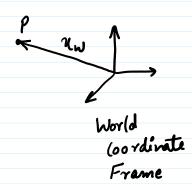
9. Perspedive Projection



Camera lies on the world coordinate frame.

Pinhole

(amera
(coordinate
Frame (c)

Frame (w)

Image Plane is at a distance
of 'f' from the Camera frame 'c'
This distance is alled as
"Fow Length (f)"

Pinhole

Pinhole

(amera

(coordinate

World

(coordinate Frame (c)

World (00 rdinate Frame (w)

The goal is to know the relative position of 'I'wrt W' to take from point?

In 'W' to point no in the image plane

Plane
Plane
Pinhole

(amera
(coordinate
Frame (c)

World (oordinate Frame (w)

$$X_i = \begin{bmatrix} n_i \\ y_i \end{bmatrix}$$

$$X_c = \begin{bmatrix} x_c \\ y_c \\ z_c \end{bmatrix}$$

$$\chi_{\omega} = \begin{bmatrix} \chi_{\omega} \\ y_{\omega} \\ z_{\omega} \end{bmatrix}$$

mage Coordinates

Coordinates

World (oordinates

Steps in 3D to 2D huging Model:—

(1) (oordinate Transformation

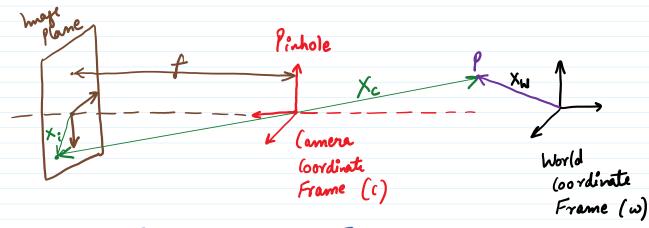
World (oordinates

Coordinates

2 Perspective Projection

Coordinates Coordinates

Perspedeur Projedien: -



$$X_{i} = \begin{bmatrix} x_{i} \\ y_{i} \end{bmatrix}$$

$$X_{c} = \begin{bmatrix} x_{c} \\ y_{c} \\ z_{c} \end{bmatrix}$$

$$x_{c} = \begin{bmatrix} x_{c} \\ y_{c} \\ z_{c} \end{bmatrix}$$

$$x_{c} = \begin{bmatrix} x_{c} \\ y_{c} \\ z_{c} \end{bmatrix}$$

$$x_{c} = \begin{bmatrix} x_{c} \\ y_{c} \\ z_{c} \end{bmatrix}$$

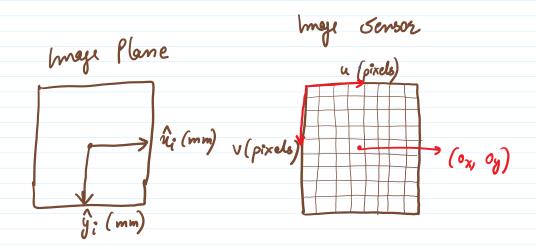
ordinates (coordinates

From diagram,

$$\frac{\mathcal{U}^{\circ}}{f} = \frac{\mathcal{U}_{c}}{2c}$$
 and $\frac{\mathcal{Y}^{\circ}}{f} = \frac{\mathcal{Y}_{c}}{2c}$

$$\Rightarrow u_i = \int \frac{u_c}{z_c} \quad \text{and} \quad y_i = \int \frac{y_c}{z_c} \quad -0$$

where (ni, yi) are the coordinates of points on the image.



If my and my are the pixel densities (pixels/mm) in x and y directions,

- => Top-left comer is origin.
- =) (0x, 0y) is the principle point where optical axis pieces.

Then fixel coordinates be comes:

$$u = m_{x}Ni = m_{x}f\frac{n_{c}}{y_{c}} + o_{x}$$

$$V = m_{y}y_{i} = m_{y}f\frac{x_{c}}{z_{c}} + o_{y}$$

fixel focal dangth

Pixel dennity and food length are unknown.

are properties of the Camera.

Let $fn = m_n f$ $fy = m_g f$

> Put in equation @

 $u = \int_{\infty} \frac{u_c}{2c} + O_x, \quad v = \int_{\infty} \frac{g_c}{2c} + O_y$

$$u = \left(\frac{n_c}{2c} + \frac{0_x}{0_x} \right), \quad v = \left(\frac{1}{2} \frac{g_c}{2c} + \frac{0_y}{2c} \right)$$

4 unknowns

(fu, fy) -> focal length i'n x and y direction.

(ox, oy) -> Principle poput.

(fx, fy, ox, oy) -> Intrinsic Parameters of the camera.

(amera's Internal Geometry"
amera's Internal Geometry"
Guillet W. 7 W. G.