

LIVE SESSION 9 (NOC24_CS39)

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unsupervised algo

**

LDA: Latent Dirichlet Allocation

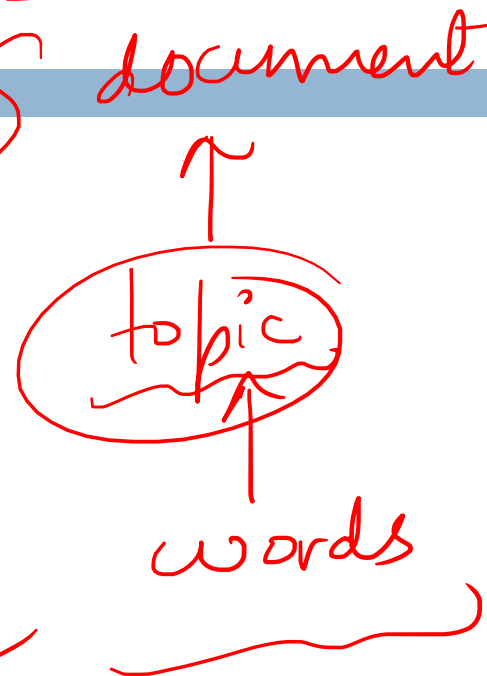
hidden / ~~not known~~ a priori (not known beforehand)
topics are unknown / hidden in the data
The document \in topics topics are believed to be present. \therefore text is generated based on topics

Dirichlet: distribution of distributions

Document \equiv topics \equiv words

Dirichlet is distribution of topics in doc.

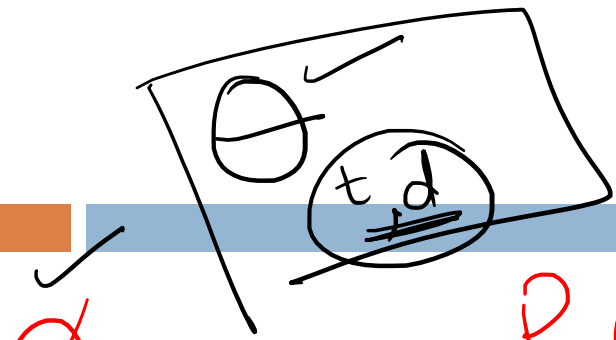
Δ ~~topic~~
distribution of words in a topic



Allocation: once we have Dirichlet, we will
allocate topics to documents & words of the

document to topics

LDA: each word in each doc. comes from a topic
& the topic is selected from a per-
document distribution of topics



$\alpha_{t,d}$ = $P(t|d)$ = prob. distribution of topics in a document.



