

# Lab-report:05

Course Name: Digital Image Processing Course Code: CSE438 Section No: 03

#### **Submitted To:**

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**Problem 1:** Apply Fourier transform to transform any image (above) from the spatial domain to the frequency domain. Apply inverse Fourier transform to transform the image from the frequency domain to the spatial domain.

#### Code:

```
gray img1 = imread('gray image1.png');
gray img2 = imread('gray image2.png');
gray img3 = imread('gray image3.png');
gray img1 = im2double(gray img1);
gray img2 = im2double(gray img2);
gray img3 = im2double(gray img3);
fourier img1 = fft2(gray img1);
fourier_img2 = fft2(gray_img2);
fourier img3 = fft2(gray img3);
reconstructed img1 = ifft2(fourier img1);
reconstructed_img2 = ifft2(fourier_img2);
reconstructed img3 = ifft2(fourier img3);
figure;
subplot(3, 4, 1);
imshow(gray img1);
title('Original Img1');
subplot(3, 4, 2);
imshow(real(fourier img1), []);
title('Fourier Transform');
subplot(3, 4, 3);
imshow(reconstructed img1);
title('Reconstructed Img1');
subplot(3, 4, 5);
imshow(gray img2);
title('Original Img2');
subplot(3, 4, 6);
```

```
imshow(real(fourier_img2), []);
title('Fourier Transform');
subplot(3, 4, 7);
imshow(reconstructed_img2);
title('Reconstructed Img2');
subplot(3, 4, 9);
imshow(gray_img3);
title('Original Img3');
subplot(3, 4, 10);
imshow(real(fourier_img3), []);
title('Fourier Transform');
subplot(3, 4, 11);
imshow(reconstructed_img3);
title('Reconstructed_Img3');
```

Original Img1

Fourier Transform Reconstructed Img1

Original Img2

Fourier Transform Reconstructed Img2

Original Img3

Fourier Transform Reconstructed Img3

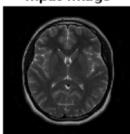
**Problem 2:** Apply three types of high pass filtering in the frequency domain in Figure 1 and find out which one is better to produce the enhanced image (sharpen) for the given image (output must show all steps as shown in Figure 2).

# i. Ideal high pass filter (IHPF)

# Code: clc; clear; close all; a = imread('gray img.png'); a = im2double(a); subplot(2,3,1); imshow(a);

```
title('Input Image');
[m,n] = size(a); D0 = 10; A = fft2(a); subplot(2,3,2);
imshow(uint8(abs(A)));
title('centered fourier spectrum');
A_shift = fftshift(A); A_real = abs(A_shift); subplot(2,3,3);
imshow(uint8(A_real));
title('filtered fourier spectrum');
A high = zeros(m,n);
D = zeros(m,n);
for u=1:m
   for v=1:n
      D(u,v) = sqrt((u-(m/2))^2 + (v-(n/2))^2;
      if D(u,v) \leq D0
                                 A high(u,v) = 0;
           filt(u,v) = 0;
      else
           A_high(u,v) = A_shift(u,v);
           filt(u,v) = 1;
       end
   end
end
subplot(2,3,4);
imshow(filt)
title('Ideal High pass filter')
subplot(2,3,5);
mesh(filt)
title('surface plot HPF')
B = fftshift(A_high); B_inverse = ifft2(B); B_real = abs(B_inverse);%Taking
subplot(2,3,6);
imshow(B_real);
title('processed image');
```

Input Image

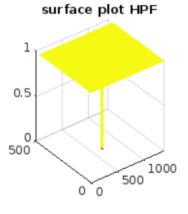


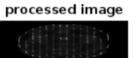
centered fourier spectrumfiltered fourier spectrum





Ideal High pass filter





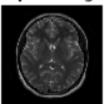
## ii. Butterworth high pass filter (BHPF)

#### **Code:**

```
clc;
clear;
close all;
% Read the image
a = imread('gray img.png');
a = rgb2gray(a);
a = im2double(a);
[m,n] = size(a);
subplot(2,3,1)
imshow(a)
```

```
title('Input image');
A = fft2(a);
subplot(2,3,2);
imshow(uint8(abs(A)));
title('Centered Fourier Spectrum');
A shift = fftshift(A);
A_real = abs(A_shift);
subplot(2,3,3)
imshow(uint8(A_real));
title('Filtered Fourier Spectrum');
D0 = 30;
order = 2;
for u = 1:m
   for v = 1:n
       D = sqrt((u - m/2)^2 + (v - n/2)^2);
       H(u,v) = 1 / (1 + (D0 / D)^(2*order));
   end
end
H_high = H .* A_shift;
H_high_real = H .* A_real;
H_high_shift = fftshift(H_high);
H_high_image = ifft2(H_high_shift);
subplot(2,3,4)
imshow(H)
title('Butterworth High Pass Filter');
subplot(2,3,5);
mesh(H)
title('Surface Plot BHPF')
subplot(2,3,6)
imshow(abs(H_high_image));
title('Butterworth High Pass Filtered Image');
```

