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CIS (45)

## Probability and Statistics

### Assignment # 01

#### Exercise # 3.2 :-

##### Question # 01

A probability value is a number between 0 and 1 inclusive :

$$a : 50 - 50 = 50\% = 0.5$$

$$b : 20\% = 0.2$$

$$c : \text{no chance} = 0\% = 0.0$$

##### Question # 02

Since  $0 \leq P(A) \leq 1$  is always true, the following values then 0 or greater than 1 cannot be probabilities.

Values less than 0 : -1

Values greater than 1 : 2,  $5/3$ ,  $\sqrt{2}$

##### Question # 07

Let  $H$  = getting a home run

$$P(H) = 73/476 = 0.1534$$

Yes ; this is very different from his lifetime probability of  $567/7932 = 0.715$ . It is about twice as high.

### Exercise # 3.3 :-

#### Question # 01

- NO, it's possible for a cardiac surgeon to be a female.
- NO, it's possible for a female college student to drive a motorcycle.
- Yes, a person treated with Lipitor would not be in the group that was given no treatment.

#### Question # 02

- $P(\bar{A}) = 1 - P(A) = 1 - 0.05 = 0.95$
- Let  $B$  = a randomly selected woman over the age of 25 has a bachelor's degree.
- $P(\bar{B}) = 1 - P(B) = 1 - 0.0218 = 0.782$

#### Question # 05

Make a chart like following.

		Green	Yellow	
flower	purple	5	4	9
	white	3	2	5
		8	6	14

These are following two approaches :

$$\begin{aligned} 1. P(G \text{ or } W) &= P(G) + P(W) - P(G \& W) \\ &= \frac{0}{14} + \frac{5}{14} - \frac{3}{14} \\ &= \frac{10}{14} \Rightarrow \frac{5}{7} \\ &= 0.714 \end{aligned}$$

$$\begin{aligned}
 2. \quad P(G \text{ or } W) &= P(GP \text{ or } GW \text{ or } YW) \\
 &= P(GP) + P(GW) + P(YW) \\
 &= \frac{5}{14} + \frac{3}{14} + \frac{2}{14} \\
 &= \frac{10}{14} \Rightarrow \frac{5}{7} \\
 &= 0.714
 \end{aligned}$$

### Exercise # 3.4 :-

#### Question # 03

Let  $T$  = getting tails when tossing a coin.

Let  $3$  = getting a three then rolling a dice

$$P(T \text{ and } 3) = P(T) \cdot P(3|T) = \left(\frac{1}{2}\right) \cdot \left(\frac{1}{6}\right) = \frac{1}{12}$$

#### Question # 21

Refer to the table at below:

$$\begin{aligned}
 p(\text{Pos}_1 \text{ and } \text{Pos}_2) &= P(\text{Pos}_1) \cdot P(\text{Pos}_2) \\
 &= \left(\frac{83}{99}\right) \cdot \left(\frac{82}{98}\right) \\
 &= 0.702
 \end{aligned}$$

		Test Result		
		Pos	Neg	
Pregnant?	Yes	80	5	85
	No	3	11	14
		83	16	99

#### Question # 23

Refer to the table for exercise # 21.

$$\begin{aligned}
 P(\text{Yes}_1 \text{ and } \text{Yes}_2) &= P(\text{Yes}_1) \cdot P(\text{Yes}_2) \\
 &= \left(\frac{85}{99}\right) \cdot \left(\frac{84}{98}\right) \\
 &= 0.736
 \end{aligned}$$



### Exercise # 3.5 :-

#### Question # 01 -

It is not true that "at least one of them has group A blood," then "none of them has group A blood".

#### Question # 03 -

It is not true that "none of them is correct," then "at least one of them is correct".

#### Question # 07 -

Let  $B$  = a child is a boy.

$P(B) = 0.5$ , for each birth

$$\begin{aligned} P(\text{at least one girl}) &= 1 - P(\text{all boys}) \\ &= 1 - P(B_1 \text{ and } B_2 \text{ and } B_3 \text{ and } B_4 \text{ and } B_5) \\ &= 1 - P(B_1) \cdot P(B_2) \cdot P(B_3) \cdot P(B_4) \cdot P(B_5) \\ &= 1 - (0.5)(0.5)(0.5)(0.5)(0.5) \\ &= 1 - 0.03125 \\ &= 0.96875 \end{aligned}$$

Yes; that probability is high enough to be "very confident" of getting at least one girl. Since 0.03125 is less than 0.05, the accepted of an unusual event.