$\beta_{w,t}$ = $P(w|t)$ = prob. distribution of words in a topic

$$LDA = \sum_{t \in T} P(\underbrace{w|t}) \cdot P(t|d)$$

$$P(w|t)$$

LDA

$$= \sum_{t \in T} P(w|t, d) \cdot P(t|d)$$

Assume we have conditional independence

$$\prod$$

$$\sum_{t \in T}$$

$$P(w|t) \cdot P(t|d)$$

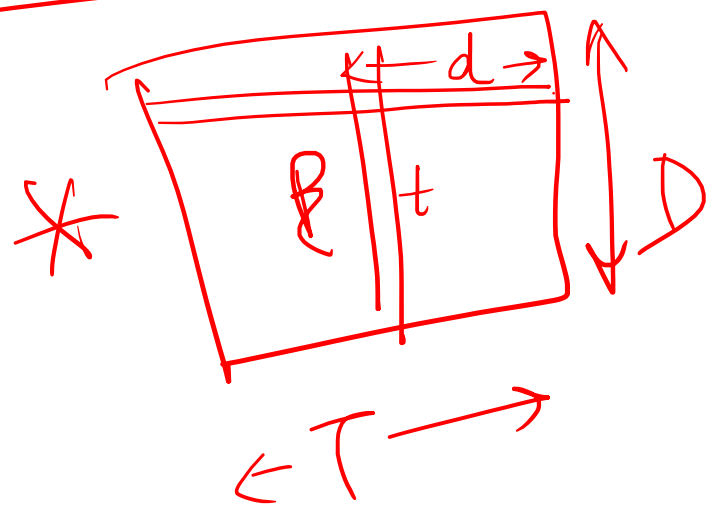
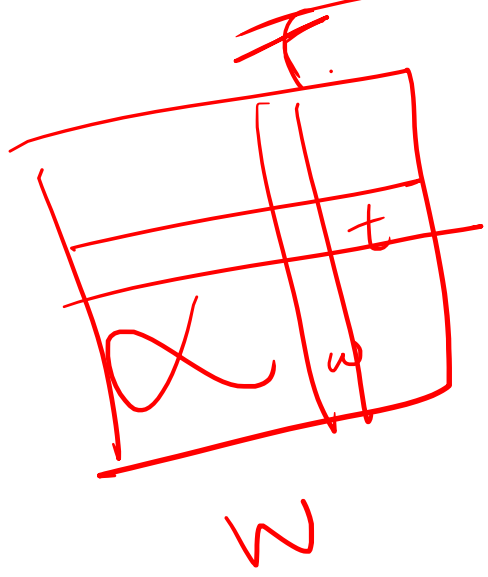
T : # topics

$W(V)$: # words in the entire collection of documents vocabulary

Goal

$$P(w|d) =$$

$$\sum_{t=1}^T \underline{P(w|t)} \cdot \underline{p(t|d)}$$



$\theta \phi$

Dirichlet parameters (α, ξ)

→ control if all words have same probability in a topic

OR

will that topic have extreme bias towards some words

dataset : all news articles of ^{France} country from 2018

I want to make use of LDA to find out topics

eg. } France won 2018 world cup

Document has words (V) { football,
world cup

2018

winners
france

(N) (S)

~~Given~~: Self Random assignment of topics to words in a doc

Doc	T3	T2	T1	T3	T1
	football	world cup	2018	winners	<u>france</u>

Given K = No. of topics = 3

Doc	T1	T2	T3
	2	1 0	2

Plus, you also have a count how many times a word is associated with a given topic

	T_1	T_2	T_3
Football	1	0	35
<u>World Cup</u>	10	8 7	1
Golf	42	1	0
winners	0	0	20
France	50	0	1

Idea: After random initialization, you want to

converge at a point where words signify the

topic that you're trying to figure out so

"we can go on reassigning the topic of
each word at every pass".

↓ reduce the count of world cup & τ_2 from 1 to 0
& remove the topic assigned to it so

