

Natural Language Processing

Assignment 4

Type of Question: MCQ

Number of Questions: 7 Total Marks: $(4 \times 1) + (3 \times 2) = 10$

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1. Baum-Welch algorithm is an example of - **[Marks 1]**

- A) Forward-backward algorithm
- B) Special case of the Expectation-maximisation algorithm
- C) Both A and B
- D) None

Answer: C

Solution: Theory.

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2. Once a day (e.g. at noon), the weather is observed as one of state 1: rainy state 2: cloudy state 3: sunny The state transition probabilities are :

0.4	0.3	0.3
0.2	0.6	0.2
0.1	0.1	0.8

Given that the weather on day 1 ($t = 1$) is sunny (state 3), what is the probability that the weather for the next 7 days will be “sun-sun-rain-rain-sun-cloudy-sun”?

[Marks 2]

- A) 1.54×10^{-4}
- B) 8.9×10^{-2}
- C) 7.1×10^{-7}
- D) 2.5×10^{-10}

Answer: A

Solution:

$O = \{S3, S3, S3, S1, S1, S3, S2, S3\}$

$P(O \mid \text{Model})$

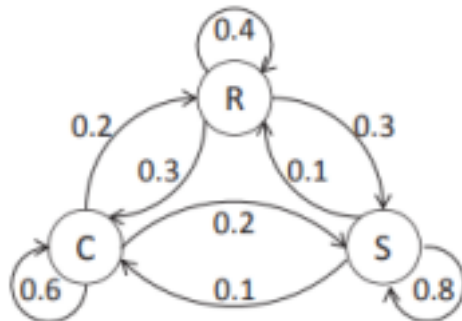
$= P(S3, S3, S3, S1, S1, S3, S2, S3 \mid \text{Model})$

$= P(S3) P(S3|S3) P(S3|S3) P(S1|S3) P(S1|S1) P(S3|S1) P(S2| S3)$

$P(S3|S2) = Q3 \cdot a_{33} \cdot a_{33} \cdot a_{31} \cdot a_{11} \cdot a_{13} \cdot a_{32} \cdot a_{23}$

$= (1)(0.8)(0.8)(0.1)(0.4)(0.3)(0.1)(0.2)$

$= 1.536 \times 10^{-4}$



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3. In the question 2, the expected number of consecutive days of sunny weather is:

- A) 2
- B) 3
- C) 4
- D) 5

[Marks 1]

Answer: D

Solution:

$\text{Exp}(i) = 1/(1-p_{ii})$ So for sunny the $\text{exp} = 1/(1-0.8) = 5$

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4. You are building a model distribution for an infinite stream of word tokens. You know that the source of this stream has a vocabulary of size 1200. Out of these 1200 words you know of 200 words to be stop words each of which has a probability of 0.001. With only this knowledge what is the maximum possible entropy of the modelled distribution. (Use log base 10 for entropy calculation) [Marks 2]

- A) 2.079
- B) 4.5084
- C) 2.984
- D) 3.0775

Answer: D

Solution: There are 200 stopwords with each having an occurrence probability of 0.001. Hence,

$$P(\text{Stopwords}) = 200 * 0.001 = 0.2$$

$$P(\text{non-stopwords}) = 1 - 0.2 = 0.8$$

For maximum entropy, the remaining probability should be uniformly distributed. For every non-stopword w , $P(w) = 0.8/(1200 - 200) = 0.8/1000 = 0.0008$. Finally, the value of the entropy would be,

$$\begin{aligned} H &= E(\log(1/p)) \\ &= -200(0.001 * \log(0.001)) - 1000(0.0008 \log(0.0008)) \\ &= -200(0.001 * (-3)) - 1000(0.0008 * (-3.0969)) \\ &= 0.6 + 2.4775 \\ &= 3.0775 \end{aligned}$$

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5. Suppose you have the input sentence “Sachin Tendulkar is a great player”.

And you know the possible tags each of the words in the sentence can take.

- Sachin: NN, NNS, NNP, NNPS
- Tendulkar: NN, NNS, NNP, NNPS
- is: VB
- a: DT
- great: ADJ
- player: NN, NNS, NNP

How many possible hidden state sequences are possible for the above sentence and States? **[Marks 1]**

- A) $4 \times 3 \times 3$
- B) 4^{3^3}
- C) $2^4 \times 2^3 \times 2^3$
- D) 3×4^2

Answer: D

Solution: Each possible hidden sequence can take only one POS tag for each of the words. Hence the total possibility will be a product of the number of candidates for each word.

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6. What are the space and time complexity order of the Viterbi algorithm? K is the

number of states and N number of time steps.

[Marks 1]

- A) KN, K^2N
- B) K^2N, KN
- C) K^2N, K^2N
- D) KN, KN

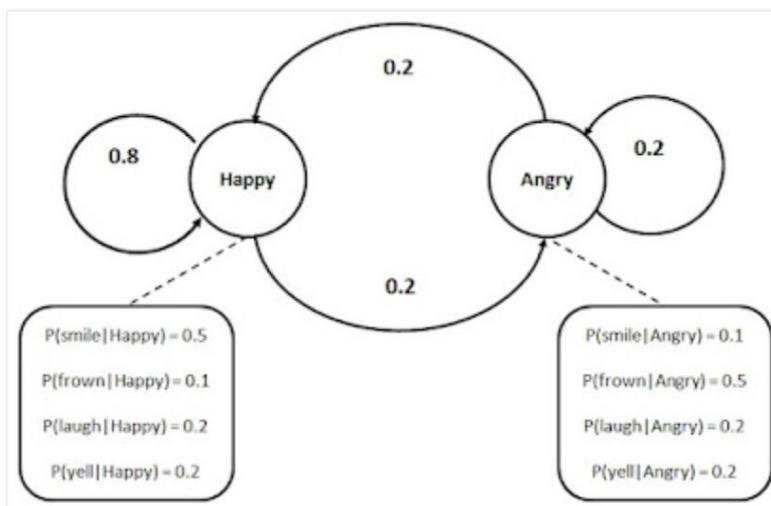
Answer: A

Solution: The sum-product algorithm is polynomial. The time complexity is $O(K^2N)$, the space complexity is $O(KN)$, where K is the number of states and N number of time steps.

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7. Mr. X is happy someday and angry on other days. We can only observe when he smiles, frowns, laughs, or yells but not his actual emotional state. Let us start on day 1 in a happy state. There can be only one state transition per day. It can be either a happy state or an angry state. The HMM is shown below-

Assume that q_t is the state on day t and o_t is the observation on day t. Answer the following questions;



What is $P(o_2 = \text{frown})$?

[Marks 2]

- A) 0.56
- B) 0.18
- C) 0.03
- D) 0.78

Answer: B

Solution: We need to find the probability of observation *frown* on day 2. But we don't know whether he is happy or not on day 2 (we know he was happy on day 1). Hence, the probability of the observation is the sum of products of observation probabilities and all possible hidden state transitions.

$$\begin{aligned} P(o_2 = \text{frown}) &= P(o_2 = \text{frown} \mid q_2 = \text{Happy}) + P(o_2 = \text{frown} \mid q_2 = \text{Angry}) \\ &= P(\text{Happy} \mid \text{Happy}) * P(\text{frown} \mid \text{Happy}) + P(\text{Angry} \mid \text{Happy}) * P(\text{frown} \mid \text{Angry}) \\ &= (0.8 * 0.1) + (0.2 * 0.5) = 0.08 + 0.1 = 0.18 \end{aligned}$$