

Final Probability Project by Sabrina

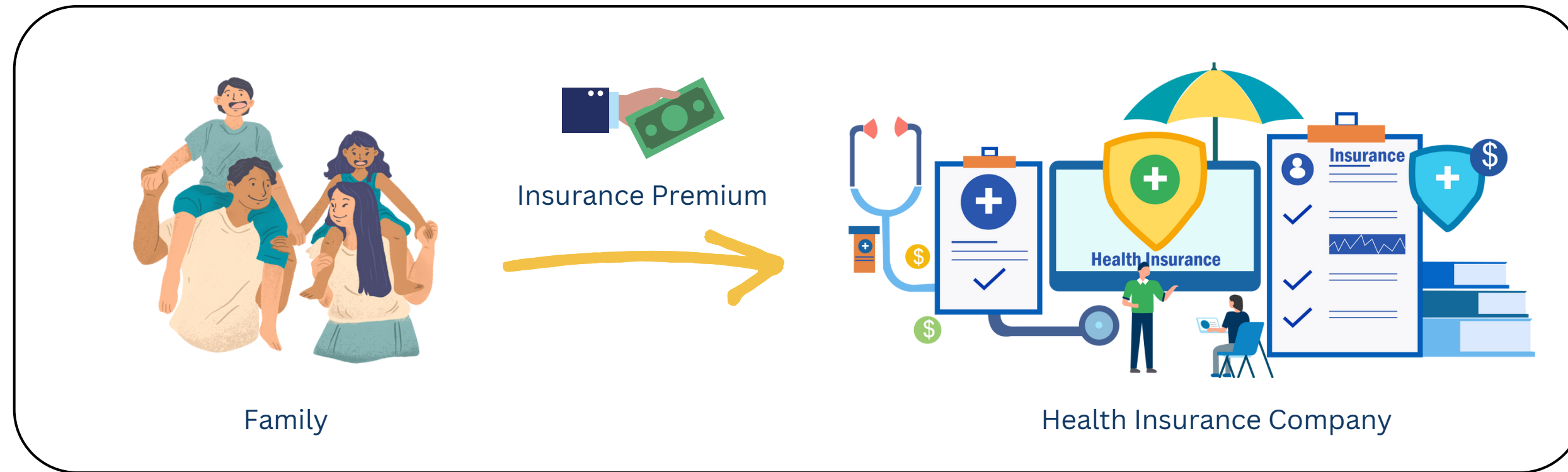
Probability Course - Sekolah Data Pacmann

Outline

- Introduction
- Dataset
- Descriptive Statistic Analysis
- Categorical Variables Analysis
- Continuous Variables Analysis
- Variables Correlation
- Hypothesis Testing
- Conclusion

Introduction

Introduction



Dataset

- The dataset provided is personal health billing data.

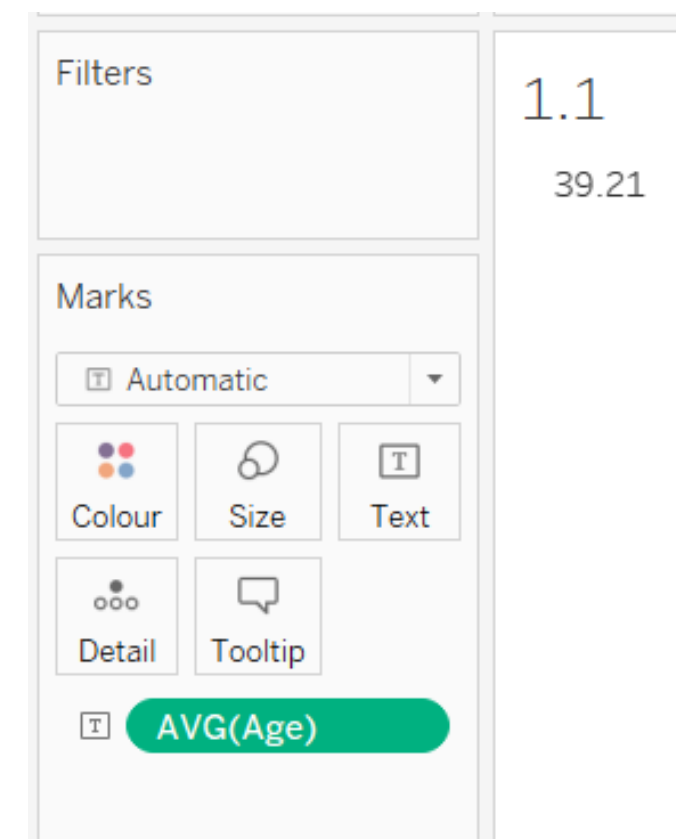
Variable	Description	Value
age	Age of primary beneficiary	18 to 64
sex	primary beneficiary's gender	male and female
bmi	Body mass index, providing an understanding of body weights that are relatively high or low relative to height, objective index of body weight (kg/m ²) using the ratio of height to weightm ideally 18.5 to 24.9	15.96 to 53.13
children	Number of children covered by health insurance / Number of dependents	0 to 5
smoker	Whether the primary beneficiary is a smoker or non-smoker	yes and no
region	The beneficiary's residential area in the US	northeast, southeast, southwest, northwest
charges	Individual medical costs billed by health insurance (in USD)	1,121 to 63,770

Descriptive Statistics Analysis

Mean of Age

- Objective: The average age of the primary beneficiary.