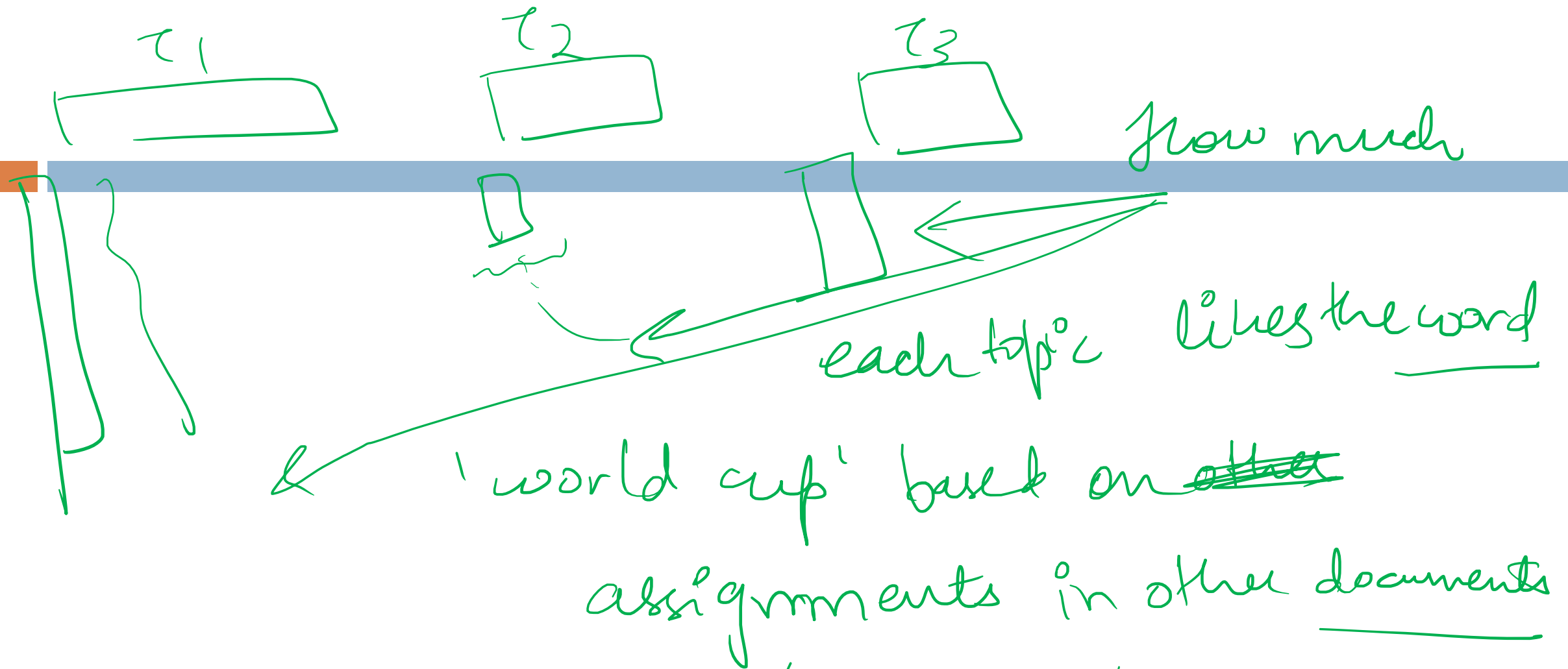
then the count changes

Reassign the topic based on probability distribution

Topic 1 Topic 2 Topic 3

	τ_1	τ_2	τ_3
Doc	2	0	2

How much doc likes each topic based on other assignments in the doc



	τ_1	τ_2	τ_3
world cup	10	7	1

How much doc likes \times How much topic likes
each topic a word.

Repeat for all words in corpus in one pass & depending on how many passes you're in LDA setup, this process "reassigning" topics for all words at every pass & after that; a stage will come when whole convergence would happen]



Question 1

In Topic modeling which hyperparameters tuning used for represents document-topic Density? *distribution*

- a) Dirichlet hyperparameter Beta
- ☒ b) Dirichlet hyperparameter alpha
- c) Number of Topics (K)
- d) None of them

Answer - b) Dirichlet hyperparameter alpha

Question 2

n Topic modeling which hyper parameters tuning used for represents Word-Topic Density?

- a) Alpha parameter
- b) Number of Topics (K)
- ☒ c) Beta parameter
- d) None of them

Ans: c

Question 3

Classically, topic models are introduced in the text analysis community for_____ topic discovery in a corpus of documents.

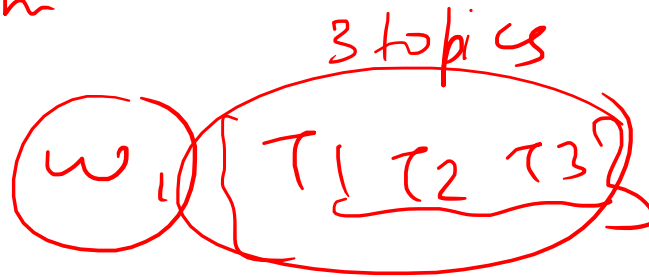
- a) Unsupervised.
- b) Supervised.
- c) Semi-automated.
- d) None of the above.

