



# INTERNATIONAL INSTITUTE OF INFORMATION TECHNOLOGY, HYDERABAD

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RA WORK

VIRTUAL LAB – STRUCTURAL LAB

PART-1

Single	1 - 14
Continuous	15- 21
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Plate	25-29
Truss	30-35

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## Notations

$E$  = modulus of elasticity,  $\text{N/mm}^2$

$I$  = moment of inertia,  $\text{m}^4$

$\ell$  = span length of the bending member,  $\text{m}$

$M$  = maximum bending moment,  $\text{kN-m}$ .

$P$  = total concentrated load,  $\text{kN}$ .

$R$  = reaction load at bearing point,  $\text{kN}$ .

$V$  = shear force,  $\text{kN}$ .

$W$  = total uniform load,  $\text{kN}$ .

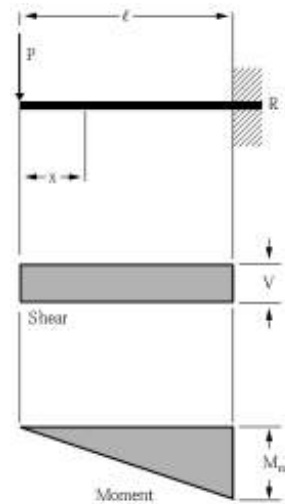
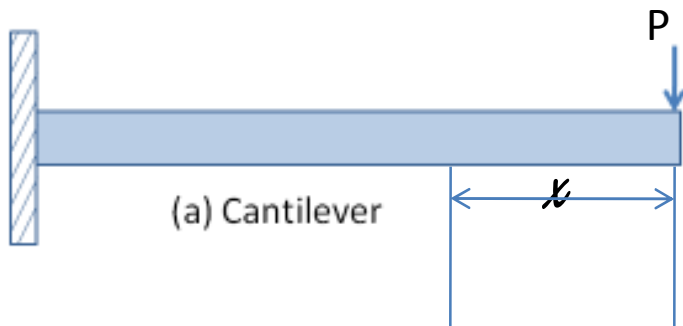
$w$  = load per unit length,  $\text{kN/m}$ .

$\Delta$  = deflection or deformation,  $\text{m}$ .

$x$  = horizontal distance from reaction to point on beam,  $\text{m}$ .

## SINGLE BEAM

## SAMPLE



### GEOMETRY

Length (m)

Breadth (mm)

Depth (mm)

### BOUNDARY TYPE

- ☐ Cantilever
- ☐ Fixed
- ☒ Simple Supported

### MATERIAL

Concrete Grade

### LOADING TYPE

UDL (KN)

Point load (KN)

$$R = V \dots \dots \dots = P$$

$$M_{\max} \text{ (at fixed end)} \dots \dots \dots = P\ell$$

$$M_x \dots \dots \dots = Px$$

$$\Delta_{\max} \text{ (at free end)} \dots \dots \dots = \frac{P\ell^3}{3EI}$$

$$\Delta_x \dots \dots \dots = \frac{P}{6EI} (2\ell^3 - 3\ell^2x + x^3)$$

## SINGLE BEAM

## INPUT

**INPUT**

**GEOMETRY**

Length (m)

Breadth (mm)

Depth (mm)

**MATERIAL**

Concrete Grade

**BOUNDARY TYPE**

☒ Cantilever  
☐ Fixed  
☐ Simple Supported

**LOADING TYPE**

UDL (KN)

Point load (KN)

Selected type of beam for using formulations (radio button)

Length can be varied from 1 m to 4 m, in gaps of 0.1 m

Selected dimension is shown in the box which will be used for calculations

Empty box should take the value zero.

This number shows the increment or decrement of original number

'x' distance from the right end where point load is to be applied

## SINGLE BEAM

## CALCULATIONS

### Input Data

$$l = 3 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$d = 0.25 \text{ m}$$

### Youngs Modulus

$$\begin{aligned} E &= 5000 \times \text{sqrt}(30) \\ &= 27386.12 \text{ N/mm}^2 \\ &= 2.73 \times 10^7 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} I &= (b \cdot d^3) / 12 \\ &= 3.25 \times 10^{-4} \text{ m}^4 \end{aligned}$$

### Beam Type selected

Cantilever

### Deflection Calculations

$$\Delta_x = \frac{P}{6EI} (2l^3 - 3l^2x + x^3)$$

### Shear Force Calculations

$$V = P$$

### Bending Moment Calculations

$$M_x = Px$$

At any  
point 'x'

## SINGLE BEAM

## CALCULATIONS

Any doubts:

Information missing:

### List of figures & Equations:

- |           |   |
|-----------|---|
| Figure 1  | Simple Beam—Uniformly Distributed Load  |
| Figure 2  | Simple Beam—Concentrated Load at Any Point  |
| Figure 3  | Cantilever Beam—Uniformly Distributed Load  |
| Figure 4  | Cantilever Beam—Concentrated Load at Free End   |
| Figure 5  | Cantilever Beam—Concentrated Load at Any Point  |
| Figure 6  | Beam Fixed at Both Ends—Uniformly Distributed Load                                    |
| Figure 7  | Beam Fixed at Both Ends—Concentrated Load at Center                                   |
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| Figure 9  | Continuous Beam—Two Equal Spans—Uniform Load on One Span                              |
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| Figure 12 | Continuous Beam—Two Equal Spans—Uniformly Distributed Load                            |
| Figure 13 | Continuous Beam—Two Equal Spans—Two Equal Concentrated Loads Symmetrically Placed     |
| Figure 14 | Continuous Beam—Two Unequal Spans—Uniformly Distributed Load                          |
| Figure 15 | Continuous Beam—Two Unequal Spans—Concentrated Load on Each Span Symmetrically Placed |

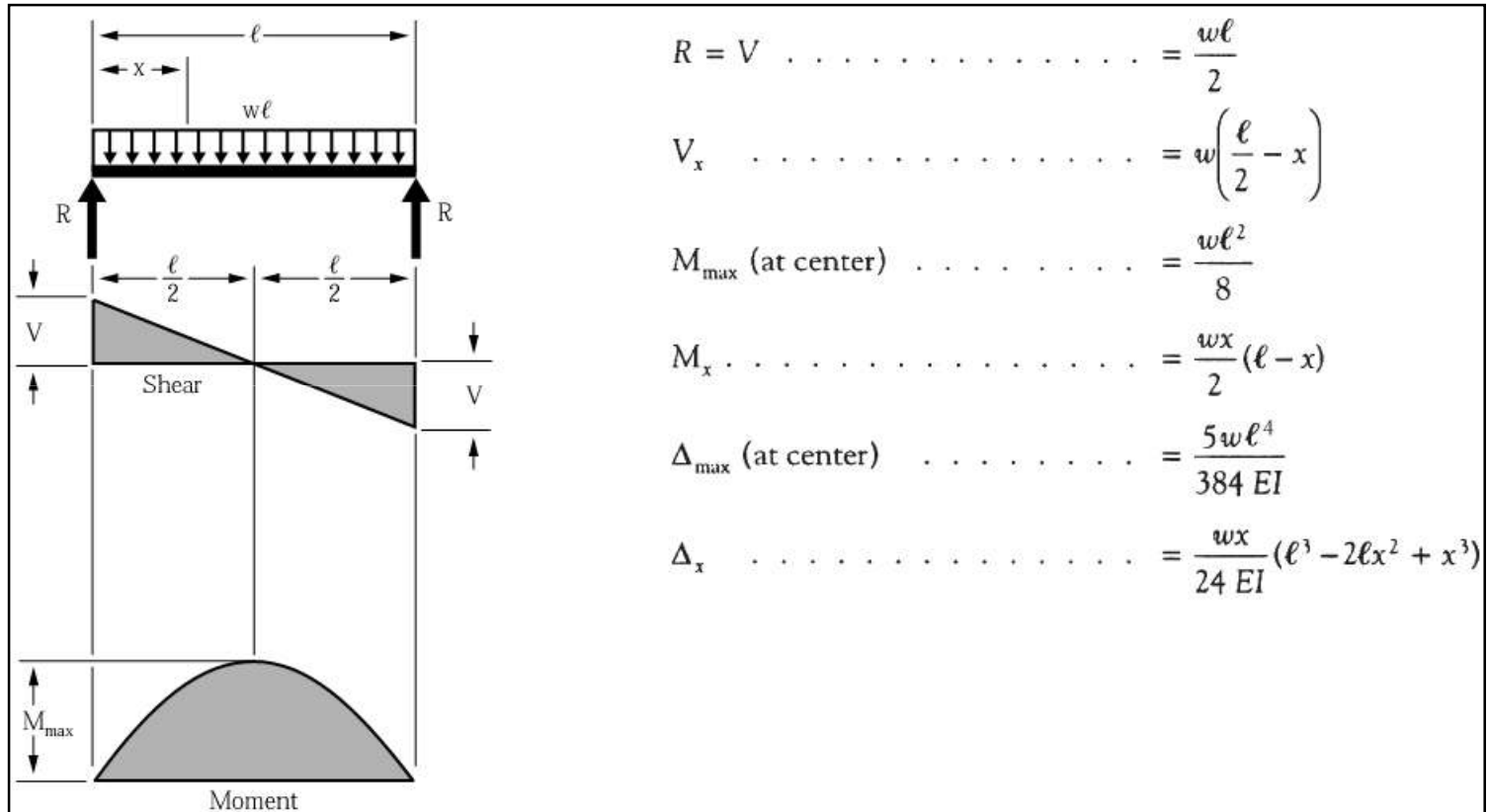
**Figure 1****Simple Beam—Uniformly Distributed Load**