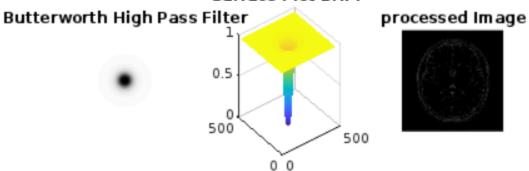








#### Surface Plot BHPF

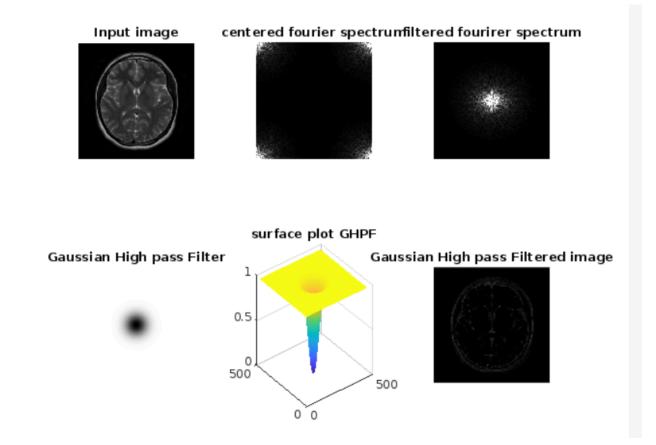


# iii. Gaussian high pass filter (GHPF)

#### **Code:**

```
clc;
clear;
close all;
a = imread('gray img.png');
a = rgb2gray(a);
a = im2double(a);
[m,n] =size(a);
subplot(2,3,1)
imshow(a)
title('Input image');
A = fft2(a);
subplot(2,3,2);
```

```
imshow(uint8(abs(A)));
title('centered fourier spectrum');
A_shift = fftshift(A);
A_real = abs(A_shift);
subplot(2,3,3)
imshow(uint8(A_real));
title('filtered fourirer spectrum');
D0 = 30;
for u=1:m
   for v=1:n
       D = sqrt((u-m/2).^2+(v-n/2).^2);
       H(u,v) = 1 - \exp(-(D^2)/(2*D0.^2));
   end
end
H high = H.*A shift;
H high real = H.*A real;
H_high_shift = fftshift(H_high);
H_high_image = ifft2(H_high_shift);
subplot(2,3,4)
imshow(H)
title('Gaussian High pass Filter');
subplot(2,3,5);
mesh(H)
title('surface plot GHPF')
subplot(2,3,6)
imshow(abs(H high image));
title('Gaussian High pass Filtered image');
```



For producing enhanced images (sharpening), the Butterworth High Pass Filter (BHPF) is better than IHPF and BHPF.

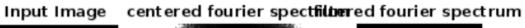
**Problem 3:** Apply three types of low pass filtering in the frequency domain in Figure 1 and find out which one is better to produce the smoothen image for the given image (output must show all steps as shown in Figure 2).

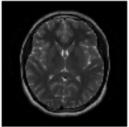
#### i. Ideal low pass filter (ILPF)

```
Code:
clc;
clear;
close all;
a = imread('gray img.png');
a = im2double(a);
```

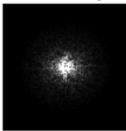
```
subplot(2,3,1);
imshow(a);
title('Input Image');
[m,n] = size(a);
D0 = 50;
A = fft2(a);
subplot(2,3,2);
imshow(uint8(abs(A)));
title('centered fourier spectrum');
A_shift = fftshift(A);
A_real = abs(A_shift);
subplot(2,3,3);
imshow(uint8(A real));
title('filtered fourier spectrum ');
A low = zeros(m,n);
d = zeros(m,n);
for u = 1:m
   for v = 1:n
       d(u,v) = sqrt((u-(m/2))^2 + (v-(n/2))^2;
       if d(u,v) \le D0
           A_low(u,v) = A_shift(u,v);
           filt(u,v) = 1;
       else
           A_low(u,v) = 0;
           filt(u,v) = 0;
       end
   end
subplot(2,3,4);
imshow(filt)
title('Ideal Low pass filter')
subplot(2,3,5);
```

