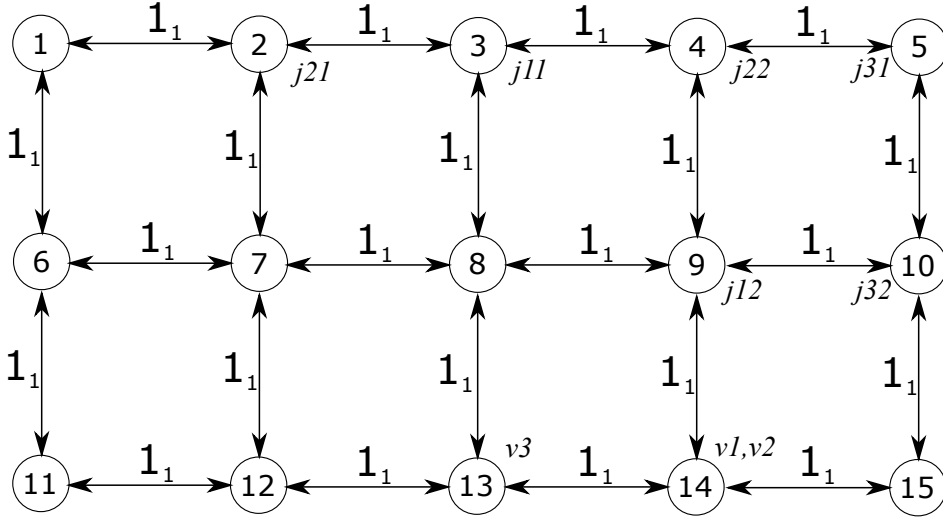


Figure 1: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 1 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{13, 14\}, \mathcal{O} = \{13, 14\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J}\}$$

$$L_{j11} = 3, L_{j12} = 9, L_{j21} = 2, L_{j22} = 4, L_{j31} = 5, L_{j32} = 10$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [5, 15], \tau_{j21} = [0, T], \tau_{j22} = [5, 15], \tau_{j31} = [0, T], \tau_{j32} = [5, 15]$$

$$S_{j11} = 3, S_{j12} = 3, S_{j21} = 3, S_{j22} = 2, S_{j31} = 2, S_{j32} = 1$$

$$\mathcal{V} = \{v1, v2\}, \mathcal{V}_{j1} = \{v1, v2\}, \mathcal{V}_{j2} = \{v1, v2\}, \mathcal{V}_{j3} = \{v2\}$$

$$OR = 15, C = 1, D = 1, \rho = 1, v = 1, T = 20$$

Instance 2

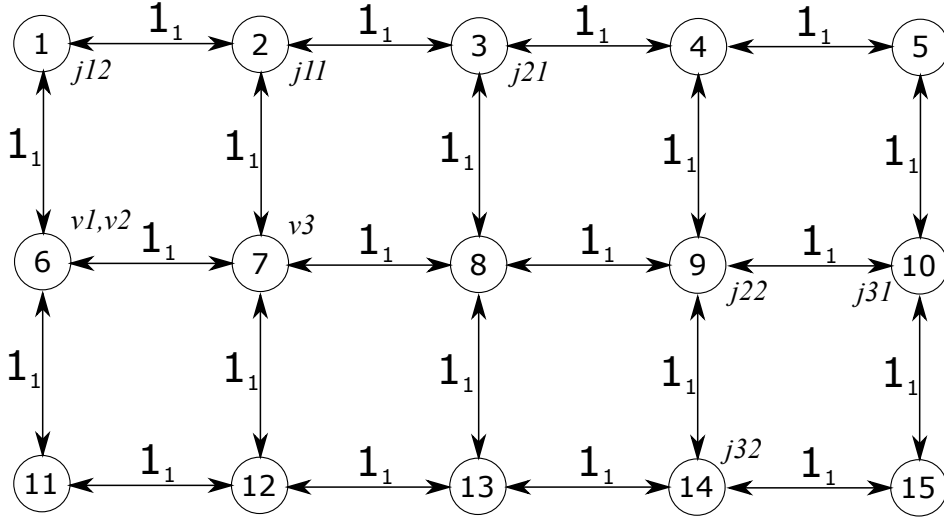


Figure 2: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 2 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 8, 15\}, \mathcal{O} = \{1, 8, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J}\}$$

