

# Neural Networks

## Perceptron and Adaline

# INTRODUCTION

The project focuses on the implementation and evaluation of Perceptron and Adaline, two fundamental neural network models, for pattern recognition tasks. The goal is to develop "A Detectors" and "E Detectors" that can identify patterns resembling the letters 'A' and 'E' in a set of training and test patterns. This project offers an opportunity to explore the behaviour and performance of these neural networks in pattern classification.

Project Components:

### 1. Perceptron Training for A and E Detection:

- The project begins by creating a set of 25 training patterns for 'A' and 'E' detection. These patterns are transformed into column vectors, with 'ON' pixels represented as '1' and 'OFF' pixels as '-1'. These patterns will be used to train a Perceptron.

- For the 'A' detector, first five target patterns (t1, t2, t3, t4, t5) are labelled as '+1,' and for the 'E' detector, the corresponding five targets patterns (t6, t7, t8, t9, t10) are labelled as '+1' and all the remaining corresponding targets of other vowels are labelled as -1. The project tracks the training process, including the number of patterns prompting weight changes during each epoch.

### 2. Adaline Training for A and E Detection:

- The project then applies the Adaline (Widrow-Hoff) training algorithm to create 'A' and 'E' Detectors. Different values of the learning rate ( $\alpha$ ) are tested, and the progression of training is observed.

- Instead of monitoring pattern changes, the Mean Squared Error (MSE) for each epoch is calculated and plotted as a learning curve.

- The final values of bias and weights are recorded for analysis.

### 3. Testing with Three Test Sets:

- The project evaluates the trained detectors using three test sets (TSET 1, TSET 2, TSET 3) of varying noise levels.

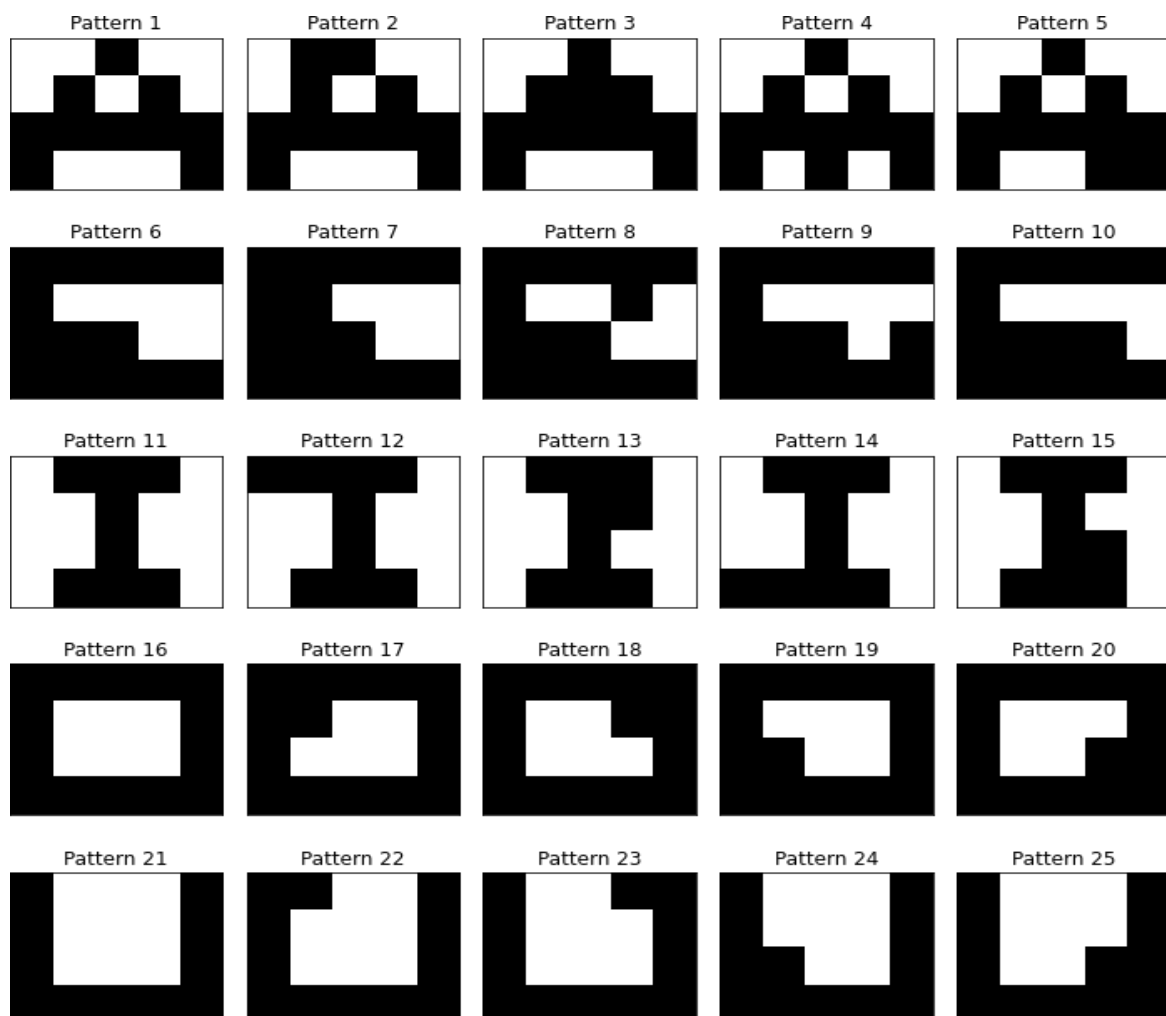
- Patterns are classified as 'HIT' or 'MISS' for each set, and the Hit Ratio (accuracy) is calculated for assessing detector performance.

Objectives:

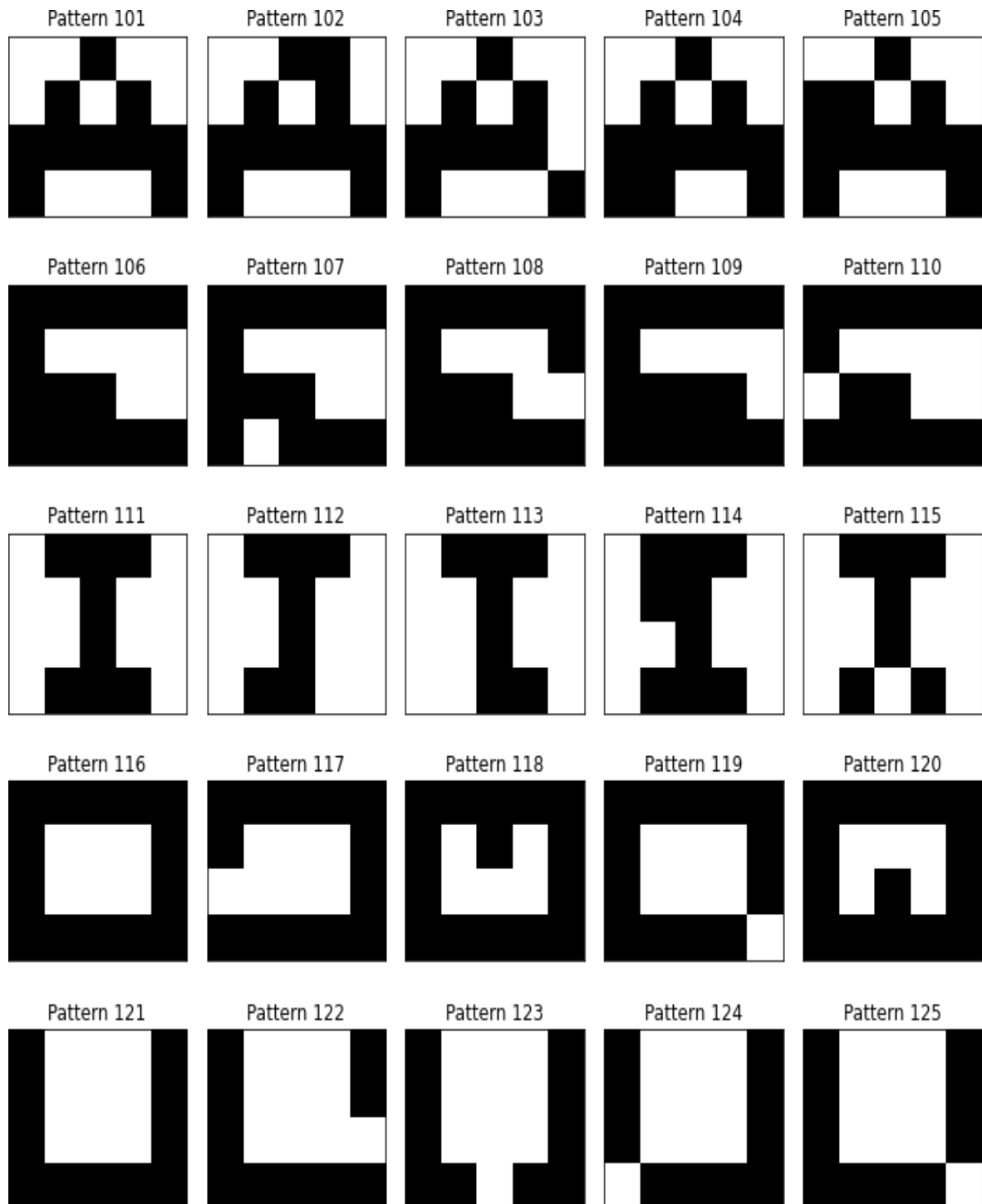
The primary objectives of this project are to:

- Implement Perceptrons and Adaline for 'A' and 'E' pattern detection.
- Analyse the impact of different learning rates ( $\alpha$ ) on training.
- Observe how the detectors perform on progressively more challenging test sets.
- Assess the differences between Perceptrons and Adaline in terms of training and testing.

