

Preparation of Papers for IEEE Trans on Industrial Electronics

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and Third C. Author3, *Membership*

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THIS ???

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- 1) New manuscripts cannot exceed **8 pages** (3 for letters). Only a very limited overlength (1/2 page at most) is tolerated. Note that usually in the review process the reviewers tend to ask for more explanations, also note that the maximum allowed length is 8 pages on initial/first submission, including authors' bios and photos.
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- 3) The only file which has to be submitted (uploaded) is the **manuscript in PDF format**.
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experimental results should therefore not be submitted since they will be subject to an “Immediate reject” decision. An experimental rig, which must be used by the authors for verification, must contain hardware components other than a PC/laptop.

Figures that are composed of only black lines and shapes. These figures should have no shades or half-tones of gray. Only black and white.

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A conclusion section is not required. Although a conclusion may review the main points of the paper, do not replicate the abstract as the conclusion. A conclusion might elaborate on the importance of the work or suggest applications and extensions.

Reference numbers are set flush left and form a column of their own, hanging out beyond the body of the reference. The reference numbers are on the line, enclosed in square brackets. In all references, the given name of the author or editor is abbreviated to the initial only and precedes the last name. Use them all; use et al. exceptionally if more than 6 author names were listed. Use commas around Jr., Sr., and III in names.

Other than books [?], [?], [?], [?], capitalize only the first word in a paper title, except for proper nouns and element symbols.

Because replication is required for scientific progress, papers submitted for publication must provide sufficient information to allow readers to perform similar experiments or calculations and use the reported results. Although not everything need be disclosed, a paper must contain new, useable, and fully described information.

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II. INTRODUCTION

Text of the introduction.

- minimum effort control - minimizing the control effort, where the effort is defined as maximum amplitude of the control [1]–[3]
- minimum effort control in robotics (kinematically redundant manipulators) [4]–[7],
- traditional control methods of power converters, carrier-based PWM techniques (sinusoidal, TIPWM) and space vector-based techniques (SVPWM).

III. MOTIVATION AND PRINCIPLES

A. Redundant Voltage Source Network

The problem of redundant voltage source network, degrees of freedom. Analogy to voltage source converters. Clarke's transform, A matrix, vector x as a vector of final voltages with minimum amplitudes.

$$\begin{aligned} x &= [\dots]^T, \\ A &= [\dots], \end{aligned} \quad (1)$$

Motivation -> minimize voltage needed.

B. Optimization problem definition

Linear system, minimum infinity norm, solution vector x. Primal problem definition...

$$\min_{Ax=y} \|x\|_{\infty}, \quad (2)$$

C. Solution using linear programming???

Note sure if this is to include in the paper.....Solution using linear programming - linprog() in Matlab environment, suitable for mathematical modeling and rapid method development for any type of converter. Not effective for real-time application...

IV. PROPOSED SOLUTION

A. Solution way for $m(m+1)$ matrices

.....

If matrix A is of size $m(m+1)$ and if its rank is m (its rows are independent), then we have

$\exists x_0$ such that $Ax_0 = y$ and a is a nonzero element of kernel of A (it satisfies $Aa = 0$). Then (1) is equivalent to minimize $\|x\|_{\infty}$ subject to $x = x_0 + sa$; which amounts solving an optimization problem in one dimension minimize $\|x_0 + sa\|_{\infty}$: (3) For the the optimal solution of (3), there will be some indices $i \neq j$ such that the components satisfy $(x_0 + sa)_i = (x_0 + sa)_j$: This have two solutions (if properly dened)

$$\begin{aligned} s^1 &= \frac{-x_i^0 + x_j^0}{a_i - a_j}, \\ s^2 &= \frac{-x_i^0 - x_j^0}{a_i + a_j}. \end{aligned}$$