$$L_{j11} = 2, L_{j12} = 1, L_{j21} = 3, L_{j22} = 9, L_{j31} = 10, L_{j32} = 14$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [5, 15], \tau_{j21} = [0, T], \tau_{j22} = [2, 15], \tau_{j31} = [0, T], \tau_{j32} = [5, 15]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 2, S_{j22} = 3, S_{j31} = 3, S_{j32} = 3$$

$$\mathcal{V} = \{v1, v2\}, \mathcal{V}_{j1} = \{v1\}, \mathcal{V}_{j2} = \{v1\}, \mathcal{V}_{j3} = \{v1\}$$

$$OR = 10, C = 1, D = 1, \rho = 1, v = 1, T = 20$$

Instance 3

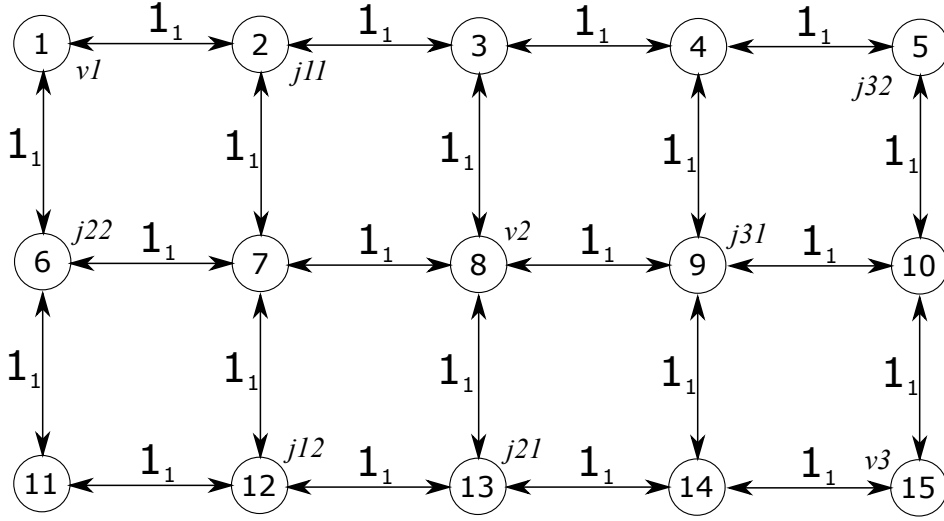


Figure 3: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 3 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 8, 15\}, \mathcal{O} = \{1, 8, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J}\}$$

$$L_{j11} = 2, L_{j12} = 11, L_{j21} = 13, L_{j22} = 6, L_{j31} = 9, L_{j32} = 5$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [4, 8], \tau_{j21} = [0, T], \tau_{j22} = [8, 10], \tau_{j31} = [0, T], \tau_{j32} = [6, 8]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 2, S_{j22} = 3, S_{j31} = 3, S_{j32} = 3$$

$$\mathcal{V} = \{v1, v2, v3\}, \mathcal{V}_{j1} = \{v1, v2\}, \mathcal{V}_{j2} = \{v1, v2\}, \mathcal{V}_{j3} = \{v2, v3\}$$

$$OR = 10, C = 1, D = 1, \rho = 1, v = 1, T = 15$$

Instance 4

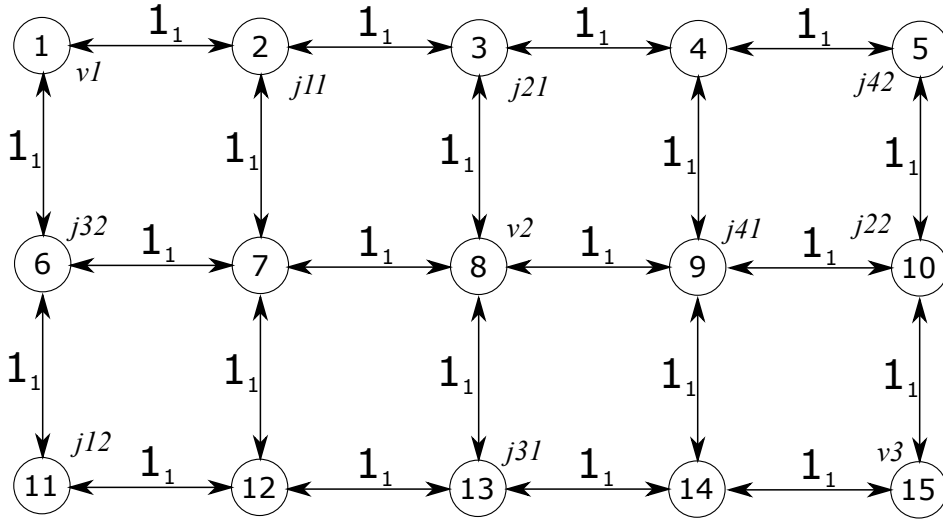


Figure 4: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 4 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 8, 15\}, \mathcal{O} = \{1, 8, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3, j4\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J}\}$$

