Multiple Linear Regression Model

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Installing the libraries

```
library(tinytex)
library(ggplot2)
library(tidyverse)
## -- Attaching packages -----
                                                 ----- tidyverse 1.3.1 --
## v tibble 3.1.6
                     v dplyr 1.0.7
## v tidyr 1.1.4
                     v stringr 1.4.0
          2.0.1
## v readr
                     v forcats 0.5.1
## v purrr
          0.3.4
## Warning: package 'tibble' was built under R version 4.1.2
## -- Conflicts ----- tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
library(rvest)
## Warning: package 'rvest' was built under R version 4.1.2
##
## Attaching package: 'rvest'
## The following object is masked from 'package:readr':
##
##
      guess_encoding
library(naniar)
library(corrplot)
```

corrplot 0.90 loaded

In multiple linear regression the equation is like:

```
y = a_0 + a_1 x_1 + a_2 x_2 + \cdots
```

where a_0 is the y intercept, and a_1 is slope, which can be compared with linear regression: y = mx + c where c is y intercept and m is slope

In multiple linear regression model, we will plot scatter plot first to understand the relation between variables, whether or not the variables are linearly correlated:

Loading data:

You can download the dataset from kaggle: https://www.kaggle.c om/nehalbirla/vehicle-dataset-from-cardekho

```
vehicle <- read.csv("car.csv")</pre>
head(vehicle)
                        name year selling_price km_driven
##
                                                           fuel seller_type
               Maruti 800 AC 2007
                                         60000
                                                   70000 Petrol Individual
                                                    50000 Petrol Individual
## 2 Maruti Wagon R LXI Minor 2007
                                         135000
        Hyundai Verna 1.6 SX 2012
                                         600000
                                                   100000 Diesel Individual
## 4 Datsun RediGO T Option 2017
                                         250000
                                                  46000 Petrol Individual
     Honda Amaze VX i-DTEC 2014
                                         450000 141000 Diesel Individual
                                                  125000 Petrol Individual
       Maruti Alto LX BSIII 2007
                                         140000
## 6
   transmission
## 1
          Manual First Owner
## 2
          Manual First Owner
          Manual First Owner
## 3
          Manual First Owner
## 5
          Manual Second Owner
          Manual First Owner
colnames(vehicle)
## [1] "name"
                                      "selling_price" "km_driven"
                      "year"
## [5] "fuel"
                      "seller_type"
                                      "transmission" "owner"
```

Lets make scatter plot to see how strongly variables are correlated, we are interested in Mileage,lh and lc

```
str(vehicle)
## 'data.frame':
                4340 obs. of 8 variables:
## $ name
                  : chr "Maruti 800 AC" "Maruti Wagon R LXI Minor" "Hyundai Verna 1.6 SX" "Datsun Red
## $ year
                 : int 2007 2007 2012 2017 2014 2007 2016 2014 2015 2017 ...
## $ selling_price: int 60000 135000 600000 250000 450000 140000 550000 240000 850000 365000 ...
## $ km_driven : int 70000 50000 100000 46000 141000 125000 25000 60000 25000 78000 ...
                  : chr "Petrol" "Petrol" "Diesel" "Petrol" ...
## $ seller_type : chr "Individual" "Individual" "Individual" "Individual" ...
## $ transmission : chr "Manual" "Manual" "Manual" ...
## $ owner
                  : chr "First Owner" "First Owner" "First Owner" "First Owner" ...
# we will first convert fuel, seller_type, transmission, owner in factor variable
vehicle$fuel <- as.factor(vehicle$fuel)</pre>
vehicle$seller_type <- as.factor(vehicle$seller_type)</pre>
```

```
vehicle$transmission <- as.factor(vehicle$transmission)
vehicle$owner <- as.factor(vehicle$owner)</pre>
```

