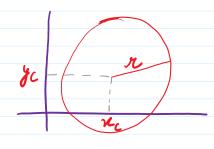
Propaties of Circles:-

A virde is defined as the set of points that are all at a given distance or from a center position (x, yc).

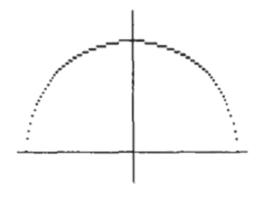


Plotting wing direct methods: 3-

O fytheyorean theorem in Certenan Coordinates as

$$(x - x_c)^2 + (y - y_c)^2 = x^2$$

 $y = y_c \pm \sqrt{x^2 - (x_c - x_c)^2}$ — (1)
plothing wing this equation with $(x_c, y_c) = (0, 0)$



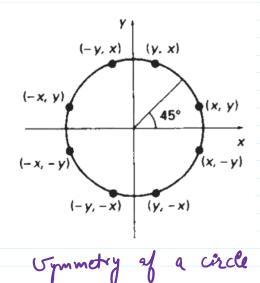
-> 5 pacing between the plotted pixels is not uniform.

-> (ouriderable computation at each step.

-> Sampling x by fixing y?

Delating boundary points wing polar coordinates to and O.

 $\begin{array}{ll}
x = x_c + r \cos \theta \\
y = y_c + r \sin \theta
\end{array}$



Equation 0 -> multiplications & square root calculations

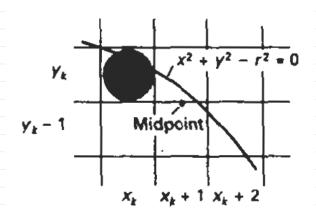
Egnation 3 -> square root & trignom etric calculations.

Midpoint Uscle Agorithm/
Bresenham's Circle Algorithm:—

Sampling at unit intervals and determine the closest pivel possition to the specified circle path at each step.

$$f_{\text{circle}}(x,y) = x^2 + y^2 - x^2$$

$$f_{\text{circle}}(x,y) = \begin{cases} \langle 0, & \text{if } (x,y) \text{ is inside circle boundary.} \\ = 0, & \text{if } (x,y) \text{ is on the circle boundary.} \\ \geq 0, & \text{if } (x,y) \text{ is outside circle boundary.} \end{cases}$$



Which pexel?

(rentl, yk) or (rentl, yk-1)

De cision Parameter?

Gircle function finde (x,y) evaluated at the mid point between the two pixels. $R_k = f_{circle}(x_k + 1, y_k - 1/2)$

G. ...12 1... 1² .2

$$= (\chi_{k} + 1)^{2} + (y_{k} - \frac{1}{2})^{2} - y_{k}^{2}$$

hitial decinon parameter, $\rho_0 = 5_4 - r$ $\rho_0 = 1 - r \quad (\text{for } r \text{ as entergy})$

Algonothm:

1. Input radius or and circle center (ncyc), and obtain the first point on the circumference of a circle centered on the origin as

2. Calculate the initial value of the decision parameter as $\rho_0 = \frac{S}{y} - r$

3. At each no position, starting at k=0, perform the following test:-

If $\rho_k < 0$, the next point along the circle centered on (0,0) is

$$\rho_{k+1} = \rho_k + 2 \kappa_{k+1} + 1$$

-> Otherwise, the next point along
the circle centered on (0,0) is

(xK+1,yK) and

- 4. Determine symmetry points in the other seven octants.
- S. More each alcolated pixel position (n,y)

 onto the circular path centered on (n,y)

 and plot the coordinate values:

6. Repert steps 3 through 5 until nzy.

Example: -
$$x = 10$$
, for first quadrant, $p_0 = 1-r = -9$

Origin (0,0) is the laster

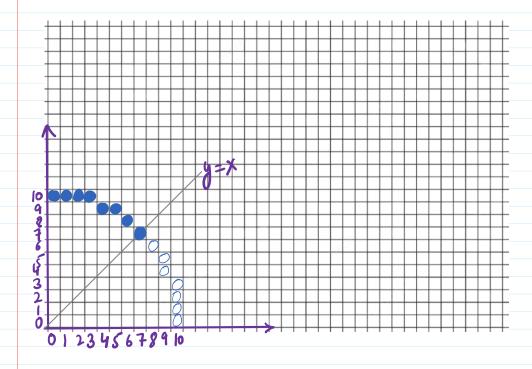
Initial point is (20, y0) = (0, 10)

and initial incremental terms for alensty

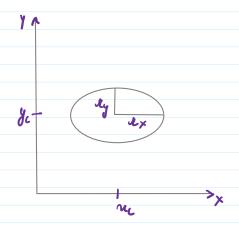
delinon parameters are

0

K	PK	(XK+1) JK+1)	2x _{kti}	2ykti
0	-9	(1, 6)	2	20
Ī	-6	(2, 10)	4	20
2	-1	(3,10)	6	20
3	6	(4,9)	8	18
Ÿ	-3	(5,9)	10	18
5	8	(6,8)	12	16
6	5	(4,4)	14	14



Properties of Ellipses:



Ellipse centered at (xc, yc) with

semi major axis to and semiminon axis ty.

$$\left(\frac{x-u_c}{x_n}\right)^2 + \left(\frac{y-y_c}{y_0}\right)^2 = 1 \qquad -0$$

$$u = u_c + x_x \cos \theta \qquad - 2$$

$$y = y_c + x_y \sin \theta$$

"Midpoint Ellipse Algorithm"

→ book :- Computer Coraphics,

by Donald Hearn and Baker