Pr(u) =
$$[F_1(u) F_2(u) F_3(u) F_4(u)]$$

Pr(u) = $[F_1(u) F_2(u) F_3(u) F_4(u)]$

Property P

05451 15K5n-1

 $F_1(u) = 2u^3 - 3u^2 + 1$ $F_2(u) = -2u^3 + 3u^2$ F3(4) = 4(42-24+1) tk+1 $F_4(u) = 4(u^2 - u) t_{k+1}$ where Fi, F2, F3, F3 are alled the Blendly Functions.

 $=) \quad P_{\kappa}(a) = (F)[a]$ parametri given position and values fangent vectors

where Fis a blending function metrix and G is the geometric function.

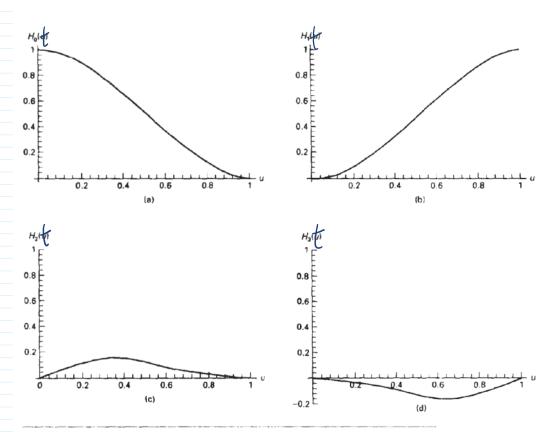


Figure 10-28
The Hermite blending functions.

blending functions becomes, $H_0(t) = 2t^3 - 3t^2 + 1$ $H_1(t) = -2t^3 + 3t^2$ $H_2(t) = t^3 - 2t^2 + t$ $H_3(t) = t^3 - t^2$

"Hermite Polynomial Blending Functions

New Section 2 Page

A special case for cubic splines.

The matrix (B) for solving languat vectors will become,

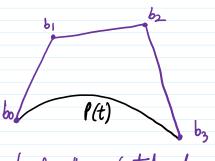
$$\begin{bmatrix}
1 & 0 & -\frac{1}{2} \\
1 & 4 & 1 & -\frac{1}{2} \\
1 & 1 & 4 & 1 & -\frac{1}{2} \\
1 & 1 & 4 & 1 & -\frac{1}{2} \\
1 & 1 & 1 & 1 & -\frac{1}{2} \\
1 & 1 & -\frac{1}{2} \\
1 & 1 & -\frac{1}{2} \\
1 & 1 & -\frac{1}{2} \\
1 & 1 & 1 & -\frac{1}{2}$$

(onstant Matrix

=) Leus computations

bezier (urves :-

User defined avous.

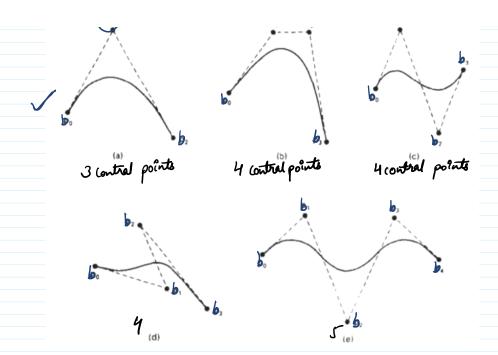


bob, b2 b3 is the contral polyson.









Mothematically,

$$f(t) = \sum_{i=0}^{n} b_i J_i^n(t)$$
 osts1

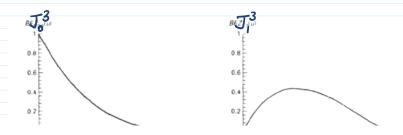
where Jin are called the Burnstein Blending Functions.

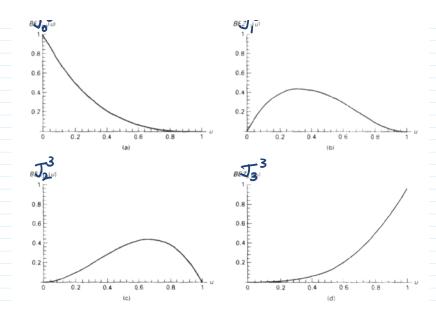
Burnstien Polynomials
$$\int_{i}^{n}(t) = {n \choose i} t^{i} (1-t)^{n-i} = \frac{n!}{i!(n-i)!} t^{i} (1-t)^{n-i}$$
Where, $J_{o}^{o}(t) = 1$

$$J_{i}^{n}(t) = 0 \text{ for } i \notin \{0, -.., n\}$$

$$\sum_{i=0}^{n} J_{i}^{n}(t) = 1$$

Fon n=3





$$J_0^3(t) = t^0(1-t)^3 = (1-t)^3$$

$$J_1^3(t) = 3t(1-t)^2$$

$$J_2^3(t) = 3t^2(1-t)$$

$$J_3^3(t) = t^3$$

$$P(t) = b_0 J_0^3 + b_1 J_1^3 + b_2 J_2^3 + b_3 J_3^3$$

$$P(t) = [(1-t)^3 \quad 3t(1-t)^2 \quad 3t^2(1-t) \quad t^3] \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

$$= \begin{bmatrix} t^{3} & t^{2} & t & 1 \end{bmatrix} \begin{bmatrix} -1 & 3 & -3 & 1 \\ 3 & -6 & 3 & 0 \\ -3 & 3 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} b_{0} \\ b_{1} \\ b_{3} \end{bmatrix}$$

berier Jurfaces 3-

Two sets of berier weres on be und to during an object surface by specifying an input much of

$$P(u,v) = \sum_{j=0}^{m} \sum_{k=0}^{n} b_{j,k} \mathcal{T}_{i,m}(v) \mathcal{T}_{k,n}(u)$$

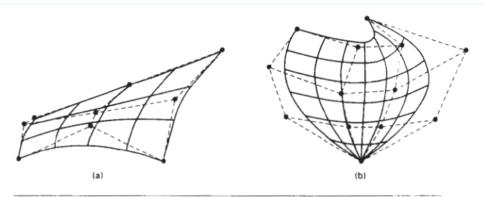


Figure 10-39 Bézier surfaces constructed for (a) m = 3, n = 3, and (b) m = 4, n = 4. Dashed lines connect the control points.