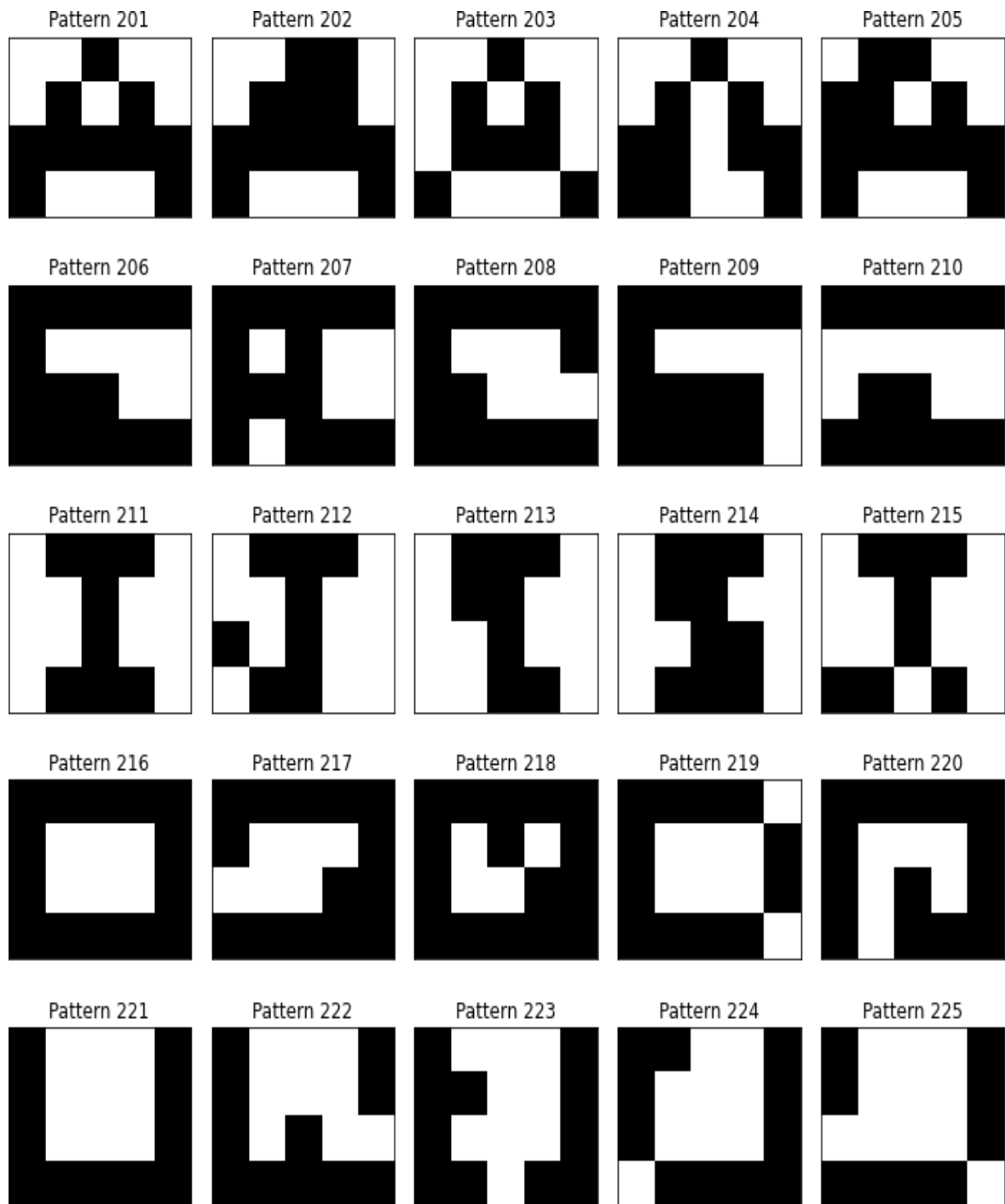
### **PATTERN FIGURES OF TRAINING SET:**



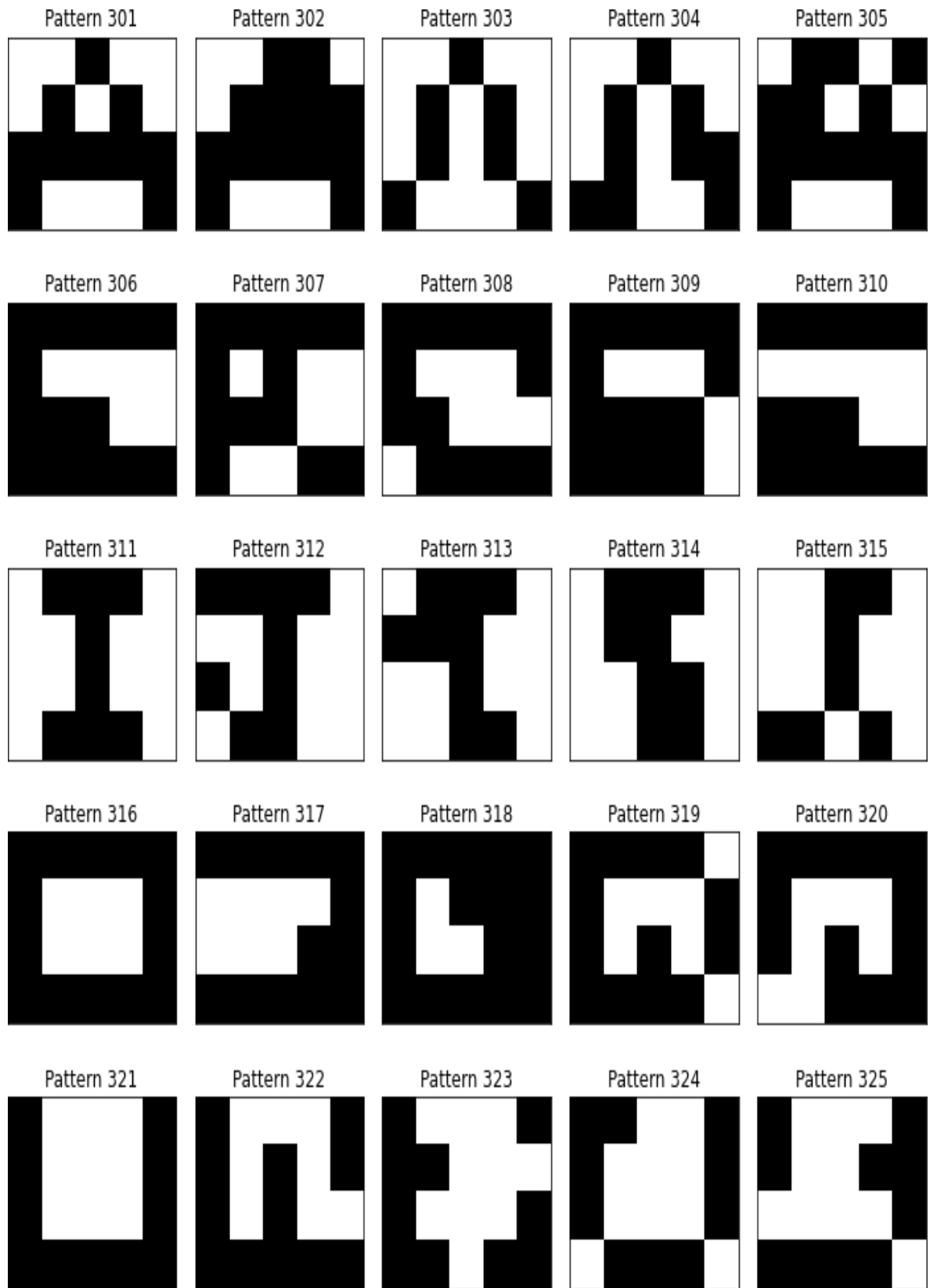
## PATTERN FIGURES OF TEST SET 1:



