# Syntax -CKY, PCFGs

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Week 5: Lecture 3

#### CKY Algorithm

- Let n be the number of words in the input. Think about n + 1 lines separating them, numbered 0 to n.
- $x_{ij}$  will denote the words between line i and j
- We build a table so that  $x_{ij}$  contains all the possible non-terminal spanning for words between line i and j.
- We build the Table bottom-up.

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#### Home Exercise

Use CKY algorithm to find the parse tree for "Book the flight through Houston" using the CNF form shown in the previous slide.

#### CKY for CFG

а	pilot 2	likes	flying	planes
1	2	3	4	5

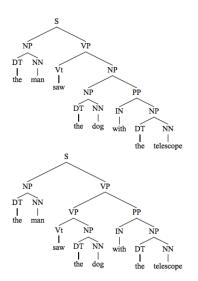
 $S \rightarrow NP \ VP$   $VP \rightarrow VBG \ NNS$   $VP \rightarrow VBZ \ NP$   $NP \rightarrow DT \ NN$   $NP \rightarrow JJ \ NNS$   $DT \rightarrow a$   $NN \rightarrow pilot$   $VBZ \rightarrow likes$   $VBG \rightarrow flying$   $JJ \rightarrow flying$   $NNS \rightarrow planes$ 

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DT	NP	-	-	SS
	NN	-	-	-
		VBZ	-	VP
				VP
			JJ VBG	NP VP
				NNS

 $\begin{array}{lll} S & \rightarrow & NP & VP \\ VP & \rightarrow & VBG & NNS \\ VP & \rightarrow & VBZ & VP \\ VP & \rightarrow & VBZ & NP \\ NP & \rightarrow & DT & NN \\ NP & \rightarrow & JJ & NNS \\ DT & \rightarrow & a \\ NN & \rightarrow & pilot \\ VBZ & \rightarrow & likes \\ VBG & \rightarrow & flying \\ JJ & \rightarrow & flying \\ NNS & \rightarrow & planes \end{array}$ 

# What about Ambiguities?



# Probabilistic Context-free grammars (PCFGs)

#### PCFG: G = (T, N, S, R, P)

- T: set of terminals
- N: set of non-terminals
  - For NLP, we distinguish out a set  $P \subset N$  of pre-terminals, which always rewrite as terminals
- S: start symbol
- *R*: Rules/productions of the form  $X \to \gamma$ ,  $X \in N$  and  $\gamma \in (T \cup N)*$

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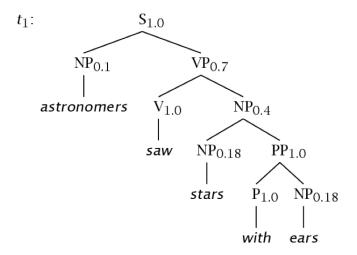
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- *R*: Rules/productions of the form  $X \to \gamma$ ,  $X \in N$  and  $\gamma \in (T \cup N)*$
- P(R) gives the probability of each rule.

$$\forall X \in \mathbb{N}, \sum_{X \to \gamma \in \mathbb{R}} P(X \to \gamma) = 1$$

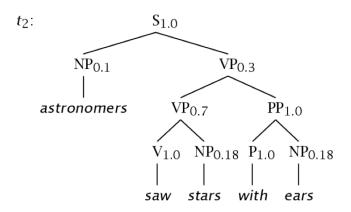
# A Simple PCFG (in CNF)

5	$\rightarrow$	NP VP	1.0	NP →	NP PP	0.4
VP	$\rightarrow$	V NP	0.7	NP →	astronomers	0.1
VP	$\rightarrow$	VP PP	0.3	NP →	ears	0.18
PP	$\rightarrow$	P NP	1.0	NP →	saw	0.04
Р	$\rightarrow$	with	1.0	NP →	stars	0.18
V	$\rightarrow$	saw	1.0	NP →	telescope	0.1

### Example Trees



# Example Trees



# Probability of trees and strings

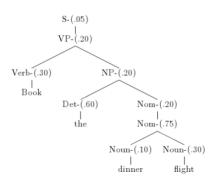
- P(t): The probability of tree is the product of the probabilities of the rules used to generate it
- $P(w_{1n})$ : The probability of the string is the sum of the probabilities of the trees which have that string as their yield

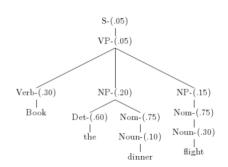
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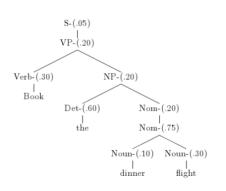
"Book the dinner flight"

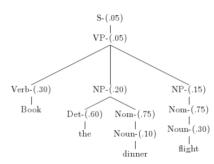
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# "Book the dinner flight"





#### **Probabilities**

- Parse tree 1:  $.05 \times .20 \times .30 \times .20 \times .60 \times .20 \times .75 \times .10 \times .30 = 1.62 \times 10^{-6}$
- Parse tree 2:  $.05 \times .05 \times .30 \times .20 \times .60 \times .75 \times .10 \times .15 \times .75 \times .30 = 2.28 \times 10^{-7}$

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- Real text tends to have grammatical mistakes. PCFG avoids this problem by ruling out nothing, but by giving implausible sentences a low probability
- In practice, a PCFG is a worse language model for English than an n-gram model
- All else being equal, the probability of a smaller tree is greater than a larger tree

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• How to learn the rule probabilities in the grammar *G*?