Now converting the factor to numeric to check the correlation between variables

```
vehicle$fuel <- as.numeric(vehicle$fuel)
vehicle$seller_type <- as.numeric(vehicle$seller_type)
vehicle$transmission <- as.numeric(vehicle$transmission)
vehicle$owner <- as.numeric(vehicle$owner)

vehicle$name <- as.factor(vehicle$name)

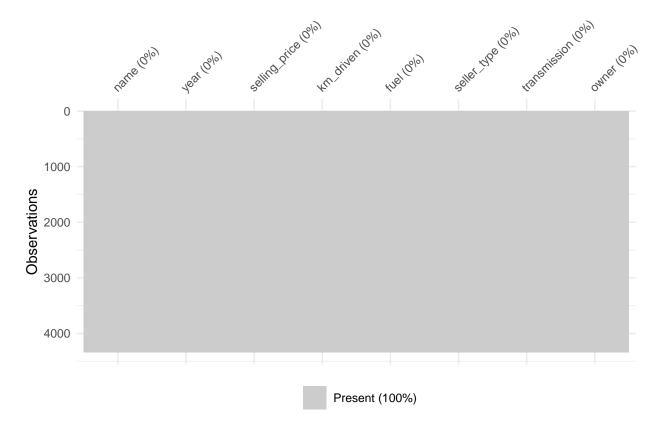
vehicle$name <- as.numeric(vehicle$name)</pre>
```

Now checking the missing values in the data if any:

```
sum(is.na(vehicle))
## [1] 0
```

Visualizing the missing values if any:

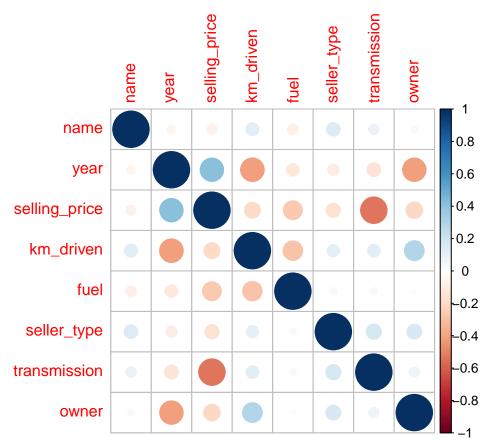
```
vis_miss(vehicle)
```



Here we can see that there is no missing values in the data :

Lets draw a corrplot to see how varibales are related to each other :

```
cort <- cor(vehicle)
corrplot(cort)</pre>
```



```
colnames(vehicle)
## [1] "name"
                       "year"
                                       "selling_price" "km_driven"
## [5] "fuel"
                       "seller_type"
                                       "transmission"
                                                       "owner"
model_lm_1 <- lm(selling_price~.,data = vehicle)</pre>
summary(model_lm_1)
##
## Call:
## lm(formula = selling_price ~ ., data = vehicle)
## Residuals:
        Min
                  1Q
                       Median
                                    3Q
                                            Max
                       -27635
## -1149547 -163275
                                115782 7527991
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -7.106e+07 3.803e+06 -18.687 < 2e-16 ***
## name
                -4.301e+01 1.664e+01 -2.585 0.00976 **
                3.663e+04 1.881e+03 19.467 < 2e-16 ***
## year
## km_driven
                -9.648e-01 1.689e-01
                                      -5.712 1.19e-08 ***
## fuel
                -9.358e+04 4.717e+03 -19.837 < 2e-16 ***
## seller_type -1.947e+04 1.477e+04 -1.318 0.18753
```