## PATTERN FIGURES OF TEST SET 2:



### PATTERN FIGURES OF TEST SET 3:

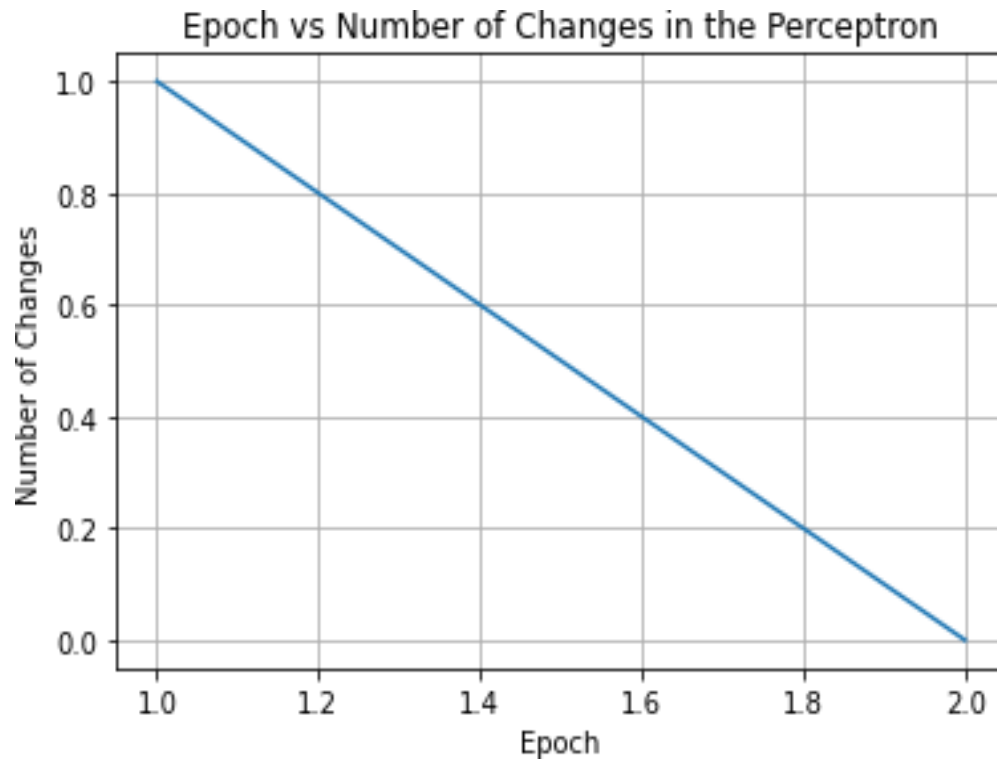


## **PART I: PERCEPTRON**

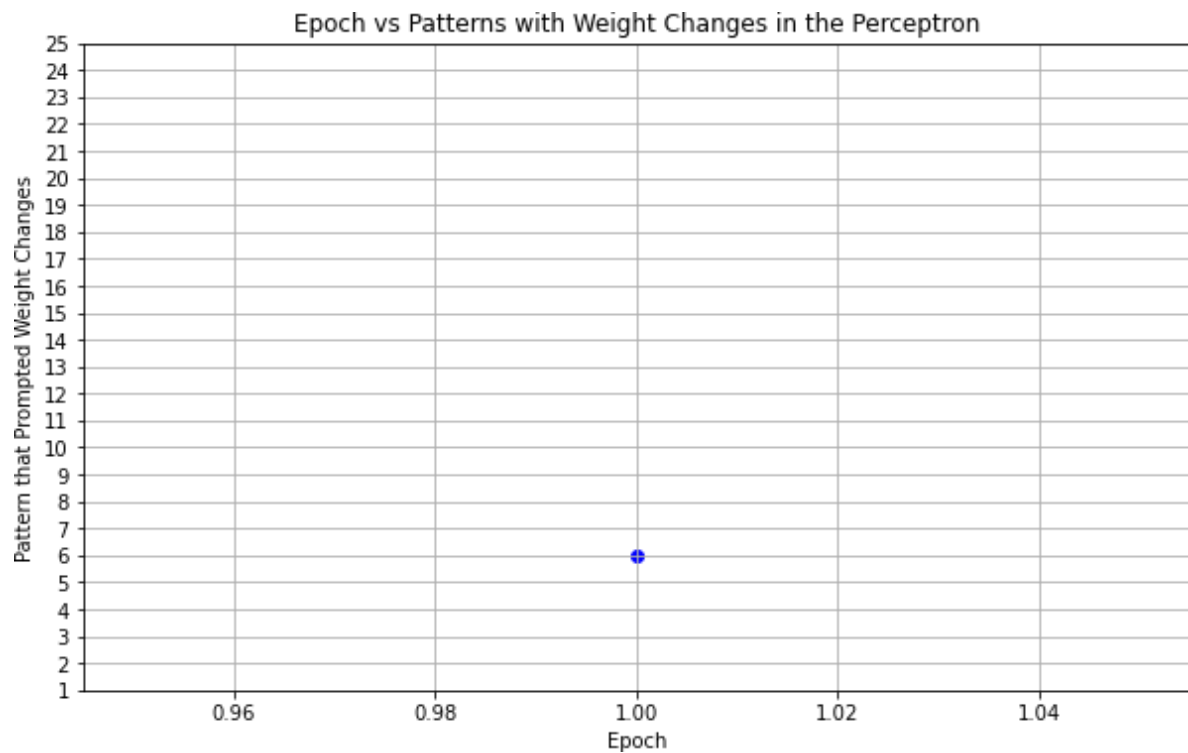
### **I.1 PERCEPTRON “A DETECTOR”**

Number of the 25 training patterns that prompted a change of weights ( $e \neq 0$ ) in each epoch of training and plotting these numbers, from epoch 1 to the last epoch trained.

```
patterns that changed in epoch 1: [6]
Number of Changes in weights in epoch 1: 1
patterns that changed in epoch 2: []
Number of Changes in weights in epoch 2: 0
Training complete in epoch 2.
Number of Changes in weights in each epoch: [1, 0]
weights: [-2 -2 -2 -2 -2 2 -2 -2 -2 2 -2 -2 -2 2 2 -2 -2 2 2 -2]
bias: -2
```



**Plotting the pattern numbers that prompted Weight changes in each epoch.**



**A TABLE of trained final weights and bias for A perceptron.**

weights: [-2 -2 -2 -2 -2 2 -2 -2 -2 2 -2 -2 -2 2 2 -2 -2 2 2 -2]  
 bias: -2

b	-2
W1	-2
W2	-2
W3	-2
W4	-2
W5	-2
W6	2
W7	-2
W8	-2
W9	-2
W10	2
W11	-2
W12	-2
W13	-2

W14	2
W15	2
W16	-2
W17	-2
W18	2
W19	2
W20	-2

### Results for TSET1 with 'A' Detector Perceptron:

Perceptron outputs for the test set\_1\_A:  
[1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1]  
Number of correct classficitaions: 25  
Number of attempted classifications: 25  
Hit Ratio: 1.0  
Accuracy: 100.00%

There are no patterns classified incorrectly in TSET1

P101	HIT
P102	HIT
P103	HIT
P104	HIT
P105	HIT
P106	HIT
P107	HIT
P108	HIT
P109	HIT
P110	HIT
P111	HIT
P112	HIT
P113	HIT
P114	HIT
P115	HIT
P116	HIT
P117	HIT
P118	HIT
P119	HIT
P120	HIT
P121	HIT
P122	HIT
P123	HIT
P124	HIT
P125	HIT



### Results for TSET2 with 'A' Detector Perceptron:

Perceptron outputs for the test set\_2\_A:

$$[1, 1, 1, 1, -1, -1, -1, -1, -1, -1, \overline{-1}, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1]$$

Number of correct classfictaions: 24

Number of attempted classifications: 25

Hit Ratio: 0.96

Accuracy: 96.00%

### Patterns classified incorrectly in TSET2: pt205

P201	HIT
P202	HIT
P203	HIT
P204	HIT
P205	MISS
P206	HIT
P207	HIT
P208	HIT
P209	HIT
P210	HIT
P211	HIT
P212	HIT
P213	HIT
P214	HIT
P215	HIT
P216	HIT
P217	HIT
P218	HIT
P219	HIT
P220	HIT
P221	HIT
P222	HIT
P223	HIT
P224	HIT
P225	HIT

### Results for TSET3 with 'A' Detector Perceptron:

Perceptron outputs for the test set 3 A:

$$[1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, 1, -1, -1, -1, -1, -1, \\ -1, -1, -1, -1, -1, -1]$$

```
Number of correct classfifications: 23
```

```
Number of attempted classifications: 25
```

Hit Ratio: 0.92

Accuracy: 92.00%

Patterns classified incorrectly in TSET3: pt305, pt314

P301	HIT
P302	HIT
P303	HIT
P304	HIT
P305	MISS
P306	HIT
P307	HIT
P308	HIT
P309	HIT
P310	HIT
P311	HIT
P312	HIT
P313	HIT
P314	MISS
P315	HIT
P316	HIT
P317	HIT
P318	HIT
P319	HIT
P320	HIT
P321	HIT
P322	HIT
P323	HIT
P324	HIT
P325	HIT

### Results for Testing 'A' detector Perceptron with 25 Training Patterns

Perceptron outputs for the training\_patterns:

```
[1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1]
```

Number of correct classficitaions: 25

Number of attempted classifications: 25

Hit Ratio: 1.0

Accuracy: 100.00%

There are no patterns classified incorrectly in 25 training patterns.

P1	HIT
P2	HIT
P3	HIT
P4	HIT
P5	HIT
P6	HIT
P7	HIT
P8	HIT
P9	HIT

P10	HIT
P11	HIT
P12	HIT
P13	HIT
P14	HIT
P15	HIT
P16	HIT
P17	HIT
P18	HIT
P19	HIT
P20	HIT
P21	HIT
P22	HIT
P23	HIT
P24	HIT
P25	HIT

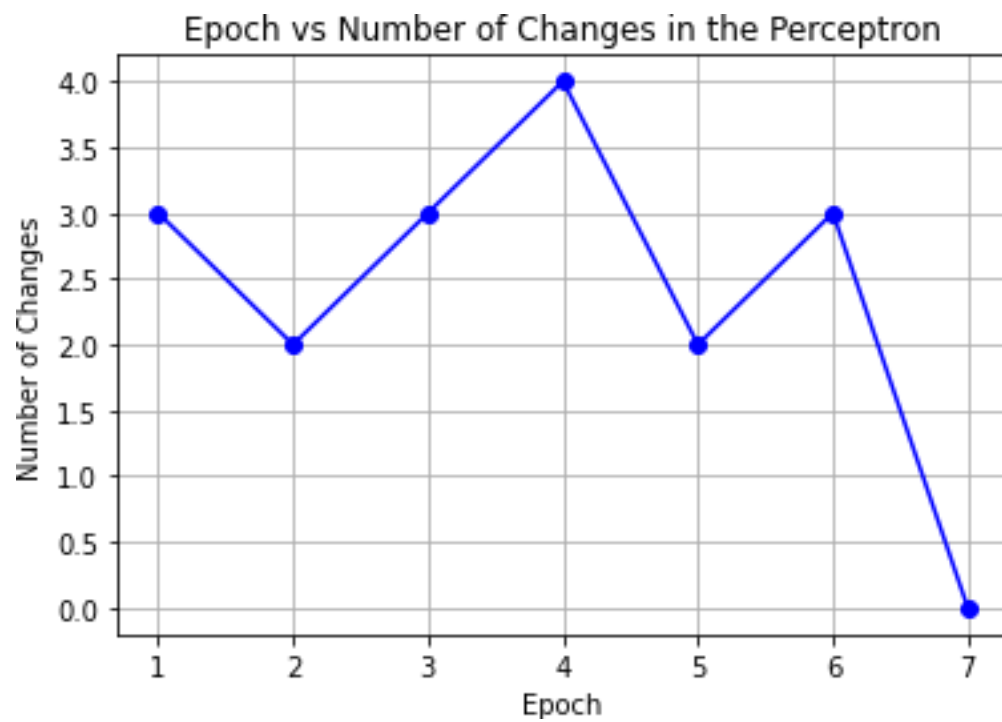
## I.2 PERCEPTRON “E DETECTOR”

Number of the 25 training patterns that prompted a change of weights ( $e \neq 0$ ) in each epoch of training and plotting these numbers, from epoch 1 to the last epoch trained.

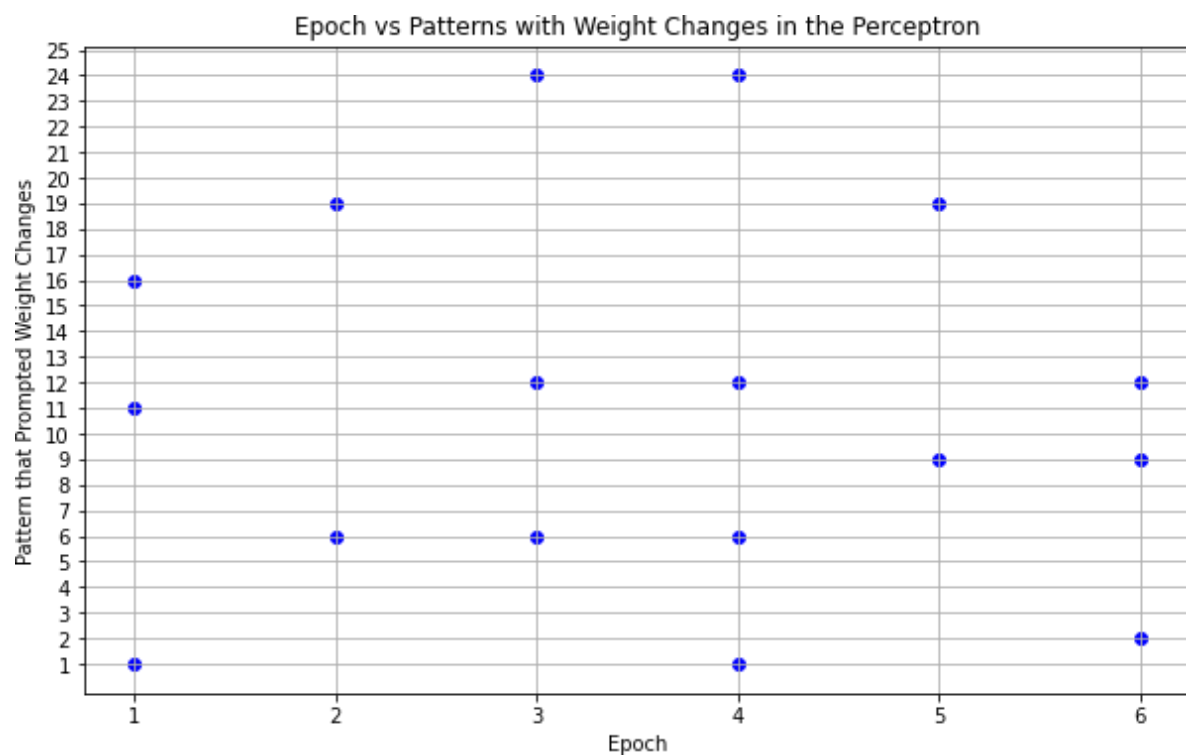
```

patterns that changed in epoch 1: [1, 11, 16]
Number of Changes in weights in epoch 1: 3
patterns that changed in epoch 2: [6, 19]
Number of Changes in weights in epoch 2: 2
patterns that changed in epoch 3: [6, 12, 24]
Number of Changes in weights in epoch 3: 3
patterns that changed in epoch 4: [1, 6, 12, 24]
Number of Changes in weights in epoch 4: 4
patterns that changed in epoch 5: [9, 19]
Number of Changes in weights in epoch 5: 2
patterns that changed in epoch 6: [2, 9, 12]
Number of Changes in weights in epoch 6: 3
patterns that changed in epoch 7: []
Number of Changes in weights in epoch 7: 0
Training complete in 7 epochs.
Number of Changes in weights in each epoch: [3, 2, 3, 4, 2, 3, 0]
weights:[ 2 14  2  2  2  2  6 -2 -6 -2  6 -2  6  2  2 -
2 14 -6
-10  2]
bias:-14