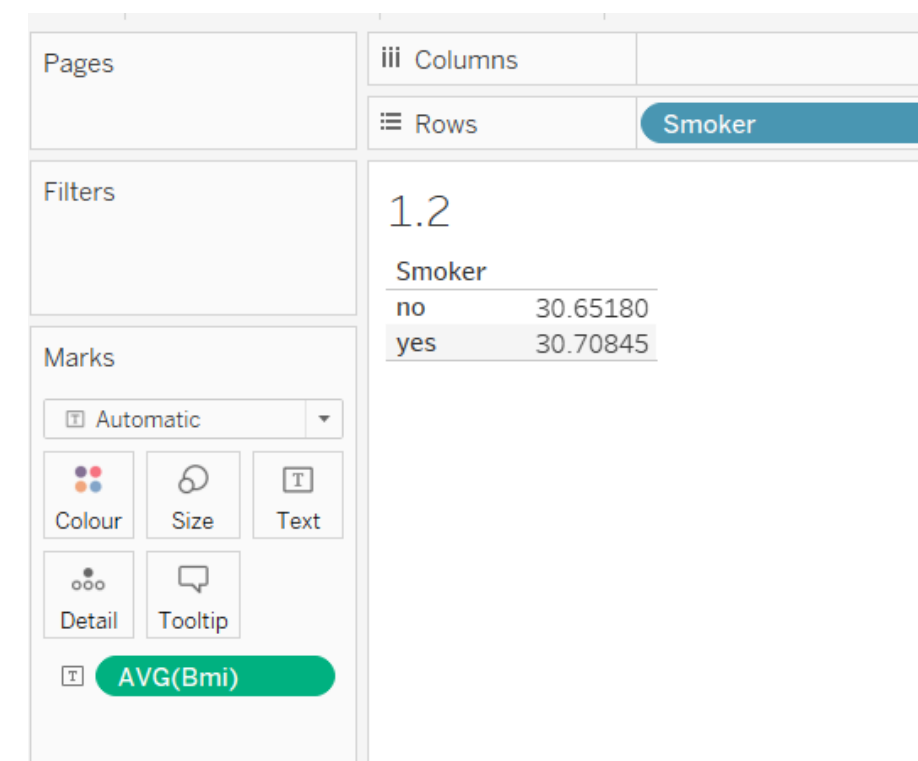
RESULT: The average age is 39



Mean of BMI who Smokes

- Objective: The average BMI of the primary beneficiary who smokes

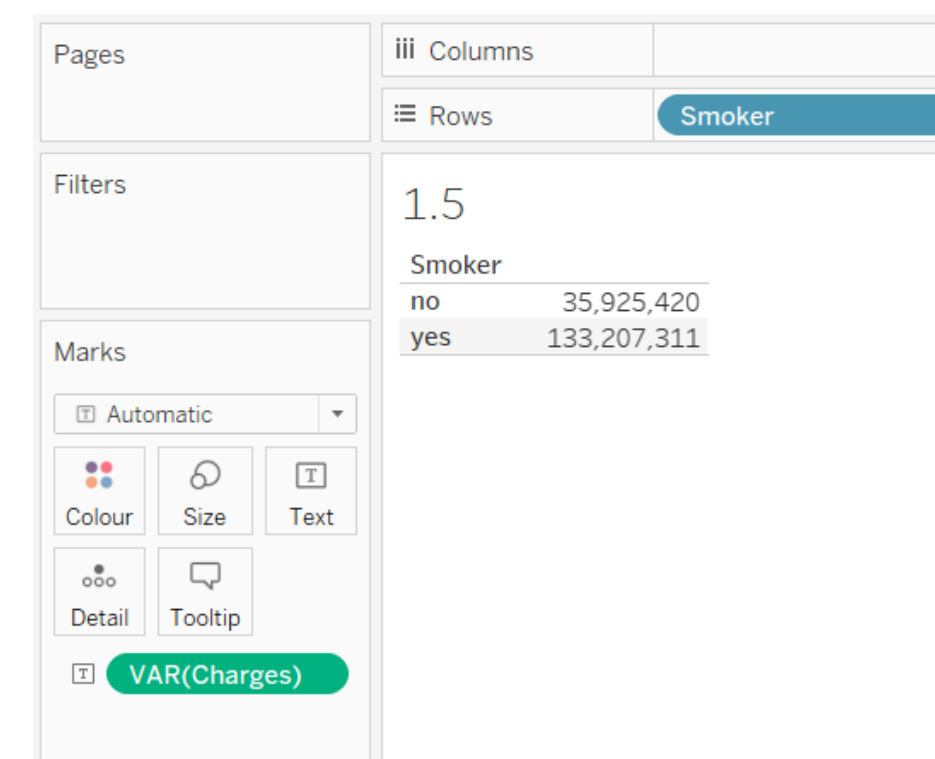
RESULT: The average BMI of a smoker is 30.7



Variance of the data charges of smokers and non-smokers

Objective: Is the variance of the data charges of smokers and non-smokers the same?

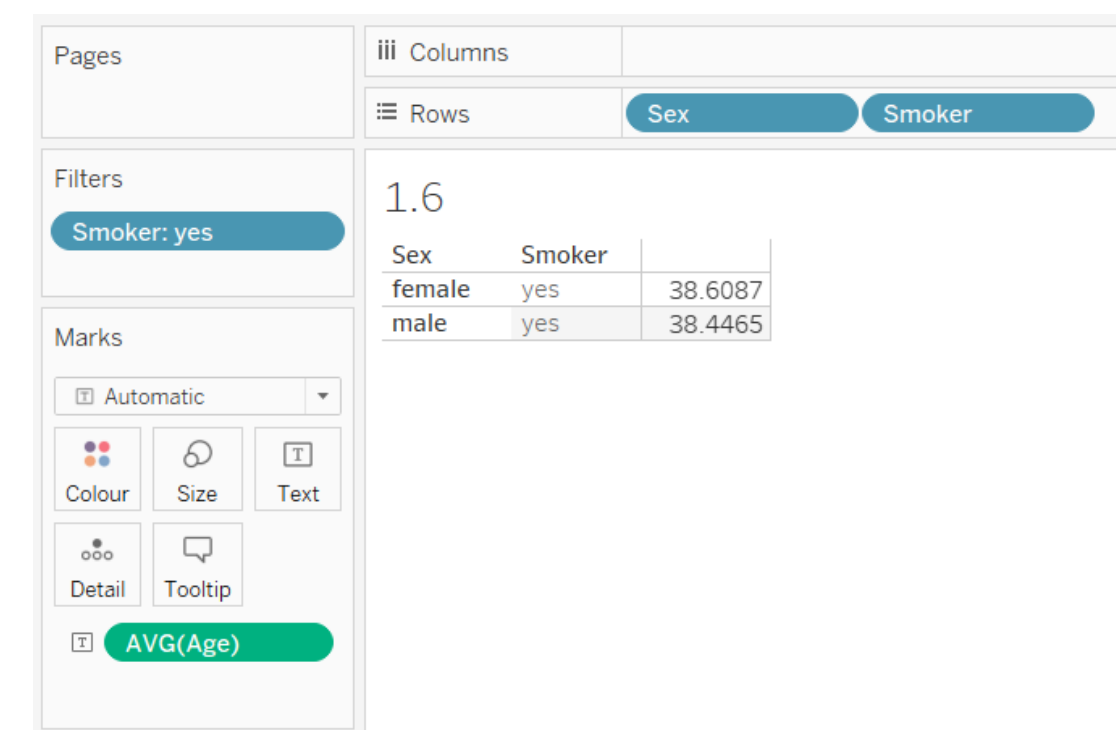
RESULT: No. The variance of a smoker is higher.



Mean of Age, Gender, and a Smoker

- Objective: Is the average age of women and men who smoke the same?

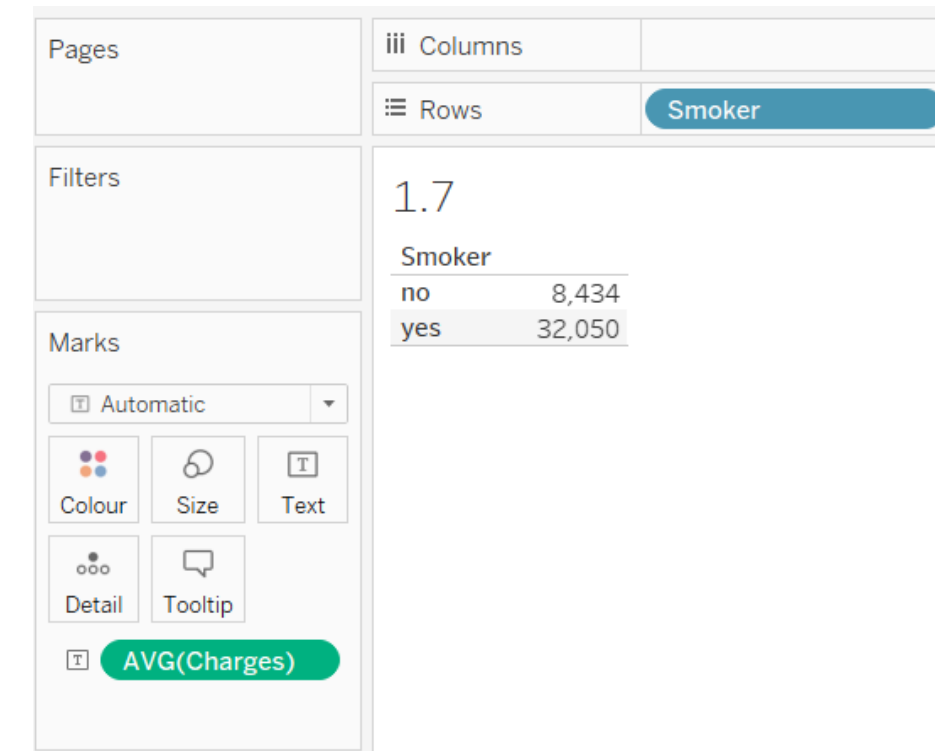
RESULT: Yes, the average age of male smokers & female smokers is 38 years.