$$L_{j11} = 2, L_{j12} = 11, L_{j21} = 4, L_{j22} = 10, L_{j31} = 13, L_{j32} = 6, L_{j41} = 9, L_{j42} = 5$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}, \mathcal{P}_{j41} = \emptyset, \mathcal{P}_{j42} = \{j41\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [4, 8], \tau_{j21} = [0, T], \tau_{j22} = [9, 11], \tau_{j31} = [0, T], \tau_{j32} = [8, 10], \tau_{j41} = [0, T], \tau_{j42} = [6, 8]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 0, S_{j22} = 1, S_{j31} = 2, S_{j32} = 3, S_{j41} = 3, S_{j42} = 1$$

$$\mathcal{V} = \{v1, v2, v3\}, \mathcal{V}_{j1} = \{v1, v2\}, \mathcal{V}_{j2} = \{v2, v3\}, \mathcal{V}_{j3} = \{v1, v2\}, \mathcal{V}_{j4} = \{v2, v3\}$$

$$OR = 10, C = 1, D = 1, \rho = 1, v = 1, T = 15$$

Instance 5

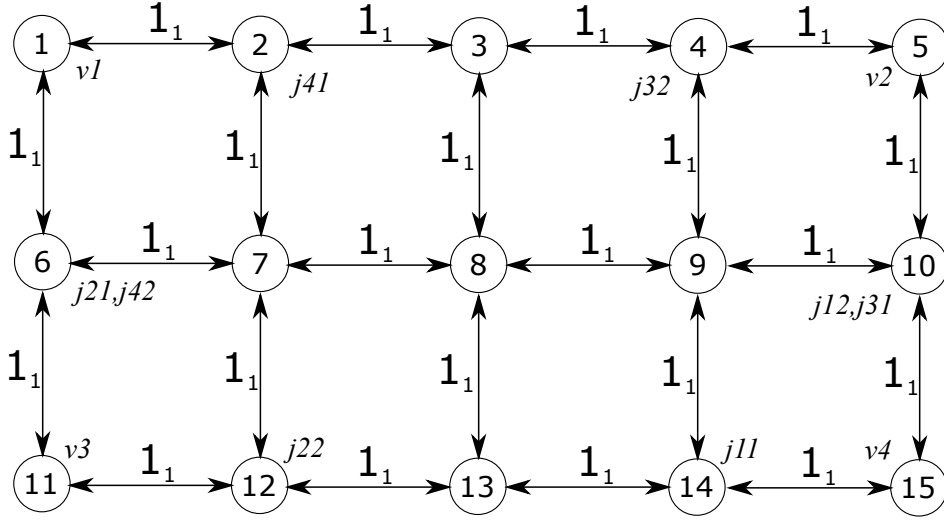


Figure 5: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 5 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 5, 11, 15\}, \mathcal{O} = \{1, 5, 11, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3, j4\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J}\}$$

$$L_{j11} = 14, L_{j12} = 10, L_{j21} = 6, L_{j22} = 12, L_{j31} = 10, L_{j32} = 4, L_{j41} = 2, L_{j42} = 6$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}, \mathcal{P}_{j41} = \emptyset, \mathcal{P}_{j42} = \{j41\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [8, 10], \tau_{j21} = [0, T], \tau_{j22} = [8, 10], \tau_{j31} = [0, T], \tau_{j32} = [8, 10], \tau_{j41} = [0, T], \tau_{j42} = [8, 10]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 1, S_{j22} = 1, S_{j31} = 1, S_{j32} = 1, S_{j41} = 1, S_{j42} = 1$$