```



**Plotting the pattern numbers that prompted Weight changes in each epoch.**



### TABLE of trained final weights and bias for E perceptron.

```
weights:[ 2 14 2 2 2 2 6 -2 -6 -2 6 -2 6 2 2 -  
2 14 -6 -10 2]  
bias:-14
```

b	-14
W1	2
W2	14
W3	2
W4	2
W5	2
W6	2
W7	6
W8	-2
W9	-6
W10	-2
W11	6
W12	-2
W13	6
W14	2
W15	2
W16	-2
W17	14
W18	-6
W19	-10
W20	2

### Results for TSET1 with 'E' Detector Perceptron:

```
Perceptron outputs for the test set_1_E:  
[-1, -1, -1, -1, -1, 1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1,  
-1, -1, 1, -1, -1, -1]  
Number of correct classficitaions: 24  
Number of attempted classifications: 25  
Hit Ratio: 0.96  
Accuracy: 96.00%
```

Patterns classified incorrectly in TSET1: pt122

P101	HIT
P102	HIT
P103	HIT
P104	HIT
P105	HIT
P106	HIT
P107	HIT
P108	HIT
P109	HIT
P110	HIT
P111	HIT
P112	HIT
P113	HIT
P114	HIT
P115	HIT
P116	HIT
P117	HIT
P118	HIT
P119	HIT
P120	HIT
P121	HIT
P122	MISS
P123	HIT
P124	HIT
P125	HIT

### Results for TSET2 with 'E' Detector Perceptron:

Perceptron outputs for the test set 2\_E:  
 [-1, -1, -1, -1, 1, 1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, 1, -1, 1, -1, -1, -1]  
 Number of correct classficitaions: 22  
 Number of attempted classifications: 25  
 Hit Ratio: 0.88  
 Accuracy: 88.00%

Patterns classified incorrectly in TSET2: pt205, pt220, pt222

P201	HIT
P202	HIT
P203	HIT
P204	HIT
P205	MISS
P206	HIT
P207	HIT
P208	HIT
P209	HIT

P210	HIT
P211	HIT
P212	HIT
P213	HIT
P214	HIT
P215	HIT
P216	HIT
P217	HIT
P218	HIT
P219	HIT
P220	MISS
P221	HIT
P222	MISS
P223	HIT
P224	HIT
P225	HIT

### Results for TSET3 with 'E' Detector Perceptron:

Perceptron outputs for the test set\_3\_E:

[-1, -1, -1, -1, 1, 1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, 1, 1, -1, -1]

Number of correct classficitaions: 22

Number of attempted classifications: 25

Hit Ratio: 0.88

Accuracy: 88.00%

Patterns classified incorrectly in TSET3: pt305, pt322, pt323

P301	HIT
P302	HIT
P303	HIT
P304	HIT
P305	MISS
P306	HIT
P307	HIT
P308	HIT
P309	HIT
P310	HIT
P311	HIT
P312	HIT
P313	HIT
P314	HIT
P315	HIT
P316	HIT
P317	HIT
P318	HIT
P319	HIT
P320	HIT

P321	HIT
P322	MISS
P323	MISS
P324	HIT
P325	HIT

### Results for Testing 'E' detector Perceptron with 25 Training Patterns

Perceptron outputs for the training\_patterns :  
 [-1, -1, -1, -1, -1, 1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1]  
 Number of correct classficitaions: 25  
 Number of attempted classifications: 25  
 Hit Ratio: 1.0  
 Accuracy: 100.00%

There are no patterns classified incorrectly in 25 training patterns.

P1	HIT
P2	HIT
P3	HIT
P4	HIT
P5	HIT
P6	HIT
P7	HIT
P8	HIT
P9	HIT
P10	HIT
P11	HIT
P12	HIT
P13	HIT
P14	HIT
P15	HIT
P16	HIT
P17	HIT
P18	HIT
P19	HIT
P20	HIT
P21	HIT
P22	HIT
P23	HIT
P24	HIT
P25	HIT



### **I.3 COMMENTS:**

The comments and observations based on all the above results are discussed below:

- The perceptron, a simple binary classifier, is effective in learning and classifying patterns when they are linearly separable, as observed. The speed and efficiency of training are influenced by the separability of patterns.
- It's worth noting that the performance of perceptrons may degrade when patterns are not linearly separable. It would be interesting to explore scenarios where more complex neural network architectures might be necessary.

The notable key differences between the "A Detector" and "E Detector" are

#### **I). Training Process Duration:**

- The "A Detector" required only two epochs to complete its training, indicating that patterns resembling the letter 'A' are highly linearly separable. The majority of patterns were correctly classified in the first epoch.
- In contrast, the "E Detector" underwent seven epochs to complete its training. This suggests that patterns resembling the letter 'E' are less linearly separable, and the training process was more protracted.

#### **II). Pattern Changes during Training:**

- In the "A Detector," only one pattern prompted a weight change in epoch 1, while the following epochs had no pattern changes. This indicates that most "A" patterns are quite distinct from the others, making training easier.
- The "E Detector" experienced pattern changes in every epoch of training, and the number of patterns changing weight was higher than in the "A Detector." The need for constant pattern changes implies that "E" patterns are not as easily separable.

#### **III). Testing Accuracy:**

- The "A Detector" demonstrated high accuracy in all three test sets: 100% accuracy in Test Set 1, 96% accuracy in Test Set 2, and 92% accuracy in Test Set 3.
- The "E Detector" also performed well in Test Set 1 with 96% accuracy but faced more challenges in Test Sets 2 and 3, achieving 88% accuracy. This suggests that the "E Detector" is less robust in classifying 'E' patterns in noisier or more complex scenarios.

#### **IV). Pattern Numbers:**

- The "A Detector" showed that patterns across all epochs did not change, indicating that the detector was consistently accurate in recognizing 'A' patterns in the training set.
- In contrast, the "E Detector" underwent constant changes in patterns during training, reflecting the need for adjustments in the model's weights to correctly classify 'E' patterns.

## **PART II: ADALINE:**

### **II.1 ADALINE “A DETECTOR”**

Results of Mean Square Error in each epoch of training and final value of the BIAS and 4 of the 20 weights in the network at the end of each epoch.

**All the observations are listed when ALPHA = 0.1, 0.01, 0.001**

OBSERVATIONS FOR ALPHA\_1: 0.1

Epoch 1: MSE = 1882263820279.4207  
Epoch 2: MSE = 1.03379380188956e+25  
Epoch 3: MSE = 5.678317000573412e+37  
Epoch 4: MSE = 3.1189279487043548e+50  
Epoch 5: MSE = 1.7131328786732566e+63  
Epoch 6: MSE = 9.409721251209038e+75  
Epoch 7: MSE = 5.1684755530480135e+88  
Epoch 8: MSE = 2.838887447279345e+101  
Epoch 9: MSE = 1.5593150931259472e+114  
Epoch 10: MSE = 8.564846633777523e+126  
Epoch 11: MSE = 4.704411454972366e+139  
Epoch 12: MSE = 2.5839910606681996e+152  
Epoch 13: MSE = 1.4193082100750023e+165  
Epoch 14: MSE = 7.7958311305666335e+177  
Epoch 15: MSE = 4.282014476129916e+190  
Epoch 16: MSE = 2.3519811636111482e+203  
Epoch 17: MSE = 1.2918721841831072e+216  
Epoch 18: MSE = 7.095863547238703e+228  
Epoch 19: MSE = 3.8975434332824216e+241  
Epoch 20: MSE = 2.1408028372014423e+254