Charges & Smoking habit

Objective: Which is higher, the average charges of smokers or non-smokers?

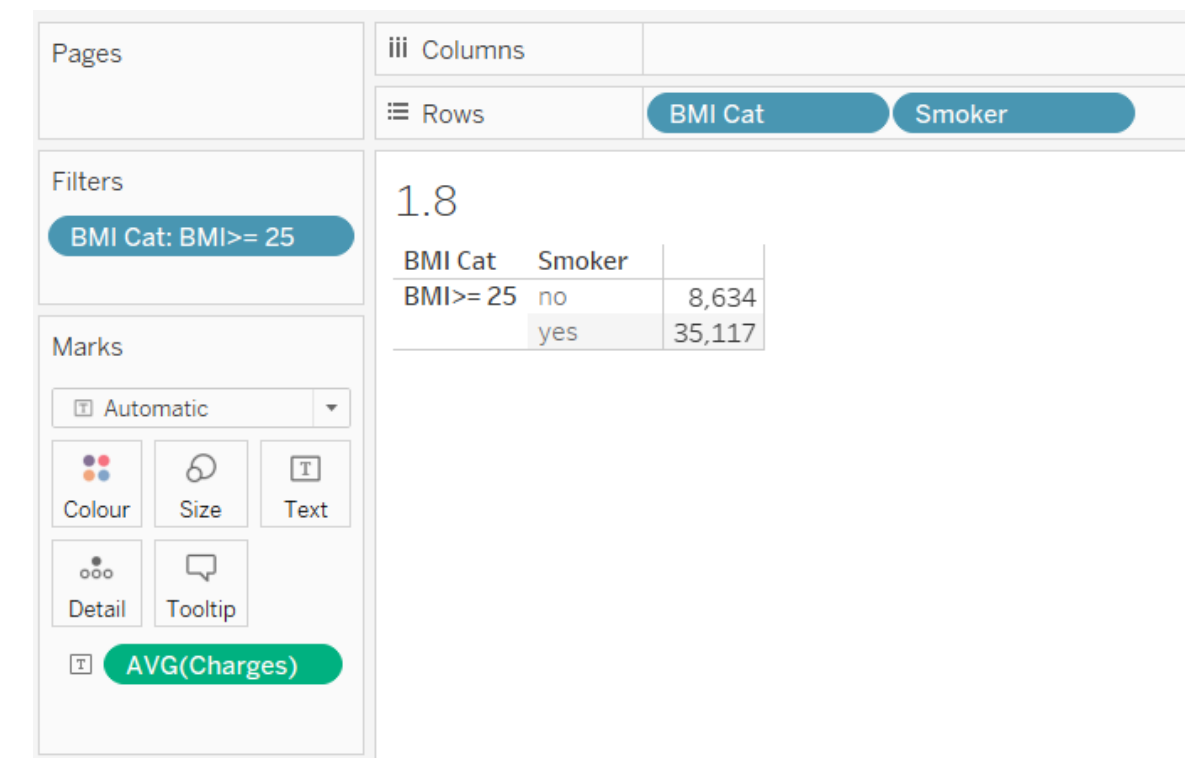
RESULT: The average charge of a smoker is higher by around \$23K



Charges, Smoking Habit, and BMI

- Objective: Which is higher, the average charges of smokers whose BMI is above 25 or non-smokers whose BMI is above 25?

RESULT: The average charge of a smoker with BMI ≥ 25 is higher by around \$26K

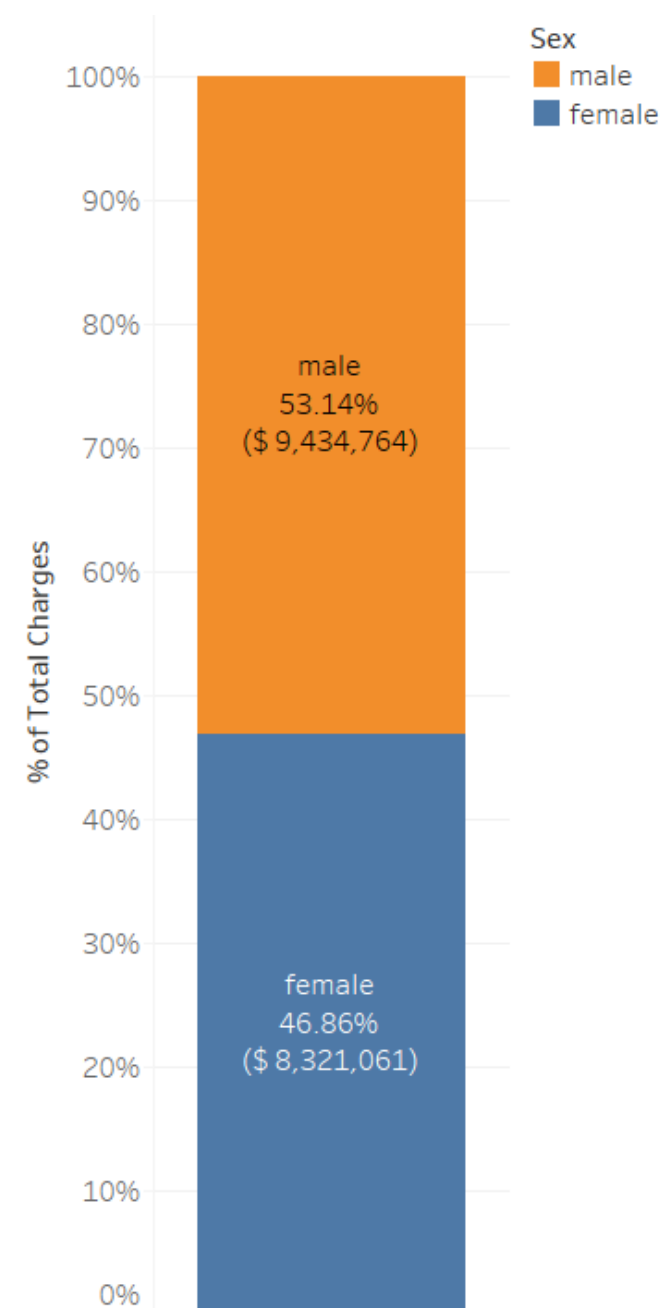


Analysis

- The average age of a smoker **is lower than** the average age of all the primary beneficiaries by one year.
- The average BMI of a smoker is 30.7. Based on the CDC, the average **BMI value of 30.7 falls within the obesity class 1 range.**
- The average charge of a smoker with BMI ≥ 25 is **higher by around \$26K.**