Answer - a) Unsupervised

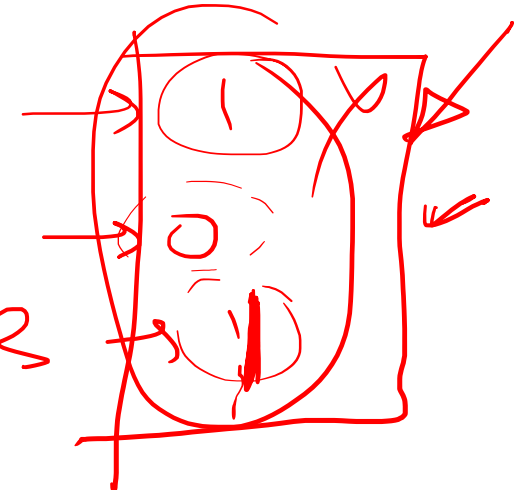
- LDA is an unsupervised learning algorithm, meaning it doesn't use labeled data to guide its learning process. It operates solely on the assumption that documents are generated from a fixed number of topics, and the goal is to uncover these topics. Without external guidance or criteria, it cannot determine the optimal number of topics.

$$|V| = 5$$

spam ham



email 1
email 2
email 3



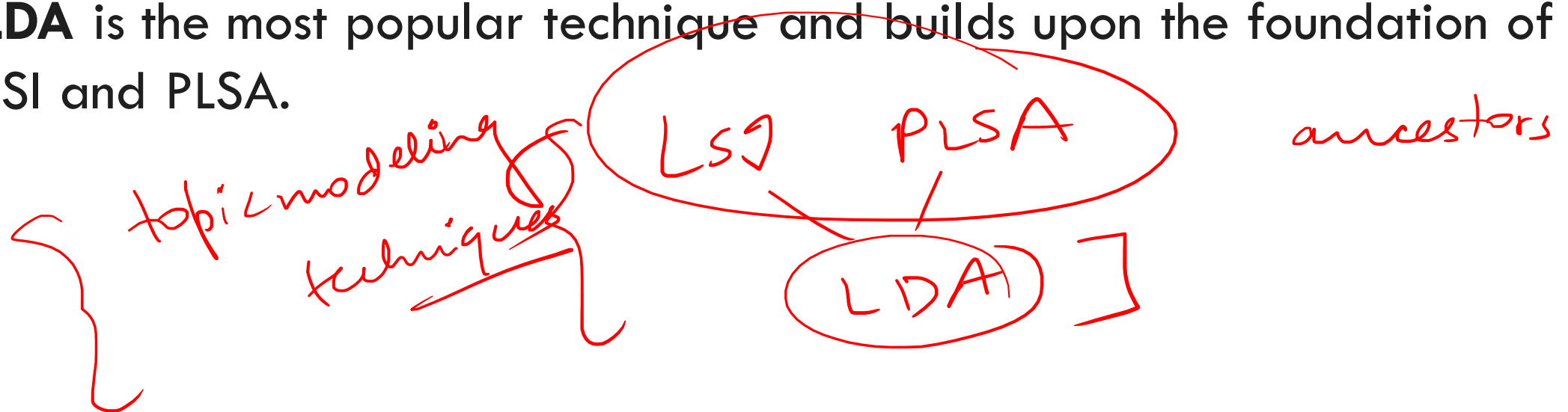
Question 4

Topic model techniques is/are _____ .

- a) Latent semantic indexing (LSI).
- b) Probabilistic latent semantic analysis (PLSA).
- c) Latent Dirichlet allocation (LDA).
- d) All of the above.

Answer - d) All of the above

- Latent semantic indexing (LSI), probabilistic latent semantic analysis (PLSA), and latent Dirichlet allocation (LDA) are all **topic model techniques**.
- **LSI** and **PLSA** are considered forerunners to LDA. They identify underlying themes in documents.
- **LDA** is the most popular technique and builds upon the foundation of LSI and PLSA.



Question 5

_____ is a scoring of how rare the word is across documents.

☒ a) Inverse Document frequency.

☐ b) Term frequency.

☐ c) File frequency.

☐ d) None of the above.