$$\mathcal{V} = \{v1, v2, v3, v4\}, \mathcal{V}_{j1} = \{v1\}, \mathcal{V}_{j2} = \{v2\}, \mathcal{V}_{j3} = \{v3\}, \mathcal{V}_{j4} = \{v4\}$$

$$OR = 12, C = 1, D = 1, \rho = 1, v = 1, T = 17$$

Instance 6

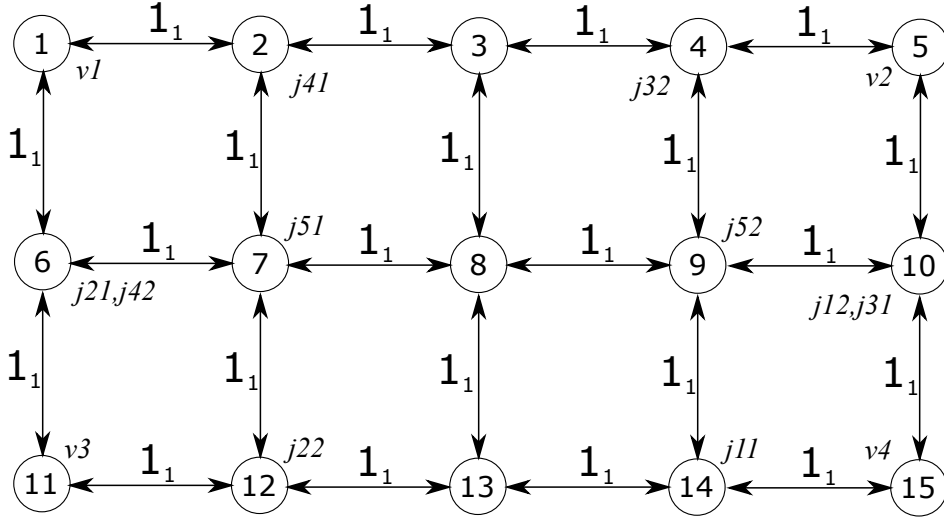


Figure 6: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 6 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 5, 11, 15\}, \mathcal{O} = \{1, 5, 11, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3, j4, j5\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J}\}$$

$$L_{j11} = 14, L_{j12} = 10, L_{j21} = 6, L_{j22} = 12, L_{j31} = 10, L_{j32} = 4, L_{j41} = 2, L_{j42} = 6, L_{j51} = 7, L_{j52} = 9$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset,$$

$$\mathcal{P}_{j32} = \{j31\}, \mathcal{P}_{j41} = \emptyset, \mathcal{P}_{j42} = \{j41\}, \mathcal{P}_{j51} = \emptyset, \mathcal{P}_{j52} = \{j51\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [8, 12], \tau_{j21} = [0, T], \tau_{j22} = [8, 12], \tau_{j31} = [0, T],$$

$$\tau_{j32} = [8, 12], \tau_{j41} = [0, T], \tau_{j42} = [8, 12], \tau_{j51} = [0, T], \tau_{j52} = [2, 10]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 1, S_{j22} = 1, S_{j31} = 1, S_{j32} = 1, S_{j41} = 1, S_{j42} = 1, S_{j51} = 0, S_{j52} = 0$$

$$\mathcal{V} = \{v1, v2, v3, v4\}, \mathcal{V}_{j1} = \{v1\}, \mathcal{V}_{j2} = \{v2\}, \mathcal{V}_{j3} = \{v3\}, \mathcal{V}_{j4} = \{v4\}, \mathcal{V}_{j5} = \{v1, v2, v3, v4\}$$