transmission -8.838e+05 2.203e+04 -40.118 < 2e-16 ***

-1.710e+04 5.926e+03 -2.886 0.00392 **

owner

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 429500 on 4332 degrees of freedom
## Multiple R-squared: 0.4498, Adjusted R-squared: 0.449
## F-statistic: 506 on 7 and 4332 DF, p-value: < 2.2e-16
model_lm <- lm(selling_price~year+km_driven+fuel+seller_type+transmission+owner, data = vehicle)
summary(model_lm)
##
## Call:
## lm(formula = selling_price ~ year + km_driven + fuel + seller_type +
      transmission + owner, data = vehicle)
##
## Residuals:
##
       Min
                      Median
                 1Q
                                   ЗQ
                                           Max
## -1171869 -169573
                      -25668
                               119142 7549809
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -7.122e+07 3.805e+06 -18.718 < 2e-16 ***
               3.670e+04 1.883e+03 19.493 < 2e-16 ***
## km_driven
               -9.974e-01 1.685e-01 -5.918 3.51e-09 ***
## fuel
               -9.278e+04 4.710e+03 -19.698 < 2e-16 ***
## seller_type -2.425e+04 1.467e+04 -1.653 0.09835 .
## transmission -8.868e+05 2.201e+04 -40.285 < 2e-16 ***
               -1.676e+04 5.928e+03 -2.827 0.00472 **
## owner
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 429800 on 4333 degrees of freedom
## Multiple R-squared: 0.449, Adjusted R-squared: 0.4482
## F-statistic: 588.5 on 6 and 4333 DF, p-value: < 2.2e-16
gc()
            used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 1213946 64.9
                         2027054 108.3 2027054 108.3
## Vcells 2382295 18.2
                         8388608 64.0 8388606 64.0
```

* represents the significance of variable in the model.

 $\#\#^{***}$ represent highly significant $\#\#^{**}$ represent significant $\#\#^{**}$ represent less significant ## no star : represent no significance

Here we can see that seller_type is not significant for the model, we will remove this and update our model as follows:

```
model_lm1 <- lm(selling_price~year+km_driven+fuel+transmission+owner,data = vehicle)
summary(model_lm1)</pre>
```

```
##
## Call:
## lm(formula = selling_price ~ year + km_driven + fuel + transmission +
      owner, data = vehicle)
## Residuals:
       Min
                 10
                      Median
                                   30
                               115456 7562789
## -1160675 -163426
                      -26086
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -7.113e+07 3.805e+06 -18.692 < 2e-16 ***
                3.664e+04 1.883e+03 19.460 < 2e-16 ***
## year
## km_driven
               -1.016e+00 1.682e-01 -6.044 1.63e-09 ***
               -9.323e+04 4.704e+03 -19.820 < 2e-16 ***
## fuel
## transmission -8.925e+05 2.175e+04 -41.036 < 2e-16 ***
               -1.802e+04 5.880e+03 -3.064 0.0022 **
## owner
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 429800 on 4334 degrees of freedom
## Multiple R-squared: 0.4487, Adjusted R-squared: 0.448
## F-statistic: 705.3 on 5 and 4334 DF, p-value: < 2.2e-16
model_lm2 <- lm(selling_price~year+km_driven+fuel+transmission,data = vehicle)</pre>
summary(model_lm2)
##
## lm(formula = selling_price ~ year + km_driven + fuel + transmission,
      data = vehicle)
##
## Residuals:
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -1152345 -165847
                      -25623
                              114607 7567473
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -7.492e+07 3.602e+06 -20.799 < 2e-16 ***
                3.850e+04 1.783e+03 21.599 < 2e-16 ***
## year
## km driven
               -1.085e+00 1.669e-01 -6.502 8.85e-11 ***
               -9.304e+04 4.708e+03 -19.762 < 2e-16 ***
## fuel
## transmission -8.933e+05 2.177e+04 -41.037 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 430300 on 4335 degrees of freedom
## Multiple R-squared: 0.4475, Adjusted R-squared: 0.4469
## F-statistic: 877.6 on 4 and 4335 DF, p-value: < 2.2e-16
model_lm3 <- lm(selling_price~year+km_driven+transmission,data = vehicle)</pre>
summary(model_lm3)
```

```
##
## Call:
## lm(formula = selling_price ~ year + km_driven + transmission,
      data = vehicle)
## Residuals:
      Min
                1Q Median
                                  30
## -1262774 -164383 -31830 103566 7443587
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -9.445e+07 3.616e+06 -26.119 <2e-16 ***
                4.803e+04 1.792e+03 26.803
                                            <2e-16 ***
## year
## km_driven
                1.543e-01 1.614e-01 0.956
                                            0.339
## transmission -9.153e+05 2.269e+04 -40.329 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 449200 on 4336 degrees of freedom
## Multiple R-squared: 0.3977, Adjusted R-squared: 0.3973
## F-statistic: 954.3 on 3 and 4336 DF, p-value: < 2.2e-16
```