Answer - a) Inverse Document frequency

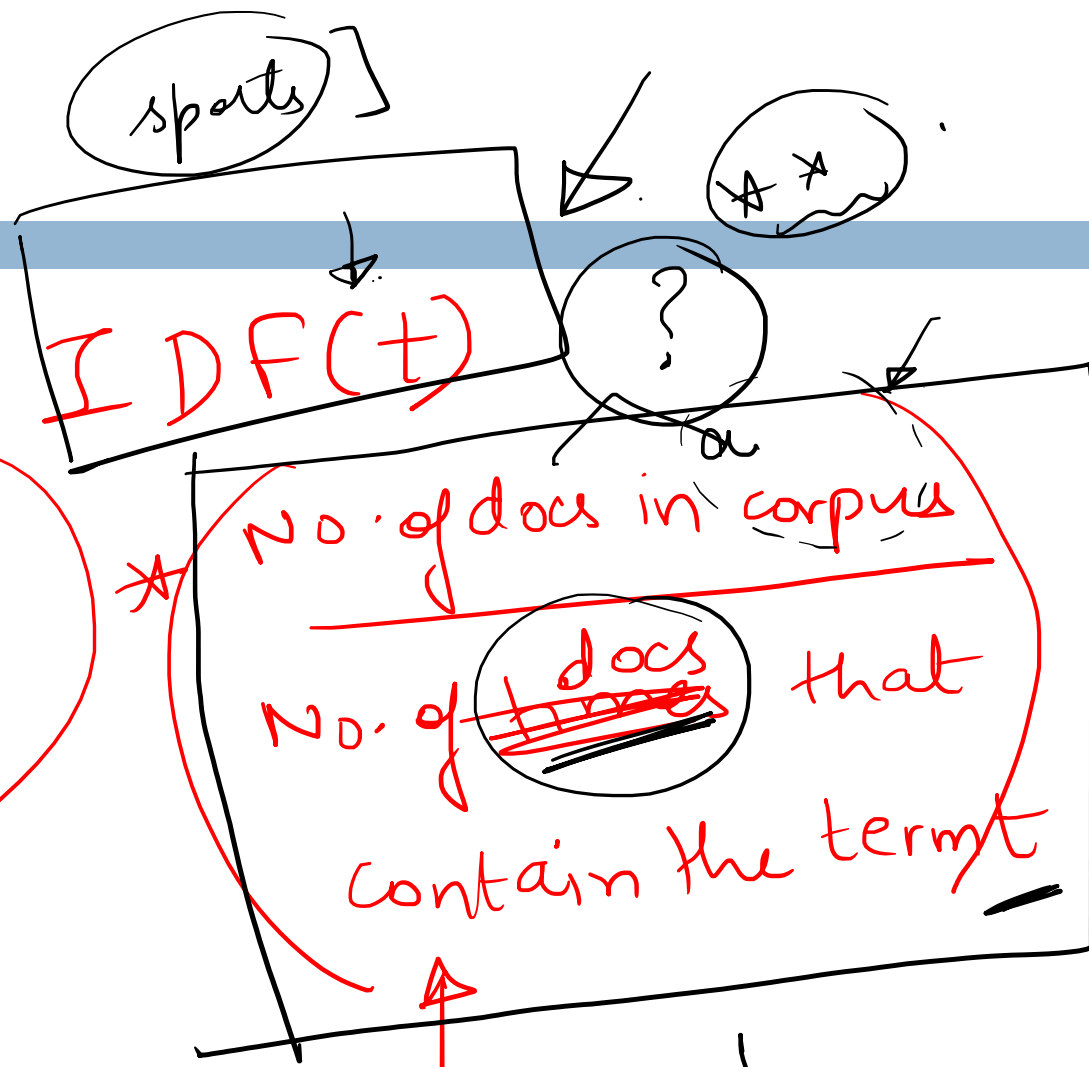
raw count

$$TF - IDF = TF(t, d) * IDF(t)$$

= $\frac{\text{No. of times } t \text{ appears in } d}{\text{No. of terms in } d}$

all terms

gives higher weightage to terms that occur less freq.