Figure 2

## Simple Beam—Concentrated Load at Any Point

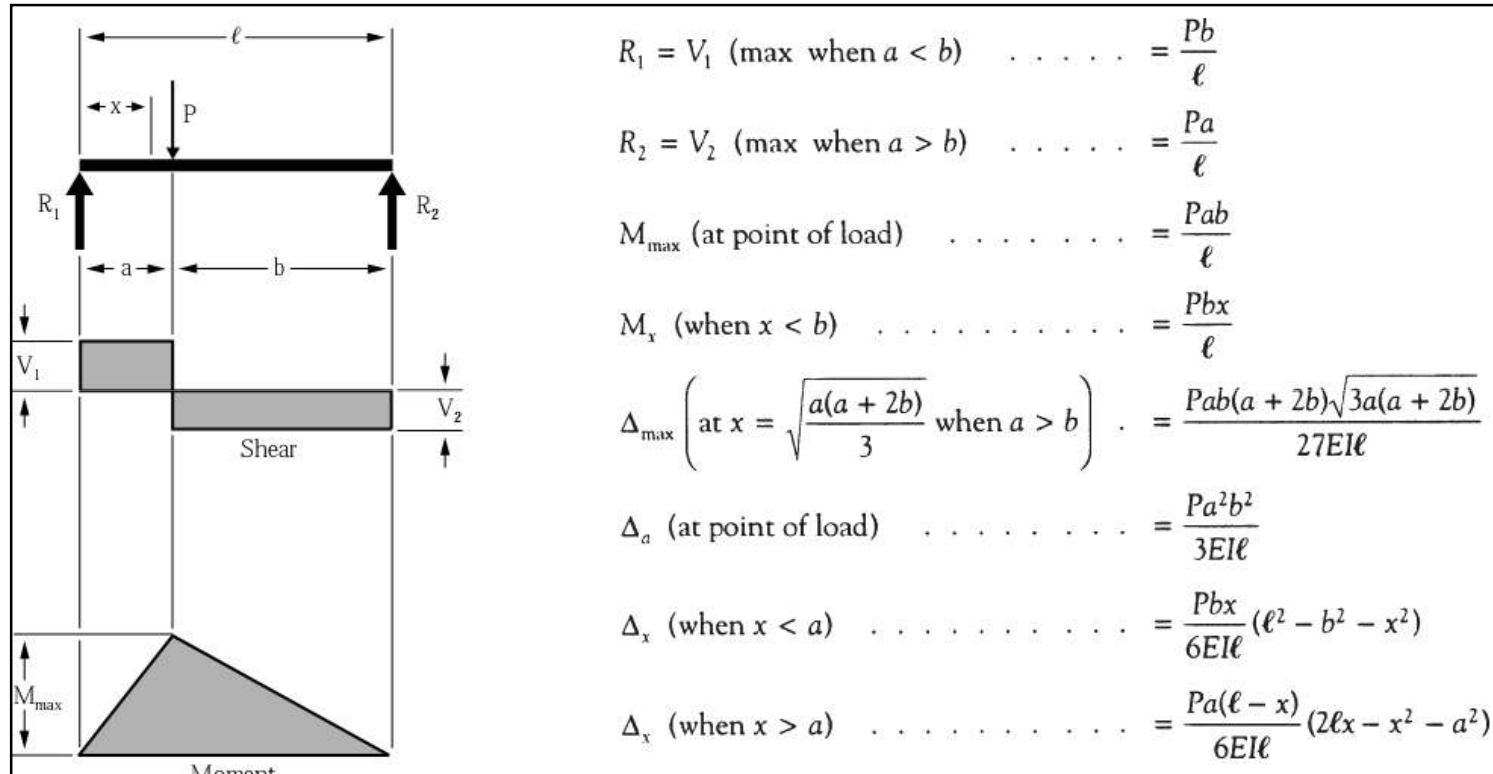
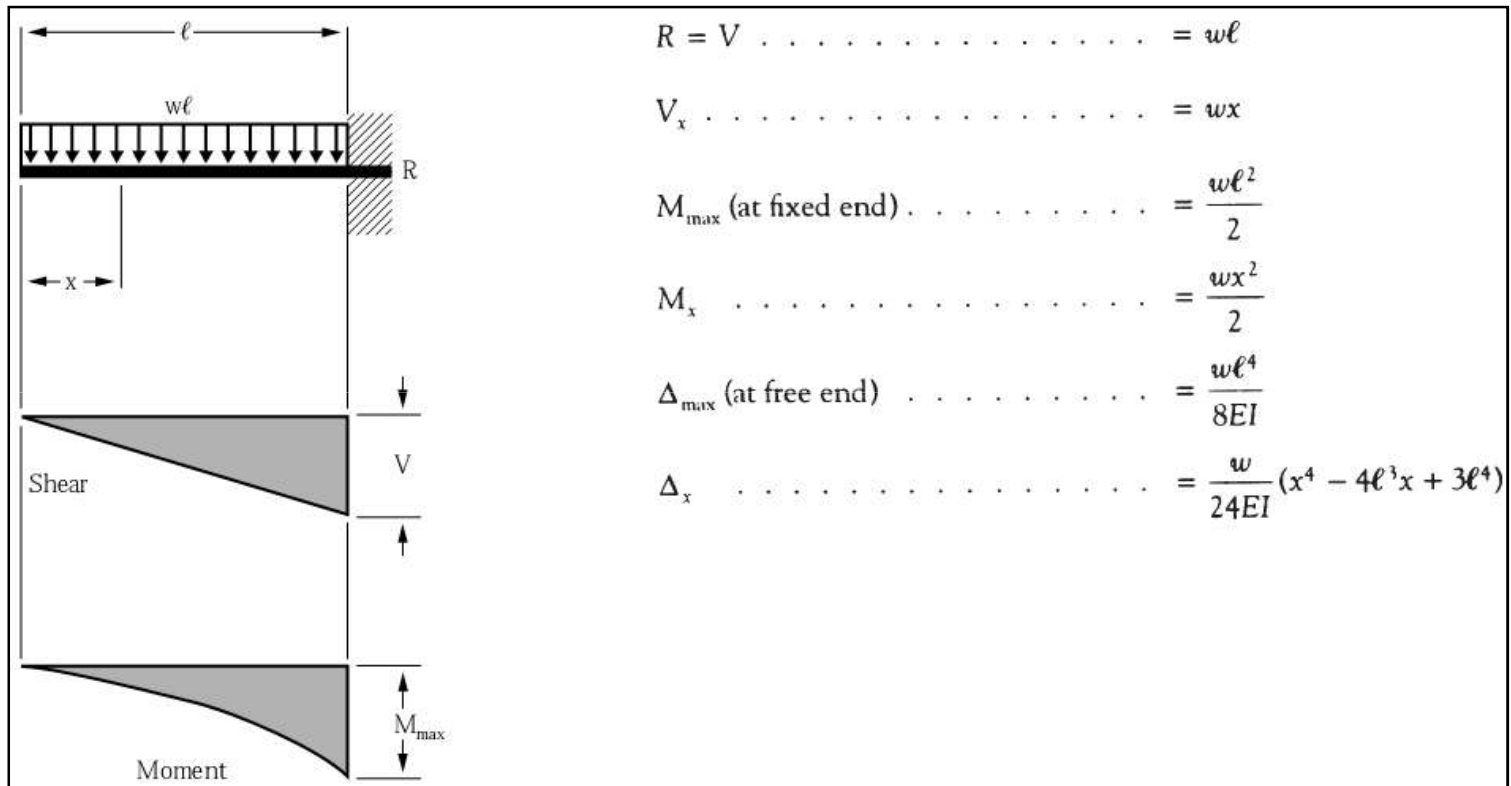