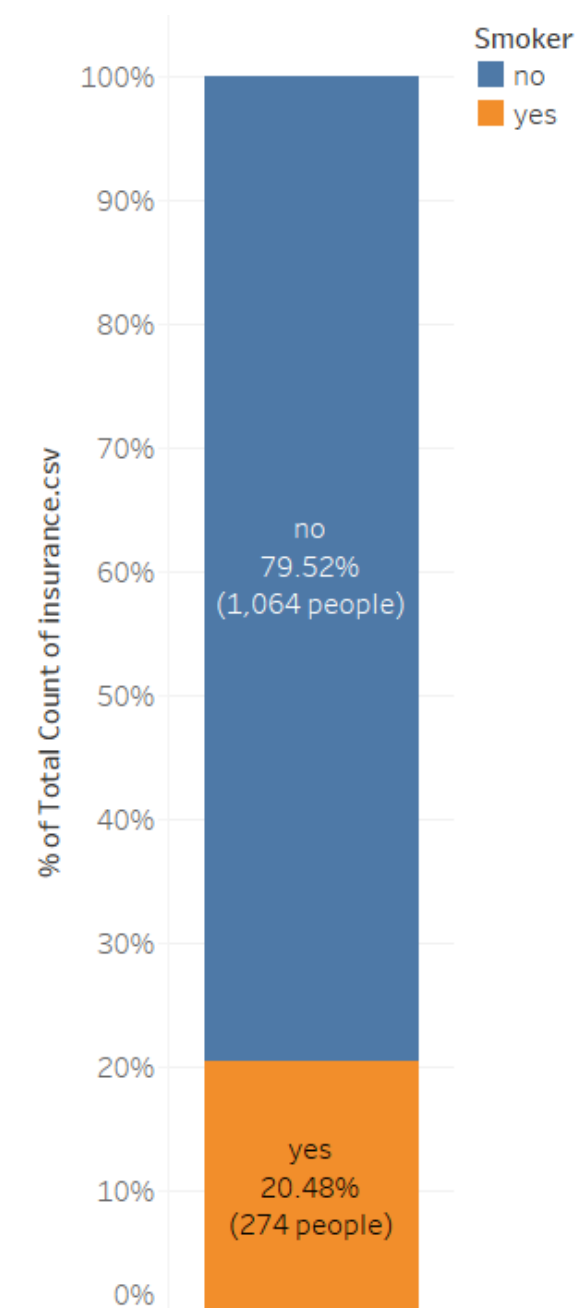
Categorical Variables Analysis

Gender & Charges



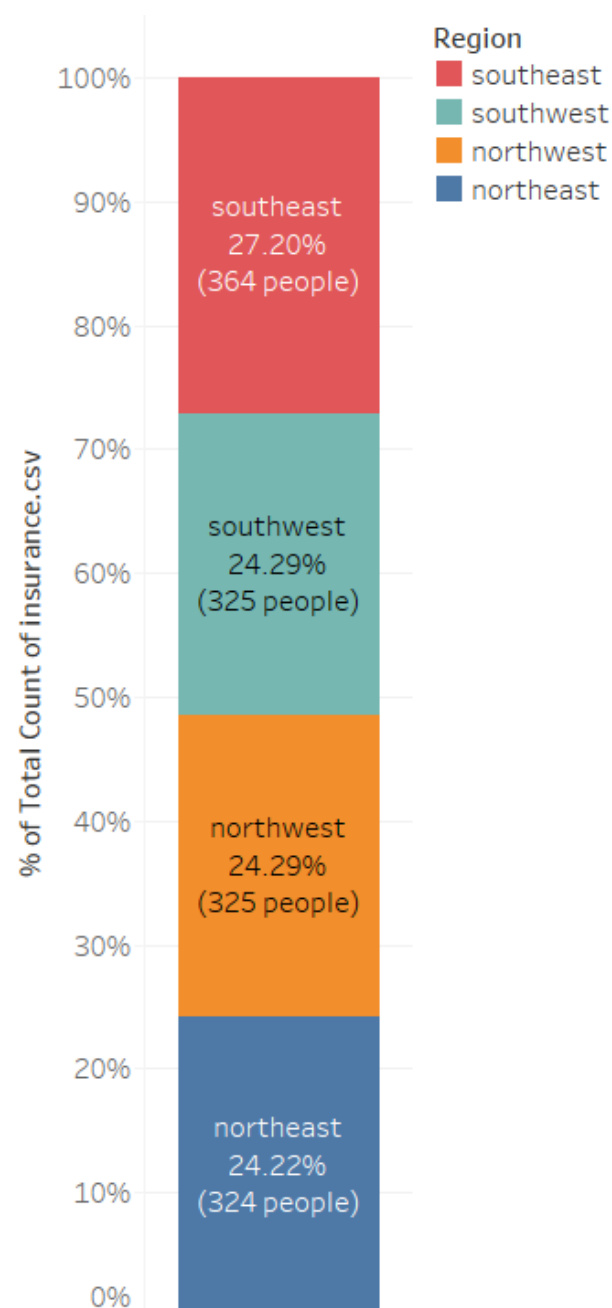
RESULT: The male beneficiaries have a higher proportion of around 6%.

Smoking Habit



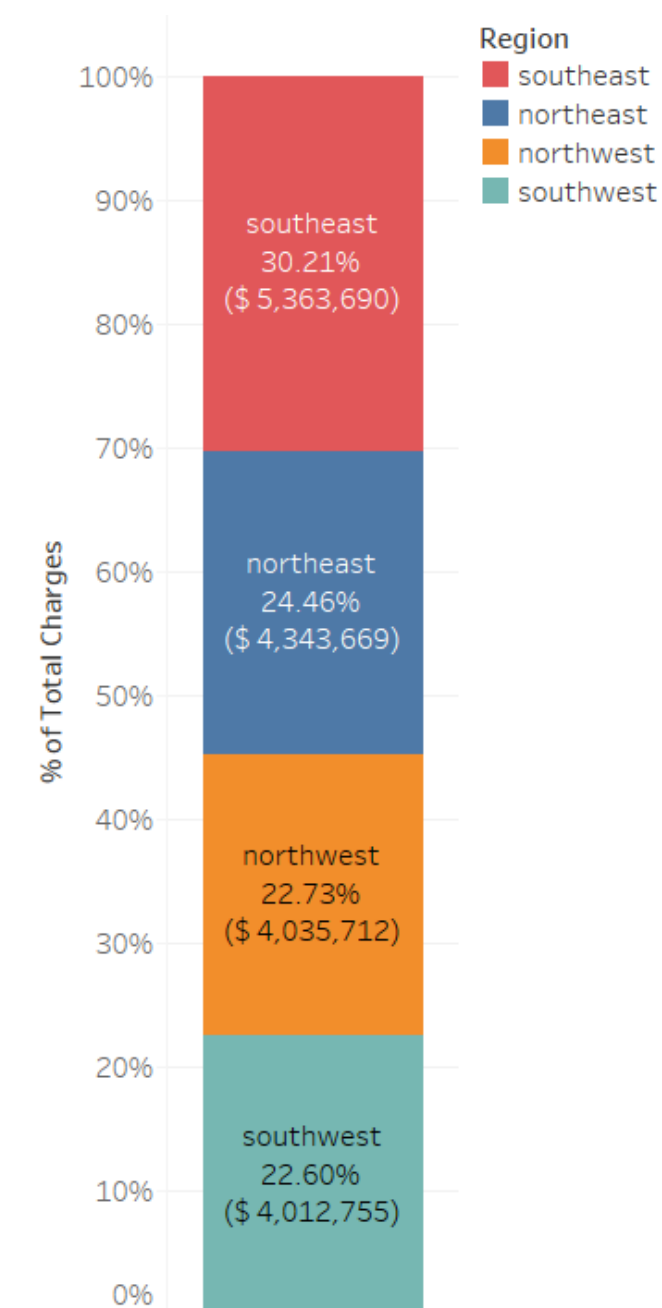
RESULT: Non-Smokers have a higher proportion of around 60%.