$$OR = 12, C = 1, D = 1, \rho = 1, v = 1, T = 17$$

Instance 7

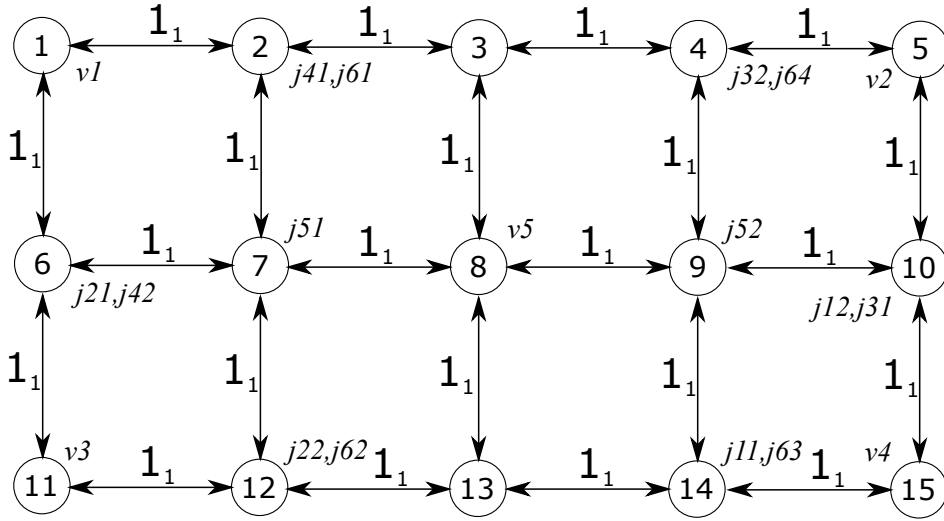


Figure 7: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 7 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 5, 8, 11, 15\}, \mathcal{O} = \{1, 5, 8, 11, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3, j4, j5, j6\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J} \setminus \{j6\}\} \cup \{j61, j62, j63, j64\}$$

$$L_{j11} = 14, L_{j12} = 10, L_{j21} = 6, L_{j22} = 12, L_{j31} = 10, L_{j32} = 4, L_{j41} = 2, L_{j42} = 6,$$

$$L_{j51} = 7, L_{j52} = 9, L_{j61} = 2, L_{j62} = 12, L_{j63} = 14, L_{j64} = 4$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}, \mathcal{P}_{j41} = \emptyset, \mathcal{P}_{j42} = \{j41\},$$

$$\mathcal{P}_{j51} = \emptyset, \mathcal{P}_{j52} = \{j51\}, \mathcal{P}_{j61} = \emptyset, \mathcal{P}_{j62} = \{j61\}, \mathcal{P}_{j63} = \{j62\}, \mathcal{P}_{j64} = \{j63\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [8, 12], \tau_{j21} = [0, T], \tau_{j22} = [8, 12], \tau_{j31} = [0, T], \tau_{j32} = [8, 12], \tau_{j41} = [0, T],$$

$$\tau_{j42} = [8, 12], \tau_{j51} = [0, T], \tau_{j52} = [2, 10], \tau_{j61} = [0, T], \tau_{j62} = [0, T], \tau_{j63} = [0, T], \tau_{j64} = [10, 15]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 1, S_{j22} = 1, S_{j31} = 1, S_{j32} = 1, S_{j41} = 1, S_{j42} = 1,$$

$$S_{j51} = 0, S_{j52} = 0, S_{j61} = 0, S_{j62} = 0, S_{j63} = 0, S_{j64} = 0$$

$$\mathcal{V} = \{v1, v2, v3, v4, v5\}, \mathcal{V}_{j1} = \{v1\}, \mathcal{V}_{j2} = \{v2\}, \mathcal{V}_{j3} = \{v3\}, \mathcal{V}_{j4} = \{v4\}, \mathcal{V}_{j5} = \{v1, v2, v3, v4\}, \mathcal{V}_{j6} = \{v5\}$$