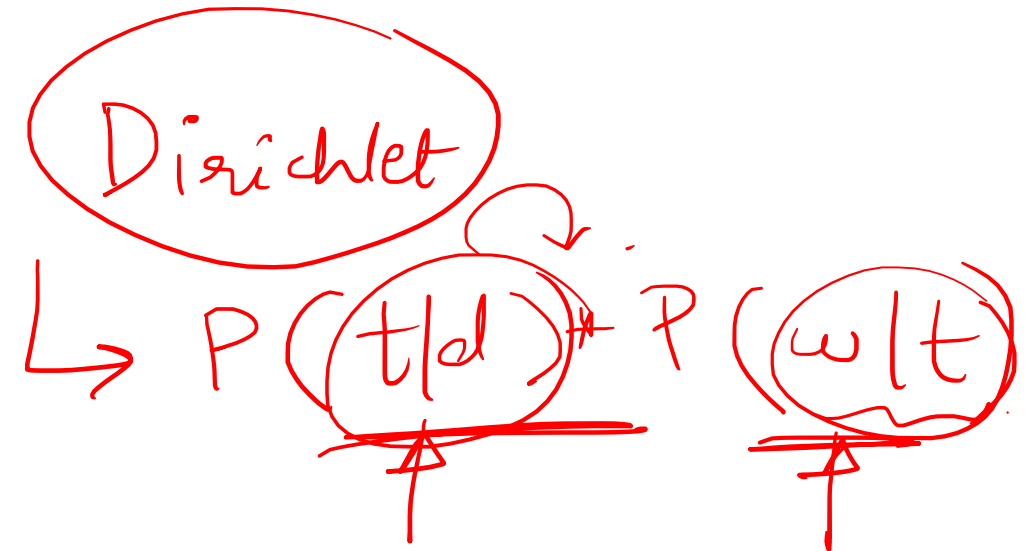


Question 6

Latent Dirichlet Allocation (LDA) and Latent Semantic Allocation (LSA) are based on _____ assumptions.

- a) Distributional hypothesis.
- ~~b) Statistical mixture hypothesis.~~
- ~~c) Both of the above.~~
- d) Not any from (a) and (b).

Answer - c) Both of the above



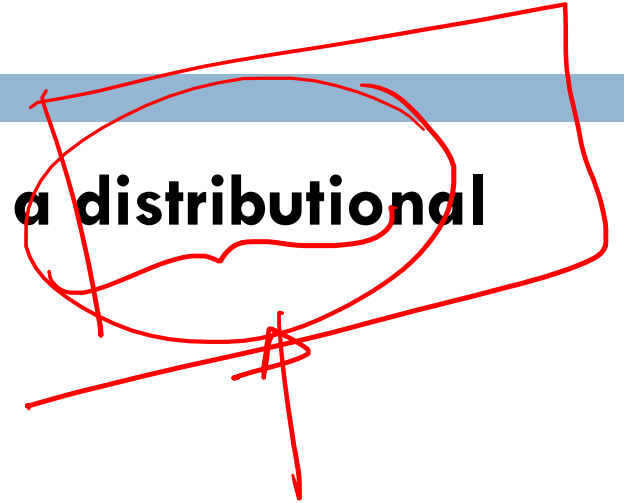
pitch trophy
worldcup cricket
sports

- **Distributional hypothesis:** This assumption applies to both LDA and LSA. It states that words with similar meanings tend to appear in similar contexts within documents. This allows the models to identify relationships between words based on how often they co-occur.
- **Statistical mixture hypothesis:** This assumption is particularly important for LDA. ~~It suggests~~ that documents are a mixture of latent topics, and each topic is characterized by a probability distribution over words. This allows LDA to not only identify topics but also represent the proportion of each topic within a document.
 $\rightarrow P(w|t) * P(t|d)$
- LSA leverages the distributional hypothesis to uncover semantic relationships, while LDA builds upon that foundation with the statistical mixture hypothesis to model documents as a combination of latent topics.

Question 7

One of the basic assumptions of LDA and LSA as a **distributional hypothesis** which means _____.

- ☒ a) Similar topics make use of similar words.
- b) Different topics make use of similar words.
- c) Similar topics make use of different words.
- d) None of the above.



Question 8

Latent Semantic analysis

D.H.T.S.H.

One of the basic assumptions of LDA and LSA as a statistical mixture hypothesis which means _____.

- ☒ a) Documents talk about several topics.
- b) Similar topics make use of similar words.
- c) Documents talk about prefixed topics.
- d) None of the above.

] Distributional hypothesis

You just specify K (# of topics) ✓ ~~(N)~~ ~~(K)~~ ~~(D)~~]

Question 9

- **LSA, LDA also ignores syntactic information and treats documents as bags of words. True/False**

True

* [lovely, beautiful \in aesthetics
 D.H. sunrise, sunset \in nature / photography S.H. / D.H.]