Figure 3

## Cantilever Beam–Uniformly Distributed Load



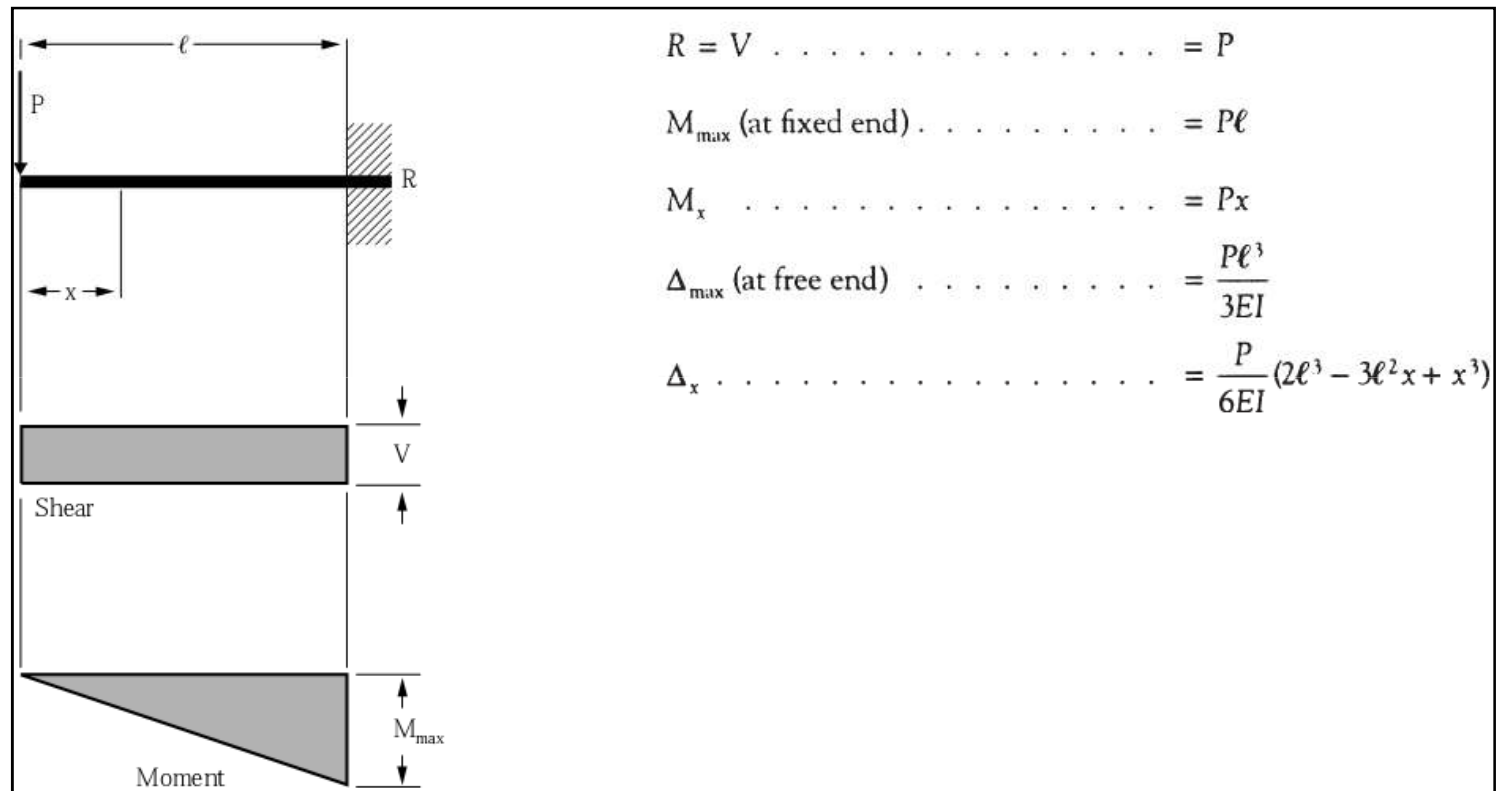
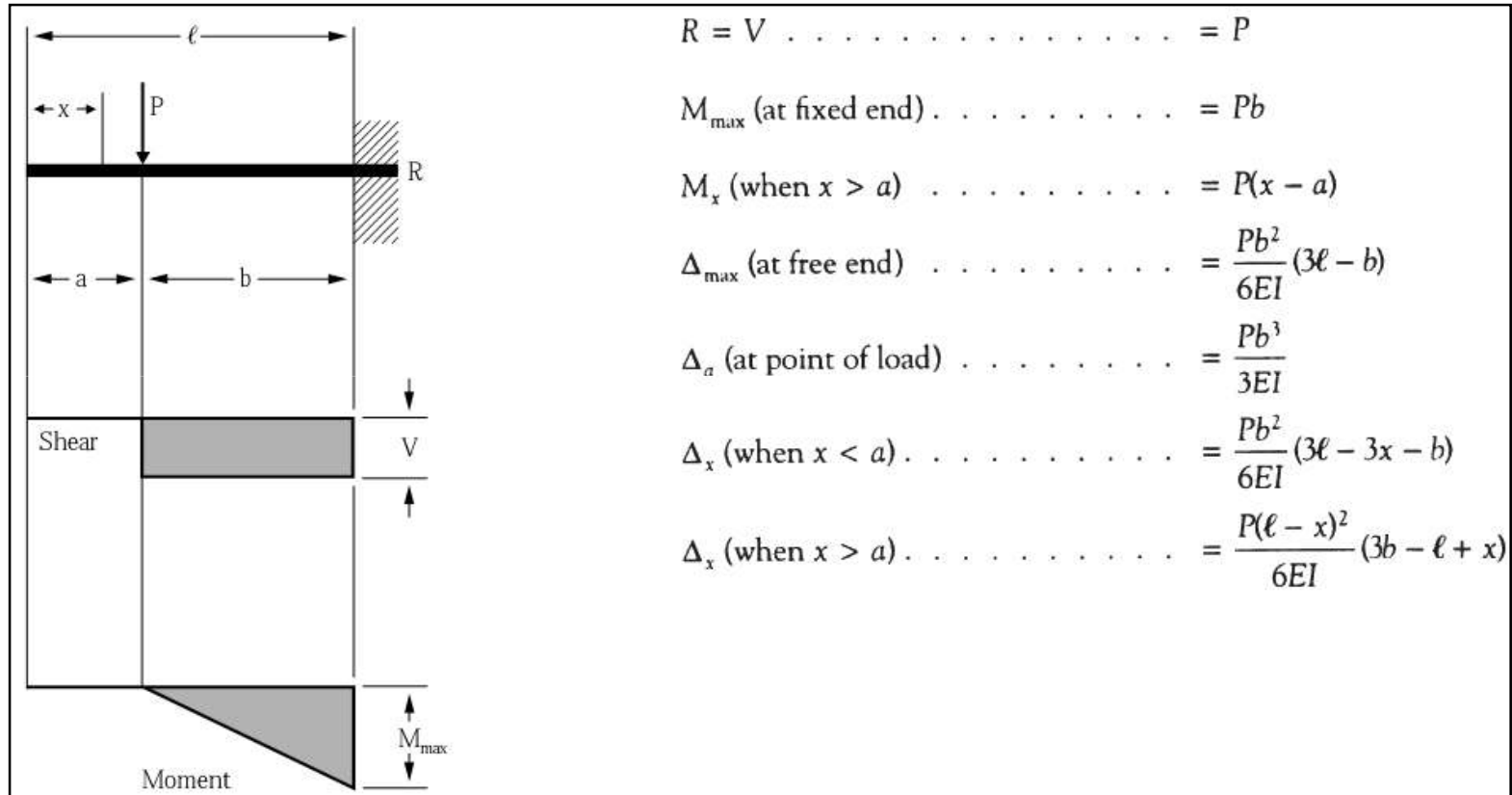
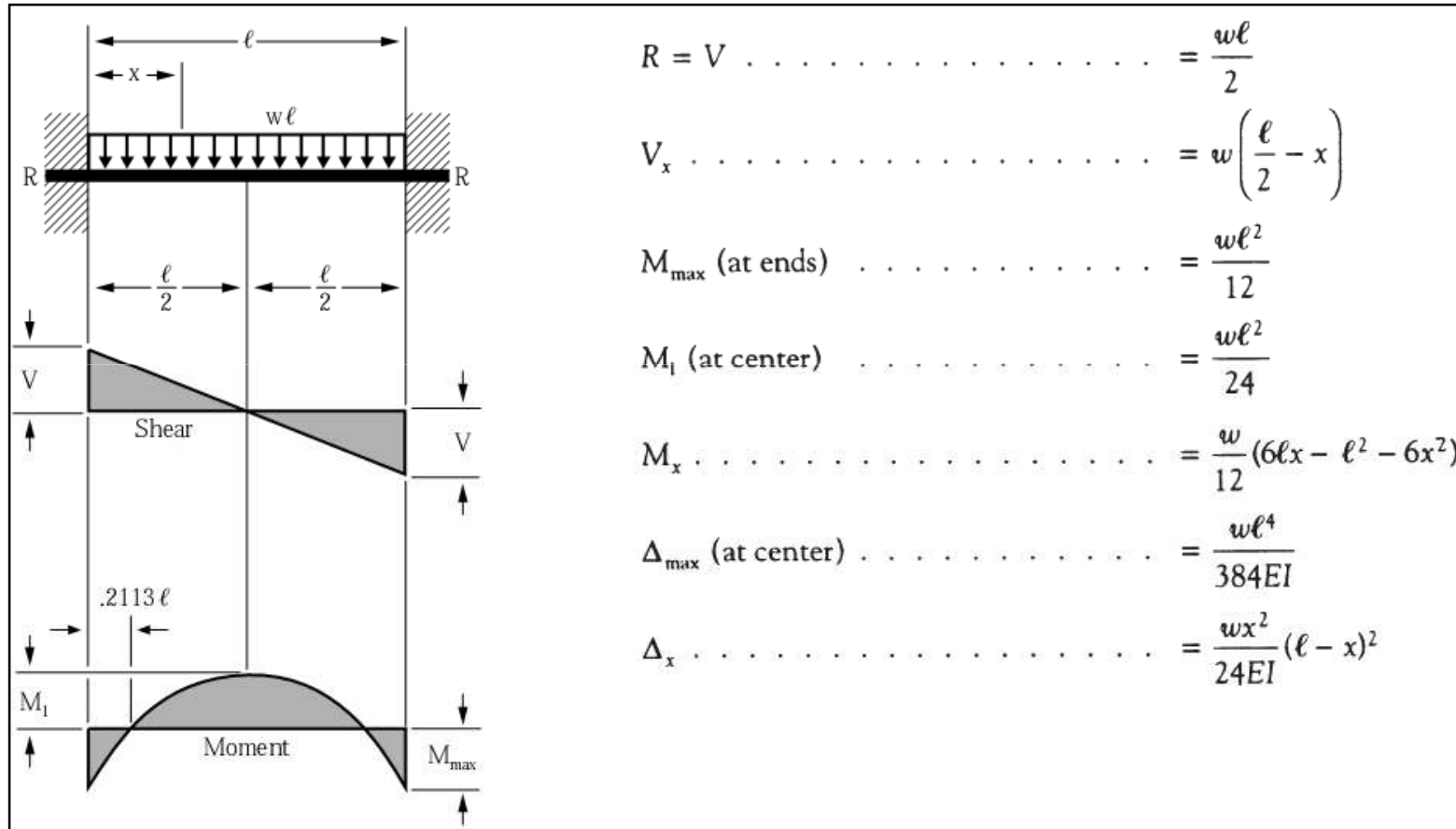
**Figure 4****Cantilever Beam–Concentrated Load at Free End**