$$OR = 14, C = 1, D = 1, \rho = 1, v = 1, T = 20$$

Instance 8

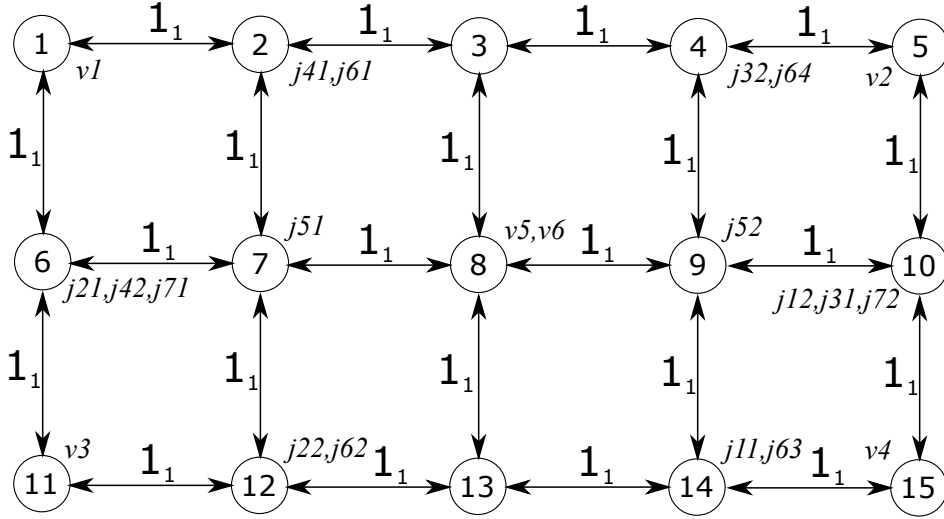


Figure 8: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 8 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 5, 8, 11, 15\}, \mathcal{O} = \{1, 5, 8, 11, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3, j4, j5, j6, j7\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J} \setminus \{j6\}\} \cup \{j61, j62, j63, j64\}$$

$$L_{j11} = 14, L_{j12} = 10, L_{j21} = 6, L_{j22} = 12, L_{j31} = 10, L_{j32} = 4,$$

$$L_{j41} = 2, L_{j42} = 6, L_{j51} = 7, L_{j52} = 9, L_{j61} = 2, L_{j62} = 12, L_{j63} = 14, L_{j64} = 4, L_{j71} = 6, L_{j72} = 10$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}, \mathcal{P}_{j41} = \emptyset, \mathcal{P}_{j42} = \{j41\},$$

$$\mathcal{P}_{j51} = \emptyset, \mathcal{P}_{j52} = \{j51\}, \mathcal{P}_{j61} = \emptyset, \mathcal{P}_{j62} = \{j61\}, \mathcal{P}_{j63} = \{j62\}, \mathcal{P}_{j64} = \{j63\}, \mathcal{P}_{j71} = \emptyset, \mathcal{P}_{j72} = \{j71\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [8, 12], \tau_{j21} = [0, T], \tau_{j22} = [8, 12], \tau_{j31} = [0, T], \tau_{j32} = [8, 12], \tau_{j41} = [0, T], \tau_{j42} = [8, 12],$$

$$\tau_{j51} = [0, T], \tau_{j52} = [2, 10], \tau_{j61} = [0, T], \tau_{j62} = [0, T], \tau_{j63} = [0, T], \tau_{j64} = [0, T], \tau_{j71} = [0, T], \tau_{j72} = [0, T]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 1, S_{j22} = 1, S_{j31} = 1, S_{j32} = 1, S_{j41} = 1, S_{j42} = 1,$$

$$S_{j51} = 0, S_{j52} = 0, S_{j61} = 0, S_{j62} = 0, S_{j63} = 0, S_{j64} = 0, S_{j71} = 0, S_{j72} = 0$$

$$\mathcal{V} = \{v1, v2, v3, v4, v5, v6\}, \mathcal{V}_{j1} = \{v1\}, \mathcal{V}_{j2} = \{v2\}, \mathcal{V}_{j3} = \{v3\}, \mathcal{V}_{j4} = \{v4\},$$

$$\mathcal{V}_{j5} = \{v1, v2, v3, v4\}, \mathcal{V}_{j6} = \{v5, v6\}, \mathcal{V}_{j7} = \{v5, v6\}$$

$$OR = 14, C = 1, D = 1, \rho = 1, v = 1, T = 20$$

Instance 9

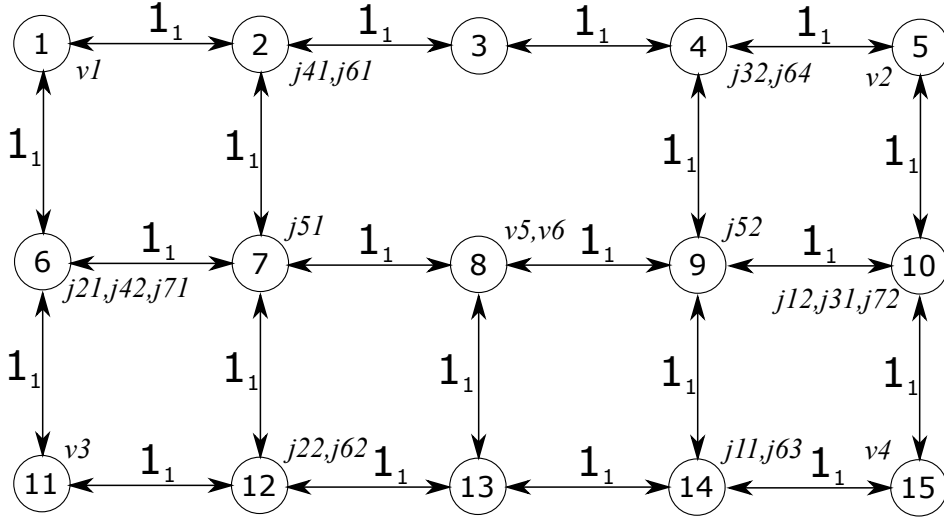


Figure 9: Finite, strongly connected, weighted, directed graph representing the plant layout for Instance 9 of the CF-EVRP.