OBSERVATIONS FOR ALPHA\_2: 0.01

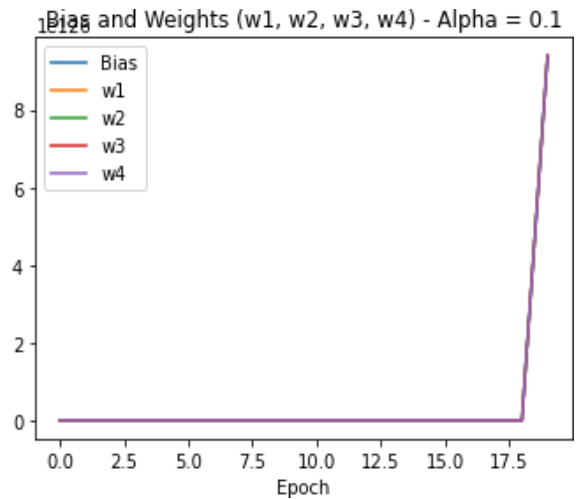
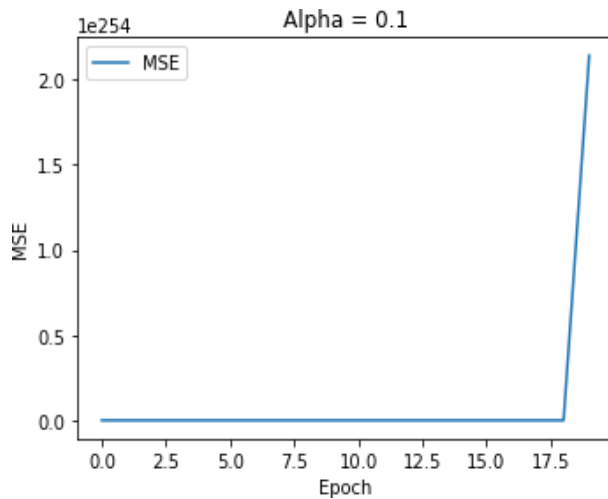
Epoch 1: MSE = 0.17213 ; W1 = -0.1087, W2 = -0.1033, W3 = -0.0042, W4 = -0.0096; bias = -0.0649  
Epoch 2: MSE = 0.04212 ; W1 = -0.0846, W2 = -0.0810, W3 = 0.0003, W4 = -0.0057; bias = -0.0907  
Epoch 3: MSE = 0.02748 ; W1 = -0.0705, W2 = -0.0706, W3 = 0.0029, W4 = -0.0021; bias = -0.1066  
Epoch 4: MSE = 0.02206 ; W1 = -0.0619, W2 = -0.0668, W3 = 0.0046, W4 = 0.0011; bias = -0.1174  
Epoch 5: MSE = 0.01952 ; W1 = -0.0563, W2 = -0.0663, W3 = 0.0058, W4 = 0.0040; bias = -0.1255  
Epoch 6: MSE = 0.01793 ; W1 = -0.0522, W2 = -0.0674, W3 = 0.0066, W4 = 0.0065; bias = -0.1321  
Epoch 7: MSE = 0.01675 ; W1 = -0.0489, W2 = -0.0693, W3 = 0.0073, W4 = 0.0088; bias = -0.1377  
Epoch 8: MSE = 0.01578 ; W1 = -0.0461, W2 = -0.0715, W3 = 0.0079, W4 = 0.0108; bias = -0.1428  
Epoch 9: MSE = 0.01495 ; W1 = -0.0435, W2 = -0.0738, W3 = 0.0085, W4 = 0.0126; bias = -0.1475  
Epoch 10: MSE = 0.01422 ; W1 = -0.0410, W2 = -0.0760, W3 = 0.0091, W4 = 0.0142; bias = -0.1520  
Epoch 11: MSE = 0.01357 ; W1 = -0.0387, W2 = -0.0782, W3 = 0.0098, W4 = 0.0157; bias = -0.1562  
Epoch 12: MSE = 0.01298 ; W1 = -0.0365, W2 = -0.0802, W3 = 0.0105, W4 = 0.0171; bias = -0.1603  
Epoch 13: MSE = 0.01243 ; W1 = -0.0343, W2 = -0.0822, W3 = 0.0112, W4 = 0.0184; bias = -0.1642

Epoch 14: MSE = 0.01192 ; W1 = -0.0323, W2 = -0.0840, W3 = 0.0119, W4 = 0.0196; bias = -0.1680  
 Epoch 15: MSE = 0.01145 ; W1 = -0.0303, W2 = -0.0858, W3 = 0.0127, W4 = 0.0207; bias = -0.1717  
 Epoch 16: MSE = 0.01102 ; W1 = -0.0284, W2 = -0.0874, W3 = 0.0136, W4 = 0.0218; bias = -0.1752  
 Epoch 17: MSE = 0.01060 ; W1 = -0.0265, W2 = -0.0891, W3 = 0.0144, W4 = 0.0227; bias = -0.1786  
 Epoch 18: MSE = 0.01022 ; W1 = -0.0248, W2 = -0.0906, W3 = 0.0153, W4 = 0.0236; bias = -0.1819  
 Epoch 19: MSE = 0.00986 ; W1 = -0.0231, W2 = -0.0920, W3 = 0.0162, W4 = 0.0244; bias = -0.1851  
 Epoch 20: MSE = 0.00952 ; W1 = -0.0216, W2 = -0.0935, W3 = 0.0172, W4 = 0.0252; bias = -0.1882  
 OBSERVATIONS FOR ALPHA\_3: 0.001  
 Epoch 1: MSE = 0.73711 ; W1 = -0.0289, W2 = -0.0256, W3 = -0.0069, W4 = -0.0102; bias = -0.0241  
 Epoch 2: MSE = 0.36113 ; W1 = -0.0471, W2 = -0.0412, W3 = -0.0093, W4 = -0.0152; bias = -0.0405  
 Epoch 3: MSE = 0.18950 ; W1 = -0.0583, W2 = -0.0506, W3 = -0.0093, W4 = -0.0171; bias = -0.0519  
 Epoch 4: MSE = 0.10877 ; W1 = -0.0651, W2 = -0.0560, W3 = -0.0079, W4 = -0.0174; bias = -0.0601  
 Epoch 5: MSE = 0.06935 ; W1 = -0.0690, W2 = -0.0590, W3 = -0.0060, W4 = -0.0168; bias = -0.0660  
 Epoch 6: MSE = 0.04919 ; W1 = -0.0711, W2 = -0.0605, W3 = -0.0040, W4 = -0.0157; bias = -0.0706  
 Epoch 7: MSE = 0.03831 ; W1 = -0.0721, W2 = -0.0610, W3 = -0.0020, W4 = -0.0146; bias = -0.0742  
 Epoch 8: MSE = 0.03208 ; W1 = -0.0724, W2 = -0.0611, W3 = -0.0002, W4 = -0.0134; bias = -0.0771  
 Epoch 9: MSE = 0.02827 ; W1 = -0.0722, W2 = -0.0608, W3 = 0.0013, W4 = -0.0124; bias = -0.0797  
 Epoch 10: MSE = 0.02578 ; W1 = -0.0718, W2 = -0.0604, W3 = 0.0026, W4 = -0.0115; bias = -0.0819  
 Epoch 11: MSE = 0.02405 ; W1 = -0.0712, W2 = -0.0599, W3 = 0.0037, W4 = -0.0107; bias = -0.0839  
 Epoch 12: MSE = 0.02277 ; W1 = -0.0705, W2 = -0.0594, W3 = 0.0047, W4 = -0.0101; bias = -0.0857  
 Epoch 13: MSE = 0.02177 ; W1 = -0.0698, W2 = -0.0590, W3 = 0.0054, W4 = -0.0095; bias = -0.0875  
 Epoch 14: MSE = 0.02097 ; W1 = -0.0690, W2 = -0.0585, W3 = 0.0060, W4 = -0.0091; bias = -0.0891  
 Epoch 15: MSE = 0.02028 ; W1 = -0.0683, W2 = -0.0581, W3 = 0.0065, W4 = -0.0087; bias = -0.0906  
 Epoch 16: MSE = 0.01969 ; W1 = -0.0676, W2 = -0.0577, W3 = 0.0069, W4 = -0.0084; bias = -0.0921  
 Epoch 17: MSE = 0.01918 ; W1 = -0.0669, W2 = -0.0574, W3 = 0.0072, W4 = -0.0081; bias = -0.0935  
 Epoch 18: MSE = 0.01871 ; W1 = -0.0662, W2 = -0.0572, W3 = 0.0075, W4 = -0.0079; bias = -0.0948  
 Epoch 19: MSE = 0.01829 ; W1 = -0.0656, W2 = -0.0569, W3 = 0.0077, W4 = -0.0077; bias = -0.0961  
 Epoch 20: MSE = 0.01790 ; W1 = -0.0649, W2 = -0.0567, W3 = 0.0079, W4 = -0.0076; bias = -0.0973  
 Final Weights for alpha = 0.01: ['-0.0216', '-0.0935', '0.0172', '0.0252', '-0.0364', '0.0852', '0.0532', '-0.2989', '0.0303', '-0.0514', '0.0

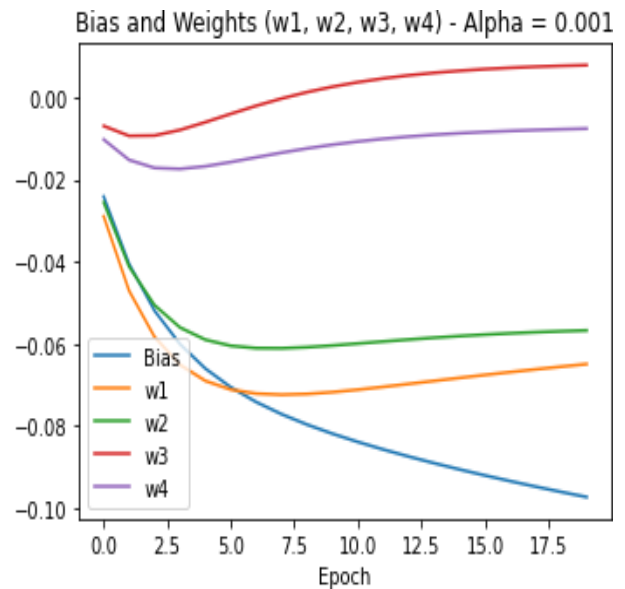
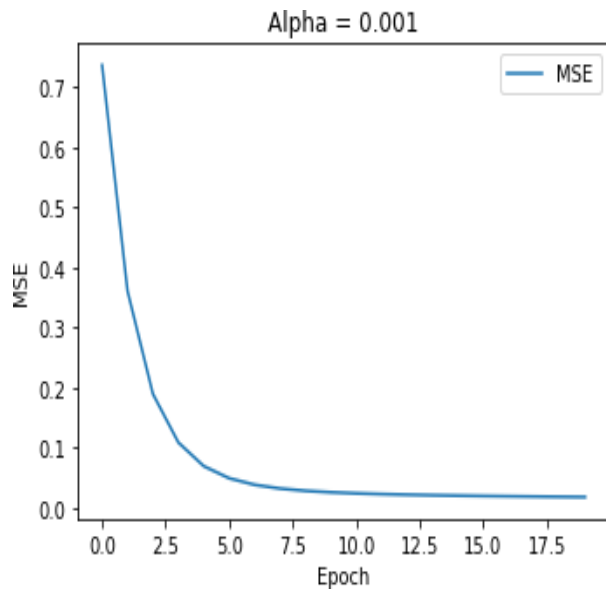
153', '-0.1373', '-0.0320', '0.0654', '0.0579', '-0.1641', '-0.0935', '-0.0153', '0.0865', '0.0172']  
 Final Bias for alpha = 0.01: -0.1882

The plots of MSE vs. epoch (the “Learning Curve”) and the plots of the 4 weights and the bias for the 3 values of alpha

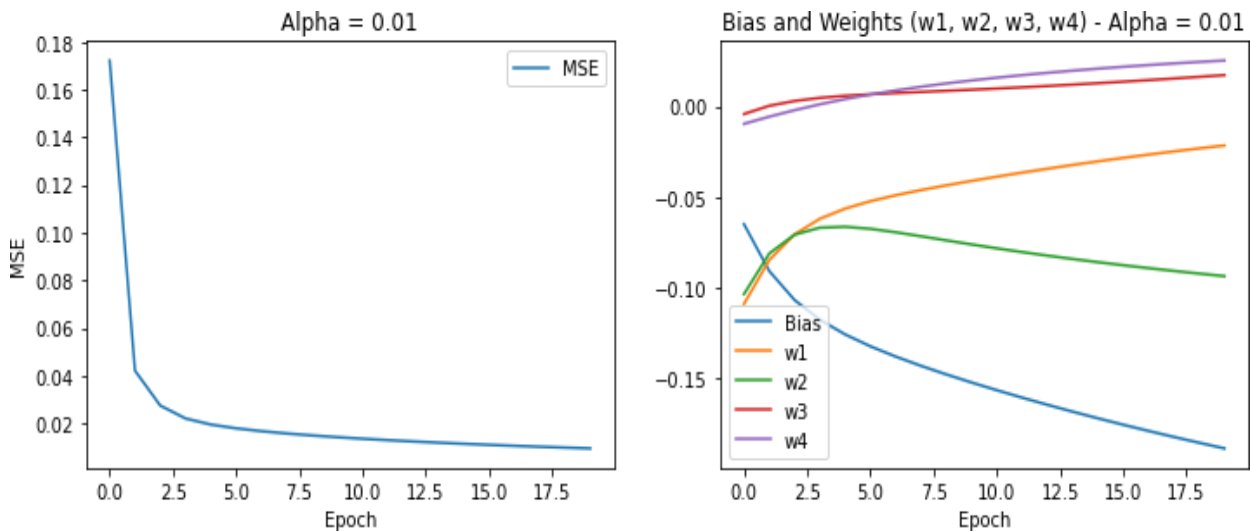
a) ALPHA = 0.1 which ended up being “too small”



b) ALPHA = 0.001 which ended up being “too large”



c) when “ALPHA = **0.01**” I got the “best trained weights”, converging at a reasonable speed.



