

1) Cauchy's Riemann Equations in Cartesian form

$$\frac{\partial u}{\partial x} = \frac{\partial v}{\partial y} \text{ and } \frac{\partial u}{\partial y} = - \frac{\partial v}{\partial x}$$

2) Cauchy's Riemann Equations in polar form

$$\frac{\partial u}{\partial r} = \frac{1}{r} \frac{\partial v}{\partial \theta} \text{ and } \frac{\partial v}{\partial r} = - \frac{1}{r} \frac{\partial u}{\partial \theta}$$

3) Milne Thomson's Method: To find $f(z)$ in terms of z

when $u(x, y)$ and $v(x, y)$ are given. If $f'(z) = \frac{\partial u}{\partial x} + i \frac{\partial v}{\partial x}$ is given then $\frac{\partial u}{\partial x}, \frac{\partial v}{\partial x}$ being functions of x, y by substituting $x=z$ and $y=0$ we get $f'(z)$ in terms of z . By integration we get $f(z)$ in terms of z .

4) Cauchy's theorem: If $f(z)$ is analytic on and within

closed curve c then $\oint_c f(z) dz = 0$

5) Cauchy's Integral Formula: $f^n(a) = \frac{n!}{2\pi i} \oint_c \frac{f(z)}{(z-a)^{n+1}} dz$

6) Cauchy's Residue Theorem: If $f(z)$ is analytic on and within a closed contour c except at finite number of

isolated singular points within c then

$\oint_c f(z)dz = 2\pi i(r_1 + r_2 + r_3 + \dots + r_n)$ where r_1, r_2, \dots, r_n are the residues at the singular points within c .

7) Residue at the pole $z = a$ of order n is given as r

$$= \frac{1}{(n-1)!} \left[\frac{d^{n-1}}{dz^{n-1}} \{ (z-a)^n f(z) \} \right]_{z=a}$$