Figure 5

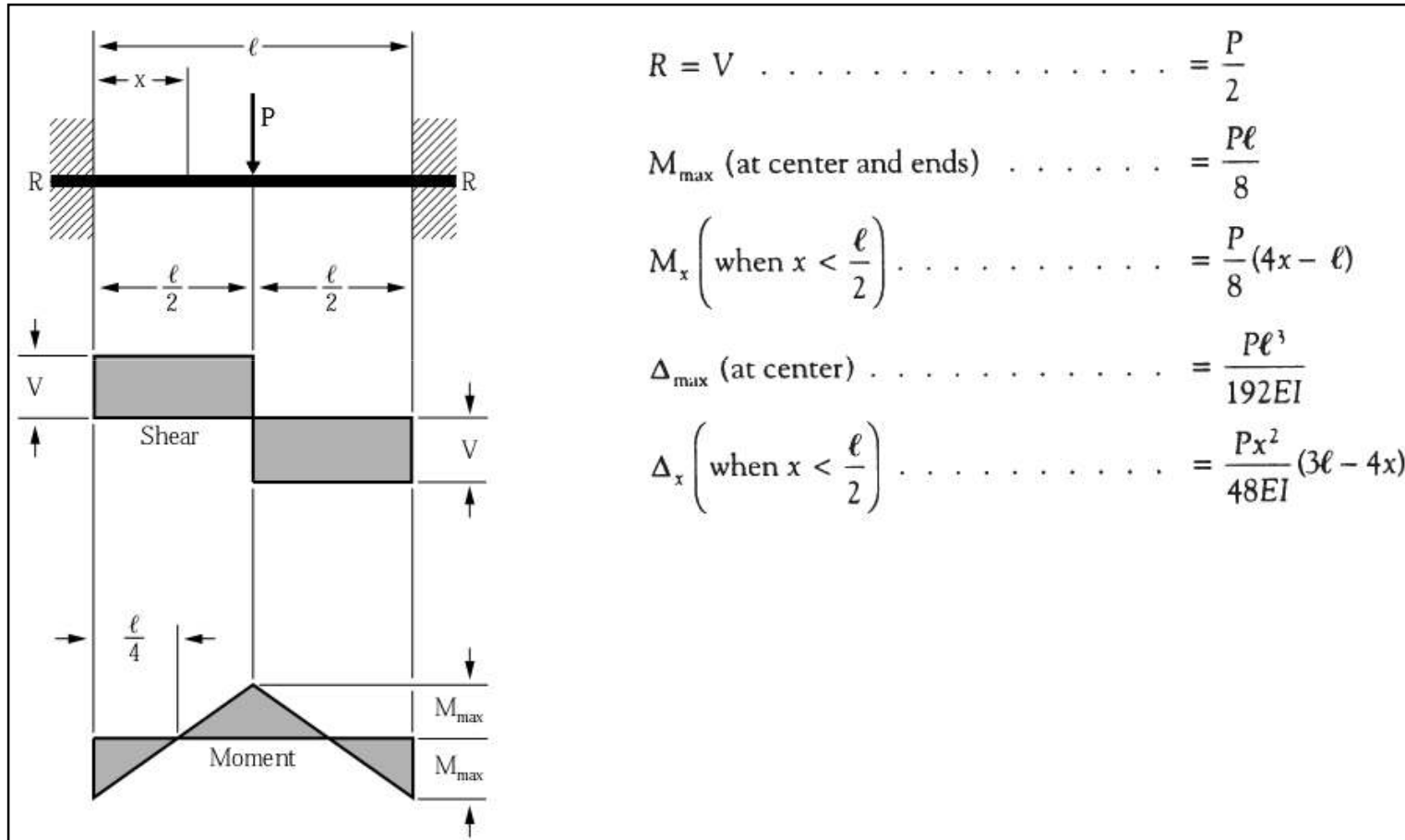
## Cantilever Beam–Concentrated Load at Any Point

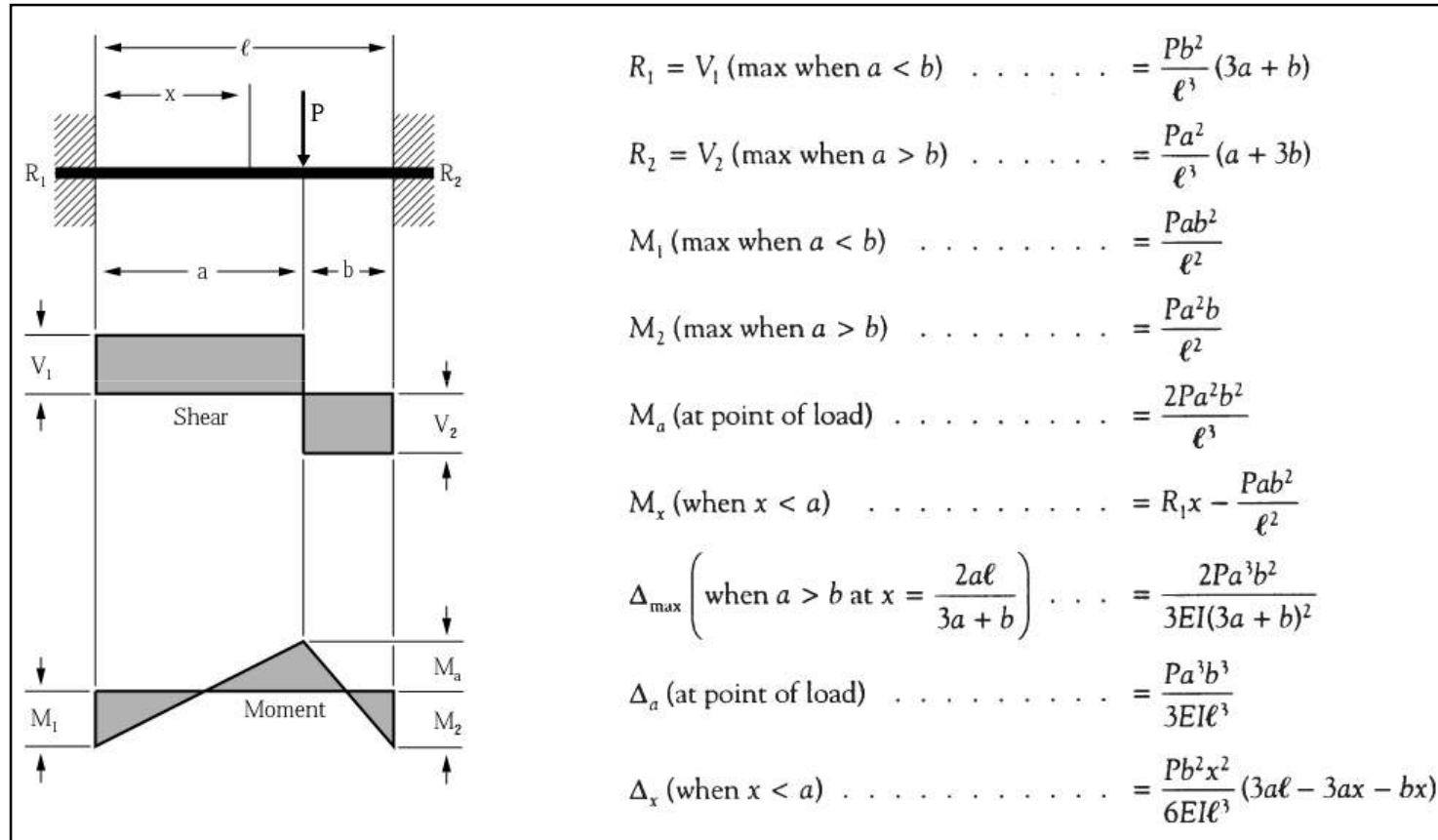


**Figure 6**                      **Beam Fixed at Both Ends—Uniformly Distributed Load**



**Figure 7**      **Beam Fixed at Both Ends—Concentrated Load at Center**



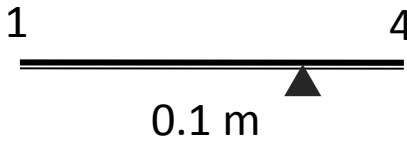
**Figure 8      Beam Fixed at Both Ends—Concentrated Load at Any Point**

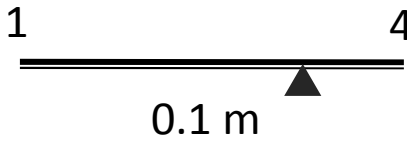
## Continuous Beams

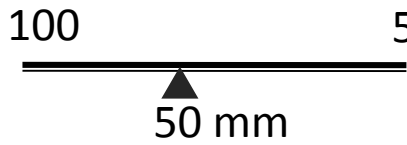
- Figure 9     Continuous Beam—Two Equal Spans—Uniform Load on One Span
- Figure 10    Continuous Beam—Two Equal Spans—Concentrated Load at Center of One Span
- Figure 11    Continuous Beam—Two Equal Spans—Concentrated Load at Any Point
- Figure 12    Continuous Beam—Two Equal Spans—Uniformly Distributed Load
- Figure 13    Continuous Beam—Two Equal Spans—Two Equal Concentrated Loads Symmetrically Placed
- Figure 14    Continuous Beam—Two Unequal Spans—Uniformly Distributed Load
- Figure 15    Continuous Beam—Two Unequal Spans—Concentrated Load on Each Span Symmetrically Placed

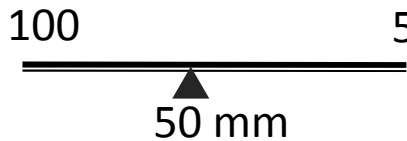


## GEOMETRY

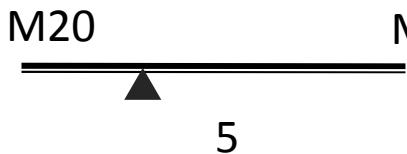
Length1 (m) 

Length2 (m) 

Breadth (mm) 

Depth (mm) 