Regions



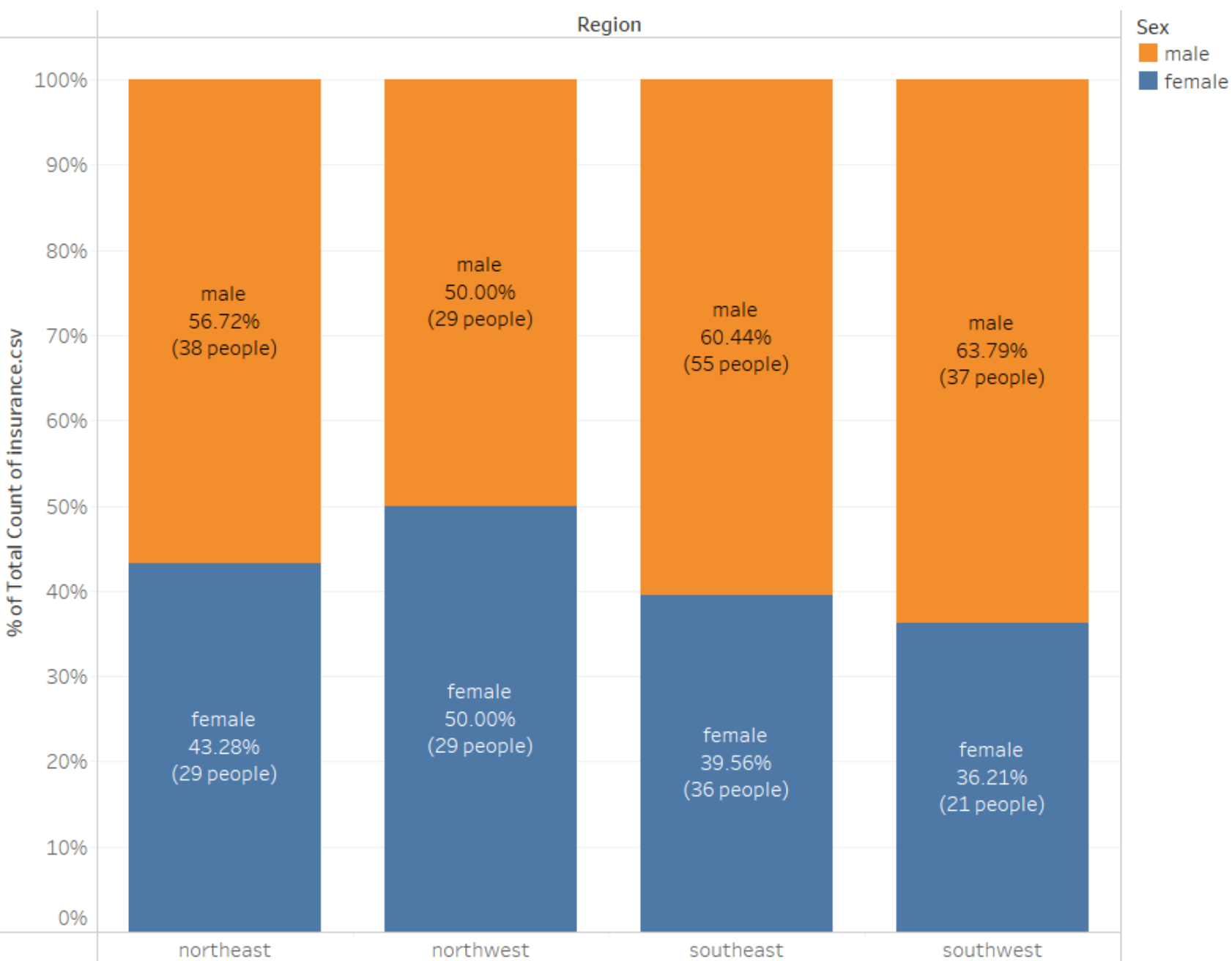
RESULT: The southeast has the highest proportion of people than other regions.

Charges & Region



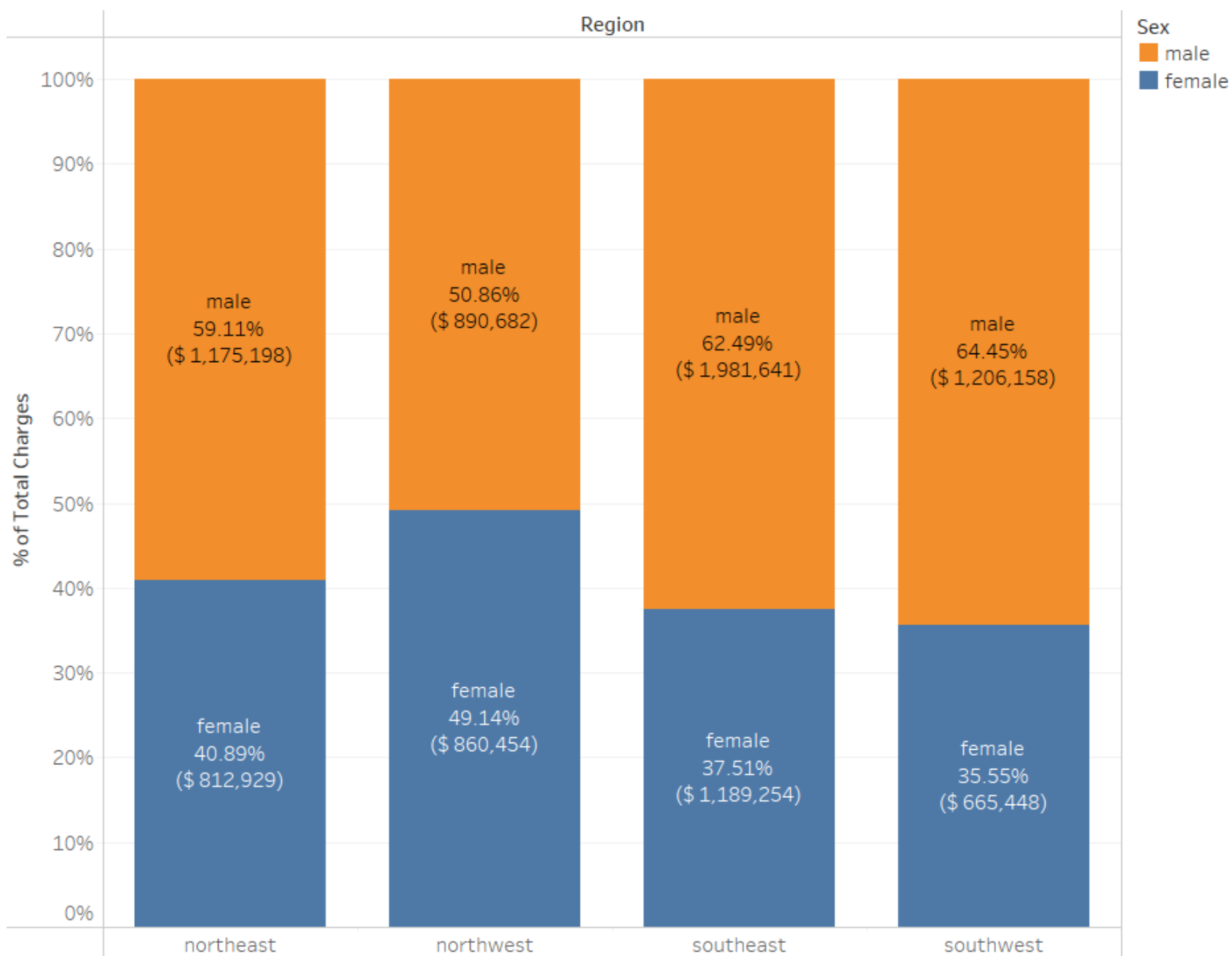
RESULT: The southeast region has the highest proportions of charge than the other regions.

