

N-gram Language Models

Pawan Goyal

CSE, IITKGP

Week 2: Lecture 4


Context Sensitive Spelling Correction

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The office is about fifteen minuets from my house

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min·u·et  *noun* \,mɪn-yə-'wet\

: a slow, graceful dance that was popular in the 17th and 18th centuries

: the music for a minuet

Context Sensitive Spelling Correction

The office is about fifteen minuets from my house

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: the music for a minuet

Use a Language Model

$P(\text{about fifteen } \mathbf{minutes} \text{ from}) > P(\text{about fifteen } \mathbf{minuets} \text{ from})$

Speech Recognition

- $P(\text{I saw a van}) \gg P(\text{eyes awe of an})$

Probabilistic Language Models: Applications

Speech Recognition

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Machine Translation

Which sentence is more plausible in the target language?

- $P(\text{high winds}) > P(\text{large winds})$

Probabilistic Language Models: Applications

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Other Applications

- Context Sensitive Spelling Correction
- Natural Language Generation
- ...

Completion Prediction

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 - ▶ Your program does not ...

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 - ▶ Please turn off your cell ...
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- *Predictive text input* systems can guess what you are typing and give choices on how to complete it.

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- **Related Task:** probability of an upcoming word:

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- A model that computes either of these is called a **language model**

Computing $P(W)$

How to compute the joint probability

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Basic Idea

Rely on the Chain Rule of Probability

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More Variables

$$P(A,B,C,D) = P(A)P(B|A)P(C|A,B)P(D|A,B,C)$$

The Chain Rule

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The Chain Rule in General

$$P(x_1, x_2, \dots, x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1, x_2) \dots P(x_n|x_1, \dots, x_{n-1})$$

Probability of words in sentences

$$P(w_1 w_2 \dots w_n) = \prod_i P(w_i | w_1 w_2 \dots w_{i-1})$$

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$P(\text{about}) \times P(\text{fifteen} \mid \text{about}) \times P(\text{minutes} \mid \text{about fifteen}) \times P(\text{from} \mid \text{about fifteen minutes})$

Estimating These Probability Values

Count and divide

$$P(\text{office} \mid \text{about fifteen minutes from}) = \frac{\text{Count}(\text{about fifteen minutes from office})}{\text{Count}(\text{about fifteen minutes from})}$$

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What is the problem

We may never see enough data for estimating these

Markov Assumption

Simplifying Assumption: Use only the previous word

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Or the couple previous words

$P(\text{office} \mid \text{about fifteen minutes from}) \approx P(\text{office} \mid \text{minutes from})$

Markov Assumption

More Formally: kth order Markov Model

Chain Rule:

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Using Markov Assumption: only k previous words

$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i | w_{i-k} \dots w_{i-1})$$

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Using Markov Assumption: only k previous words

$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i | w_{i-k} \dots w_{i-1})$$

We approximate each component in the product

$$P(w_i | w_1 w_2 \dots w_{i-1}) \approx P(w_i | w_{i-k} \dots w_{i-1})$$

P(office | about fifteen minutes from)

An N -gram model uses only $N - 1$ words of prior context.

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- Unigram: $P(\text{office})$
- Bigram: $P(\text{office} | \text{from})$
- Trigram: $P(\text{office} | \text{minutes from})$

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Markov model and Language Model

N-Gram Models

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Markov model and Language Model

An N -gram model is an $N - 1$ -order Markov Model

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- In general, an insufficient model of language:
language has long-distance dependencies:
“The computer which I had just put into the machine room on the fifth floor **crashed**.”
- In most of the applications, we can get away with N-gram models

Estimating N-grams probabilities

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Maximum Likelihood Estimate

Value that makes the observed data the “most probable”

$$P(w_i|w_{i-1}) = \frac{\text{count}(w_{i-1}, w_i)}{\text{count}(w_{i-1})}$$

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An Example

$$P(w_i|w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$

<s>I am here </s>

<s>who am I </s>

<s>I would like to know </s>

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Estimating bigrams

$P(I | <s>) =$

$P(</s> | \text{here}) =$

$P(\text{would} | I) =$

$P(\text{here} | \text{am}) =$

$P(\text{know} | \text{like}) =$

An Example

$$P(w_i | w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$

<s>I am here </s>

<s>who am I </s>

<s>I would like to know </s>

Estimating bigrams

$$P(I | <s>) = 2/3$$

$$P(</s> | \text{here}) = 1$$

$$P(\text{would} | I) = 1/3$$

$$P(\text{here} | \text{am}) = 1/2$$

$$P(\text{know} | \text{like}) = 0$$

Bigram counts from 9222 Restaurant Sentences

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

Computing bigram probabilities

Normalize by unigrams

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

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Bigram Probabilities

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

Computing Sentence Probabilities

$P(<s> \text{ I want english food } </s>)$

$= P(I \mid <s>) \times P(\text{want} \mid I) \times P(\text{english} \mid \text{want}) \times P(\text{food} \mid \text{english}) \times P(</s> \mid \text{food})$

Computing Sentence Probabilities

$P(< s> \text{ I want english food } </s>)$

$$\begin{aligned} &= P(I \mid <s>) \times P(\text{want} \mid I) \times P(\text{english} \mid \text{want}) \times P(\text{food} \mid \text{english}) \times P(</s> \mid \text{food}) \\ &= 0.000031 \end{aligned}$$

What knowledge does n -gram represent?

- $P(\text{english}|\text{want}) = .0011$
- $P(\text{chinese}|\text{want}) = .0065$
- $P(\text{to}|\text{want}) = .66$
- $P(\text{eat} | \text{to}) = .28$
- $P(\text{food} | \text{to}) = 0$
- $P(\text{want} | \text{spend}) = 0$
- $P(i | <s>) = .25$

Everything in log space

- Avoids underflow

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- Adding is faster than multiplying

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$$\log(p_1 \times p_2 \times p_3 \times p_4) = \log p_1 + \log p_2 + \log p_3 + \log p_4$$

Handling zeros

Use smoothing

SRILM

<http://www.speech.sri.com/projects/srilm/>

Number of tokens: 1,024,908,267,229

Number of sentences: 95,119,665,584

Number of unigrams: 13,588,391

Number of bigrams: 314,843,401

Number of trigrams: 977,069,902

Number of fourgrams: 1,313,818,354

Number of fivegrams: 1,176,470,663

[http://googleresearch.blogspot.in/2006/08/
all-our-n-gram-are-belong-to-you.html](http://googleresearch.blogspot.in/2006/08/all-our-n-gram-are-belong-to-you.html)

Example from the 4-gram data

serve as the inspector 66
serve as the inspiration 1390
serve as the installation 136
serve as the institute 187
serve as the institution 279
serve as the institutional 461

Google books Ngram Data

Google books Ngram Viewer

Graph these comma-separated phrases: ☐ case-insensitive

between and from the corpus with smoothing of [Search lots of books](#)