## MATERIAL

Concrete Grade 

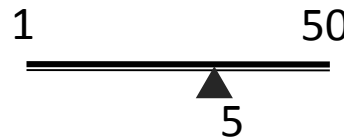
## BOUNDARY TYPE

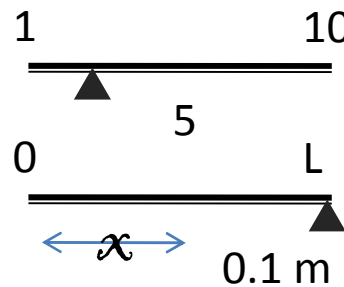
☒ Simple Supported

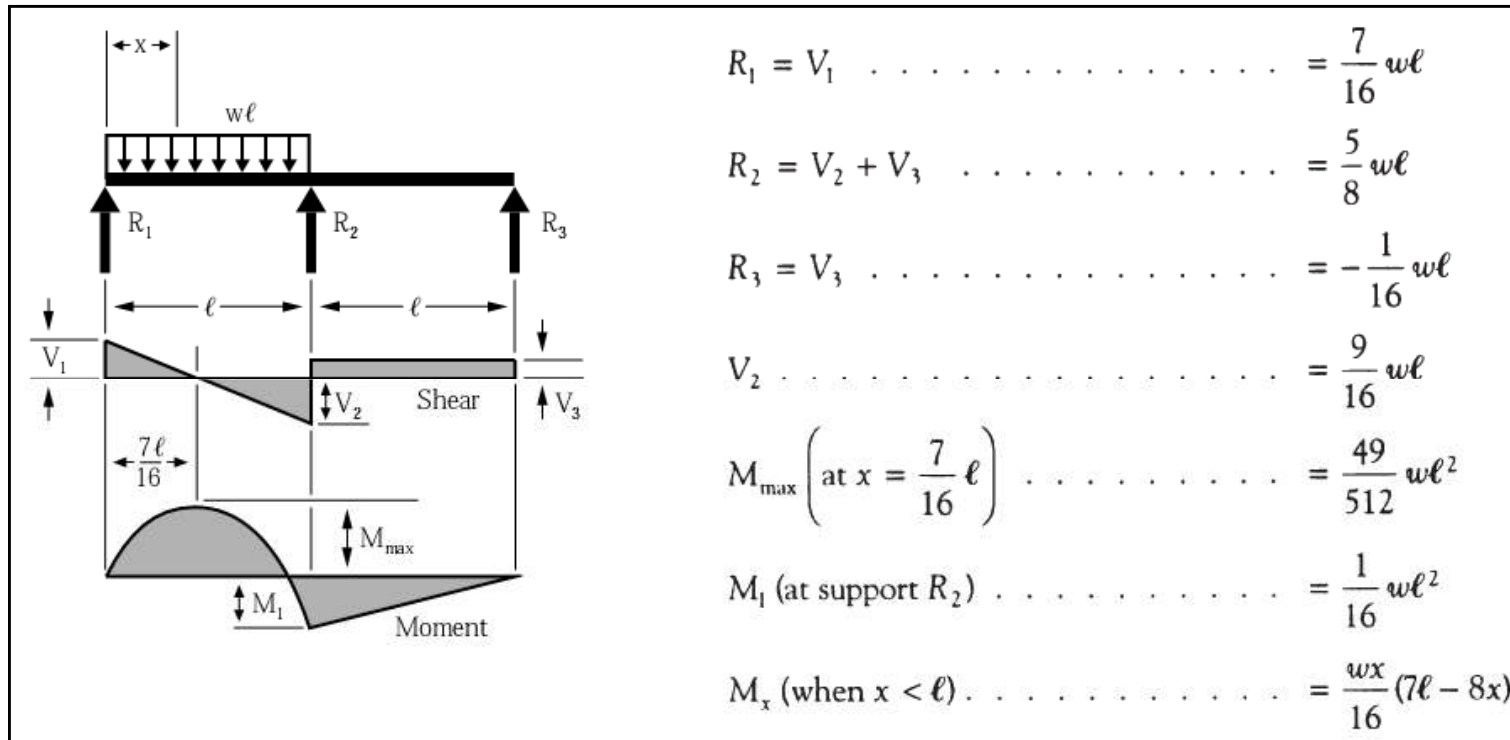
☐ Cantilever

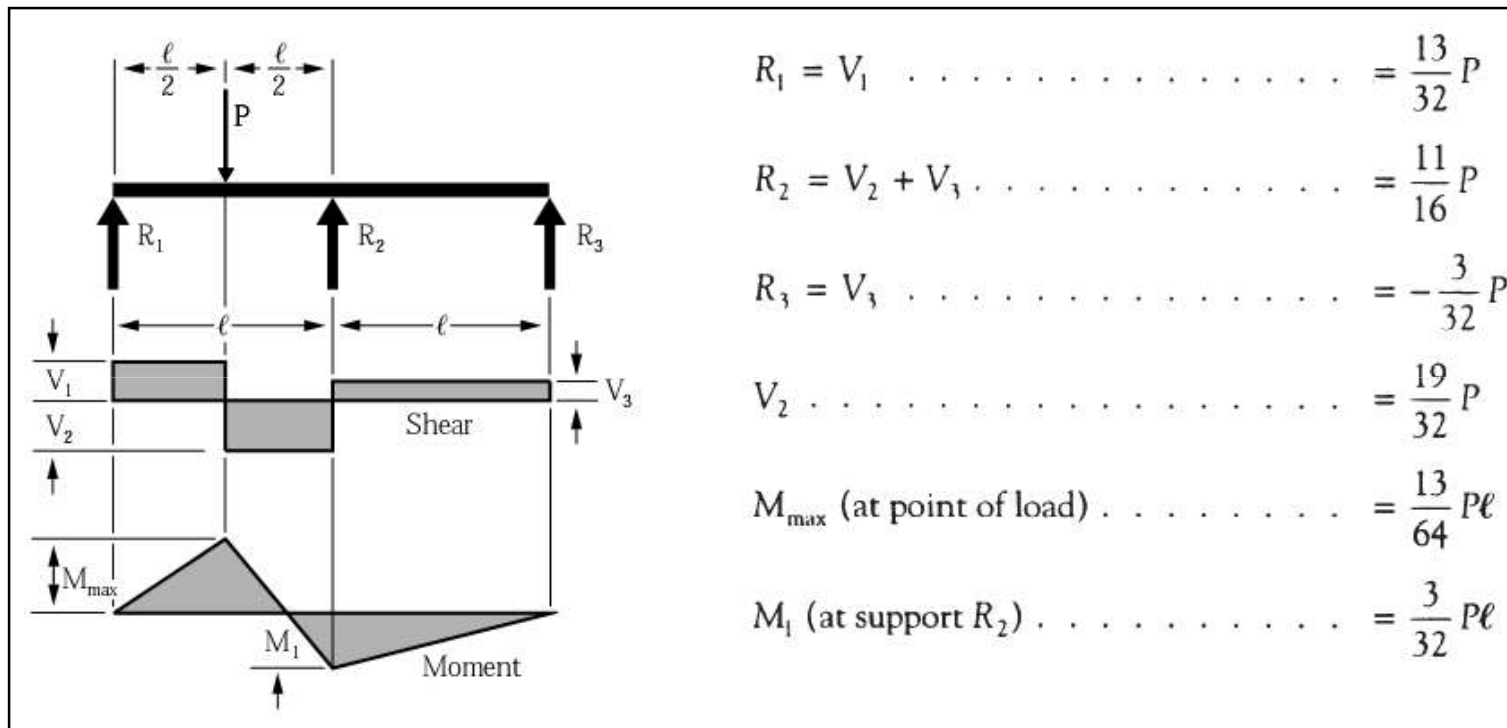
☐ Fixed

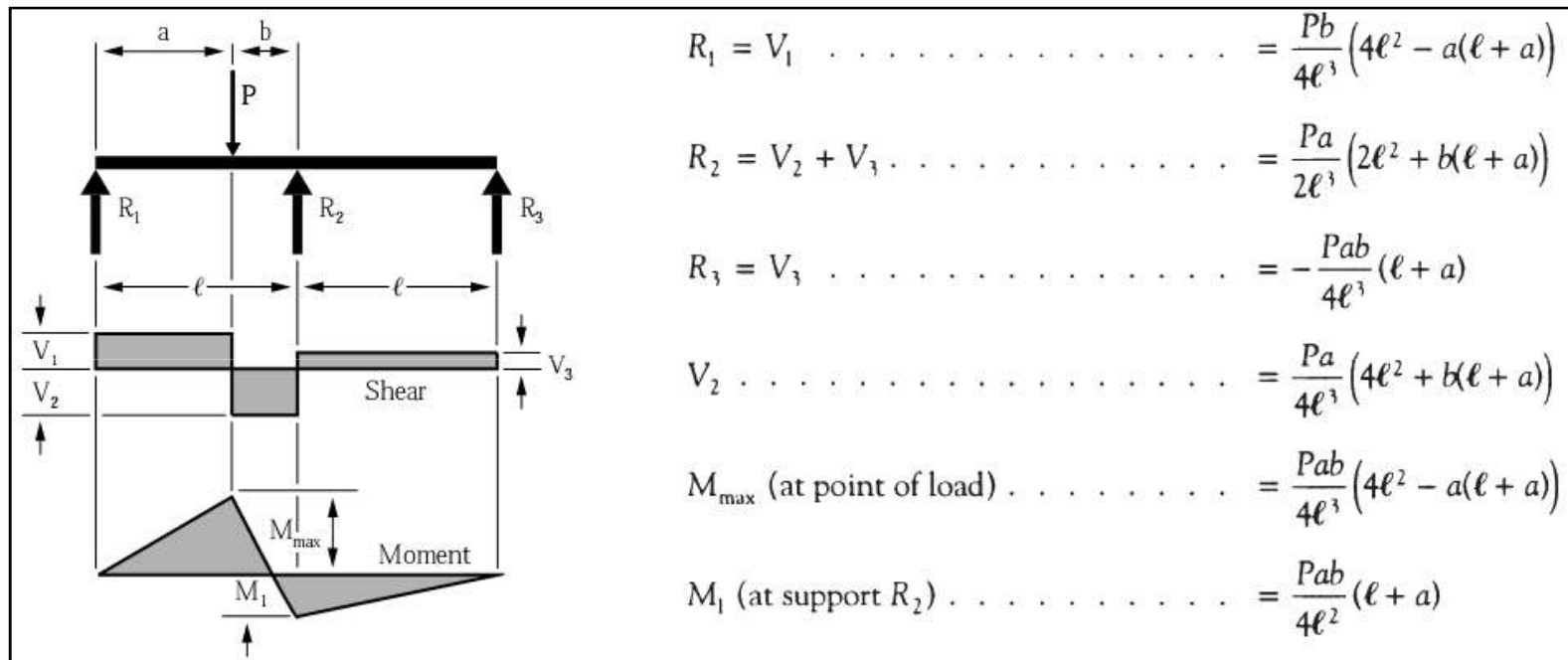
## LOADING TYPE

UDL (KN) 