Smoker and Region



RESULT: Male Smokers from the southwest have the highest proportion of people.

Smoker, Region, Charges



RESULT: Male Smokers from the southwest have the highest proportion of charges.

Female & Smoker

RESULT: The probability of a **female** given she's a **smoker** is **41.97%**.

Sex	Smoker	Nbr of Rows	Nbr of Sex	Nbr of Smoker	Nbr of Sex-Smoker	Prob. Sex given Smoker
female	no	1,338	662	1,064	547	51.41%
	yes	1,338	662	274	115	41.97%
male	no	1,338	676	1,064	517	48.59%
	yes	1,338	676	274	159	58.03%

Male & Smoker

RESULT: The probability of a **male** given he's a **smoker** is **58.3%**.

Nbr of Sex

{ FIXED [Sex]:COUNT([insurance.csv]) }

Nbr of Smoker

{ FIXED [Smoker]:COUNT([insurance.csv]) }

Nbr of Sex-Smoker

{ FIXED [Sex],[Smoker]: COUNT([insurance.csv]) }

Prob. Sex given Smoker

SUM([Nbr of Sex-Smoker])/SUM([Nbr of Smoker])

Analysis

- **The Southwest region** has the highest proportion of **male smokers & their charges**.
- **The Northwest region** has the highest proportion of **female smokers & their charges**.
- Although, **the Southeast region** has the highest proportion of **the number of people & their charges**.

Continuous Variables Analysis

Probability of someone has high charges given he's a smoker

```
# Condition 3.3
```

```
condition_3_3 = insurance[(insurance.charges>=16700) & (insurance.smoker == 'yes')]
```

```
# Count length of the data
```

```
n_condition_3_3 = len(condition_3_3)
```

```
n_insurance = len(insurance)
```

```
# Calculate each probability
```

```
pdf_condition_3_3 = np.round(n_condition_3_3/n_insurance,2)
```

```
print("The probability if a smoker has Charges >= 16.7K: ", pdf_condition_3_3)
```

```
✓ 0.4s
```

```
Python
```

```
The probability if a smoker has Charges >= 16.7K: 0.19
```

BMI vs Charges

```
# Condition 3.4
💡 Create conditional data
condition_1_1 = insurance[(insurance.bmi >= 25) & (insurance.charges >= 16700)]
condition_1_2 = insurance[(insurance.bmi < 25) & (insurance.charges >= 16700)]

# Count length of the data
n_condition1_1 = len(condition_1_1)
n_condition1_2 = len(condition_1_2)
n_insurance = len(insurance)

# Calculate each probability
pdf_condition_1_1 = np.round(n_condition1_1/n_insurance,2)
pdf_condition_1_2 = np.round(n_condition1_2/n_insurance,2)

print("The probability if BMI >=25 & Charges >= 16.7K: ", pdf_condition_1_1)
print("The probability if BMI <25 & Charges >= 16.7K: ", pdf_condition_1_2)
```

✓ 0.3s

Python

```
The probability if BMI >=25 & Charges >= 16.7K: 0.21
The probability if BMI <25 & Charges >= 16.7K: 0.04
```


BMI vs Smokers

```
# Condition 3.5
# Create conditional data
condition_2_1 = insurance[(insurance.smoker == 'yes') & (insurance.bmi >= 25) & (insurance.charges >= 16700)]
condition_2_2 = insurance[(insurance.smoker == 'no') & (insurance.bmi >= 25) & (insurance.charges >= 16700)]

# Count length of the data
n_condition2_1 = len(condition_2_1)
n_condition2_2 = len(condition_2_2)
n_insurance = len(insurance)

# Calculate each probability
pdf_condition_2_1 = np.round(n_condition2_1/n_insurance,2)
pdf_condition_2_2 = np.round(n_condition2_2/n_insurance,2)

print("The probability if a smoker & BMI >=25 & Charges >= 16.7K: ", pdf_condition_2_1)
print("The probability if a non-smoker & BMI <25 & Charges >= 16.7K: ", pdf_condition_2_2)
```

✓ 0.5s

Python

```
The probability if a smoker & BMI >=25 & Charges >= 16.7K:  0.16
The probability if a non-smoker & BMI <25 & Charges >= 16.7K:  0.05
```

Analysis

- The probability of someone who has BMI ≥ 25 & Charges $\geq \$16.7K$ is 21%
- The probability of a smoker having Charges $\geq \$16.7K$ is 19%
- The probability of a smoker with BMI ≥ 25 & Charges $\geq \$16.7K$ is 16%.
- **Thus, people who have BMI over 25 & charge more than \$16.7K need to pay a higher premium.**

Variables Correlation

Correlation Matrix

```
corrMatrix = insurance.corr()  
sn.heatmap(corrMatrix, annot=True)  
plt.show()  
✓ 3.6s
```