### **Observation of the above values of plots:**

- The primary goal in training Adaline is to minimize the cost or loss function, typically represented by the MSE. By using  $\alpha = 0.01$ , I was able to train the model to reach a minimum MSE, indicating that the model has successfully learned and can make more accurate predictions.
- With an alpha value of 0.01, the training process reached a reasonably low Mean Squared Error (MSE) quickly. This indicates that the Adaline model efficiently adjusted its weights to minimize the error with relatively few training epochs.
- While achieving a low MSE is important, it's also essential to find a balance with training time.  $\alpha = 0.01$  found this balance, allowing the model to converge efficiently without prolonging the training process unnecessarily.
- In summary, an alpha value of 0.01 is considered the best choice for training ‘A’ Adaline detector because it enabled reasonable speed of convergence and a low MSE.

### **Final and best trained weights when Alpha = 0.01 for ‘A’ Detector Adaline**

```
[ -0.02156626  -0.09345598  0.01715754  0.02519263 -0.03635294  0.0852304
  0.05317853  -0.29885377  0.03025028 -0.05136438  0.01531267 -0.1372949
6  -0.0319741   0.06539273  0.05787763 -0.16411643 -0.09345598 -0.0153126
7  0.08650757  0.01715754]

-0.18824024664617364
```

b	-0.18824024664617364
W1	-0.02156626
W2	-0.09345598
W3	0.01715754
W4	0.02519263
W5	-0.03635294
W6	0.0852304
W7	0.05317853
W8	-0.29885377
W9	0.03025028
W10	-0.05136438
W11	0.01531267
W12	-0.13729496
W13	-0.0319741
W14	0.06539273
W15	0.05787763
W16	-0.16411643
W17	-0.09345598
W18	-0.01531267
W19	0.08650757
W20	0.01715754

### Results for TSET1 with 'A' Detector Adaline:

Adaline outputs for the test set\_1\_A:

[1, 1, 1, 1, -1]

Number of correct classficitaions: 25

Number of attempted classifications: 25

Hit Ratio: 1.0

Accuracy: 100.00%

There are no patterns classified incorrectly in TSET1

P101	HIT
P102	HIT
P103	HIT
P104	HIT



P214	HIT
P215	HIT
P216	HIT
P217	HIT
P218	HIT
P219	HIT
P220	HIT
P221	HIT
P222	HIT
P223	HIT
P224	HIT
P225	HIT

### Results for TSET3 with 'A' Detector Adaline:

Adaline outputs for the test set\_3\_A:  
[1, 1, 1, 1, 1, -1]  
Number of correct classficitaions: 25  
Number of attempted classifications: 25  
Hit Ratio: 1.0  
Accuracy: 100.00%

There are no patterns classified incorrectly in TSET3

P301	HIT
P302	HIT
P303	HIT
P304	HIT
P305	HIT
P306	HIT
P307	HIT
P308	HIT
P309	HIT
P310	HIT
P311	HIT
P312	HIT
P313	HIT
P314	HIT
P315	HIT
P316	HIT
P317	HIT
P318	HIT
P319	HIT
P320	HIT
P321	HIT
P322	HIT



P323	HIT
P324	HIT
P325	HIT

### Results for testing 'A' detector Adaline with 25 Training Patterns

Adaline outputs for the training\_patterns\_A\_Ada:

[1, 1, 1, 1, 1, -1]

Number of correct classficitaions: 25

Number of attempted classifications: 25

Hit Ratio: 1.0

Accuracy: 100.00%

There are no patterns classified incorrectly in 25 training patterns.

P1	HIT
P2	HIT
P3	HIT
P4	HIT
P5	HIT
P6	HIT
P7	HIT
P8	HIT
P9	HIT
P10	HIT
P11	HIT
P12	HIT
P13	HIT
P14	HIT
P15	HIT
P16	HIT
P17	HIT
P18	HIT
P19	HIT
P20	HIT
P21	HIT
P22	HIT
P23	HIT
P24	HIT
P25	HIT

## II.2 ADALINE “E DETECTOR”

Results of Mean Square Error in each epoch of training and final value of the BIAS and 4 of the 20 weights in the network at the end of each epoch.

**All the observations are listed when ALPHA = 0.1, 0.001, 0.0001**

OBSERVATIONS FOR ALPHA\_1: 0.1

Epoch 1: MSE = 1834573856139.0762  
Epoch 2: MSE = 1.0076264680312522e+25  
Epoch 3: MSE = 5.534587734272418e+37  
Epoch 4: MSE = 3.039981805742235e+50  
Epoch 5: MSE = 1.6697701478320317e+63  
Epoch 6: MSE = 9.17154287346224e+75  
Epoch 7: MSE = 5.03765136710406e+88  
Epoch 8: MSE = 2.7670296750087875e+101  
Epoch 9: MSE = 1.5198457901187845e+114  
Epoch 10: MSE = 8.348053678659813e+126  
Epoch 11: MSE = 4.5853336354827683e+139  
Epoch 12: MSE = 2.518585212555193e+152  
Epoch 13: MSE = 1.3833827540520647e+165  
Epoch 14: MSE = 7.598503456101463e+177  
Epoch 15: MSE = 4.173628347127212e+190  
Epoch 16: MSE = 2.2924479380155425e+203  
Epoch 17: MSE = 1.2591723822580094e+216  
Epoch 18: MSE = 6.916253416048374e+228  
Epoch 19: MSE = 3.798889015435801e+241  
Epoch 20: MSE = 2.0866149464841795e+254  
Epoch 21: MSE = 1.1461145395930183e+267  
Epoch 22: MSE = 6.295260848580686e+279  
Epoch 23: MSE = 3.4577965624400424e+292  
Epoch 24: MSE = 1.899263168724422e+305  
Epoch 25: MSE = inf

OBSERVATIONS FOR ALPHA\_2: 0.001

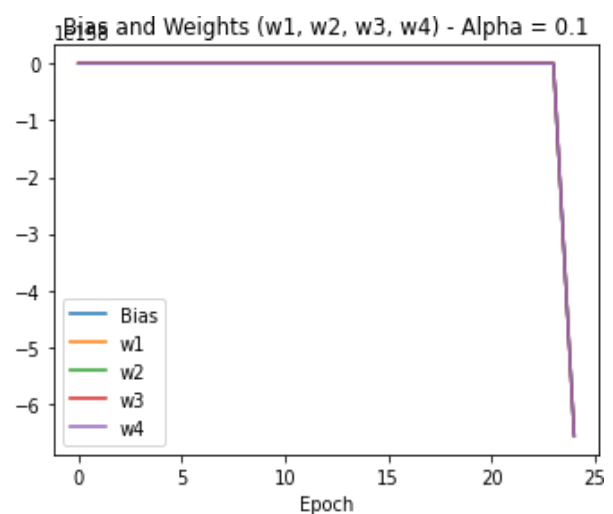
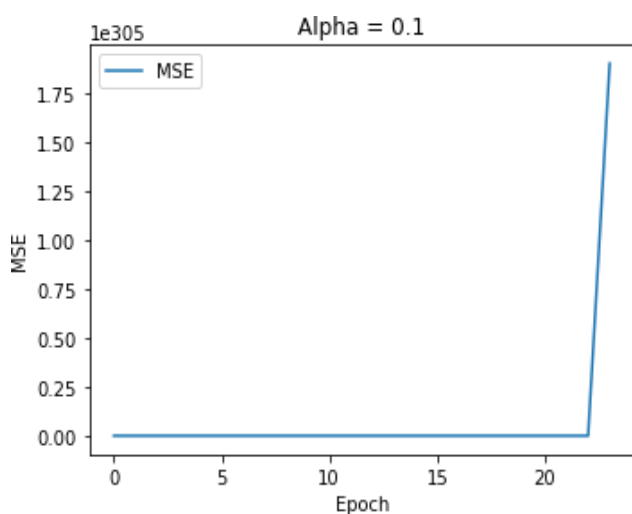
Epoch 1: MSE = 0.95807 ; W1 = 0.0041, W2 = 0.0084, W3 = -0.0102, W4 = -0.0141; bias = -0.0303  
Epoch 2: MSE = 0.83701 ; W1 = 0.0109, W2 = 0.0193, W3 = -0.0172, W4 = -0.0247; bias = -0.0563  
Epoch 3: MSE = 0.74164 ; W1 = 0.0192, W2 = 0.0316, W3 = -0.0221, W4 = -0.0329; bias = -0.0791  
Epoch 4: MSE = 0.66149 ; W1 = 0.0281, W2 = 0.0443, W3 = -0.0256, W4 = -0.0393; bias = -0.0994  
Epoch 5: MSE = 0.59199 ; W1 = 0.0373, W2 = 0.0571, W3 = -0.0280, W4 = -0.0445; bias = -0.1178  
Epoch 6: MSE = 0.53090 ; W1 = 0.0463, W2 = 0.0697, W3 = -0.0297, W4 = -0.0487; bias = -0.1345  
Epoch 7: MSE = 0.47695 ; W1 = 0.0550, W2 = 0.0818, W3 = -0.0309, W4 = -0.0523; bias = -0.1499  
Epoch 8: MSE = 0.42923 ; W1 = 0.0634, W2 = 0.0934, W3 = -0.0318, W4 = -0.0553; bias = -0.1642  
Epoch 9: MSE = 0.38702 ; W1 = 0.0713, W2 = 0.1046, W3 = -0.0325, W4 = -0.0579; bias = -0.1775  
Epoch 10: MSE = 0.34970 ; W1 = 0.0787, W2 = 0.1151, W3 = -0.0329, W4 = -0.0602; bias = -0.1898