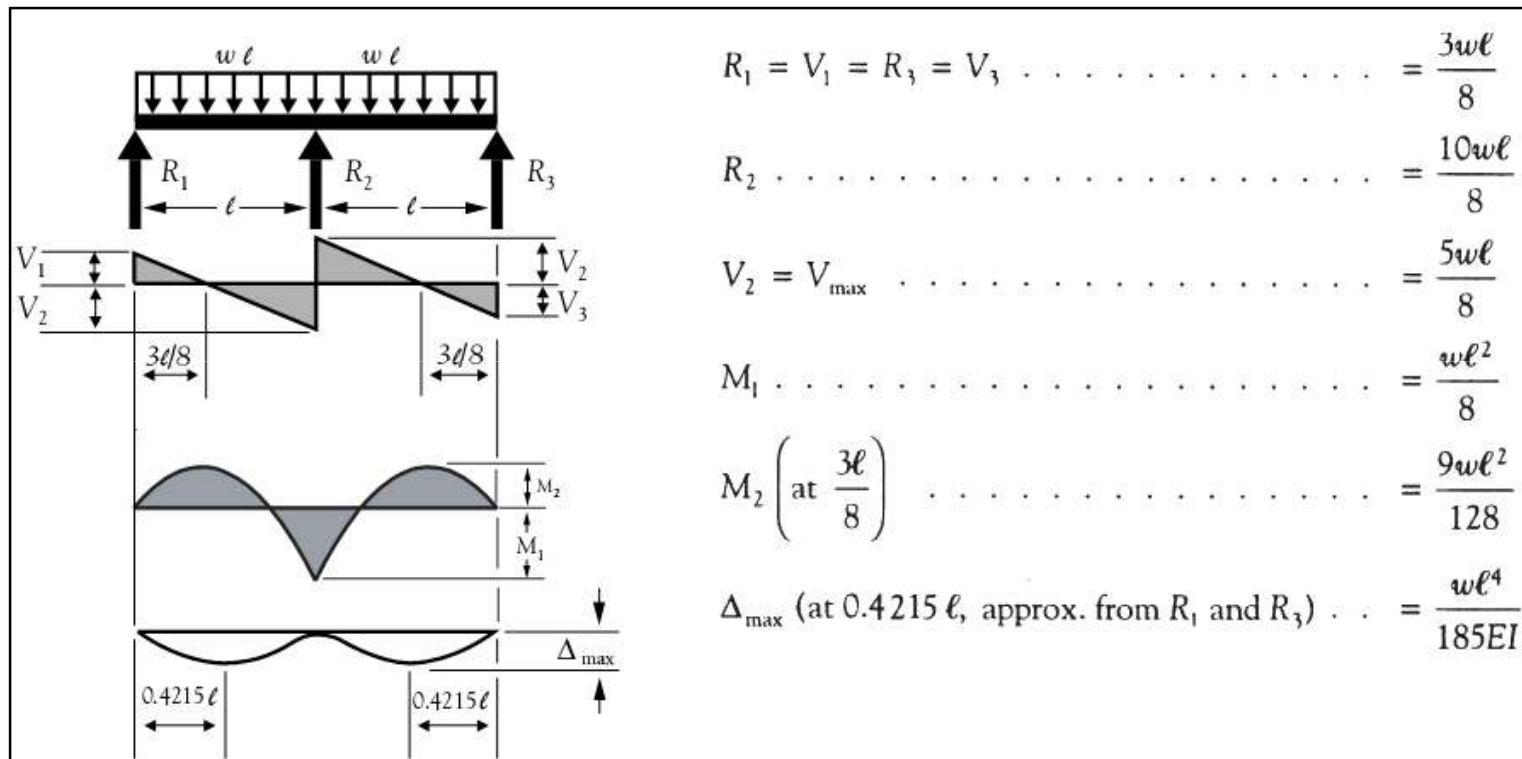
Point load (KN) 

**Figure 9      Continuous Beam—Two Equal Spans—Uniform Load on One Span**

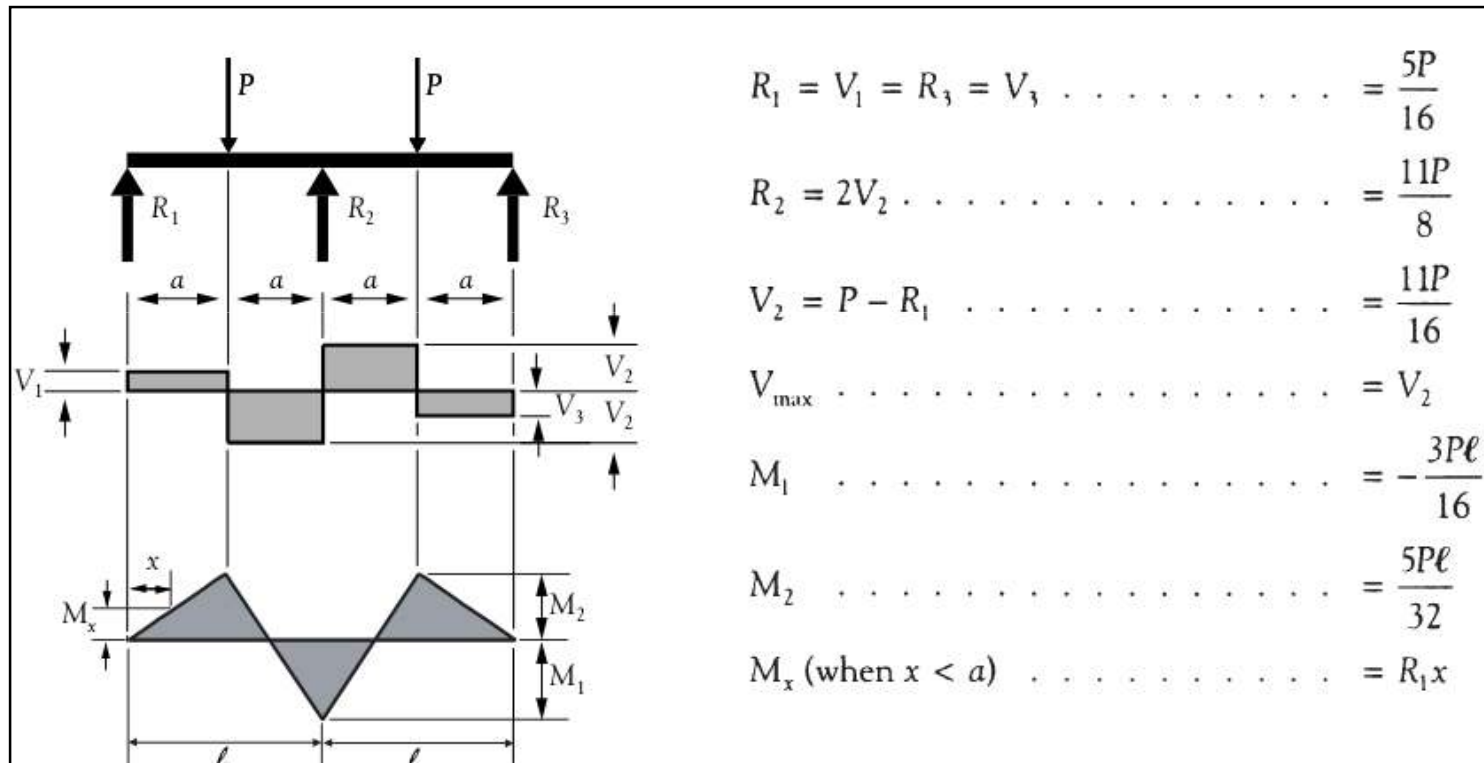
**Figure 10 Continuous Beam—Two Equal Spans—Concentrated Load at Center of One Span**

**Figure 11 Continuous Beam—Two Equal Spans—Concentrated Load at Any Point**

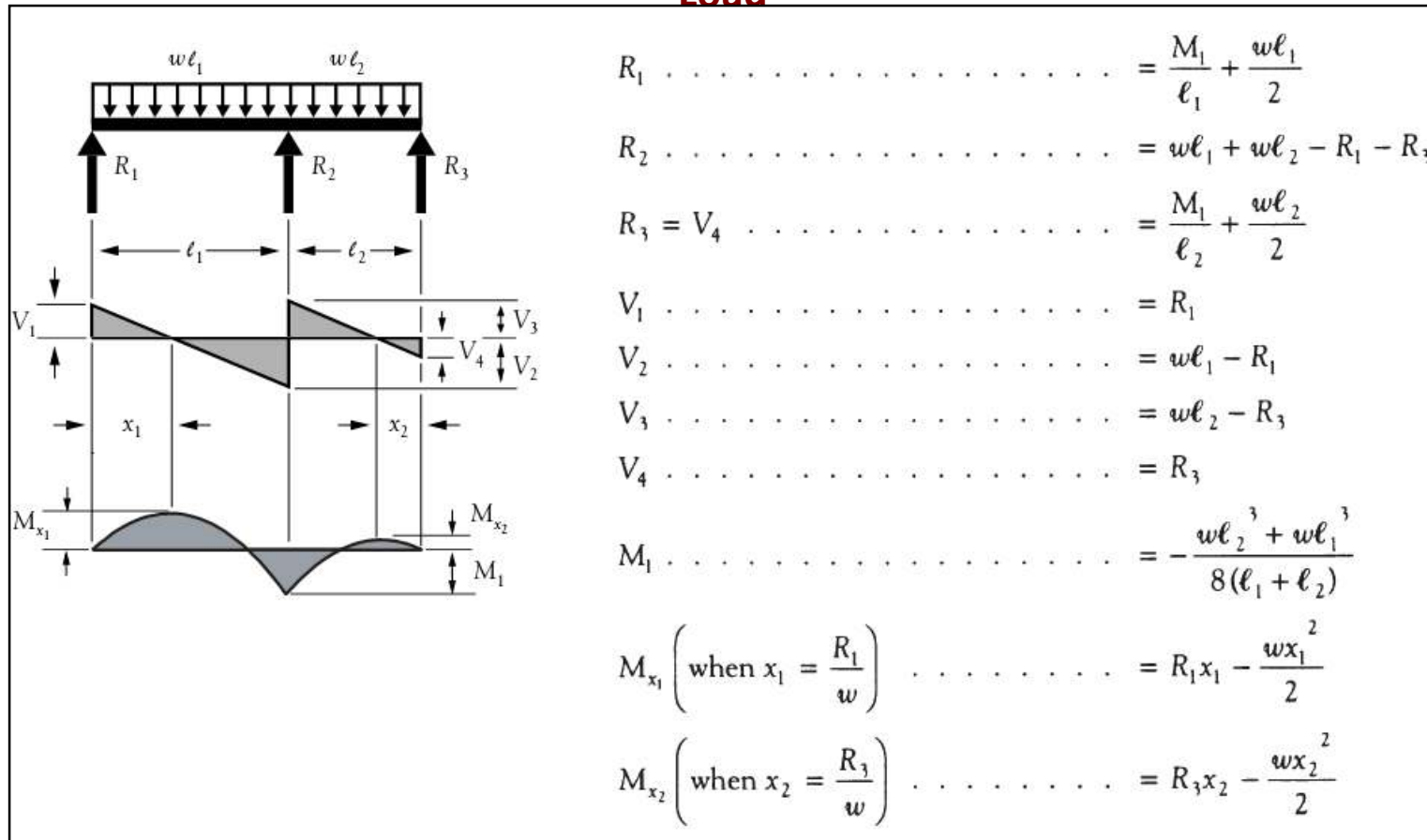
**Figure 12**                      **Continuous Beam—Two Equal Spans—Uniformly Distributed Load**