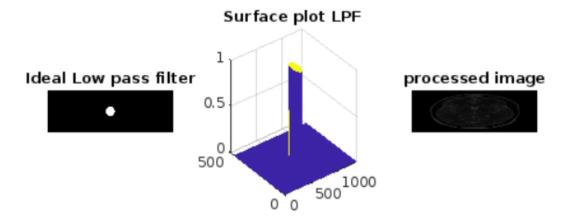
```
mesh(filt)
title('Surface plot LPF')
B = fftshift(A_low);
B_inverse = ifft2(B);
B_real = abs(B_inverse);
subplot(2,3,6);
imshow(B_real);
title('processed image');
```











# ii. Butterworth low pass filter (BLPF)

#### **Code:**

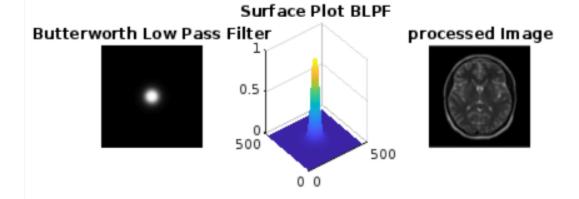
clc;

clear;

```
close all;
a = imread('gray img.png');
a = rgb2gray(a);
a = im2double(a);
[m,n] = size(a);
subplot(2,3,1)
imshow(a)
title('Input image');
A = fft2(a);
subplot(2,3,2);
imshow(uint8(abs(A)));
title('Centered Fourier Spectrum');
A shift = fftshift(A);
A_real = abs(A_shift);
subplot(2,3,3)
imshow(uint8(A real));
title('Filtered Fourier Spectrum');
D0 = 30;
order = 2;
for u = 1:m
   for v = 1:n
       D = sqrt((u - m/2)^2 + (v - n/2)^2);
       H(u,v) = 1 / (1 + (D / D0)^(2*order));
 end
end
H_low = H .* A_shift;
H_low_real = H .* A_real;
H_low_shift = fftshift(H_low);
H_low_image = ifft2(H_low_shift);
subplot(2,3,4)
imshow(H)
title('Butterworth Low Pass Filter');
```

```
subplot(2,3,5);
mesh(H)
title('Surface Plot BLPF')
subplot(2,3,6)
imshow(abs(H_low_image));
title('processed Image');
```



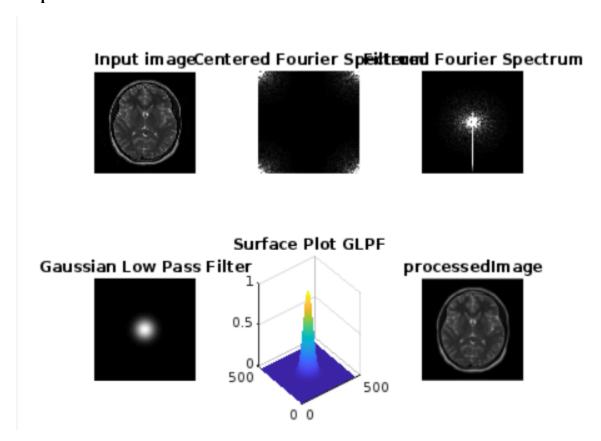


#### iii. Gaussian low pass filter (GLPF)

```
Code:
clc;
clear;
close all;
```

```
a = imread('gray img.png');
a = rgb2gray(a);
a = im2double(a);
[m,n] = size(a);
subplot(2,3,1)
imshow(a)
title('Input image');
A = fft2(a);
subplot(2,3,2);
imshow(uint8(abs(A)));
title('Centered Fourier Spectrum');
A shift = fftshift(A);
A real = abs(A shift);
subplot(2,3,3)
imshow(uint8(A real));
title('Filtered Fourier Spectrum');
D0 = 30;
for u = 1:m
   for v = 1:n
       D = sqrt((u - m/2)^2 + (v - n/2)^2);
       H(u,v) = \exp(-(D^2) / (2*D0^2));
   end
end
H_low = H .* A_shift;
H_low_real = H .* A_real;
H low shift = fftshift(H low);
H_low_image = ifft2(H_low_shift);
subplot(2,3,4)
imshow(H)
title('Gaussian Low Pass Filter');
subplot(2,3,5);
mesh(H)
```

```
title('Surface Plot GLPF')
subplot(2,3,6)
imshow(abs(H_low_image));
title('processedImage');
```



For producing smoothed images, the Gaussian Low Pass Filter (GLPF) is better than ILPF and GLPF.