$$\mathcal{N} = \{1, \dots, 15\}, \mathcal{N}_H = \{1, 5, 8, 11, 15\}, \mathcal{O} = \{1, 5, 8, 11, 15\}$$

$$\mathcal{E} = \{(1, 2), (2, 3), (3, 4), (4, 5), (1, 6), (2, 7), (4, 9), (5, 10), (6, 7), (7, 8),$$

$$(8, 9), (9, 10), (6, 11), (7, 12), (8, 13), (9, 14), (10, 15), (11, 12), (12, 13), (13, 14), (14, 15)\}$$

$$\mathcal{J} = \{j1, j2, j3, j4, j5, j6, j7\}, \mathcal{K} = \{i1, i2 \mid \forall i \in \mathcal{J} \setminus \{j6\}\} \cup \{j61, j62, j63, j64\}$$

$$L_{j11} = 14, L_{j12} = 10, L_{j21} = 6, L_{j22} = 12, L_{j31} = 10, L_{j32} = 4,$$

$$L_{j41} = 2, L_{j42} = 6, L_{j51} = 7, L_{j52} = 9, L_{j61} = 2, L_{j62} = 12, L_{j63} = 14, L_{j64} = 4, L_{j71} = 6, L_{j72} = 10$$

$$\mathcal{P}_{j11} = \emptyset, \mathcal{P}_{j12} = \{j11\}, \mathcal{P}_{j21} = \emptyset, \mathcal{P}_{j22} = \{j21\}, \mathcal{P}_{j31} = \emptyset, \mathcal{P}_{j32} = \{j31\}, \mathcal{P}_{j41} = \emptyset, \mathcal{P}_{j42} = \{j41\},$$

$$\mathcal{P}_{j51} = \emptyset, \mathcal{P}_{j52} = \{j51\}, \mathcal{P}_{j61} = \emptyset, \mathcal{P}_{j62} = \{j61\}, \mathcal{P}_{j63} = \{j62\}, \mathcal{P}_{j64} = \{j63\}, \mathcal{P}_{j71} = \emptyset, \mathcal{P}_{j72} = \{j71\}$$

$$\tau_{j11} = [0, T], \tau_{j12} = [8, 12], \tau_{j21} = [0, T], \tau_{j22} = [8, 12], \tau_{j31} = [0, T], \tau_{j32} = [8, 12], \tau_{j41} = [0, T], \tau_{j42} = [8, 12],$$

$$\tau_{j51} = [0, T], \tau_{j52} = [2, 10], \tau_{j61} = [0, T], \tau_{j62} = [0, T], \tau_{j63} = [0, T], \tau_{j64} = [0, T], \tau_{j71} = [0, T], \tau_{j72} = [0, T]$$

$$S_{j11} = 1, S_{j12} = 1, S_{j21} = 1, S_{j22} = 1, S_{j31} = 1, S_{j32} = 1, S_{j41} = 1, S_{j42} = 1,$$

$$S_{j51} = 0, S_{j52} = 0, S_{j61} = 0, S_{j62} = 0, S_{j63} = 0, S_{j64} = 0, S_{j71} = 0, S_{j72} = 0$$

$$\mathcal{V} = \{v1, v2, v3, v4, v5, v6\}, \mathcal{V}_{j1} = \{v1\}, \mathcal{V}_{j2} = \{v2\}, \mathcal{V}_{j3} = \{v3\}, \mathcal{V}_{j4} = \{v4\},$$

$$\mathcal{V}_{j5} = \{v1, v2, v3, v4\}, \mathcal{V}_{j6} = \{v5, v6\}, \mathcal{V}_{j7} = \{v5, v6\}$$

$$OR = 18, C = 1, D = 1, \rho = 1, v = 1, T = 23$$