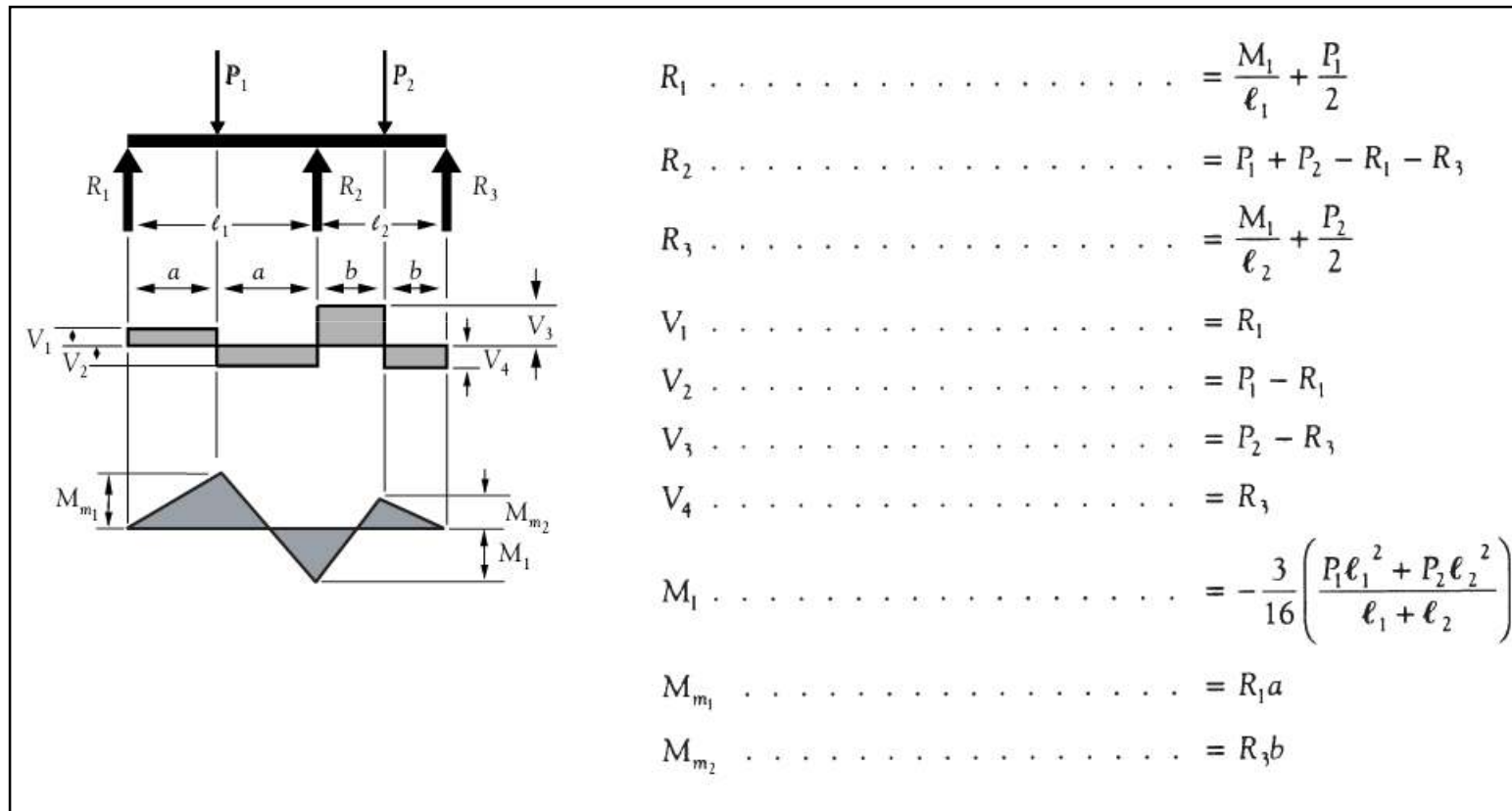
**Figure 13**                      **Continuous Beam—Two Equal Spans—Two Equal Concentrated Loads Symmetrically Placed**



**Figure 14**                      **Continuous Beam—Two Unequal Spans—Uniformly Distributed Load**



**Figure 15**                      **Continuous Beam—Two Unequal Spans—Concentrated Load on Each Span Symmetrically Placed**





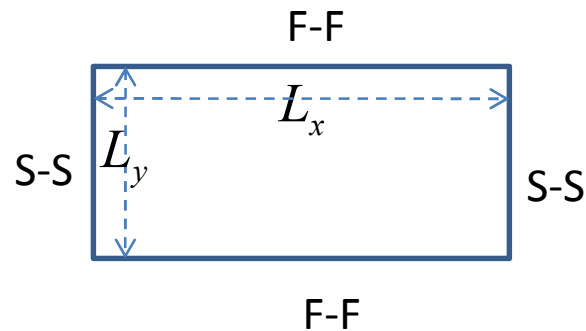
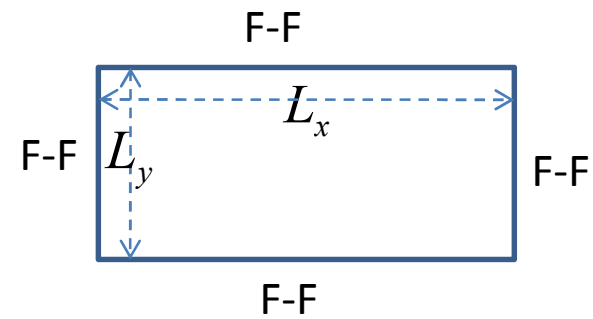
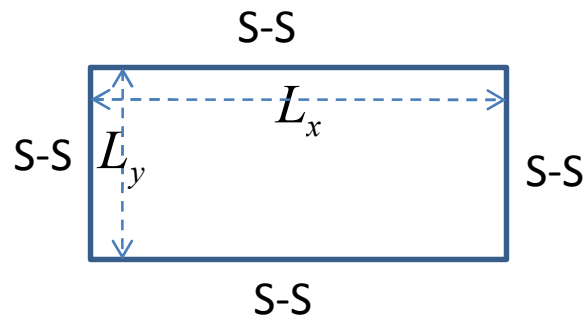
## PLATES

CASE 1: All sides simply supported with UDL

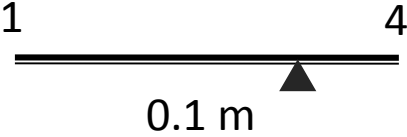
: All sides simply supported with Point load

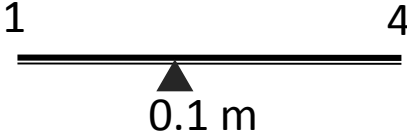
CASE 2: All sides fixed with UDL

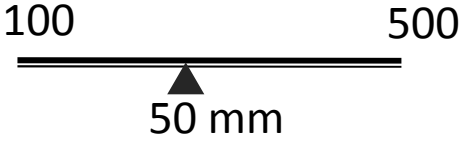
: All sides fixed with point load



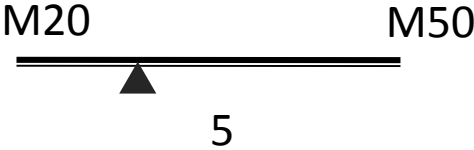
## GEOMETRY

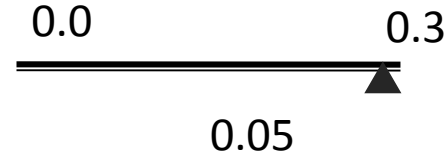
Length (m) 

Breadth (m) 

Thickness (mm) 

## MATERIAL

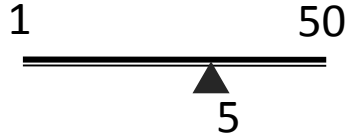
Concrete Grade 

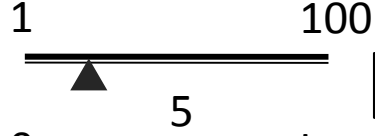
Poisson Ration  $\nu$  

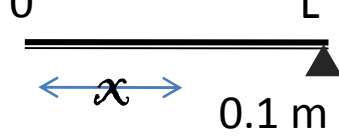
## BOUNDARY TYPE

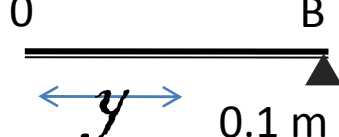
- ☒ All sides Simply supported
- ☐ All sides Fixed
- ☐ Two Simply supported & 2 F

## LOADING TYPE

UDL (KN) 

Point load (KN) 





## PLATE

## CALCULATIONS

To compute the displacement of a simply-supported rectangular plate under a uniform load.