Epoch 11: MSE = 0.31671 ; W1 = 0.0857, W2 = 0.1251, W3 = -0.0332, W4 = -0.0621; bias = -0.2014  
 Epoch 12: MSE = 0.28756 ; W1 = 0.0923, W2 = 0.1346, W3 = -0.0334, W4 = -0.0638; bias = -0.2122  
 Epoch 13: MSE = 0.26179 ; W1 = 0.0984, W2 = 0.1435, W3 = -0.0336, W4 = -0.0653; bias = -0.2223  
 Epoch 14: MSE = 0.23901 ; W1 = 0.1041, W2 = 0.1520, W3 = -0.0337, W4 = -0.0666; bias = -0.2319  
 Epoch 15: MSE = 0.21887 ; W1 = 0.1094, W2 = 0.1600, W3 = -0.0337, W4 = -0.0678; bias = -0.2409  
 Epoch 16: MSE = 0.20105 ; W1 = 0.1144, W2 = 0.1676, W3 = -0.0337, W4 = -0.0688; bias = -0.2494  
 Epoch 17: MSE = 0.18528 ; W1 = 0.1190, W2 = 0.1747, W3 = -0.0337, W4 = -0.0697; bias = -0.2574  
 Epoch 18: MSE = 0.17132 ; W1 = 0.1233, W2 = 0.1815, W3 = -0.0337, W4 = -0.0704; bias = -0.2649  
 Epoch 19: MSE = 0.15894 ; W1 = 0.1273, W2 = 0.1879, W3 = -0.0337, W4 = -0.0711; bias = -0.2721  
 Epoch 20: MSE = 0.14797 ; W1 = 0.1310, W2 = 0.1940, W3 = -0.0336, W4 = -0.0717; bias = -0.2788  
 Epoch 21: MSE = 0.13824 ; W1 = 0.1344, W2 = 0.1998, W3 = -0.0336, W4 = -0.0722; bias = -0.2852  
 Epoch 22: MSE = 0.12959 ; W1 = 0.1376, W2 = 0.2052, W3 = -0.0335, W4 = -0.0726; bias = -0.2913  
 Epoch 23: MSE = 0.12190 ; W1 = 0.1405, W2 = 0.2104, W3 = -0.0335, W4 = -0.0729; bias = -0.2970  
 Epoch 24: MSE = 0.11505 ; W1 = 0.1432, W2 = 0.2153, W3 = -0.0334, W4 = -0.0732; bias = -0.3025  
 Epoch 25: MSE = 0.10895 ; W1 = 0.1458, W2 = 0.2200, W3 = -0.0333, W4 = -0.0734; bias = -0.3077  
 OBSERVATIONS FOR ALPHA\_3: 0.0001  
 Epoch 1: MSE = 0.99668 ; W1 = 0.0006, W2 = 0.0010, W3 = -0.0010, W4 = -0.0014; bias = -0.0030  
 Epoch 2: MSE = 0.98212 ; W1 = 0.0012, W2 = 0.0020, W3 = -0.0020, W4 = -0.0028; bias = -0.0060  
 Epoch 3: MSE = 0.96799 ; W1 = 0.0018, W2 = 0.0030, W3 = -0.0029, W4 = -0.0041; bias = -0.0089  
 Epoch 4: MSE = 0.95425 ; W1 = 0.0025, W2 = 0.0041, W3 = -0.0038, W4 = -0.0054; bias = -0.0118  
 Epoch 5: MSE = 0.94088 ; W1 = 0.0031, W2 = 0.0051, W3 = -0.0047, W4 = -0.0067; bias = -0.0146  
 Epoch 6: MSE = 0.92787 ; W1 = 0.0038, W2 = 0.0062, W3 = -0.0055, W4 = -0.0079; bias = -0.0174  
 Epoch 7: MSE = 0.91520 ; W1 = 0.0045, W2 = 0.0073, W3 = -0.0064, W4 = -0.0091; bias = -0.0202  
 Epoch 8: MSE = 0.90283 ; W1 = 0.0053, W2 = 0.0085, W3 = -0.0071, W4 = -0.0103; bias = -0.0229  
 Epoch 9: MSE = 0.89077 ; W1 = 0.0060, W2 = 0.0096, W3 = -0.0079, W4 = -0.0114; bias = -0.0256  
 Epoch 10: MSE = 0.87900 ; W1 = 0.0068, W2 = 0.0108, W3 = -0.0086, W4 = -0.0125; bias = -0.0282  
 Epoch 11: MSE = 0.86749 ; W1 = 0.0076, W2 = 0.0119, W3 = -0.0094, W4 = -0.0136; bias = -0.0308  
 Epoch 12: MSE = 0.85624 ; W1 = 0.0084, W2 = 0.0131, W3 = -0.0100, W4 = -0.0146; bias = -0.0334  
 Epoch 13: MSE = 0.84524 ; W1 = 0.0092, W2 = 0.0143, W3 = -0.0107, W4 = -0.0157; bias = -0.0360

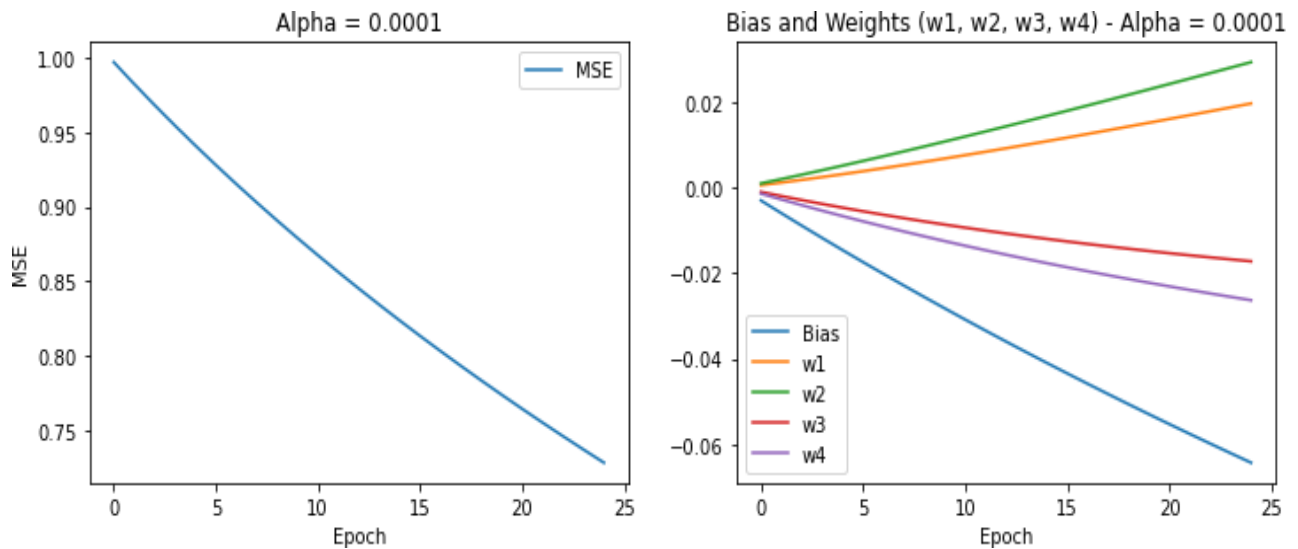
Epoch 14: MSE = 0.83447 ; W1 = 0.0100, W2 = 0.0155, W3 = -0.0114, W4 = -0.0167; bias = -0.0385  
Epoch 15: MSE = 0.82392 ; W1 = 0.0108, W2 = 0.0167, W3 = -0.0120, W4 = -0.0177; bias = -0.0410  
Epoch 16: MSE = 0.81358 ; W1 = 0.0117, W2 = 0.0180, W3 = -0.0126, W4 = -0.0186; bias = -0.0434  
Epoch 17: MSE = 0.80345 ; W1 = 0.0125, W2 = 0.0192, W3 = -0.0132, W4 = -0.0195; bias = -0.0458  
Epoch 18: MSE = 0.79351 ; W1 = 0.0134, W2 = 0.0204, W3 = -0.0137, W4 = -0.0205; bias = -0.0482  
Epoch 19: MSE = 0.78376 ; W1 = 0.0143, W2 = 0.0217, W3 = -0.0143, W4 = -0.0214; bias = -0.0506  
Epoch 20: MSE = 0.77419 ; W1 = 0.0152, W2 = 0.0229, W3 = -0.0148, W4 = -0.0222; bias = -0.0530  
Epoch 21: MSE = 0.76480 ; W1 = 0.0160, W2 = 0.0242, W3 = -0.0153, W4 = -0.0231; bias = -0.0553  
Epoch 22: MSE = 0.75557 ; W1 = 0.0169, W2 = 0.0255, W3 = -0.0158, W4 = -0.0239; bias = -0.0576  
Epoch 23: MSE = 0.74650 ; W1 = 0.0178, W2 = 0.0268, W3 = -0.0163, W4 = -0.0247; bias = -0.0598  
Epoch 24: MSE = 0.73758 ; W1 = 0.0187, W2 = 0.0280, W3 = -0.0168, W4 = -0.0255; bias = -0.0621  
Epoch 25: MSE = 0.72882 ; W1 = 0.0197, W2 = 0.0293, W3 = -0.0172, W4 = -0.0263; bias = -0.0643  
Final Weights for alpha = 0.001: ['0.1458', '0.2200', '-0.0333', '-0.0734', '0.0462', '0.0640', '0.2684', '-0.0543', '-0.1099', '-0.0208', '0.1298', '-0.0941', '0.1021', '0.0210', '0.0053', '-0.0929', '0.2200', '-0.1298', '-0.2839', '-0.0333']  
Final Bias for alpha = 0.001: -0.3077

**The plots of MSE vs. epoch (the “Learning Curve”) and the plots of the 4 weights and the bias for the 3 values of alpha**

