

## **Orthogonal Trajectory :-**

### **i) For Cartesian equation**

**Step 1:-** Differentiate given equation w.r.to x.

**Step 2:-** Eliminate constant by using given equation (if any )

**Step 3:** put  $\frac{dy}{dx} = \frac{dx}{d}$  (Given Diff. Equation).

**Step 4:** Separate variable .

**Step 5:** Take Integration (gives orthogonal Trajectory).

### **ii) Polar Equation :-**

**Step 1:-** Differentiate given equation w.r.to  $\theta$ .

**Step 2:-** Eliminate constant by using given equation (if any )

**Step 3:** put  $\frac{dr}{d\theta} = -r^2 \frac{dx}{dy}$  (Given Diff. Equation)

**Step 4:** Separate variable .

**Step 5:** Take Integration (gives orthogonal Trajectory).

### **1) Newton's Law of cooling:-**

The temperature of body changes at a rate which is proportional to the difference in temperature between that of surrounding medium and that of the body itself.

$$\frac{dT}{dt} = -k(T - T_0)$$

$T_0$  = temperature of surrounding medium .

$T$  = temperature of body.

$t$  = time at that instant.

After separation variable equation is

$$\frac{dT}{(T - T_0)} = -k dt$$

**3) Rectilinear Motion:-** Motion of body along a straight line

**D'Alembert's Principle:-**

Mass X acceleration = Net Forces

i) Velocity ( $v$ ) =  $\frac{dx}{dt}$

ii) Acceleration ( $a$ ) =  $\frac{dv}{dt} = \frac{d^2x}{dt^2}$

Net forces action on a body are:-

1) Weight of the body ( $mg$ ) \*when body is thrown upward then  $mg$  is negative =  $(-mg)$

\*when body is fall from rest then  $mg$  is positive =  $(+mg)$

2) Air resistance or simply resistance:-

\*resistance is always negative  $m \times$

$a = \pm mg - \text{resistance}$  for acceleration:-

- i) if acceleration directed towards origin take negative.
- ii) Positive if away from origin.

Simple electric circuit

**Kirchhoff's law:-** The algebraic sum of the voltage drops around any closed circuit is equal to the resultant electromotive force in the circuit.

Sr.no	element	symbol	unit
1	Quantity of electricity	Q	columb
2	Current	I	Ampere(A)
3	Resistance <sup>®</sup>		Ohm
4	Inductance(L)		Henry(H)
5	Capacitance©		Farad
6	Electromotive force (voltage/battery)		Volt

2) Voltage drop across resistance(R) =  $Ri$

3) Voltage drop across inductance =  $L \frac{di}{dt}$

4) Voltage drop across capacitance =  $\frac{q}{c}$

Case 1:- Circuit involving L and R along with voltage source E.

$$L \frac{di}{dt} + Ri = E$$

Maximum Value of current  $I_{\max} = \frac{E}{R}$

Case 2:- Circuit involving R and C along with voltage source E.

$$Ri + \frac{q}{c} = E, \text{ where } i = \frac{dq}{dt}$$

$$R \frac{dq}{dt} + \frac{q}{c} = E$$

#### 4) Heat flow:-

Fourier's law of Heat conduction :- The rate of area and to the rate of change of temperature with respect to it's distance normal to area.

$$q = -kA \frac{dt}{dx}, \text{ where } k = \text{Thermal conductivity}$$

$$A = 2\pi r x, \quad K = \text{constant of thermal conductivity.}$$