Python

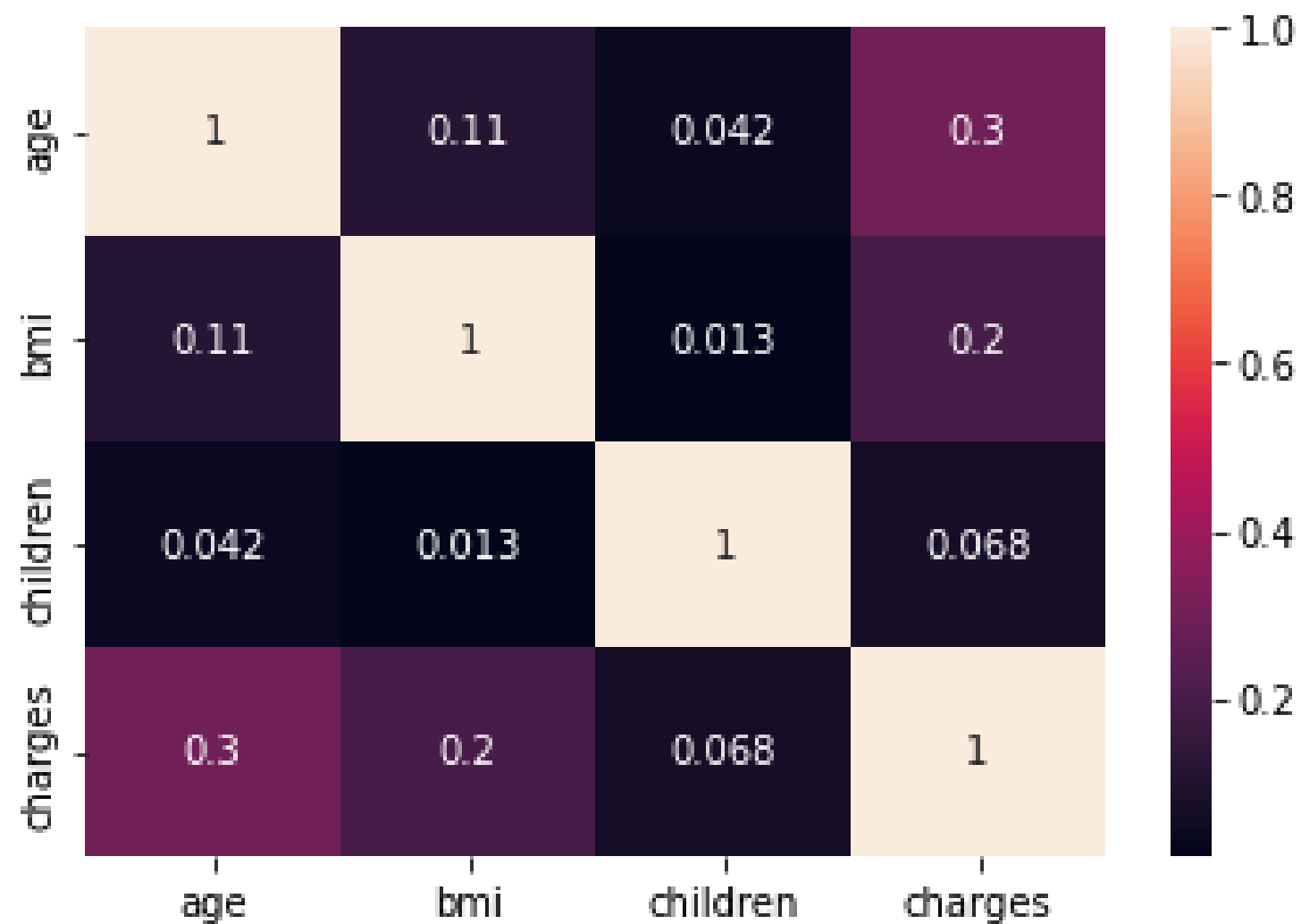


Table 1

Rule of Thumb for Interpreting the Size of a Correlation Coefficient⁴

Size of Correlation	Interpretation
.90 to 1.00 (–.90 to –1.00)	Very high positive (negative) correlation
.70 to .90 (–.70 to –.90)	High positive (negative) correlation
.50 to .70 (–.50 to –.70)	Moderate positive (negative) correlation
.30 to .50 (–.30 to –.50)	Low positive (negative) correlation
.00 to .30 (.00 to –.30)	negligible correlation

[Open in a separate window](#)

RESULT:

- Age has a low positive correlation with charges.

Correlation Matrix with High Charges & BMI

```
# Create conditional data
condition_1_1 = insurance[(insurance.bmi>=25) & (insurance.charges>=16700)]

# Create Correlation Matrix based on the condition
corrMatrix = condition_1_1.corr()
sn.heatmap(corrMatrix, annot=True)
plt.show()
```

✓ 1.3s Python

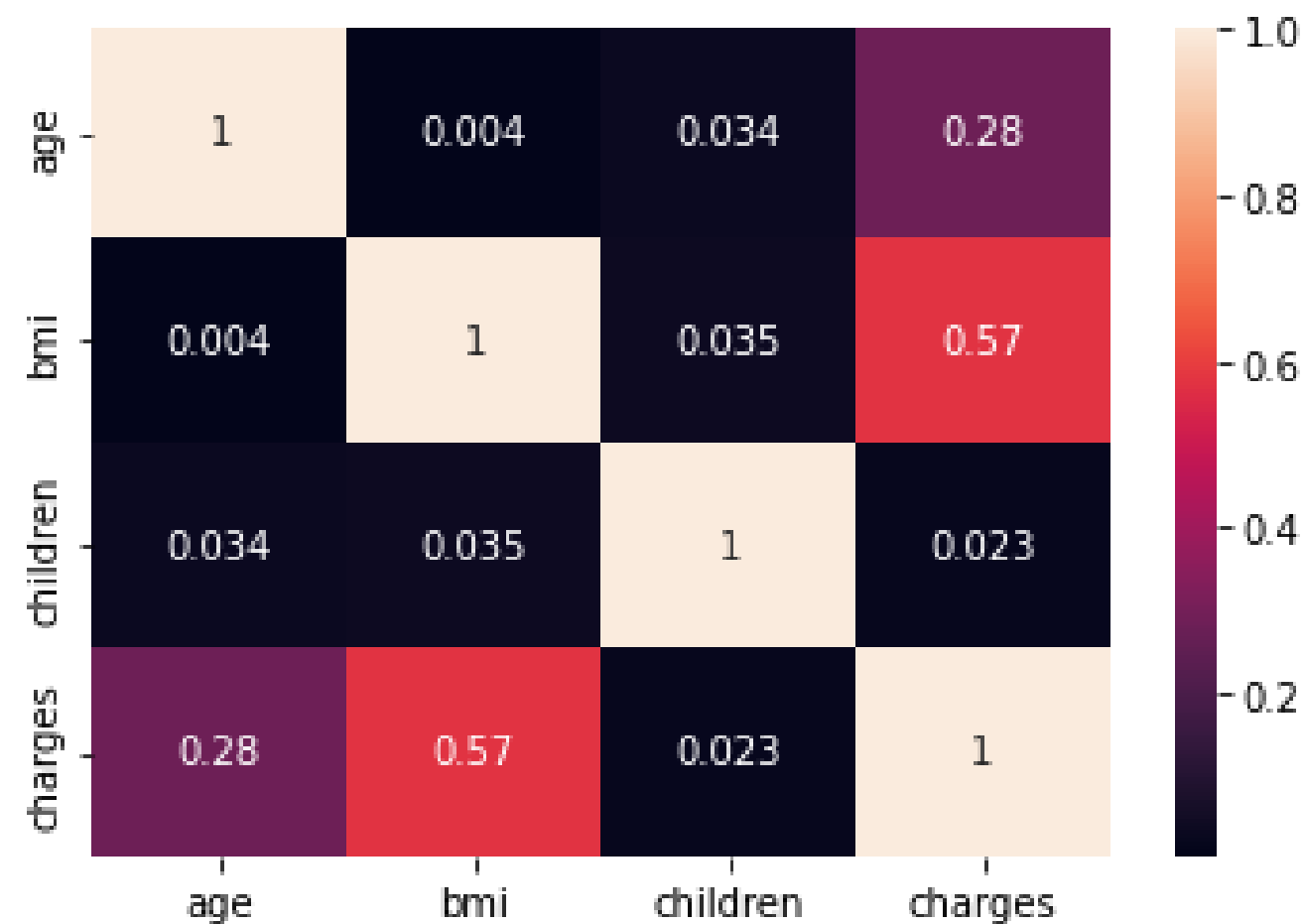


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.00 to .30 (.00 to –.30)	negligible correlation

[Open in a separate window](#)

RESULT:

- BMI has a moderate positive correlation with charges.

Correlation Matrix with Smoker, High Charges & BMI

```
# Create conditional data
condition_2_1 = insurance[(insurance.smoker == 'yes') & (insurance.bmi>=25) & (insurance.charges>=16700)]

# Create Correlation Matrix based on the condition
corrMatrix = condition_2_1.corr()
sn.heatmap(corrMatrix, annot=True)
plt.show()
```