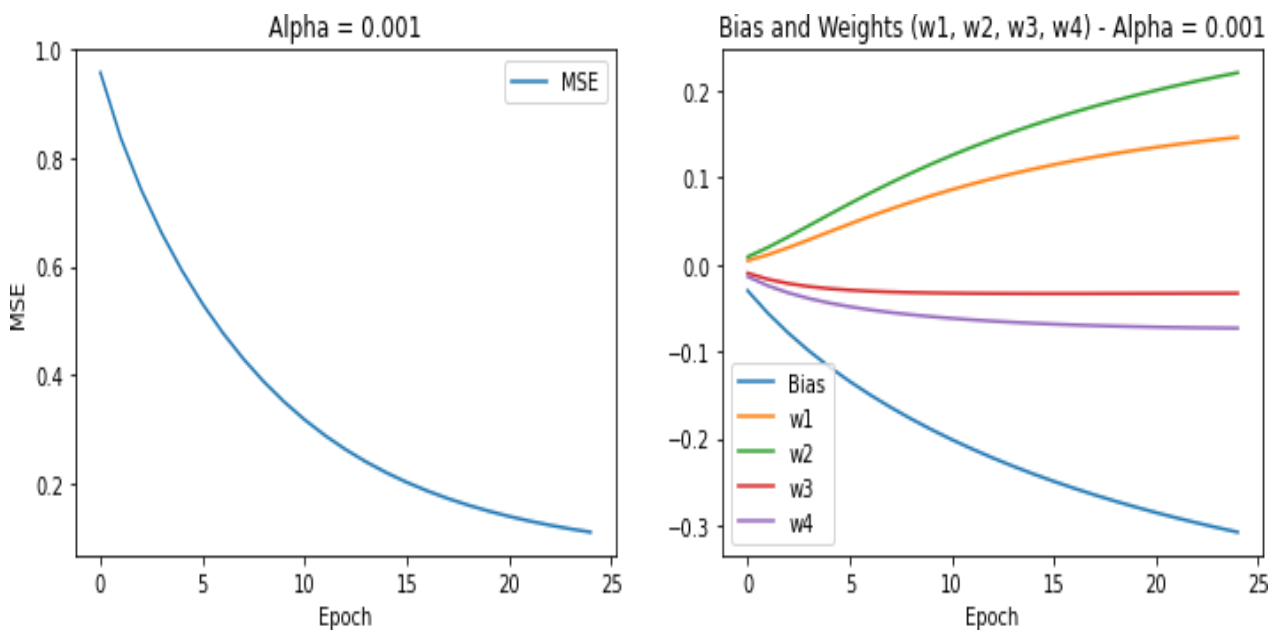
**a) ALPHA = 0.1 which ended up being “too small”**



**b)  $\text{ALPHA} = 0.0001$  which ended up being “too large”**



**c) when “ $\text{ALPHA} = 0.001$ ” I got the “best trained weights” for the Adaline ‘E’ Detector**



### **Observation of the above values of plots:**

Observing the MSE values for different alpha values (0.1, 0.001, and 0.0001) provides valuable insights into the effectiveness of the Adaline training process for 'E' detector. Here's a summary of why alpha = 0.001 is considered the best choice compared to alpha = 0.1 and alpha = 0.0001:

#### **Alpha = 0.1:**

- The MSE values for alpha = 0.1 increase dramatically with each epoch.
- This indicates that the learning rate is too high, causing the model to overshoot the optimal weights.
- The model's weights and bias are diverging instead of converging, making it unstable.
- After 25 epochs, the MSE reaches infinity, which means the weights have become extremely large and unstable.

#### **Alpha = 0.001:**

- The MSE values for alpha = 0.001 decrease consistently with each epoch.
- This indicates that the learning rate is appropriate for stable convergence.
- The model's weights and bias are converging at a reasonable speed, resulting in effective learning.
- After 25 epochs, the MSE reaches a low value, indicating that the model has successfully learned and is making accurate predictions.
- The final weights and bias for alpha = 0.001 are provided, reflecting meaningful values for prediction.

#### **Alpha = 0.0001:**

- The MSE values for alpha = 0.0001 decrease more slowly compared to alpha = 0.001.
- While this learning rate is less prone to overshooting, it converges very slowly.
- After 25 epochs, the MSE is relatively high compared to alpha = 0.001, indicating that the model has not learned as effectively.

In summary, alpha = 0.001 is considered the best choice because it strikes a balance between a stable learning process and a reasonably fast convergence. The MSE consistently decreases, and the final weights and bias are meaningful for accurate predictions. In contrast, alpha = 0.1 leads to instability, while alpha = 0.0001 converges too slowly, resulting in a higher MSE after 25 epochs.

### Final and best trained weights when Alpha = 0.001 for 'E' Detector Adaline

```
[ 0.14576987  0.22000851 -0.03334498 -0.07340166  0.04617479  0.0640043
5
 0.26843078 -0.05431692 -0.10991542 -0.02079806  0.12980594 -0.0940562
7
 0.10212764  0.02104366  0.00526549 -0.09286934  0.22000851 -0.1298059
4
 -0.28391449 -0.03334498]
```

-0.30767040851265054

b	-0.30767040851265054
W1	0.14576987
W2	0.22000851
W3	-0.03334498
W4	-0.07340166
W5	0.04617479
W6	0.06400435
W7	0.26843078
W8	-0.05431692
W9	-0.10991542
W10	-0.02079806
W11	0.12980594
W12	-0.09405627
W13	0.10212764
W14	0.02104366
W15	0.00526549
W16	-0.09286934
W17	0.22000851
W18	-0.12980594
W19	-0.28391449
W20	-0.03334498

### Results for TSET1 with 'E' Detector Adaline:

Adaline outputs for the test set\_1\_E:

```
[-1, -1, -1, -1, -1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1]
```

Number of correct classficitaions: 25  
Number of attempted classifications: 25  
Hit Ratio: 1.0  
Accuracy: 100.00%

There are no patterns classified incorrectly in TSET1

P101	HIT
P102	HIT
P103	HIT
P104	HIT
P105	HIT
P106	HIT
P107	HIT
P108	HIT
P109	HIT
P110	HIT
P111	HIT
P112	HIT
P113	HIT
P114	HIT
P115	HIT
P116	HIT
P117	HIT
P118	HIT
P119	HIT
P120	HIT
P121	HIT
P122	HIT
P123	HIT
P124	HIT
P125	HIT

### Results for TSET2 with 'E' Detector Adaline:

Adaline outputs for the test set\_2\_E:  
[-1, -1, -1, -1, -1, 1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1]  
Number of correct classficitaions: 25  
Number of attempted classifications: 25  
Hit Ratio: 1.0  
Accuracy: 100.00%

There are no patterns classified incorrectly in TSET2



P201	HIT
P202	HIT
P203	HIT
P204	HIT
P205	HIT
P206	HIT
P207	HIT
P208	HIT
P209	HIT
P210	HIT
P211	HIT
P212	HIT
P213	HIT
P214	HIT
P215	HIT
P216	HIT
P217	HIT
P218	HIT
P219	HIT
P220	HIT
P221	HIT
P222	HIT
P223	HIT
P224	HIT
P225	HIT

### Results for TSET3 with 'E' Detector Adaline:

Adaline outputs for the test set\_3\_E:  
 [-1, -1, -1, -1, 1, 1, 1, 1, 1, 1, -1]  
 Number of correct classficitaions: 24  
 Number of attempted classifications: 25  
 Hit Ratio: 0.96  
 Accuracy: 96.00%

Patterns that classified incorrectly in TSET3: pt305

P301	HIT
P302	HIT
P303	HIT
P304	HIT
P305	MISS
P306	HIT
P307	HIT
P308	HIT
P309	HIT

P310	HIT
P311	HIT
P312	HIT
P313	HIT
P314	HIT
P315	HIT
P316	HIT
P317	HIT
P318	HIT
P319	HIT
P320	HIT
P321	HIT
P322	HIT
P323	HIT
P324	HIT
P325	HIT

### Results for 'E' detector Adaline with 25 Training Patterns

Adaline outputs for the training\_patterns\_E\_Ada:

```
[-1, -1, -1, -1, -1, 1, 1, 1, 1, 1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1, -1]
```

Number of correct classficitaions: 25

Number of attempted classifications: 25

Hit Ratio: 1.0

Accuracy: 100.00%

There are no patterns classified incorrectly in 25 training patterns

P1	HIT
P2	HIT
P3	HIT
P4	HIT
P5	HIT
P6	HIT
P7	HIT
P8	HIT
P9	HIT
P10	HIT
P11	HIT
P12	HIT
P13	HIT
P14	HIT
P15	HIT
P16	HIT
P17	HIT
P18	HIT
P19	HIT

P20	HIT
P21	HIT
P22	HIT
P23	HIT
P24	HIT
P25	HIT

### **II.3 COMMENTS:**

**The comments, observations and notable key differences based on all the above results for both Adaline detectors are discussed below:**

- The choice of learning rate (alpha) significantly impacts the training process of an Adaline model. It must strike a balance between stable convergence and a reasonably fast learning rate.
- Using a high learning rate can lead to overshooting, instability, and divergence, rendering the model ineffective. On the other hand, a very low learning rate might lead to slow convergence and less effective learning.
- In both 'E' and 'A' Detector Adaline cases, the learning rate was critical in determining the model's success. In 'E' Detector Adaline,  $\alpha = 0.001$  achieved the right balance, while in 'A' Detector Adaline,  $\alpha = 0.01$  was the best choice for my models.
- 'A' Detector Adaline achieved 100% accuracy in all the 3 Test Sets while 'E' detector Adaline achieved 100% accuracy in Test set 1 and Test set 2 but achieved a 96% accuracy in Test set 3.
- The primary goal is to minimize the cost or loss function (typically represented by the MSE) to ensure that the model has successfully learned and can make accurate predictions.
- In summary, the choice of learning rate is a key factor in Adaline training, and it must be selected carefully to achieve a balance between convergence speed and stability. The optimal learning rate leads to efficient learning and lower MSE values, ensuring the model's effectiveness.

# CONCLUSION

- The Perceptron excelled when dealing with linearly separable patterns, while it struggled when patterns were not linearly separable.
- Adaline models proved to be more effective in various scenarios compared to the Perceptron by observing the accuracies.
- The importance of the learning rate in Adaline training was confirmed, and the right choice of alpha was crucial for convergence and stability.
- We know that the accuracy values indicate the model's ability to correctly classify patterns in different test sets. All Adaline models achieved higher accuracy compared to the Perceptron models, particularly in the 'A Detector' case, where Adaline achieved 100% accuracy in all test sets.
- These accuracy results reveal that both 'A Detector' and 'E Detector' Adaline models outperformed their Perceptron models in terms of accuracy.
- The slight drop in accuracy in the 'E Detector' Adaline model in Test Set 3 was **unexpected**. It may be due to the complexity of the 'E' patterns or the limited size of the training dataset. Using a larger training dataset might mitigate this.
- I expected for the best alpha value of Adaline 'A' detector will also be the best alpha choice for Adaline 'E' detector but the accuracy was more with  $\alpha = 0.001$
- In summary, these experiments emphasize the importance of understanding and selecting the right model and parameters for the given task. While Perceptrons and Adaline models are foundational building blocks in machine learning and illuminate the fundamental concepts of linearity, separability, and the role of learning rates in model training.
- The results obtained will be very useful for understanding the strengths and limitations of Perceptrons and Adaline in real-world applications.