### Input Data

#### Geometry

Width  $L_x$   
Length  $L_y$   
Thickness  $T$

#### Material

Youngs Modulus  
 $E = 5000 \times \text{sqrt}(30)$   
 $\nu = 0.3$

#### Loading

UDL (P)

### Deflection at any point (x,y)

$$D = \frac{ET^3}{12(1-\nu)}$$

$$w(x, y) = \frac{16p}{\pi^6 D} \sum_{m=1,3,5}^{\infty} \sum_{n=1,3,5}^{\infty} \frac{\sin\left(\frac{m\pi x}{L_x}\right) \sin\left(\frac{n\pi y}{L_y}\right)}{mn \left[ \left(\frac{m}{L_x}\right)^2 + \left(\frac{n}{L_y}\right)^2 \right]^2}$$

## PLATE

## CALCULATIONS

To compute the displacement of a simply-supported rectangular plate under a Point distributed load.

### Input Data

#### Geometry

Width  $L_x$   
Length  $L_y$   
Thickness  $T$

#### Material

Youngs Modulus  
 $E = 5000 \times \text{sqrt}(30)$   
 $\nu = 0.3$

#### Loading

Point load

#### Point load position

X coordinate 'a'  
Y coordinate 'b'

### Deflection at any point (x,y)

$$D = \frac{ET^3}{12(1-\nu)}$$
$$w(x, y) = \frac{4p}{\pi^4 D L_x L_y} \sum_{m=1,3,5}^{\infty} \sum_{n=1,3,5}^{\infty} \frac{\sin\left(\frac{m\pi a}{L_x}\right) \sin\left(\frac{n\pi b}{L_y}\right) \sin\left(\frac{m\pi x}{L_x}\right) \sin\left(\frac{n\pi y}{L_y}\right)}{\left[\left(\frac{m}{L_x}\right)^2 + \left(\frac{n}{L_y}\right)^2\right]^2}$$

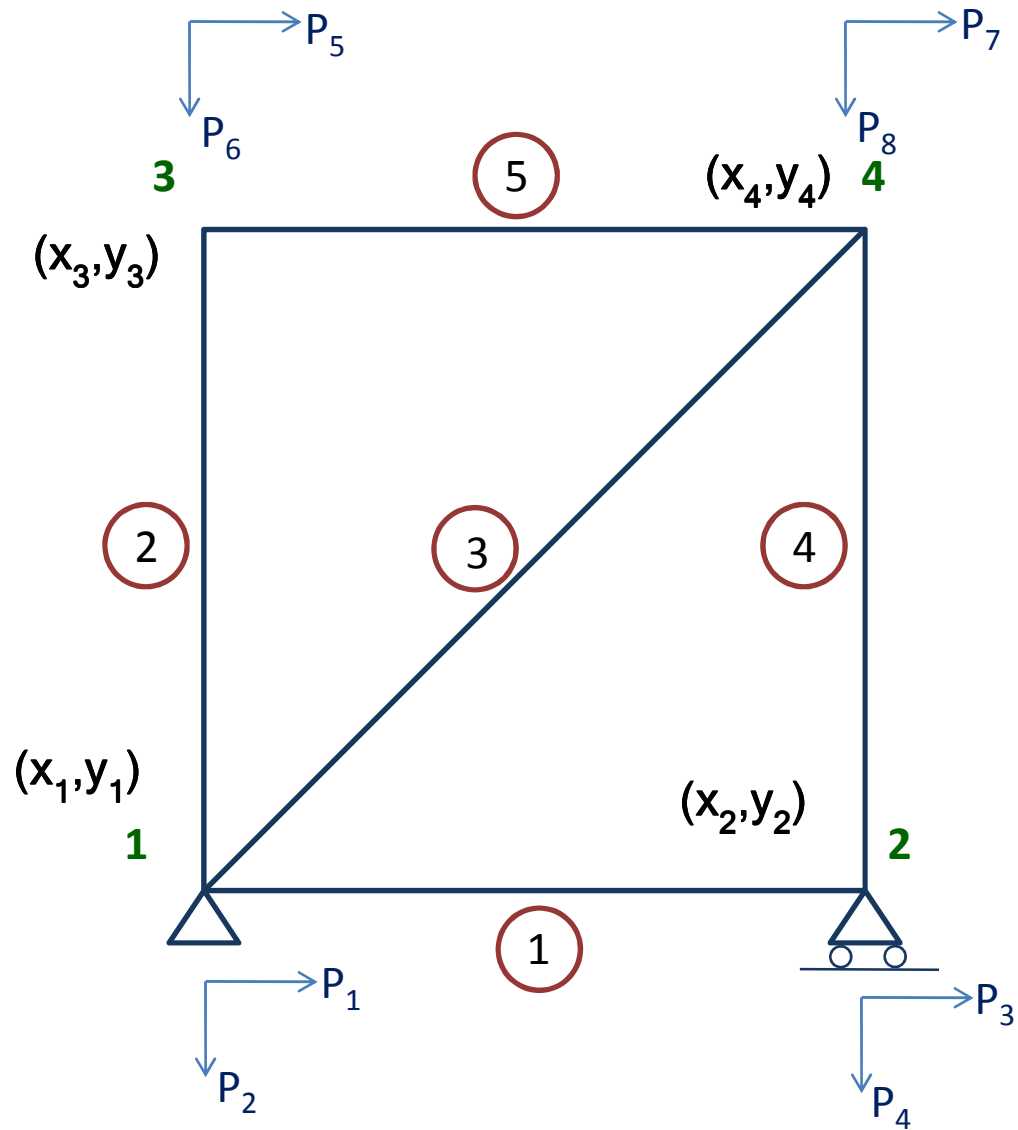
## PLATE

## CALCULATIONS

To compute the displacement of a two simply-supported and two fixed rectangular plate under a Point distributed load.

Need Update

## TRUSS FORMULATION



# TRUSS

## STEP-1

Nodal Coordinates

ND

Node Number	x	y
1	$x_1$	$y_1$
2	$x_2$	$y_2$
3	$x_3$	$y_3$
4	$x_4$	$y_4$

## STEP-3

Element connectivity

EL

Element	N1	N2	E	A
1	1	2		
2	1	3		
3	1	4		
4	2	4		
5	3	4		

## STEP-2

Element Lengths

$$l_e = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$l = (x_2 - x_1) / l_e$$

$$m = (y_2 - y_1) / l_e$$

E - elastic modulus

A - cross section area

## STEP-4

Element Stiffness Matrix

$$k_{ele} = \frac{E_e A_e}{l_e} \begin{bmatrix} l^2 & lm & -l^2 & -lm \\ lm & m^2 & -lm & -m^2 \\ -l^2 & -lm & l^2 & lm \\ -lm & -m^2 & lm & m^2 \end{bmatrix}$$

## STEP-5

### Global Stiffness Matrix

```
For i=1:size( EL,1) % iterating through all elements -----
```

```
    node1 = EL(i,2);
```

```
    node2 = EL(i,3);
```

```
    E1= EL(i,4);
```

```
    A1 = EL(i,5);
```

```
    % Calculation of  $K_{ele}$  - (step -2 then step - 4 )
```

```
    t1 = node1*2; t2 = node2*2;
```

```
    % global K
```

```
    Kgl((t1 -1):t1,(t1 -1):t1) = Kgl( (t1 -1):t1,(t1 -1):t1) + Klc(1:2,1:2);
```

```
    Kgl((t1 -1):t1,(t2 -1):t2) = Kgl( (t1 -1):t1,(t2 -1):t2) + Klc(1:2,3:4);
```

```
    Kgl((t2 -1):t2,(t1 -1):t1) = Kgl( (t2 -1):t2,(t1 -1):t1) + Klc(3:4,1:2);
```

```
    Kgl((t2 -1):t2,(t2 -1):t2) = Kgl( (t2 -1):t2,(t2 -1):t2) + Klc(3:4,3:4);
```

```
end;
```



## STEP-6

Boundary Conditions and Forces

CON = [ Node number, X-constraint , Y-Constraint ]



Fixed – 0

Free - 1

LOAD = [ Node number, X-force , Y-force ]

```
C=max(max(kgl))*10000  
  
for i=1:size(CON)  
    if(CON(i,2)==0)  
        kgl((CON(i,1)*2)-1,(CON(i,1)*2)-1)=C;  
    end  
  
    if(CON(i,3)==0)  
        kgl((CON(i,1)*2),(CON(i,1)*2))=C;  
    end  
end  
  
f(1:dof,1)=0  
for i=1:size(LOAD)  
    f(2*LOAD(i,1)-1)=LOAD(i,2);  
    f(2*LOAD(i,1))=LOAD(i,3);  
End
```

```
CON = [ 1 0 0 ;  
        2 1 0  
        4 0 0];
```

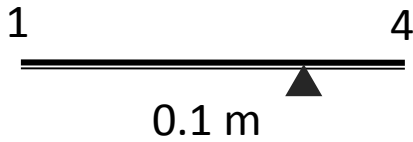
```
LOAD = [ 2 10 0 ;  
         3 10 10 ];
```

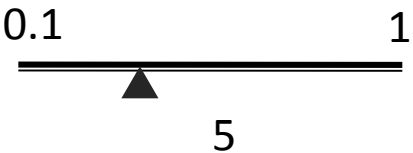
## STEP-7

Final Displacements

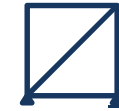
displacements = inv(kgl)\*f

## GEOMETRY

Length(l) (m) 

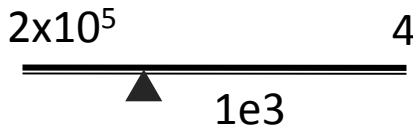
Area (A) (m<sup>2</sup>) 

## BOUNDARY TYPE

☒ CASE-I

☐ CASE-II

☐ CASE-III


## MATERIAL

Young's Modulus (E) kN/m<sup>2</sup> 

## Boundary Conditions

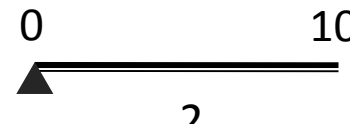
Constraint (CON)

ND	X	Y
1	<input checked="" type="radio"/>	<input checked="" type="radio"/>
2	<input type="radio"/>	<input checked="" type="radio"/>
3	<input type="radio"/>	<input type="radio"/>
4	<input type="radio"/>	<input type="radio"/>

## LOADING TYPE

Node Number (ND)  (1,2,3,4)

Point load (KN) X



Y



## FINAL OUTPUT:

The final out put should be the nodal displacements.