✓ 1.8s

Python

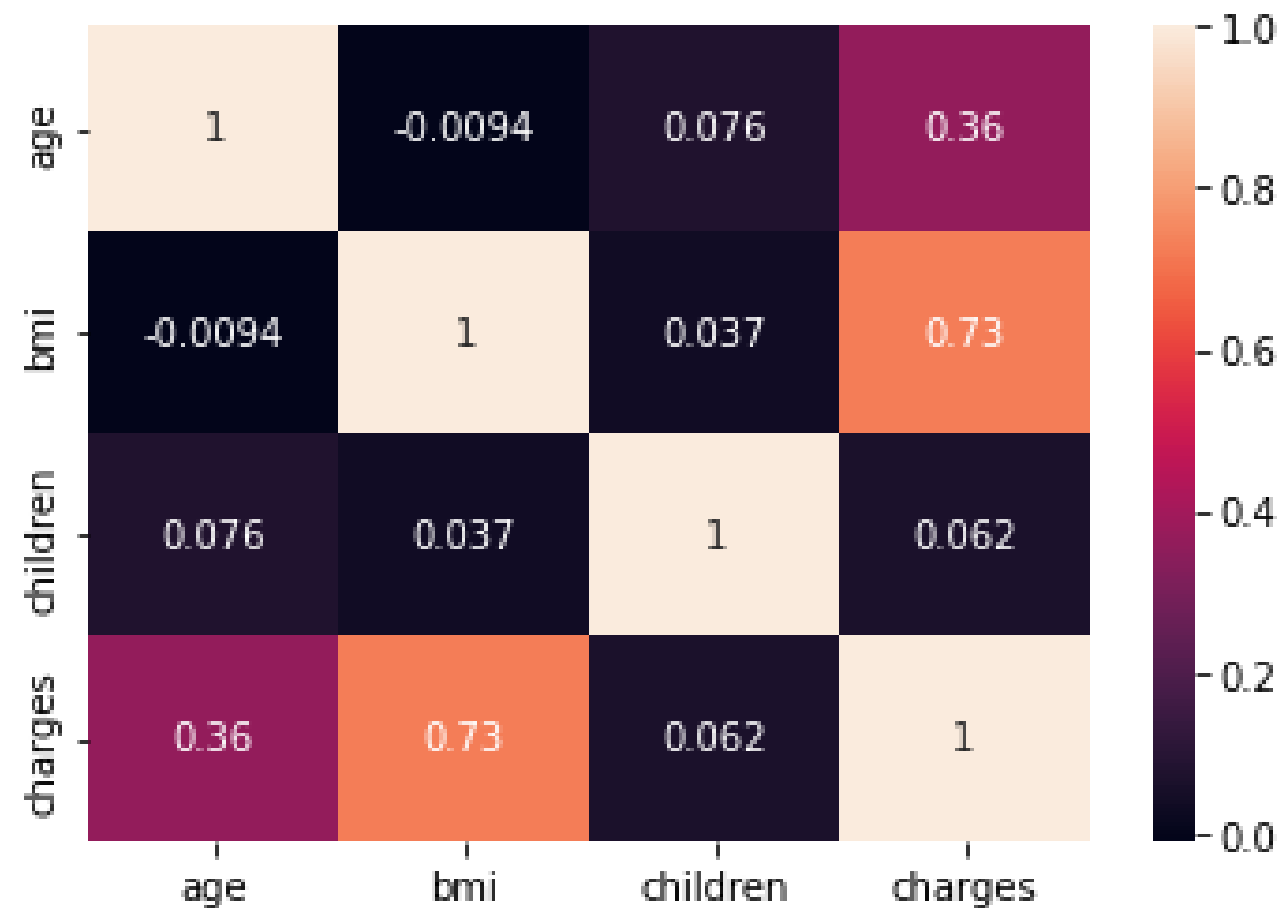


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.00 to .30 (.00 to –.30)	negligible correlation

[Open in a separate window](#)

RESULT:

- BMI has a high positive correlation with charges.
- Age has a low positive correlation with charges

Hypothesis Testing

Smoker's charges are higher than non smoker's

Null Hypothesis: A smoker's charges are greater than the non-smoker's charges
 Alternate Hypothesis: A smoker's charges are smaller than the non-smoker's charges

One-tailed
Independent t test

Significant level: 0.05 (One-tailed)

t Table

cum. prob	<i>t</i> _{.50}	<i>t</i> _{.75}	<i>t</i> _{.80}	<i>t</i> _{.85}	<i>t</i> _{.90}	<i>t</i> _{.95}
one-tail	0.50	0.25	0.20	0.15	0.10	0.05
two-tails	1.00	0.50	0.40	0.30	0.20	0.10

Independent Samples Test

		Levene's Test for Equality of Variances		t-test for Equality of Means					
		F	Sig.	t	df	Sig. (2-tailed)	Mean Difference	Std. Error Difference	90% Confidence Interval of the Difference
charges	Equal variances assumed	403.264	1 .000	46.665	1336	.000	23615.96353	506.0752904	Lower: 22782.96615, Upper: 24448.96092
	Equal variances not assumed			32.752	311.851	.000	23615.96353	721.0565602	Lower: 22426.39725, Upper: 24805.52982

Levene's Test for Equality of Variances: **1**

t-test for Equality of Means: **3**, **< .00001**

RESULT: The Results are statistically significant. Thus, we can reject the null hypothesis.

People with High BMI have higher charges than people with Low BMI

```
insurance_condition['bmi_group'] = np.where(insurance_condition['bmi']>=25, "bmi>=25", "bmi<25")
insurance_condition
```

✓ 0.3s Python

Null Hypothesis: People with High BMI have higher charges than people with Low BMI
 Alternate Hypothesis: People with High BMI have lower charges than people with Low BMI

One-tailed
Independent t test

Significant level: 0.05 (One-tailed)

t Table

cum. prob	<i>t</i> _{.50}	<i>t</i> _{.75}	<i>t</i> _{.80}	<i>t</i> _{.85}	<i>t</i> _{.90}	<i>t</i> _{.95}
one-tail	0.50	0.25	0.20	0.15	0.10	0.05
two-tails	1.00	0.50	0.40	0.30	0.20	0.10

Independent Samples Test

Levene's Test for Equality of Variances		t-test for Equality of Means						90% Confidence Interval of the Difference	
		F	Sig.	t	df	Sig. (2-tailed)	Mean Difference	Std. Error Difference	
bmi	Equal variances assumed	145.082	1 .000	31.856	1336	.000	10.355727	.325084	9.820640 10.890814
	Equal variances not assumed		2	51.246	920.106	.000	10.355727	.202077	10.023004 10.688450

Levene's Test for Equality of Variances

< .00001

RESULT: The Results are statistically significant. Thus, we can reject the null hypothesis.

Male's BMI is equal to Female's BMI

Null Hypothesis: Male's BMI is equal to Female's BMI
 Alternate Hypothesis: Male's BMI is not equal to Female's BMI

two-tailed Independent
t test

Significant level: 0.05 (Two-tailed)

		Levene's Test for Equality of Variances		t-test for Equality of Means						
		F	Sig.	t	df	Sig. (2-tailed)	Mean Difference	Std. Error Difference	95% Confidence Interval of the Difference	
									Lower	Upper
bmi	Equal variances assumed	.003	.956	1.697	1336	.090	.565379	.333213	-.088298	1.219056
	Equal variances not assumed			1.697	1335.960	.090	.565379	.333159	-.088192	1.218950

Levene's Test for Equality of Variances

RESULT: The Results are not statistically significant. Thus, we cannot reject the null hypothesis.

Conclusion

Conclusion

- The average BMI of a smoker is 30.7. Based on the CDC, the average BMI value of 30.7 falls within the obesity class 1 range.
- The Southwest region has the highest proportion of male smokers & their charges.
- The Northwest region has the highest proportion of female smokers & their charges.
- People who have BMI over 25 & charge more than \$16.7K need to pay a higher premium.
- Based on the condition that there's a group of smokers who have a BMI over 25 & charge more than \$16.7K, the BMI has a high positive correlation with charges

Thus, a group of smokers who have a BMI over 25 & charge more than \$16.7K need to pay the highest premium.

Notes

- I use three different application, such as Tableau, Python, and SPSS

Reference

- [A guide to appropriate use of Correlation coefficient in medical research](#)
- [Defining Adult Overweight & Obesity](#)
- [P Value from T Score Calculator](#)