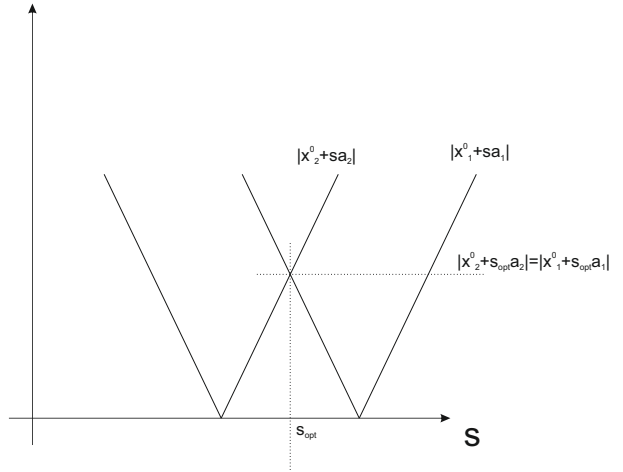
Then among all these s, we select the one with minimal $\|x_0 + sa\|_{\infty}$. We summarize the procedure in Algorithm 1.1.

Algorithm 1.1 For solving (1) with one degree of freedom

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1: Find some nonzero a such that  $Aa = 0$ 
2: Find some  $x^0$  such that  $Ax^0 = y$ 
3:  $f_{\min} \leftarrow \infty$ 
4: for i in 1 : m + 1 do
5:   for j in i + 1 : m + 1 do
6:     if  $a_i \neq a_j$  then ▷ The ratio for s is properly defined
7:        $s \leftarrow \frac{-x_i^0 + x_j^0}{a_i - a_j}$ 
8:       if  $\|x^0 + sa\|_{\infty} \leq f_{\min}$  then
9:          $f_{\min} \leftarrow \|x^0 + sa\|_{\infty}$ 
10:       $s_{\text{opt}} \leftarrow s$ 
11:   end if
12: end if
13: if  $a_i \neq -a_j$  then ▷ The ratio for s is properly defined
14:    $s \leftarrow \frac{-x_i^0 - x_j^0}{a_i + a_j}$ 
15:   if  $\|x^0 + sa\|_{\infty} \leq f_{\min}$  then
16:      $f_{\min} \leftarrow \|x^0 + sa\|_{\infty}$ 
17:      $s_{\text{opt}} \leftarrow s$ 
18:   end if
19: end if
20: end for
21: end for

```



B. Solution way for a general matrix A

....

When A is of a different size, then the kernel is no longer a line but a more dimensional space whose dimension equals to the degree of freedom. Denote the generators of this space by $a_1; \dots; a_K$. Then we have again

$$\{x \mid Ax = y\} = \{x^0 + s^1 a^1 + \dots + s^K a^K \mid s^1, \dots, s^K \in \mathbb{R}\}.$$

This means that (3) is replaced by

$$\text{minimize}_s \left\| x^0 + \sum_{k=1}^K s^k a^k \right\|_{\infty}.$$

...

Solution by ADMM

1 Solve the previous using ADMM

Create matrix $B = [a^1, \dots, a^K]$ and vector $s = [s^1; \dots; s^K]$. Then

$$\sum_{k=1}^K s^k a^k = Bs.$$

Problem (2) is equivalent to

$$\begin{array}{ll} \underset{s, z}{\text{minimize}} & \|z\|_\infty \\ \text{subject to} & x^0 + Bs - z = 0. \end{array}$$

Scaled augmented Lagrangian

$$L(s, z; \mu) = \|z\|_\infty + \frac{\rho}{2} \|x^0 + Bs - z + \mu\|^2$$

ADMM [1, Equations 3.5-3.7] is the iterative procedure

$$\begin{aligned}s^{k+1} &\leftarrow \underset{s}{\operatorname{argmin}} L(\cdot, z^k; \mu^k) \\ z^{k+1} &\leftarrow \underset{z}{\operatorname{argmin}} L(s^{k+1}, \cdot; \mu^k) \\ \mu^{k+1} &\leftarrow \mu^k + x^0 + Bs^{k+1} - z^{k+1}\end{aligned}$$

1.1 Update for s

Minimizing L with respect to s is equivalent to minimizing

$$L(s, z; \mu) = \frac{1}{2} \|x^0 + Bs - z^k + \mu^k\|^2,$$

which is the standard quadratic regression with the closed-form solution

$$s^{k+1} = (B^\top B)^{-1} B^\top (z^k - x^0 + \mu^k).$$

Matrix $C := (B^\top B)^{-1} B^\top$ can be precomputed online.

...

...Problem solving requires high processing power, not very effective in real-time environment....

