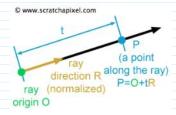
Ray can be mathematically defined as a point (origin) and a direction.



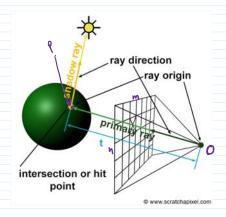
Any point on this ray (P),

P = 0+tR

O' is ray origin.

't' is distance from origin to the point P.

fay-tracing is to find mathematical solutions to compute the interrection of this ray with various types of geometry.



1=0+tR

Ray - Sphere Intersection: -

Sphere of radius is centered at origin, $n^2 + y^2 + z^2 = r^2$

Let (x, y, z) is on the surface then, $x^2 + y^2 + z^2 = x^2$ If (x, y, z) is inside the surface, $x^2 + y^2 + z^2 < x^2$ If (x, y, z) is outside the surface, $x^2 + y^2 + z^2 > x^2$

If the sphere is not in origin but an arbitrary point (Cx, Cy, Cz), then equation of sphere becomes,

 $(\zeta_x - u)^2 + (\zeta_y - y)^2 + (\zeta_2 - z)^2 = x^2 - 0$

=> Any point P that satisfies this equation is on the sphere.

We want to know if our very P=O+tR hits the sphere.

=> point P=O+tR on the very should satisfy the equation (Pn, 1y, Pz) be the coordinates of the point on the very being tested.

((x-Px)^2+(Cy-Py)+((z-Pz)^2=ve^2)

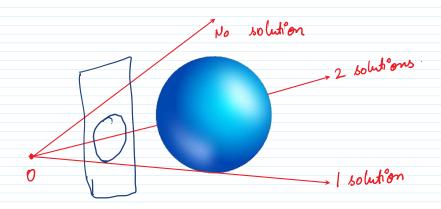
 $\frac{(C_{x}-P_{x})^{2}+(C_{y}-P_{y})+(C_{z}-P_{z})^{2}=\alpha^{2}}{\left[(C_{x}-(O_{x}+tR_{x}))^{2}+(C_{y}-(O_{y}+tR_{y}))^{2}+(C_{z}-(O_{z}+tR_{z}))^{2}-x^{2}=0} \right]$

which is a quadratic equation with, $at^2 + bt + c = 0$ $C = [C_x, C_y, C_z]$ $P = [I_x, P_y, P_z]$ where x = xadius of circle x = xadius of ray for the point being tasted.

Salving for t,

-b t \(\overline{b^2 - 4ac} \)

da



D:- Consider a ray originally from point O(-3,-3) with direction R(1,1).

Let ℓ be a point on the ray at a distant t'.

Find out whether the ray will hit/miss the

circle with equation, $n^2 + y^2 - 4 = 0$ If hit also find out the point (s) of intersection.

$$f = 0 + Rt$$

$$f_{x} = -3 + t$$

$$f_{y} = -3 + t$$

$$(-3 + t)^{2} + (-3 + t)^{2} - 4 = 0$$

$$2(-3 + t)^{2} - 4$$

$$18 + 2t^{2} - 12t - 4 = 0$$

$$2t^{2} - 12t + 14 = 0$$

$$t = -b + \sqrt{b^{2} - 4ac}$$

$$2a$$

$$(b^{2} - 4ac) = (-12)^{2} - 4 \times 2 \times 14$$

$$= 32$$

$$> 0 = 2 \text{ Solutions}$$

$$(-1.415, -1.415)$$

$$(1.415, 1.415)$$