- Both LSA and LDA focus on word co-occurrence and treat documents as bags of words, ignoring the syntactic structure and word order within the documents. This simplification allows them to handle large amounts of text data efficiently but can miss out on capturing the nuances of language conveyed through sentence structure and grammar.

S.H. $\& (w|t) \rightarrow P(t|d)$ POS
 Dependency tree

Question 10

α , β

Choose the correct statement from below –

- I. A low value of alpha will assign fewer topics to each document whereas a high value of alpha will have the opposite effect.
- II. A low value of beta will use fewer words to model a topic whereas a high value will use more words, thus making topics more similar between them.

- ☒ III. LDA cannot decide on the number of topics by itself. (correct)
→ specified by user / programmer
- a) (I).
 - b) (II).
 - c) III).
 - d) All of the above.

- Latent Dirichlet Allocation (LDA) is a powerful tool for uncovering hidden thematic structures in text data, but it has one key limitation: it can't determine the optimal number of topics on its own. Here's why:
 - **Trade-off between granularity and coherence:** Imagine a collection of documents. With a very high number of topics, LDA might identify very specific themes, like "baking cookies" or "fixing a leaky faucet." While these are technically topics, they may not be very informative. On the other hand, with too few topics, LDA might lump together unrelated concepts under a broad umbrella like "food" or "home improvement." There's a sweet spot where the topics are both specific and meaningful.
 - **The model doesn't understand meaning:** LDA is a statistical model that works with word probabilities, not semantics. It doesn't inherently "know" what a good topic is. It can only find clusters of words that frequently co-occur. The number of clusters it finds might not directly correspond to the number of meaningful themes in your data.

Question 11

- For question 8 use the following information. Suppose you are using Gibbs sampling to estimate the distributions, α and β for topic models. The underlying corpus has 3 documents and 5 words, {machine, learning, language, nature, vision} and the number of topics is 2. At certain point, the structure of the documents looks like the following Doc1: nature(1) language(1) vision(1) language(1) nature(1) nature(1) language(1) vision(1) Doc 2: nature(1) language(1) language(2) machine(2) vision(1) learning(2) language(1) nature(1) Doc3: machine(2) language(2) learning(2) language(2) machine(2) machine(2) learning(2) language(2) (number) -number inside the brackets denote the topic no. 1 and 2 denote whether the word is currently assigned to topics t1 and t2 respectively. $\eta = 0.3$ and $\alpha = 0.3$ For question 8 calculate the value upto 4 decimal points and choose your answer 8) Using the above structure the estimated value of $\beta(2)$ nature at this point is

$$\begin{aligned} \text{Doc 2} &: 1 + 1 + 1 = 3 \checkmark \\ \text{Doc 3} &: 8 \checkmark \end{aligned}$$

- 3 documents (D)

- 5 words ($|V| = 5$)

{ m/c, learning, lang, nature,
vision }

- 2 topics (K)

- $\eta = 0.3$

- $\alpha = 0.3$

nature \in T_2
 $\{2\} = ?$ "nature" ✓

Doc 1 : 0 times $\in T_2$.

Doc 2 : 0 times $\in T_2$

Doc 3 : 0 times $\in T_2$

$$\theta(2) \equiv \text{nature}$$

To calculate $\theta(2)$; the word 'nature' at this pt. in
Gibbs sampling; we need to see how many times
the word 'nature' is assigned to topic (2)

and then add smoothing term.

$$(n = \underline{\underline{0.3}})$$

$\xi(2) =$

count of nature assigned to topic 2 + η

count of all words assigned to topic 2 + η * Vocab size

~~(words)~~ (sequences)
* ~~5~~ 4 ~~sequences~~ repetitions

$$= \left(\frac{0 + 0.3}{11 + 5 * 0.3} \right)$$

$$= \left(\frac{0.3}{12.5} \right)$$

$$= \underline{\underline{0.0240}}$$

(doc1, doc2, doc3)

count of nature assigned to topic2 = 0

count of all words - - - - - =