C. Solution of Dual Problem

... Duality of ℓ_1 and ℓ_∞ norm (D. G. Luenberger) [8]. Dual problem defined by Cadzow:

The Cadzow algorithm [9], [10] is based on a solution search of the associated dual problem

$$\max_{\|\mathbf{A}^T \mathbf{u}\|_1 \leq 1} \mathbf{y}^T \mathbf{u} = \min_{\mathbf{Ax}=\mathbf{y}} \|\mathbf{x}\|_\infty, \quad (3)$$

using the alignment property between final vectors $\mathbf{A}^T \mathbf{u}^0$ and \mathbf{x}^0 to evaluate \mathbf{x}^0 :

$$[\mathbf{A}^T \mathbf{u}^0]^T \mathbf{x}^0 = \|\mathbf{A}^T \mathbf{u}^0\|_1 \|\mathbf{x}^0\|_\infty, \quad (4)$$

i.e.

$$\|\mathbf{x}^0\|_\infty = \mathbf{y}^T \mathbf{u}^0 = [\mathbf{A}^T \mathbf{u}^0]^T \mathbf{x}^0. \quad (5)$$

Primal problem

$$\begin{aligned} & \underset{x}{\text{minimize}} && \|x\|_{\infty} \\ & \text{subject to} && Ax = y. \end{aligned} \tag{1}$$

Dual problem

$$\begin{aligned} & \underset{u}{\text{maximize}} && y^\top u \\ & \text{subject to} && \|A^\top u\|_1 \leq 1. \end{aligned} \quad (2)$$

Dual problem enhanced

$$\begin{aligned} & \underset{u^+, u^-, z^+, z^-, w}{\text{maximize}} && y^\top u^+ - y^\top u^- \\ & \text{subject to} && A^\top u^+ - A^\top u^- - z^+ + z^- = 0, \\ & && \sum_i (z_i^+ + z_i^-) + w = 1, \\ & && u^+, u^-, z^+, z^-, w > 0. \end{aligned} \quad (3)$$

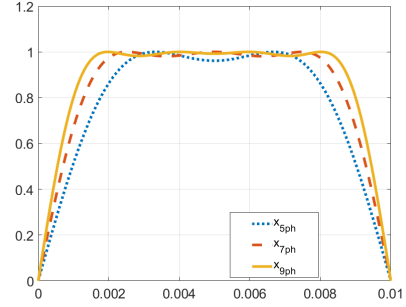


Fig. 1. Figure example

- All three problems are equivalent and they are linear problems.
- Each linear problem has a solution in an extremal point (corner) of its feasible set. The number of extremal points is finite.
- The solution set of (2) does not depend on y . Denote the finite set of extremal points by U .
- Previous two bullets imply the following: For every y , there is always some $u \in U$ which solves (2).
- I do not know how to compute the extremal points of (2) but there is a formula for computing the extremal points of (3).

This suggests that the way to go is to compute the extremal points of (3). Since they are in an enhanced space (u^*, u^*, z^*, z^*, w) , we reduce them into the original space u corresponding to problem (2). This reduction will create a superset of the extremal points of (2). But there is a way of obtaining the set of extremal points of (2) from this superset.

V. APPLICATION/CONTROL OF POWER CONVERTERS)

A. Traditional three-phase converters

Conventional three-phase converters, correlation to SVPWM and

B. Three-phase four-leg converters

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C. Multilevel converters

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D. Multiphase converters

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VI. EXPERIMENTAL RESULTS

Some experimental results.

VII. CONCLUSION

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